

Textures

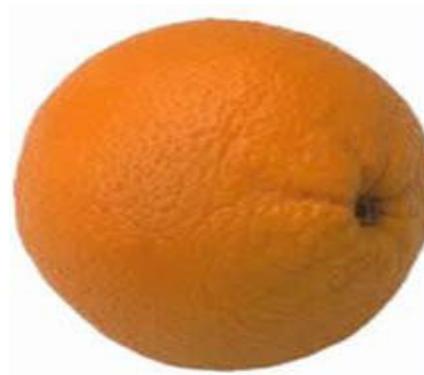
Carlos Andujar

Feb 2021

INTRODUCCIÓ

Representació de detalls superficials

Variacions de la *geometria*:

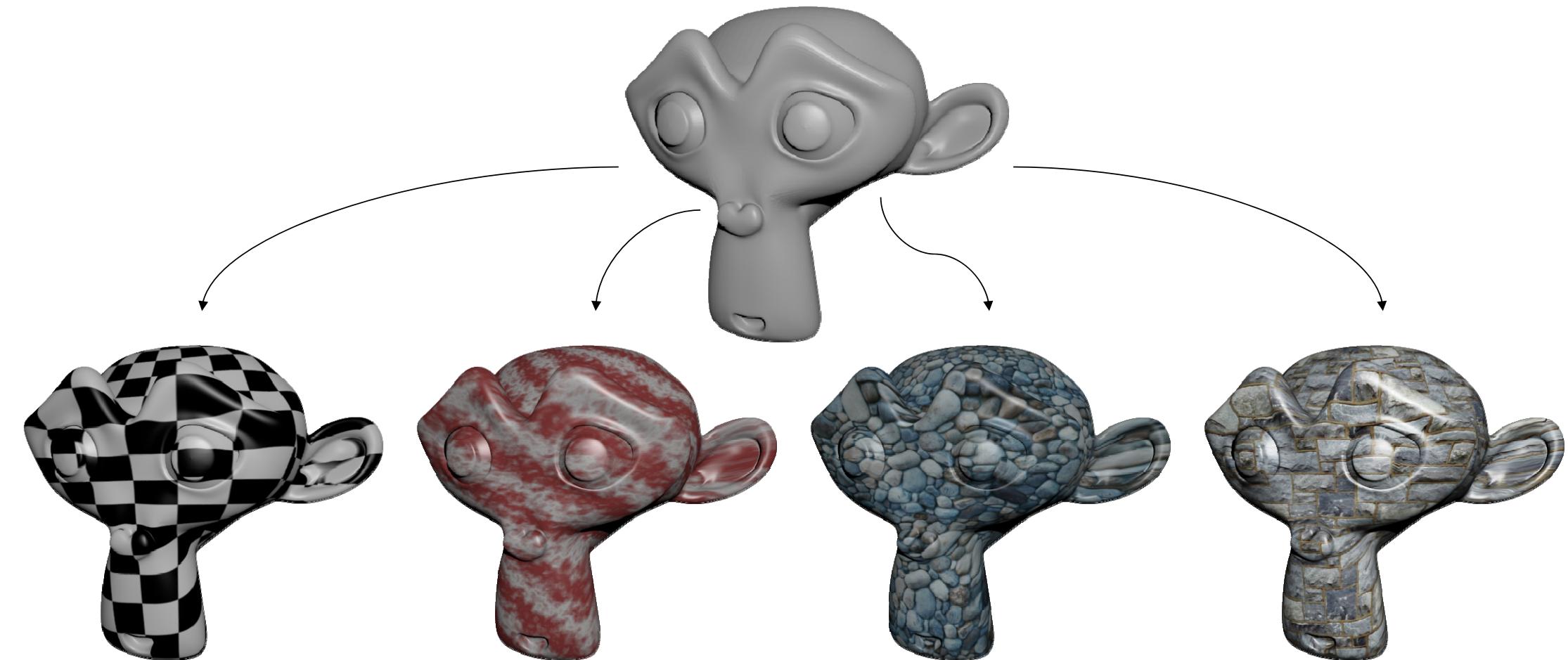


Variacions de les *propietats òptiques*:



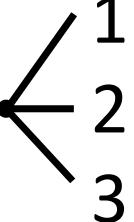


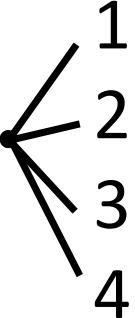
Representació de detalls superficials



DEFINICIONS

Textures

Una textura és una taula de  dimensions, on cada cel·la

enmagatzema una certa propietat amb  canals.

Habitualment les textures s'utilitzen al FS, tot i que també es poden usar en altres shaders.

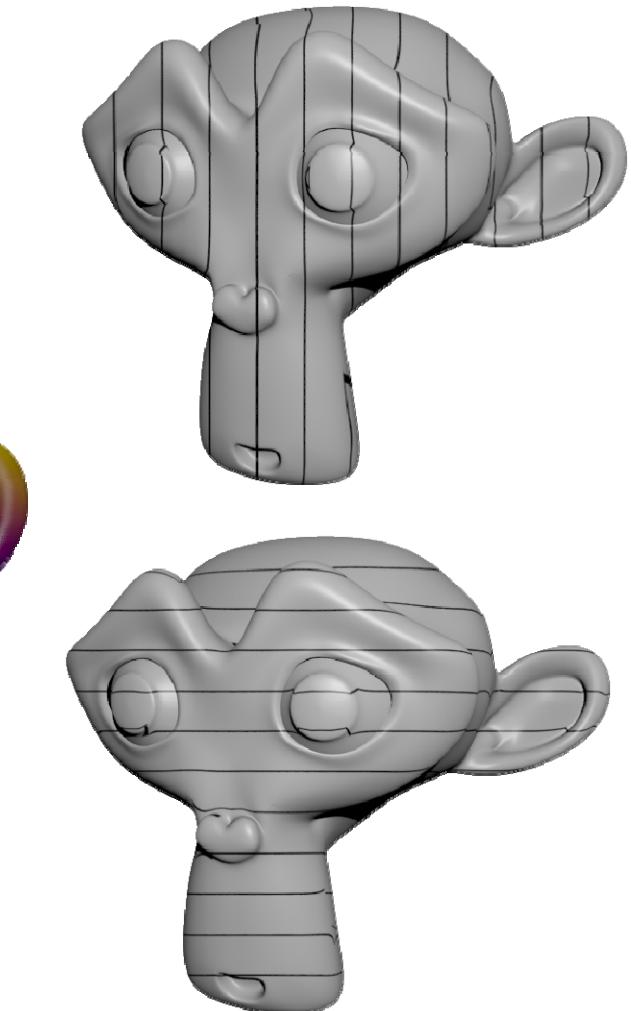
Textures

Una textura és una taula de  dimensions, on cada cel·la enmagatzema una certa propietat amb  canals.

