

APPENDIX B

Armature Reaction

Flux produced by armature winding (when current I_a flows) reacts with the flux set up by the rotor field, causing a redistribution of the total resultant flux. Such an interaction between the two fluxes is called armature reaction → This affects the terminal voltage V .

Let us examine a sequence of events that will take place when the generator delivers a load at unity pf.

- (a) If ϕ_F = rotor flux
Then E must lag ϕ_F by 90° (stated before)
- (b) I_a is in phase with V (UPF load)
- (c) I_a produces a flux ϕ_{ar} which is in phase with I_a .
Effective flux $\phi_T = \phi_F + \phi_{ar}$.
- (d) Flux ϕ_{ar} produces an EMF E_{ar} in the armature winding.
 E_{ar} = armature reaction EMF, and it lags ϕ_{ar} by 90° .

\Rightarrow Effective generated voltage

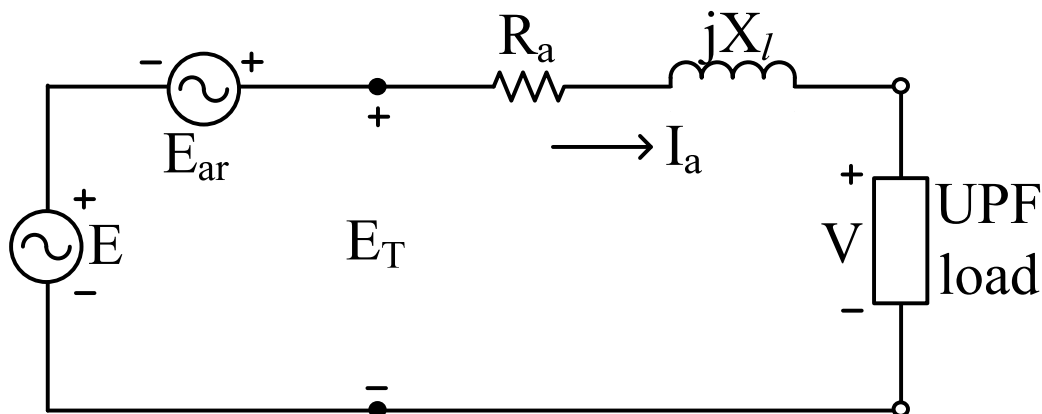
$$E_T = E + E_{ar} \Rightarrow E = E_T - E_{ar}$$

(e) Terminal voltage V is obtained by subtracting $I_a R_a$ & $jI_a X_l$ drops from E_T .

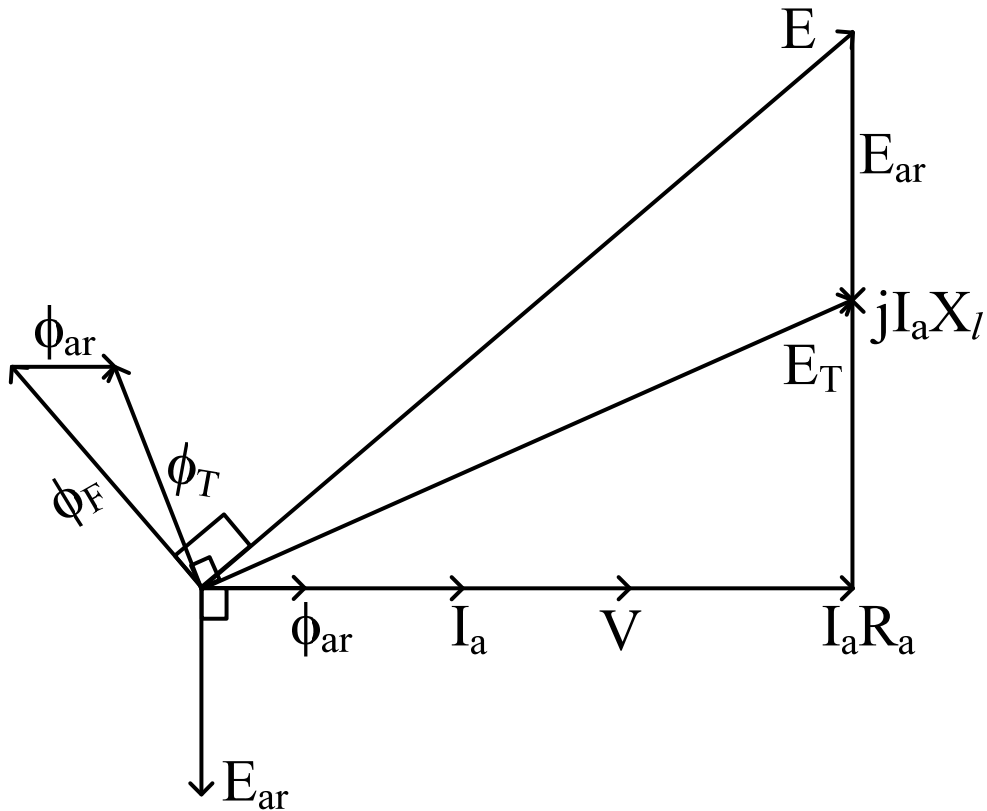
$$\Rightarrow E_T = I_a R_a + jI_a X_l + V$$

