EE3015 Tutorial #3

$$S_b = 125 \text{ MVA, } V_b = 13.2 \text{ kV}$$

$$Z_b = 13.2^2/125 = 1.3939 \Omega$$

$$X_s = 1.7/1.3939 = 1.2196 \text{ pu}$$

$$V = 13.2/V_b = 1 \angle 0^\circ \text{ pu; Ref}$$

$$V = \frac{100}{125} \angle 0^\circ = 0.8 \angle 0^\circ \text{ pu}$$

$$I_{a1} = (S/V)^* = 0.8 \angle 0^\circ \text{ pu}$$

$$E_1 = V + jX_s I_{a1} = 1\angle0^{\circ} + 1.2196\angle90^{\circ} \times 0.8\angle0^{\circ} = 1.3971\angle44.295^{\circ}$$
 pu

$$|E_1|$$
 = 1.3971 x V_b = 1.3971 x 13.2 = 18.442 kV; δ_1 = 44.295° Q_1 = 0 due to unity pf.

(b) We assume that the generator has zero internal loss. Hence if the prime mover input to the generator is reduced by 50%:

$$P_2 = P_1/2 = 100/2 = 50 \text{ MW} \rightarrow P_2 = 50/S_b = 50/125 = 0.4 \text{ pu}$$

Without changing the excitation $\rightarrow |E_2| = |E_1|$ in part (a)

$$P_2 = \frac{E_2 V}{X_s} Sin\delta_2 \rightarrow 0.4 = \frac{1.3971x1}{1.2196} Sin\delta_2$$

$$\delta_2 = \text{Sin}^{-1} \frac{0.4 \text{x} 1.2196}{1.3971} = 20.437^{\circ}$$
; $|E_2|$ remains the same as before.

$$Q_2 = \frac{V}{X_s} (E_2 \cos \delta_2 - V) = \frac{1}{1.2196} (1.3971 \cos 20.437^{\circ} - 1) = 0.2535 \text{ pu}$$

 $Q_2 = 0.2535xS_b = 0.2535x125 = 31.687$ Mvar (produced by the generator)

(c)
$$P_3 = P_1 = 0.8 \text{ pu} = \text{Constant power} \rightarrow \text{E Sin}\delta = \text{Constant}$$

This means that $E_3 \sin \delta_3 = E_1 \sin \delta_1$. However, we know E_1 and δ_1 but not E_3 and δ_3 . Hence we are not able to solve E_3 and δ_3 .

Applying the other constant power equation: $I_{a3} \cos\theta_3 = I_{a1} \cos\theta_1$. Therefore $I_{a3} \times 0.8 = 0.8 \times 1 \rightarrow I_{a3} = 1$ pu.

 $I_{a3} = 1 \angle 36.87^{\circ}$ pu; positive for leading angle (first quadrant).

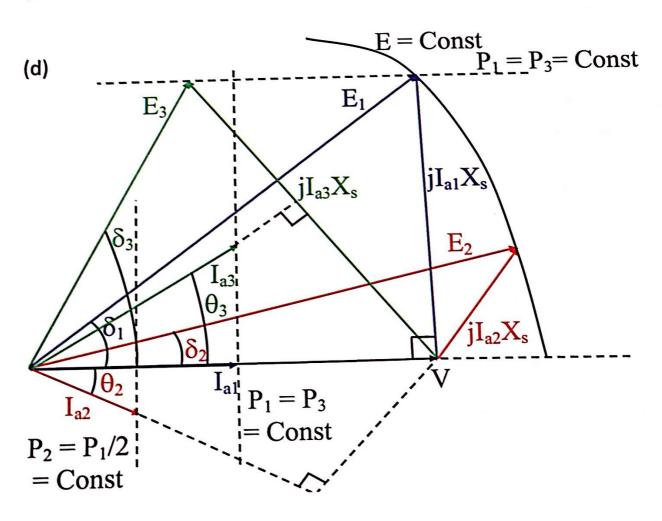
Alternative approach: Form S_3 from 100 MW, 0.8 pf leading and S_b . Obtain I_{a3} from $I_{a3} = (S_3/V)^*$.

$$E_3 = V + jX_s I_{a3} = 1\angle0^{\circ} + 1.2196\angle90^{\circ} \times 1\angle36.87^{\circ} = 1.0119\angle74.63^{\circ} pu$$

$$|E_3|$$
 = 1.0119 x V_b = 1.0119 x 13.2 = 13.357 kV; δ_3 = 74.63°

$$Q_3 = -V I_{a3} \sin \theta_3 = -1x1 \sin 36.87^{\circ} = -0.6 \text{ pu}$$

Actual $Q_3 = -0.6 \times S_b = -75$ Mvar (or 75 Mvar absorbed by the generator).