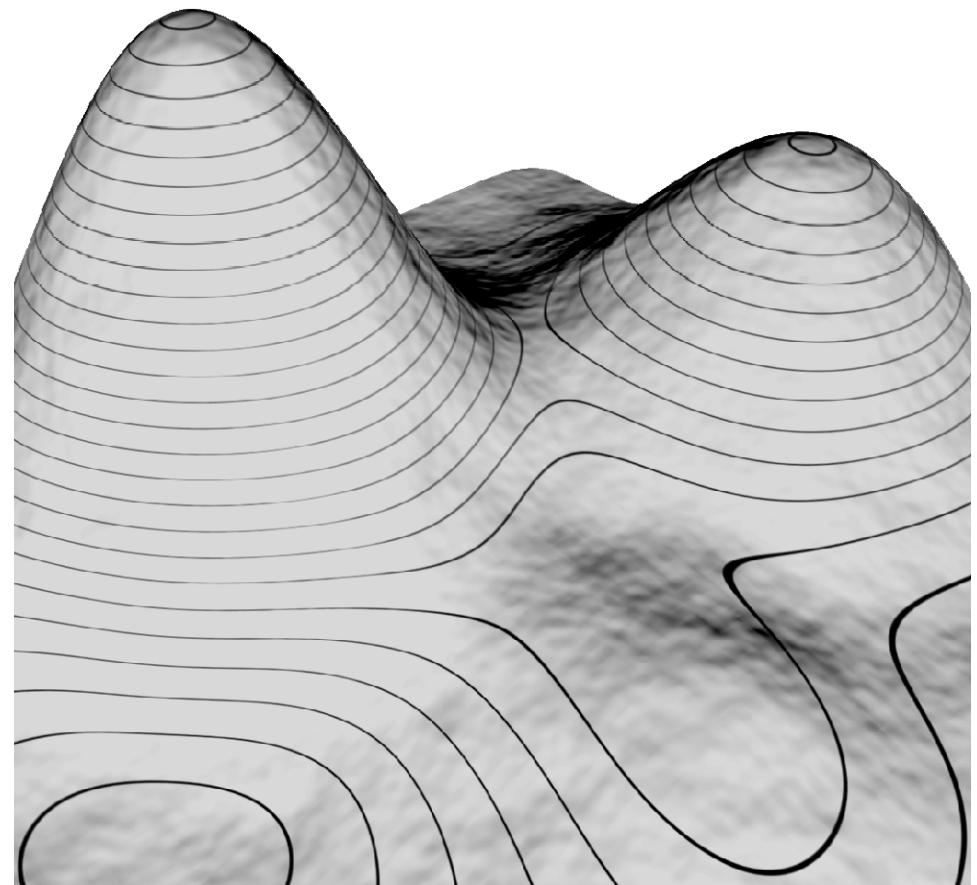
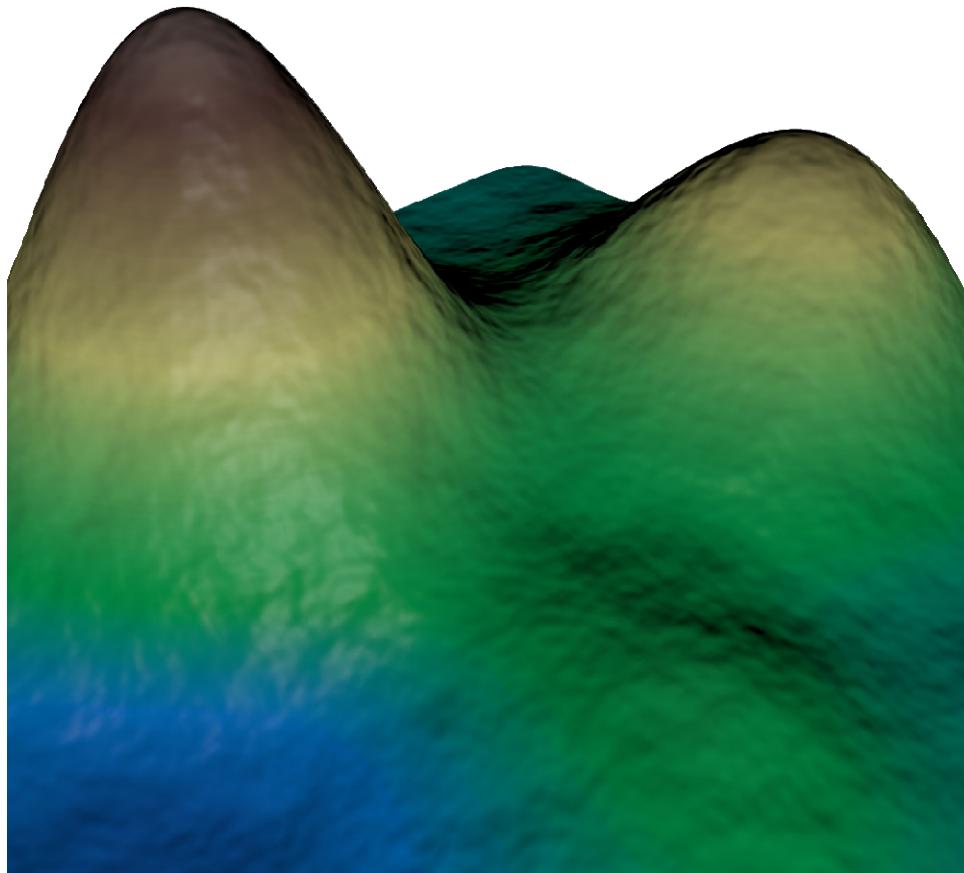
Textures 1D