Note from the phasor diagram that

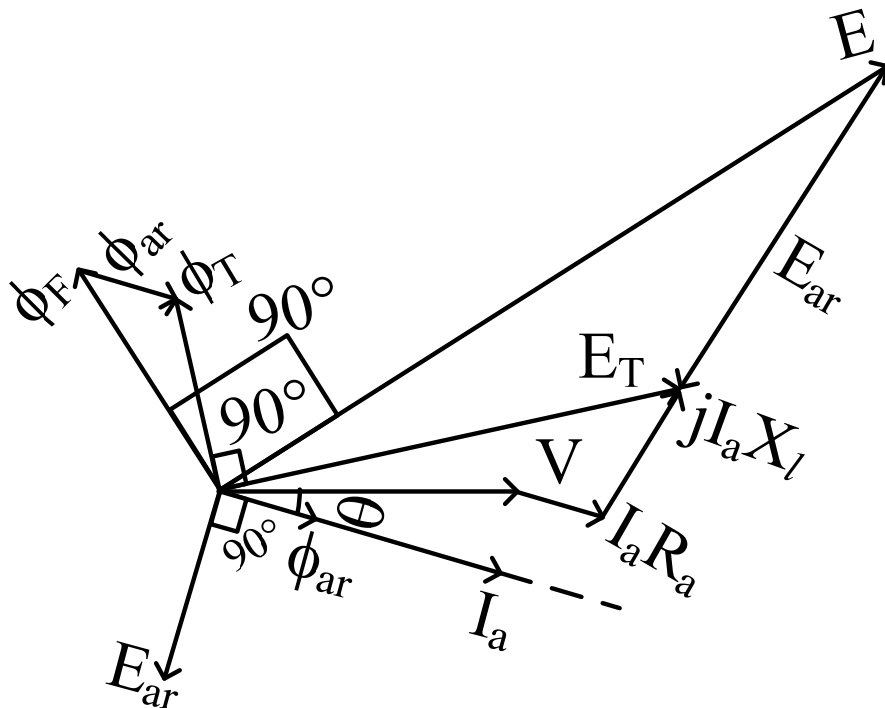
- the armature reaction has reduced the effective flux per pole (from ϕ_F to ϕ_T) at UPF load.
- armature reaction has reduced the terminal voltage.



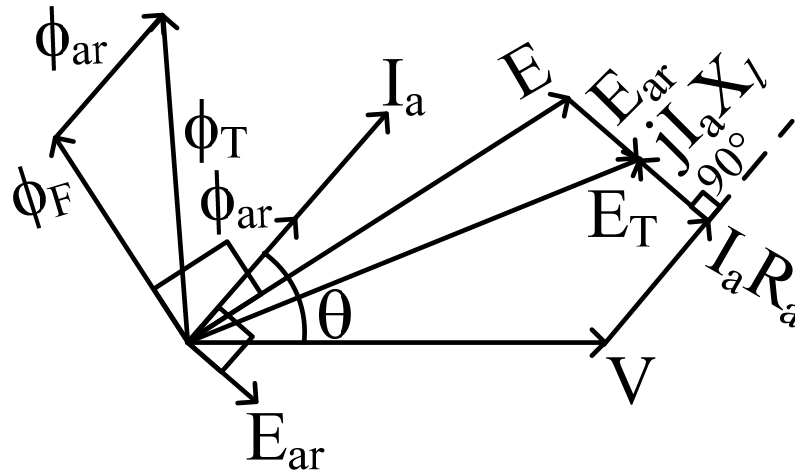
Equiv. CKT. showing the induced EMF in the armature winding due to the armature reaction.



Phasor diagram showing effect of armature reaction
when load is UPF load. ($\phi_T < \phi_F$, $V < E$)



Lagging PF load ($\phi_T < \phi_F$, $V < E$)



Leading PF loads ($\phi_T > \phi_F$, $V > E$)

Since E_{ar} lags I_a (& ϕ_{ar}) by 90° , we can also express it as

$E_{ar} = -jI_a X_{ar}$ where X_{ar} = armature reaction reactance

Since both X_{ar} & X_l are present all the time & it is rather difficult to separate them, we combine them together, and

$X_s = X_{ar} + X_l$ where X_s is called synchronous reactance.

$X_s \gg R_a$ (usually)

$Z_s =$ synchronous impedance per phase
 $= R_a + jX_s$

$$\therefore E = I_a R_a + jX_s I_a + V$$

$$\Rightarrow V = E - I_a Z_s$$

Neglecting R_a , $Z_s \simeq jX_s = j(X_{ar} + X_l)$