

MA679 Hw6

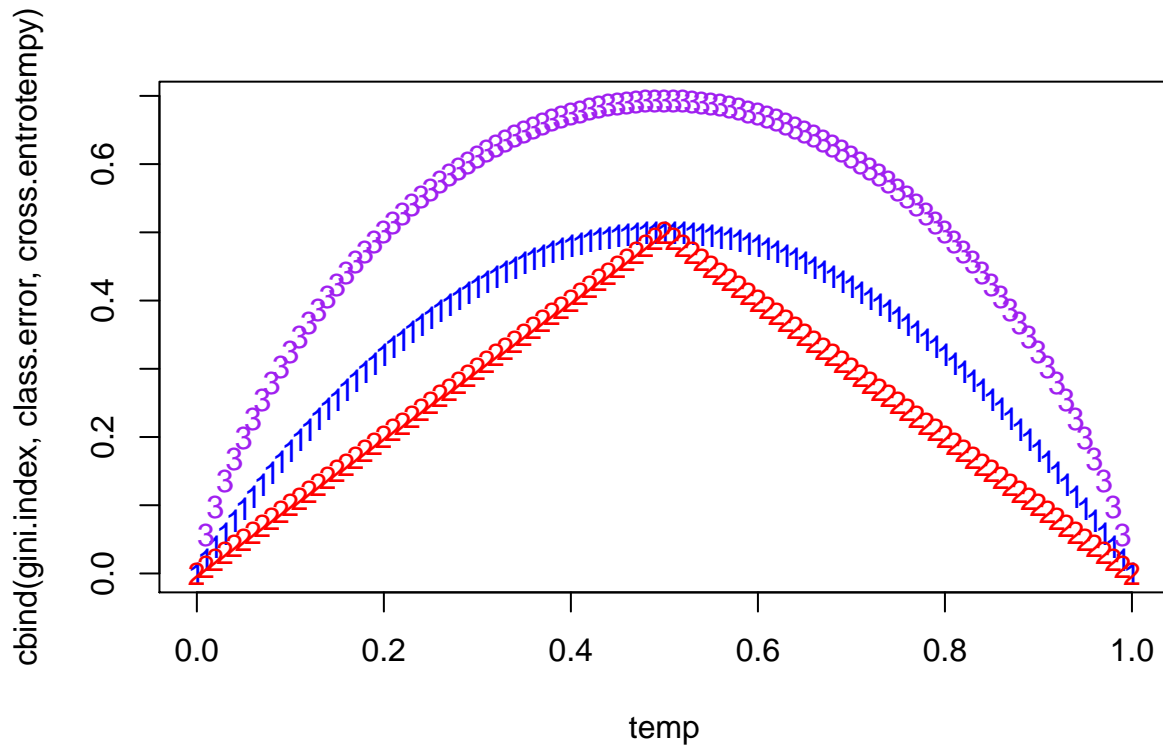
Jiahao Xu

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8.1 and 8.2 are in the next page

8.3

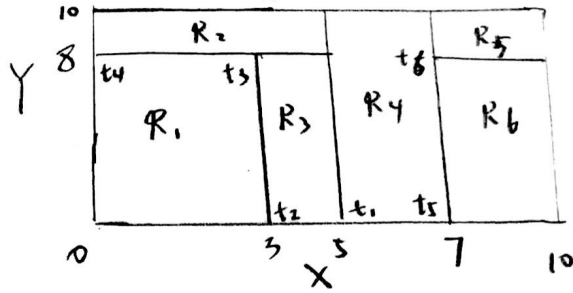
```
temp <- seq(0, 1, 0.01)
gini.index <- 2 * temp * (1 - temp)
class.error <- 1 - pmax(temp, 1 - temp)
cross.entrottemp <- -(temp * log(temp) + (1 - temp) * log(1 - temp))
matplot(temp, cbind(gini.index, class.error, cross.entrottemp), col = c("blue", "red", "purple"))
```



8.5

- #1. We classify X as Red as it is the most commonly occurring class among the 10 predictions (6 for Red)
- #2. With the average probability approach, we classify X as Green as the average of the 10 probabilities is 0.67.

8.1



8.2

$$\hat{f}_1(x) = c_1 I(x, t_1) + c_1' = \frac{1}{\lambda} f_1(x_1)$$

$$\text{Since } \hat{f}(x) = \lambda \hat{f}_1(x) \text{ and } r_i = y_i - \lambda \hat{f}_1(x_i)$$

$$f_2(x) = c_2 I(x, t_2) + c_2' = \frac{1}{\lambda} f_2(x_2)$$

$$\hat{f}(x) = \hat{\lambda} \hat{f}_1(x) + \lambda \hat{f}_2(x) \text{ and } r_i = y_i - \hat{\lambda} \hat{f}_1(x_i) - \lambda \hat{f}_2(x_i) \forall i$$

$$\therefore \hat{f}(x) = \sum_{i=1}^p f_i(x_i)$$

Figure 1: 8.1&8.2

8.7

```
library(MASS)
library(randomForest)

## randomForest 4.6-14

## Type rfNews() to see new features/changes/bug fixes.

set.seed(2)
train <- sample(1:nrow(Boston), nrow(Boston) / 2)
Boston.train <- Boston[train, -14]
Boston.test <- Boston[-train, -14]
Y.train <- Boston[train, 14]
Y.test <- Boston[-train, 14]
rf.boston1 <- randomForest(Boston.train, y = Y.train, xtest = Boston.test, ytest = Y.test, mtry = ncol(Boston.train))
rf.boston2 <- randomForest(Boston.train, y = Y.train, xtest = Boston.test, ytest = Y.test, mtry = (ncol(Boston.train) / 2))
rf.boston3 <- randomForest(Boston.train, y = Y.train, xtest = Boston.test, ytest = Y.test, mtry = sqrt(ncol(Boston.train)))
plot(1:500, rf.boston1$test$mse, col = "green", type = "l", xlab = "Number of Trees", ylab = "Test MSE")
lines(1:500, rf.boston2$test$mse, col = "red", type = "l")
lines(1:500, rf.boston3$test$mse, col = "blue", type = "l")
legend("topright", c("m = p", "m = p/2", "m = sqrt(p)"), col = c("green", "red", "blue"), cex = 1, lty = 1)
```