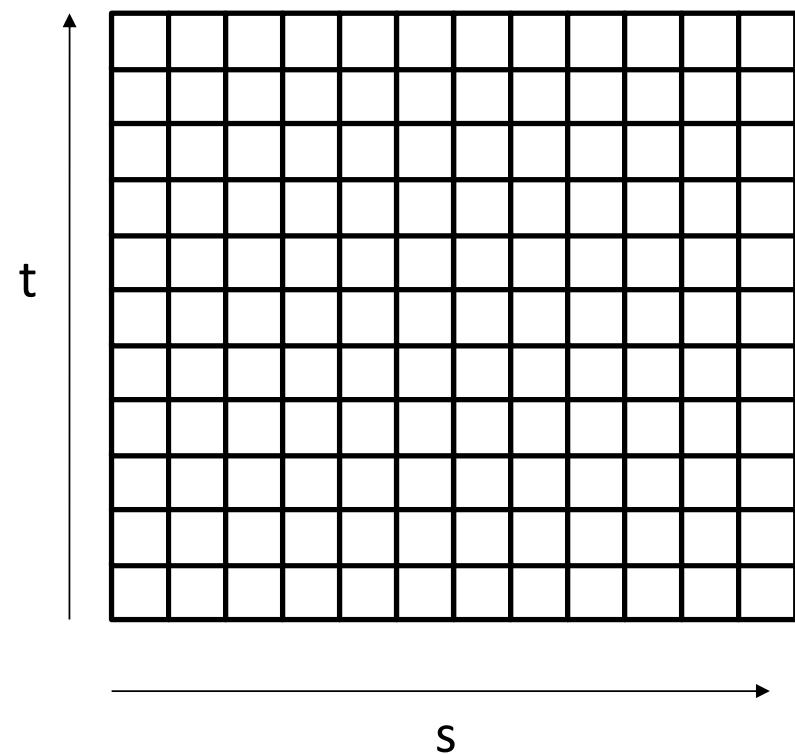
s



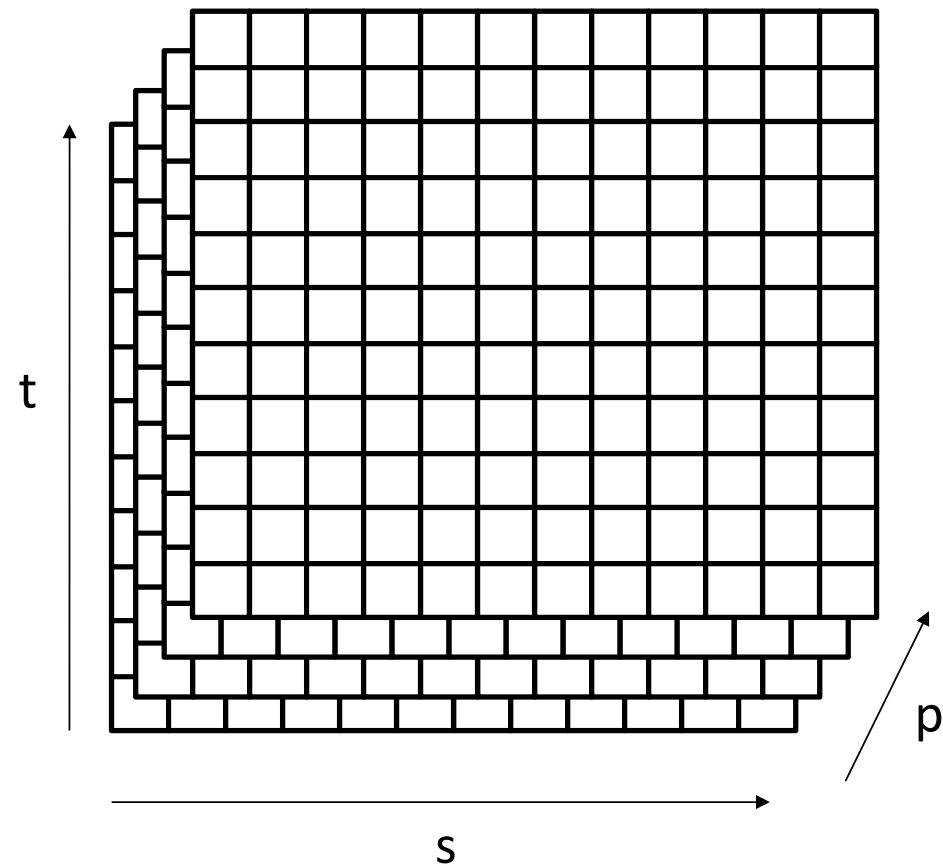
Textures 1D



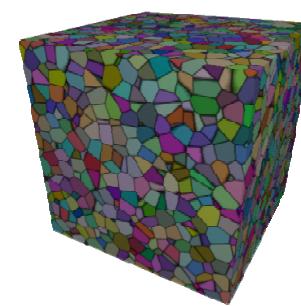
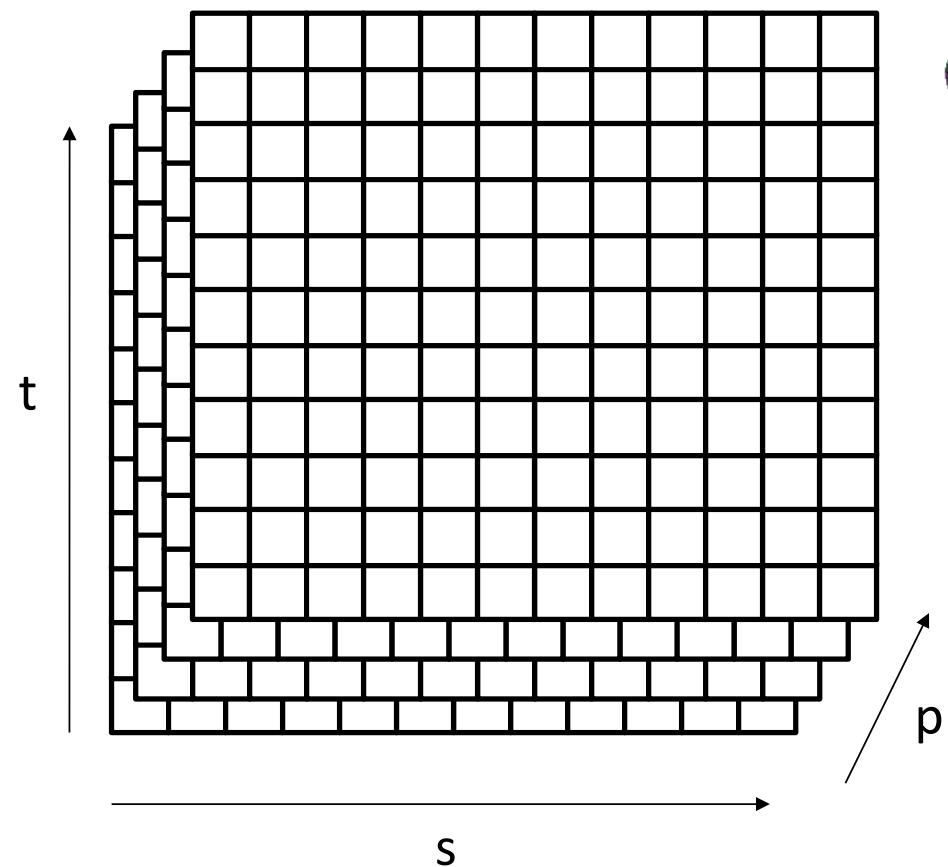
Textures 2D



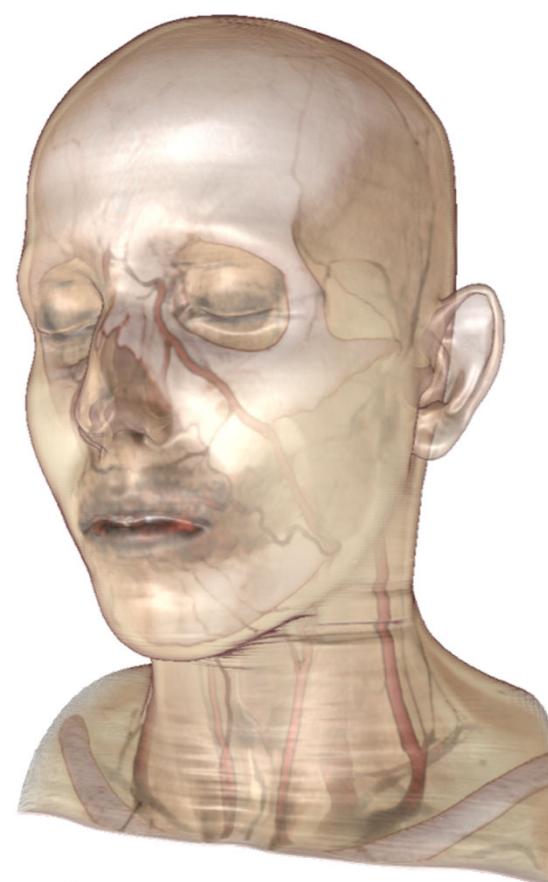
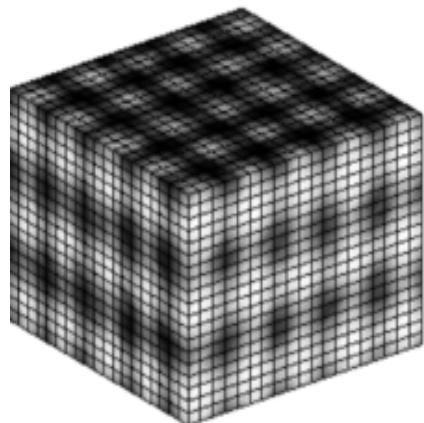
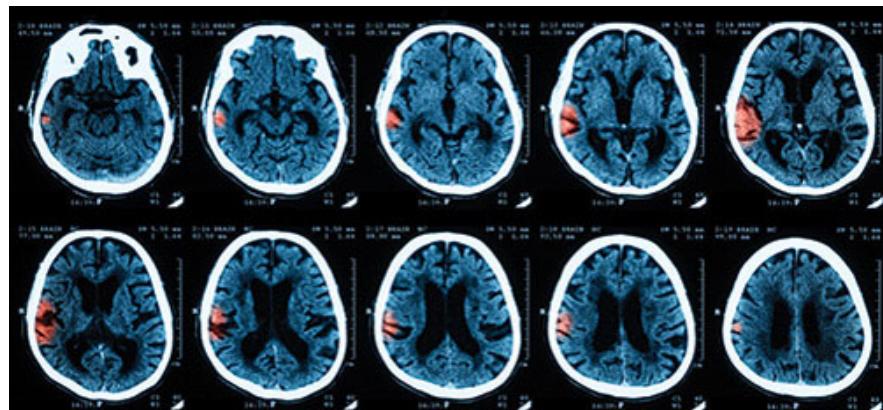
Textures 3D



Textures 3D



Textures 3D

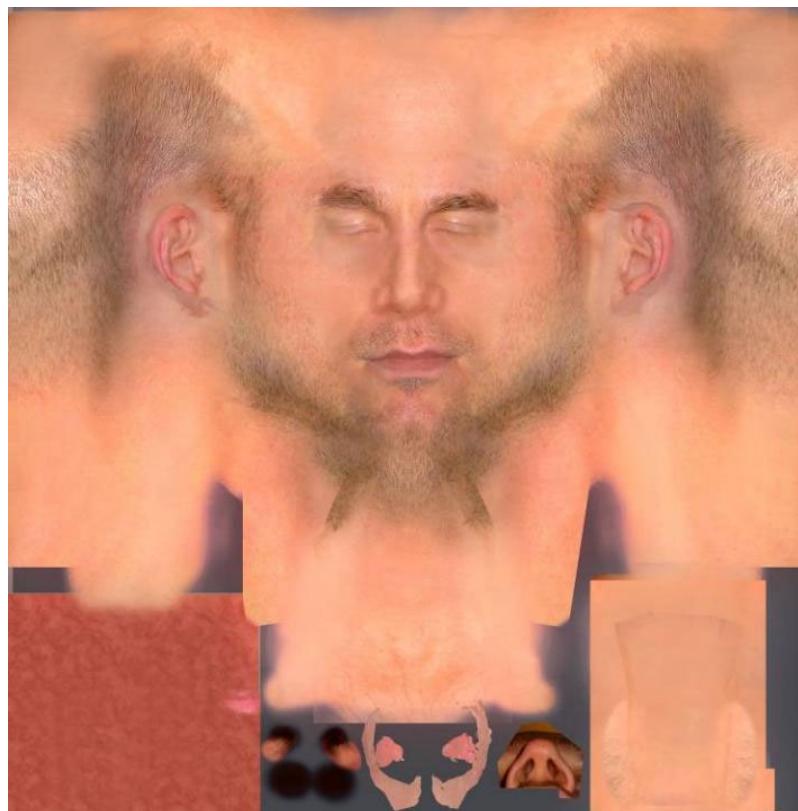


Textures

Una textura és una taula de dimensions, on cada cel·la enmagatzema una certa **propietat amb canals.**

Habitualment les textures s'utilitzen al FS, tot i que també es poden usar en altres shaders.