3.2
$$I_b = 188 \text{ A, } V_b = 13.2 \text{ kV} \rightarrow S_b = \frac{\sqrt{3}V_bI_b}{1000} = 4.298 \text{ MVA}$$

$$Z_{b} = 13.2^{2}/4.298 = 40.537 \Omega$$

$$X_{s} = 10/40.537 = 0.2467 \text{ pu}$$

$$V = \frac{13.2}{10.20} = 1 \angle 0^{\circ} \text{ pu, ref at } 0$$

$$Z_b = 13.2^2/4.298 = 40.537 \Omega$$

$$V = \frac{13.2}{V_b} = 1 \angle 0^\circ \text{ pu, ref angle} = 0^\circ$$

$$S_{old} = \frac{\sqrt{3}x13.2x0.188}{S_b} = 1 \angle 0^{\circ} \text{ pu; } 0^{\circ} \text{ because of unity pf}$$

$$I_{a, \text{ old}} = \left(\frac{S_{old}}{V}\right)^* = \left(\frac{1\angle 0^{\circ}}{1\angle 0^{\circ}}\right)^* = 1\angle 0^{\circ} \text{ pu}$$

$$E_{old} = V + jX_s I_{a, old} = 1\angle0^{\circ} + 0.2467\angle90^{\circ} \times 1\angle0^{\circ} = 1.03\angle13.857^{\circ} pu$$

$$|E_{new}| = 1.25|E_{old}|$$

Without changing the mechanical power input \rightarrow P = Constant

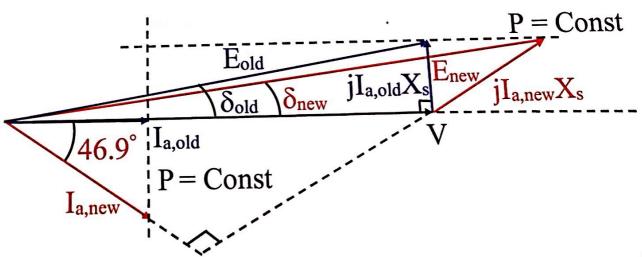
$$\mathsf{E}_{\mathsf{new}}\,\mathsf{Sin}\,\,\delta_{\mathsf{new}} = \mathsf{E}_{\mathsf{old}}\,\mathsf{Sin}\,\,\delta_{\mathsf{old}}\,\rightarrow\, 1.25\mathsf{E}_{\mathsf{old}}\,\mathsf{Sin}\,\,\delta_{\mathsf{new}} = \mathsf{E}_{\mathsf{old}}\,\mathsf{Sin}\,\,\delta_{\mathsf{old}}$$

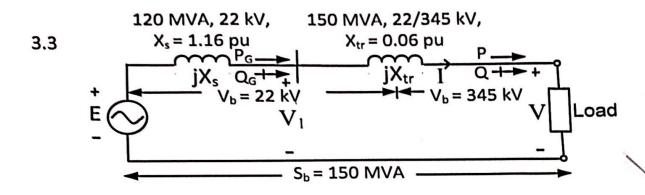
$$\delta_{\text{new}} = \text{Sin}^{-1} (\text{Sin}13.857^{\circ}/1.25) = 11.046^{\circ}$$

$$I_{a,new} = \frac{E_{new} - V}{jX_s} = \left(\frac{1.25x1.03\angle 11.046^{\circ} - 1\angle 0^{\circ}}{0.2467\angle 90^{\circ}}\right) = 1.4636\angle - 46.9^{\circ} \ pu$$

Actual $|I_{a,new}| = 1.4636 \times I_b = 1.4636 \times 188 = 275.15 A$

pf of generator = $\cos 46.9^{\circ} = 0.683 \log (I_{a,new} \log V)$





$$X_s = 1.16x \frac{150}{120} = 1.45$$
 pu after converting to $S_b = 150$ MVA

(a)
$$V = 345/V_b = 345/345 = 1 \angle 0^\circ$$
 pu

$$S_{Load} = \left(\frac{80}{0.8} \angle -36.87^{\circ}\right) / 150 = 0.667 \angle -36.87^{\circ} \text{ pu}$$

$$I = \left(\frac{S_{Load}}{V}\right)^* = \left(\frac{0.667 \angle -36.87^{\circ}}{1 \angle 0^{\circ}}\right)^* = 0.667 \angle 36.87^{\circ} \text{ pu}$$

$$V_1 = V + jX_{tr} I = 1 \angle 0^{\circ} + 0.06 \angle 90^{\circ} \times 0.667 \angle 36.87^{\circ} = 0.9765 \angle 1.88^{\circ} pu$$

Actual $|V_1| = 0.9765 \times V_b = 0.9765 \times 22 = 21.4835 \text{ kV}$

$$E = V_1 + jX_s I = 0.9765 \angle 1.88^{\circ} + 1.45 \angle 90^{\circ} \times 0.667 \angle 36.87^{\circ} = 0.8974 \angle 63.815^{\circ} pu$$

