

**Tutorial 2**

1. Write an algorithm that reverses the array  $s[1], \dots, s[n]$ .
2. Given an array  $s[1], \dots, s[n]$  such that  $n > 1$  and  $s[i] \leq s[i+1]$  for all  $i$ . Write an algorithm that insert an input value  $x$  into the array so that  $s[i] \leq s[i+1]$  for all  $i$ .
3. The algorithm for finding the maximum element of an array is in the following

```
Algorithm arrayMax(A, n)  
Input array A of n integers  
Output maximum element of A  
currentMax = A[0]  
for i = 1 to n - 1 do  
    if A[i] > currentMax then  
        currentMax = A[i]  
return currentMax
```

Determine the number of times that the statement “*currentMax* = *A*[*i*]” will be executed in the best case and in the worst case.

4. Order the following functions according to their order of growth (from the lowest to the highest).

$$n!, 5 \lg(n+100)^{10}, 2^{2^n}, n^4 + 3n^3 + 1, n \lg n, 3^n$$

5. Prove the following assertion:

If  $f(n) = O(g(n))$ , then  $g(n) = \Omega(f(n))$ .

- 6 (i) If  $f(n) = 2n^2 + 1$ , prove that  $f(n) = O(n^2)$   
(ii) If  $f(n) = 2^{n+2}$ , prove that  $f(n) = O(2^n)$   
(iii) If  $f(n) = 3 \lg n + 2$ , prove that  $f(n) = O(\lg n)$
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