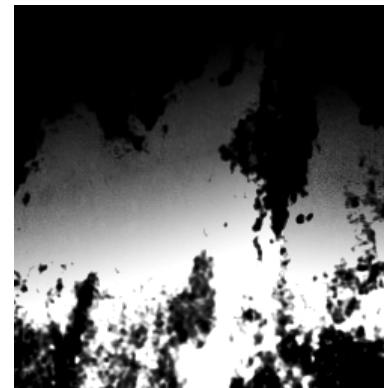
K_d (color map)



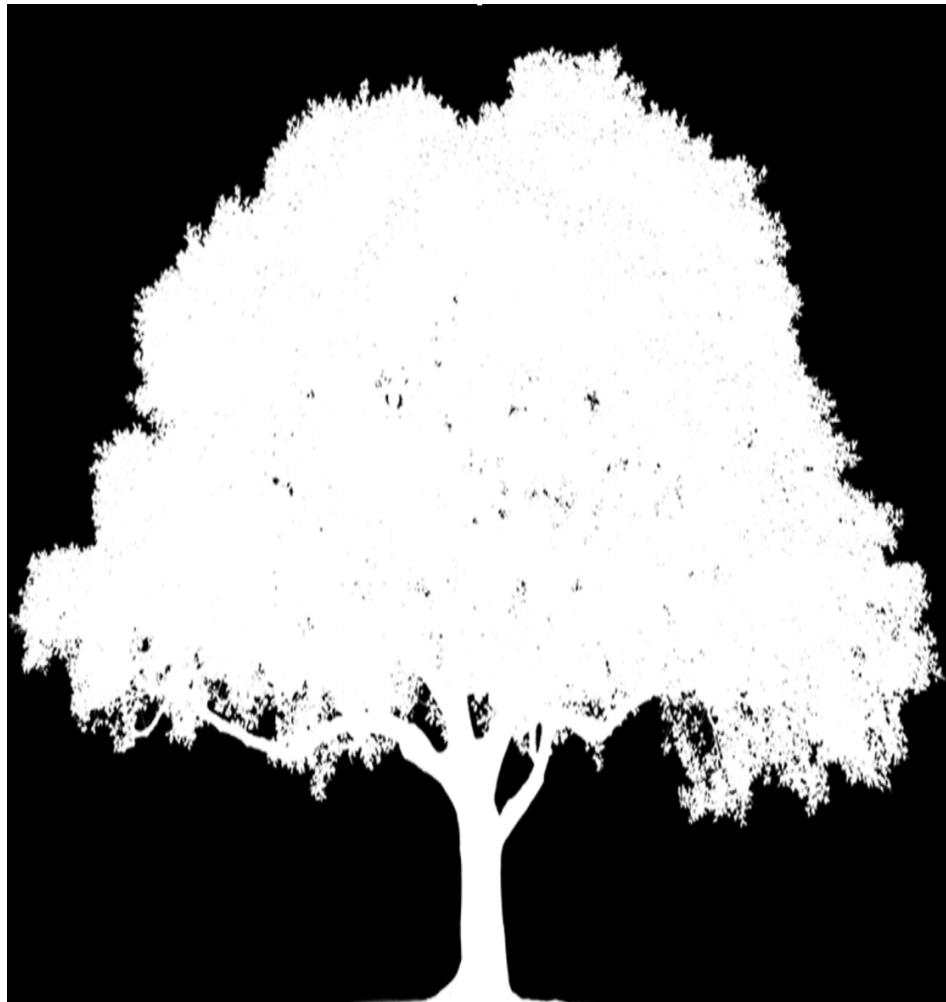
K_s (gloss map)



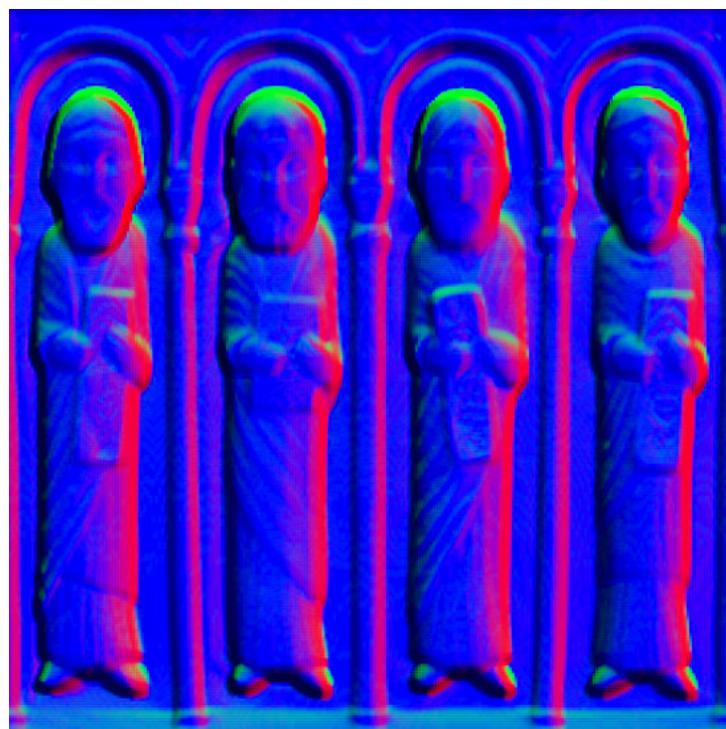
K_s (gloss map)



Opacitat (opacity map, alpha mask)



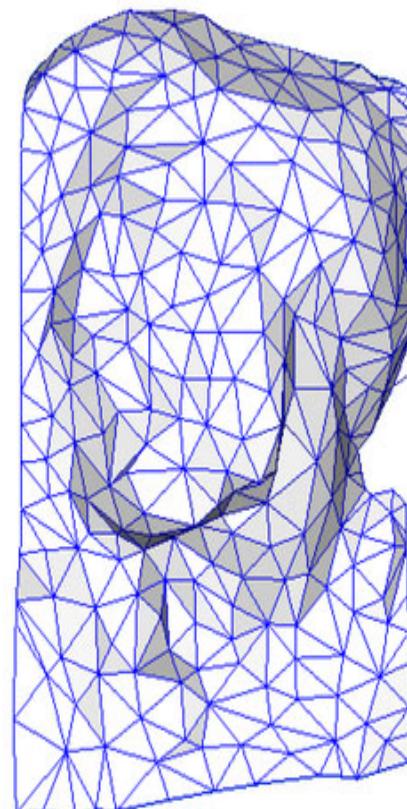
Normal (normal map)



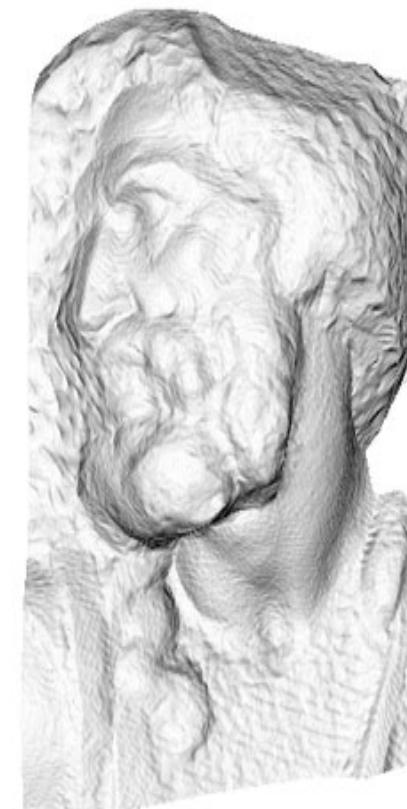
Normal (normal mapping)