Actual $|E| = 0.8974 \times V_b = 0.8974 \times 22 = 19.743 \text{ kV}$

(b) (i)
$$|E'| = 1.2|E|$$
 where $E = 0.8974 \angle 63.815^{\circ}$ from (a)

Constant load of 80 MW \rightarrow P = Constant \rightarrow E' Sin δ' = E Sin δ \rightarrow 1.2E Sin δ' = E Sin 63.815°

$$\delta' = Sin^{-1} (Sin63.815^{\circ}/1.2) = 48.4^{\circ}$$

$$I' = \frac{E' - V}{j(X_s + X_{tr})} = \left(\frac{1.2 \times 0.8974 \angle 48.4^{\circ} - 1 \angle 0^{\circ}}{1.51 \angle 90^{\circ}}\right) = 0.5657 \angle 19.49^{\circ} \text{ pu}$$

$$V_1' = V + jX_{tr} I' = 1 \angle 0^{\circ} + 0.06 \times 0.5657 \angle 109.49^{\circ} = 0.9892 \angle 1.854^{\circ} pu$$

Actual generator terminal voltage = 0.9892 x 22 = 21.762 kV

(b) (ii)
$$S_G = P_G + jQ_G = V_1'(l')^*$$

$$\begin{aligned} \mathbf{Q}_{\mathsf{G}} &= \mathsf{Imag} \Big[\mathsf{V_1'(I')}^* \Big] = \mathsf{Imag} \Big[0.9892 \angle 1.854^{\circ} \times \ 0.5657 \angle -19.49^{\circ} \Big] \\ &= \mathsf{Imag} \Big[0.5596 \angle -17.64^{\circ} \Big] = 0.5596 \times \mathsf{Sin} \Big(-17.64^{\circ} \Big) = -0.1697 \ \mathsf{pu} \end{aligned}$$

Actual reactive power output of the generator = -0.1697×150 = -25.43 Mvar or 25.43 Mvar absorebed by the generator

Alternative approach: Use
$$Q_G = \frac{V_1'}{X_s} (E'Cos\delta' - V_1')$$

Note that you cannot substitute δ' = 48.4° in the above equation since the ref angle of $V_1{}^\prime$ is NOT at zero degree. Instead you need to substitute $\delta' = 48.4^{\circ} - 1.854^{\circ} = 46.546^{\circ}$ since this is the angle difference between E' and V1'

(b) (iii)
$$S = P + jQ = V(l')^*$$

$$Q = Imag[V(I')^*] = Imag[1\angle 0^{\circ} \times 0.5657 \angle -19.49^{\circ}]$$
$$= Imag[0.5657 \angle -19.49^{\circ}] = 0.5657 \times Sin(-19.49^{\circ}) = -0.1887 \text{ pu}$$

Actual reactive power output of the generator = -0.1887×150 = -28.31 Mvar or 28.31 Mvar flowing towards the transformer

Alternative approach: Use
$$Q = \frac{V}{X_{tr}} (V_1' \cos \theta_1' - V)$$

where θ_1 ' is the phasor angle of V_1 ':

Note that no further angle adjustment is required since the ref angle of V is at zero degree.

(c) (i)
$$\delta = 90^{\circ}$$
, E = 0.8974 pu and $X_s + X_{tr} = 1.51$ pu

$$P_{\text{max}} = \frac{\text{EV}}{X_s + X_{tr}} \text{Sin} \delta \big|_{\delta = 90^{\circ}}$$

$$P_{\text{max}} = \frac{0.8974}{1.51} = 0.5943 \text{ pu}$$

Actual $P_{max} = 0.5943 \times 150 = 89.145 MW$

$$I\big|_{\delta=90^{\circ}} = \frac{E-V}{j(X_s+X_{tr})} = \left(\frac{0.8974\angle 90^{\circ}-1\angle 0^{\circ}}{1.51\angle 90^{\circ}}\right) = 0.8898\angle 48.09^{\circ} \ pu$$

Power factor = Cos 48.09° = 0.6678 lead

(c) (ii)
$$\delta = 90^{\circ}$$
, E' = 1.2 x 0.8974 pu and $X_s + X_{tr} = 1.51$ pu

$$P_{\text{max}} = \frac{E'V}{X_s + X_{tr}} \text{Sin}\delta \Big|_{\delta = 90}^{\circ}$$

$$P_{\text{max}} = \frac{1.2 \times 0.8974}{1.51} = 0.7132 \text{ pu}$$

Actual $P_{\text{max}} = 0.7132 \times 150 = 106.96 \text{ MW}$

$$I|_{\delta=90^{\circ}} = \frac{E' - V}{j(X_s + X_{tr})} = \left(\frac{1.2 \times 0.8974 \angle 90^{\circ} - 1 \angle 0^{\circ}}{1.51 \angle 90^{\circ}}\right) = 0.9733 \angle 42.88^{\circ} \text{ pu}$$

Power factor = Cos 42.88° = 0.7328 lead