Bonus Problem: Convergence in Distribution

Situation. Let $X_p \sim NegBin(n, p)$. Show that pX_p converges in distribution as $p \to 0$ and determine the limiting distribution.

Hint. Determine the mgf of pX_p and then use the MacLaurin Series representation of the exponential function. Also, the limiting distribution is continuous.