original mesh
4M triangles

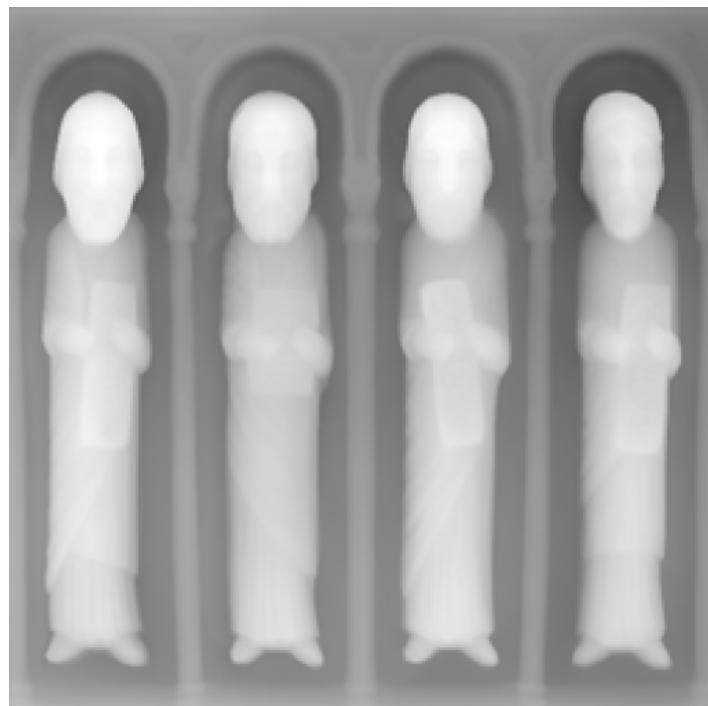


simplified mesh
500 triangles

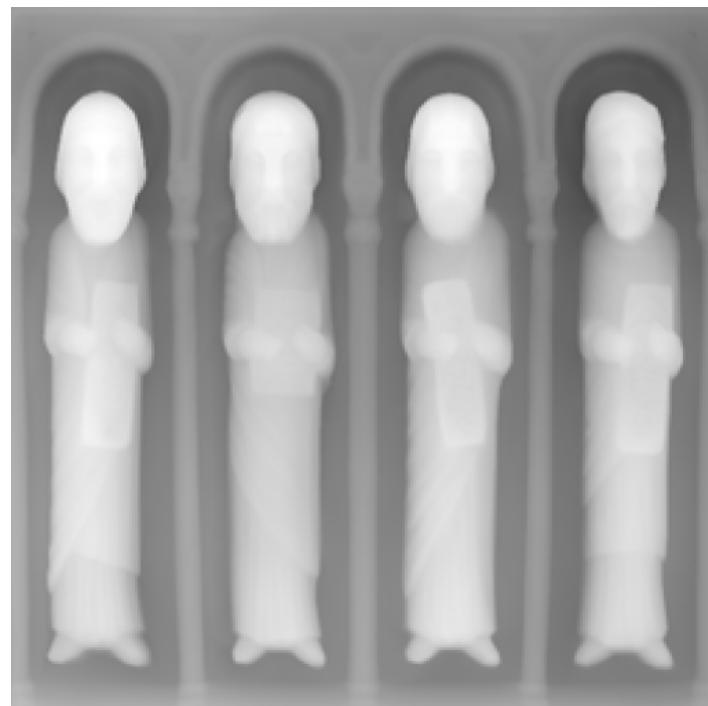


simplified mesh
and normal mapping
500 triangles

Desplaçament (bump mapping)

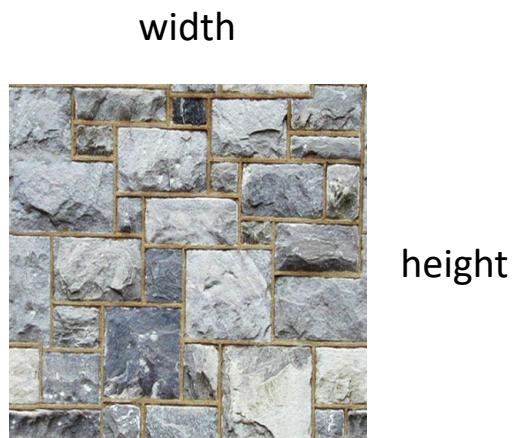


Desplaçament (displacement mapping)

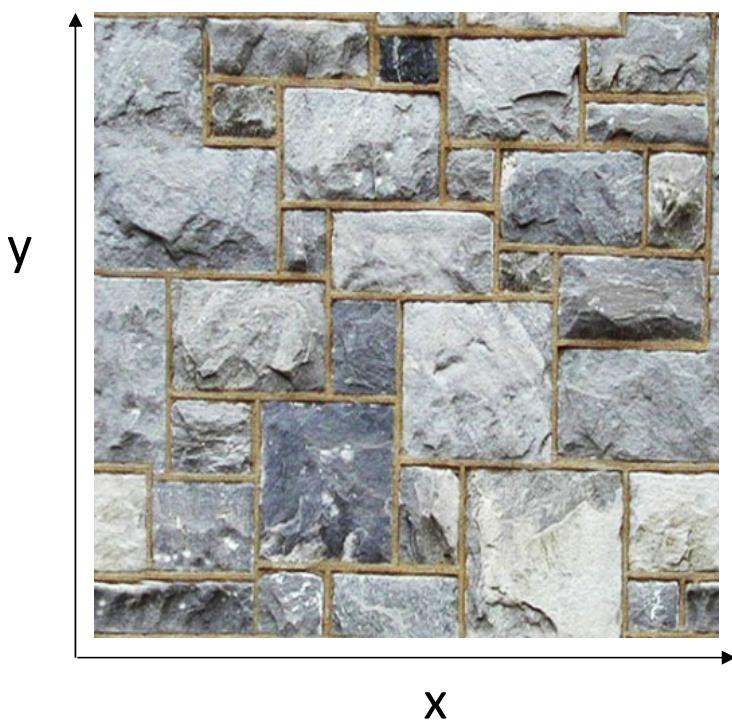


Mida d'una textura

- # texels en cada dimensió
- Habitualment w, h són potència de 2.

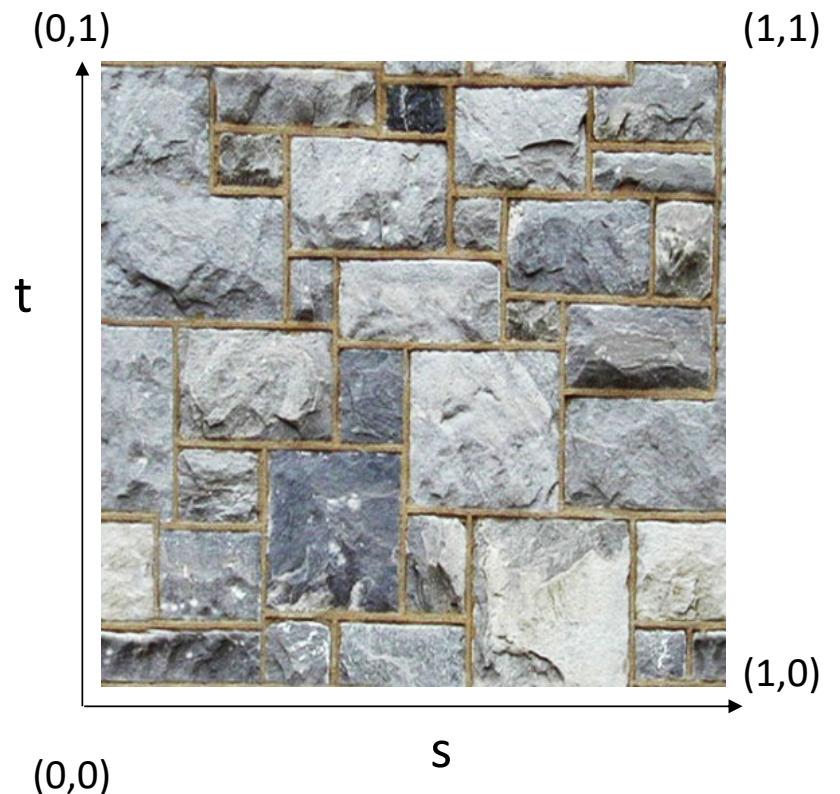


Espai normalitzat de textura



$$x \in [0, \text{width}]$$

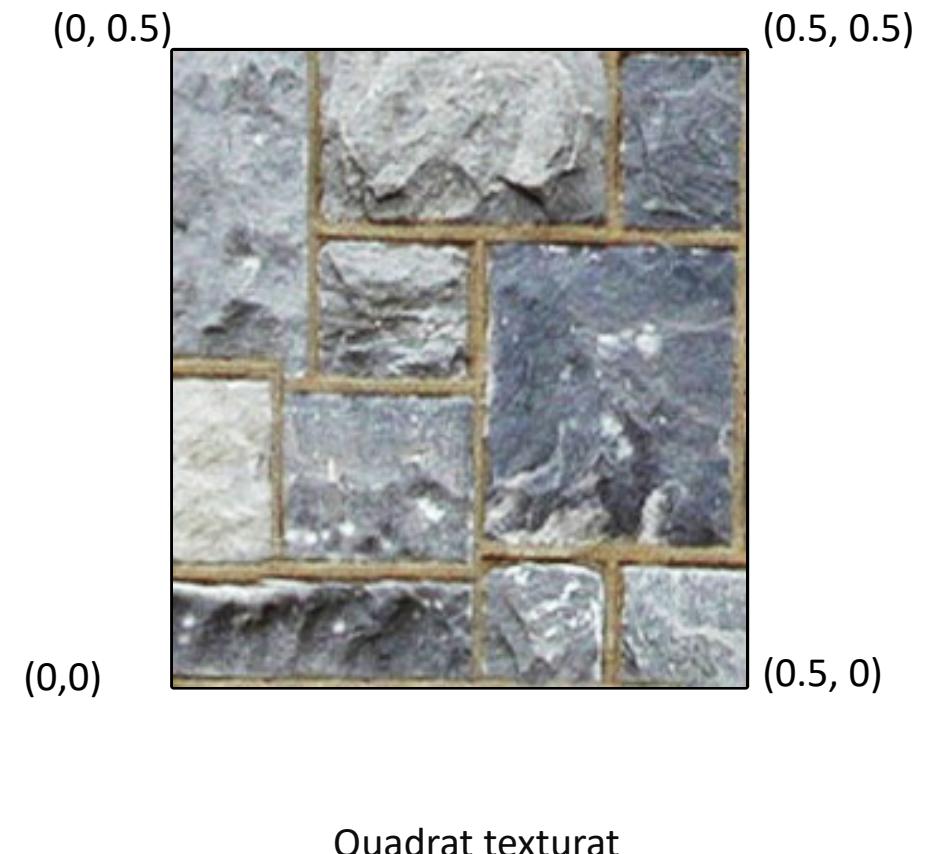
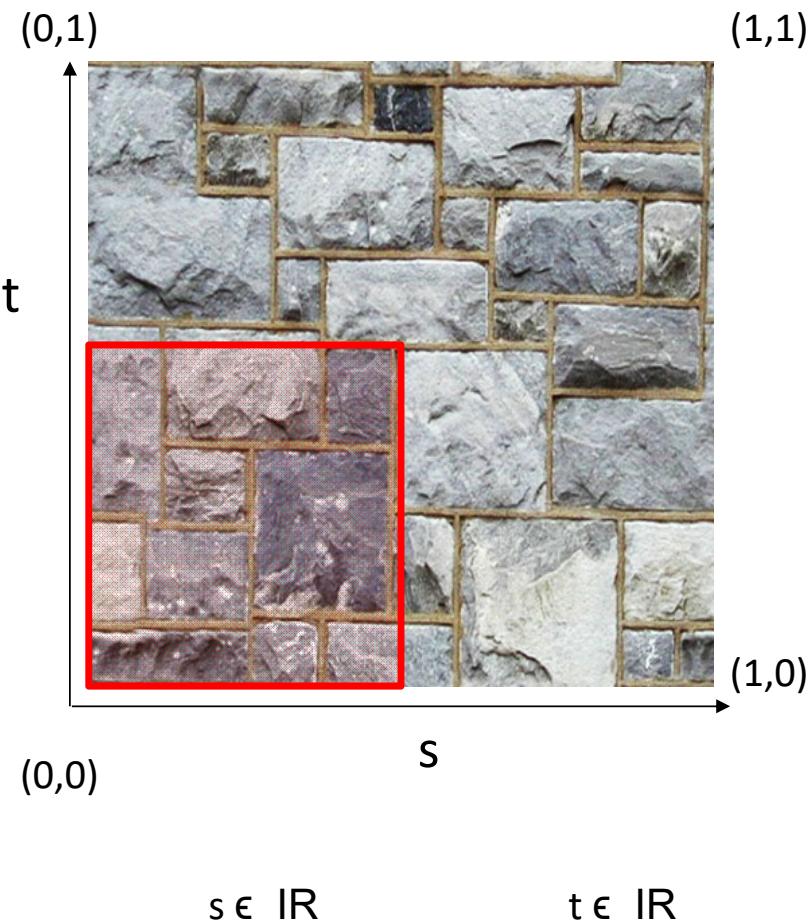
$$y \in [0, \text{height}]$$



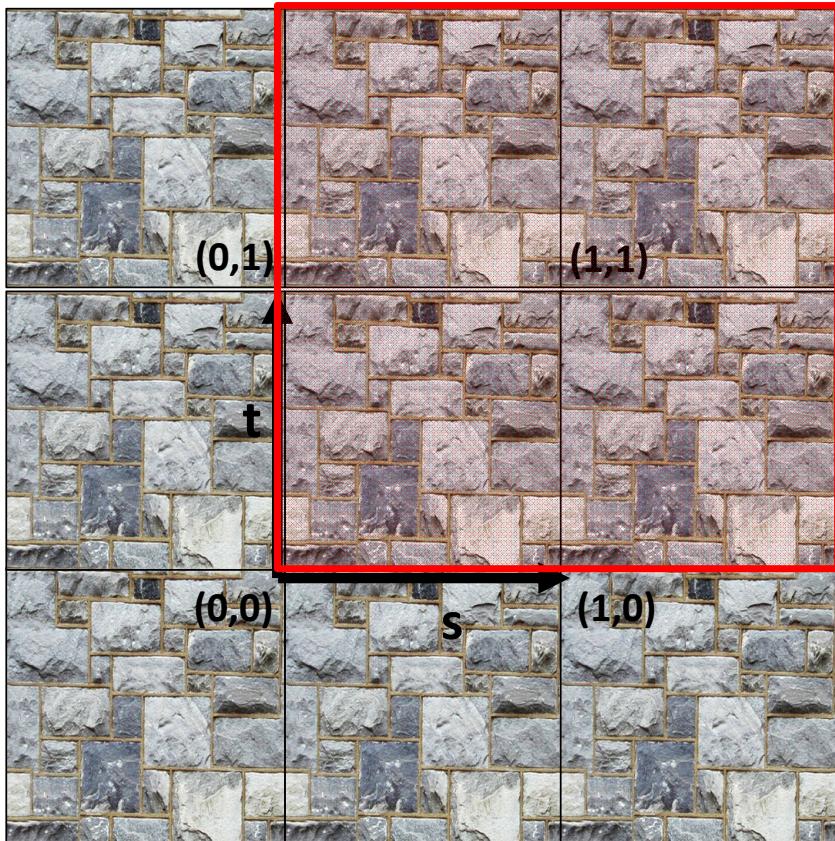
$$s \in \mathbb{R}$$

$$t \in \mathbb{R}$$

Espai normalitzat de textura



Espai normalitzat de textura



(0, 2)



(2, 2)

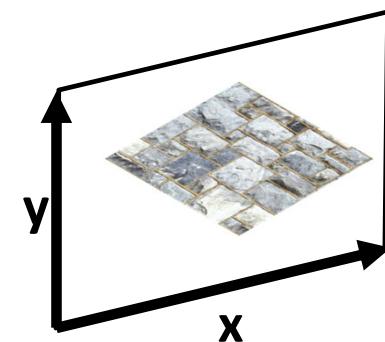
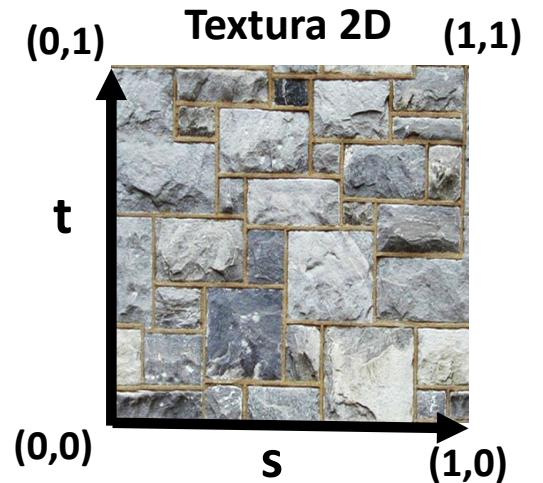
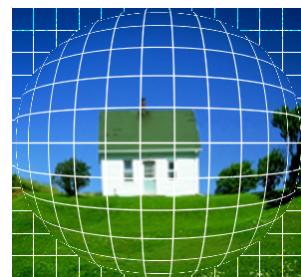
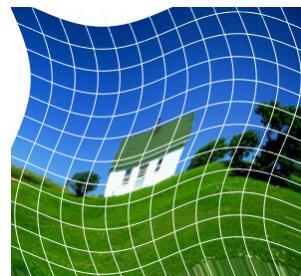
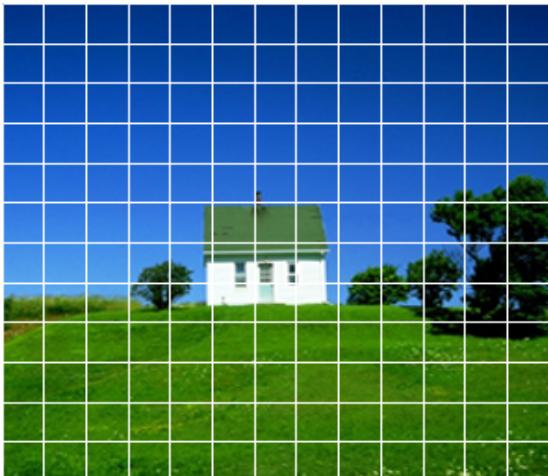
(2, 0)

Quadrat texturat

MAPPING

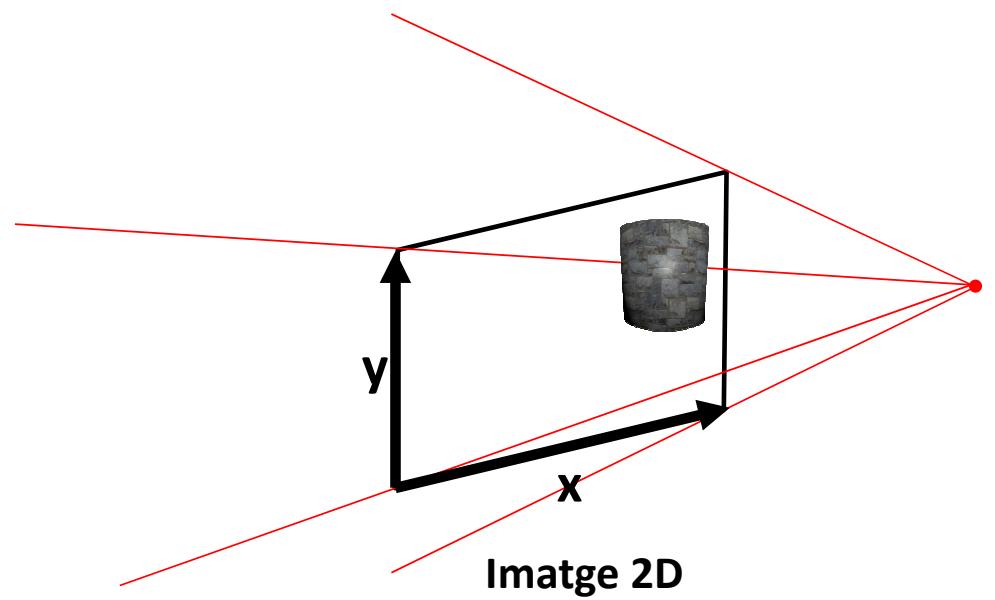
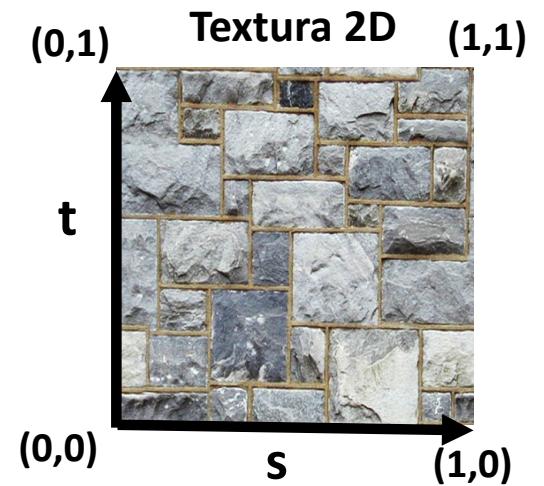


Forward / Inverse mapping



Imatge 2D

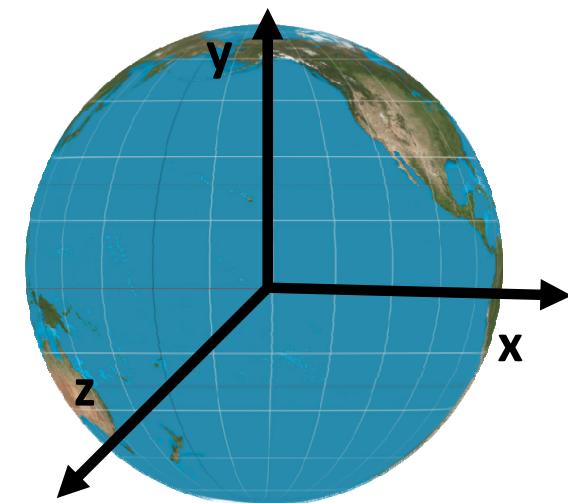
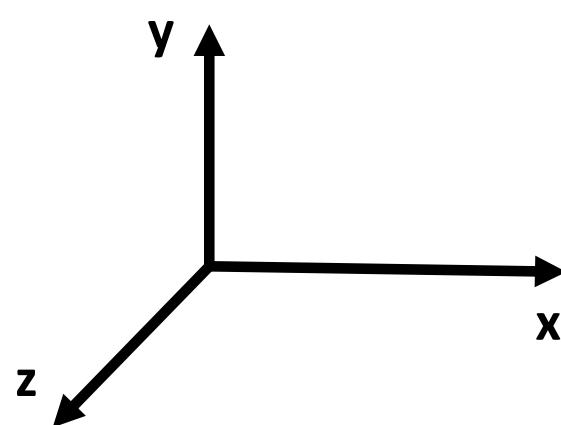
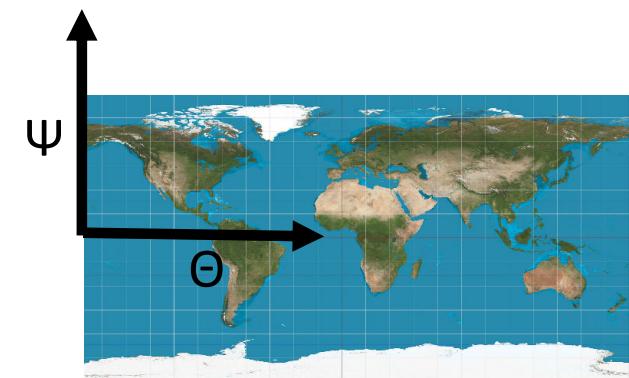
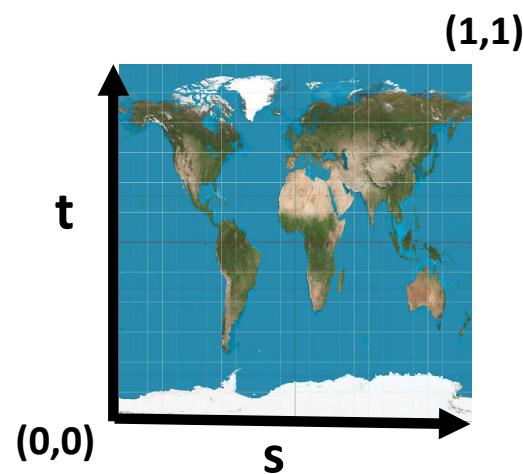
Forward / Inverse mapping



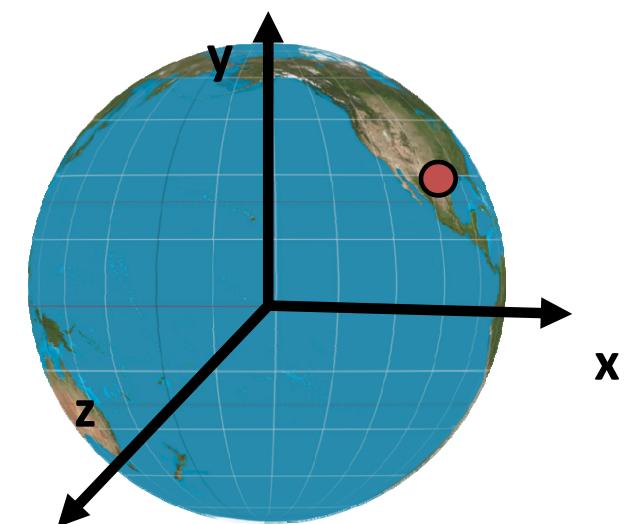
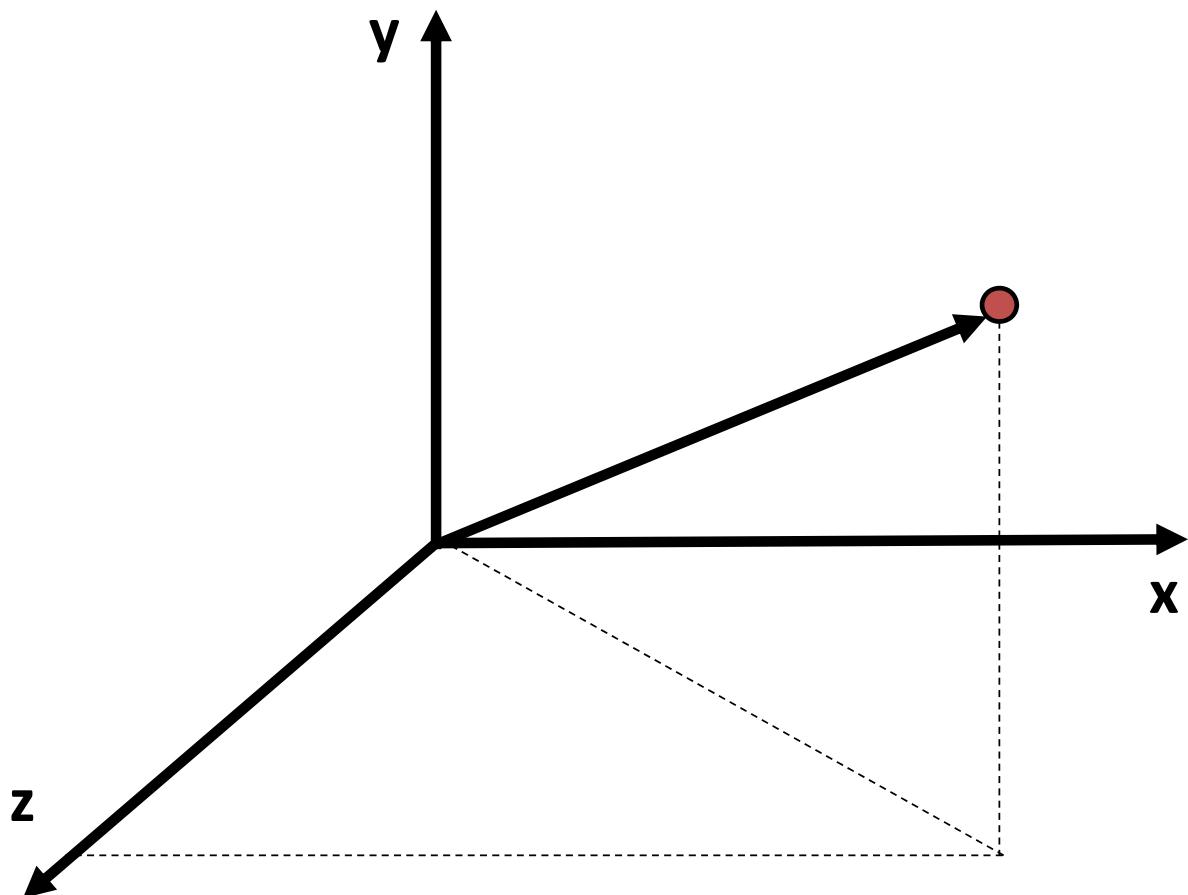
Exemple 1: Mapping esfèric

Input: $s \in [0,1]$, $t \in [0,1]$

Output: $x,y,z \in$ esfera unitat



Exemple 1: Mapping esfèric



Exemple 1: Mapping esfèric

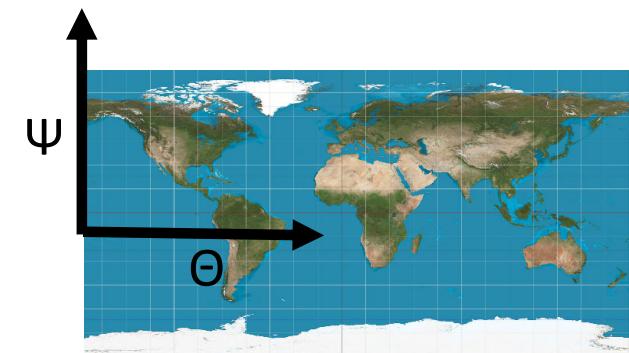
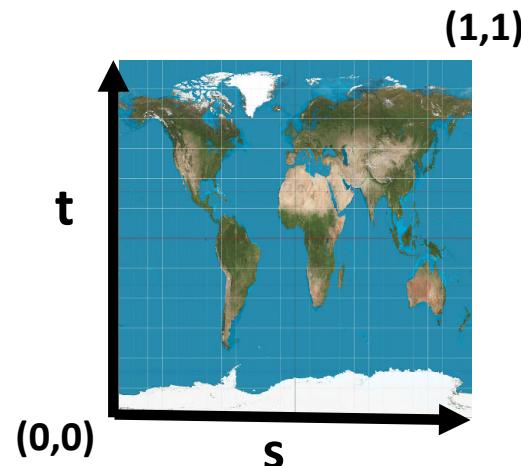
Input: $s \in [0,1]$, $t \in [0,1]$

Output: $x,y,z \in$ esfera unitat

// pas $(s, t) \rightarrow (\Theta, \Psi)$

$\Theta = 2\pi s;$

$\Psi = \pi(t-0.5);$

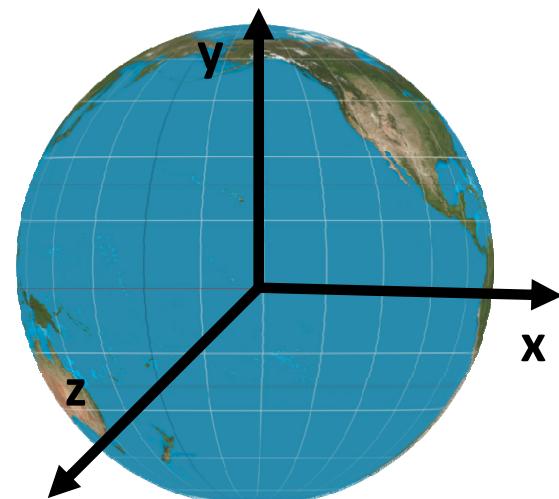


// pas esfèriques $\rightarrow (x,y,z)$

$x = \sin(\Theta)\cos(\Psi);$

$y = \sin(\Psi);$

$z = \cos(\Theta)\cos(\Psi);$



Exemple 2: Mapping cilíndric

Input: $s \in [0,1]$, $t \in [0,1]$

Output: $x,y,z \in$ cilindre $r=1$ sobre pla XZ

```
// pas (s, t) → (Θ, h)
```

```
Θ = 2πs;
```

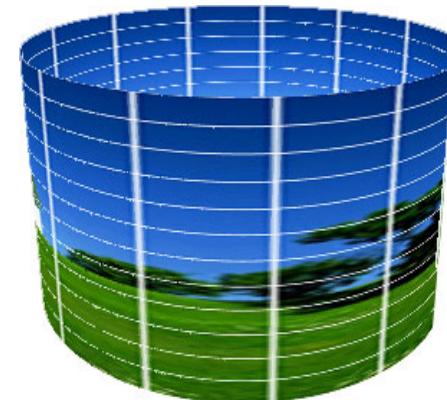
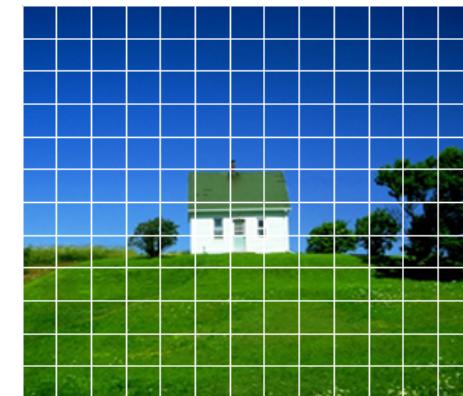
```
h = t;
```

```
// pas cilíndriques → (x,y,z)
```

```
x = sin(Θ);
```

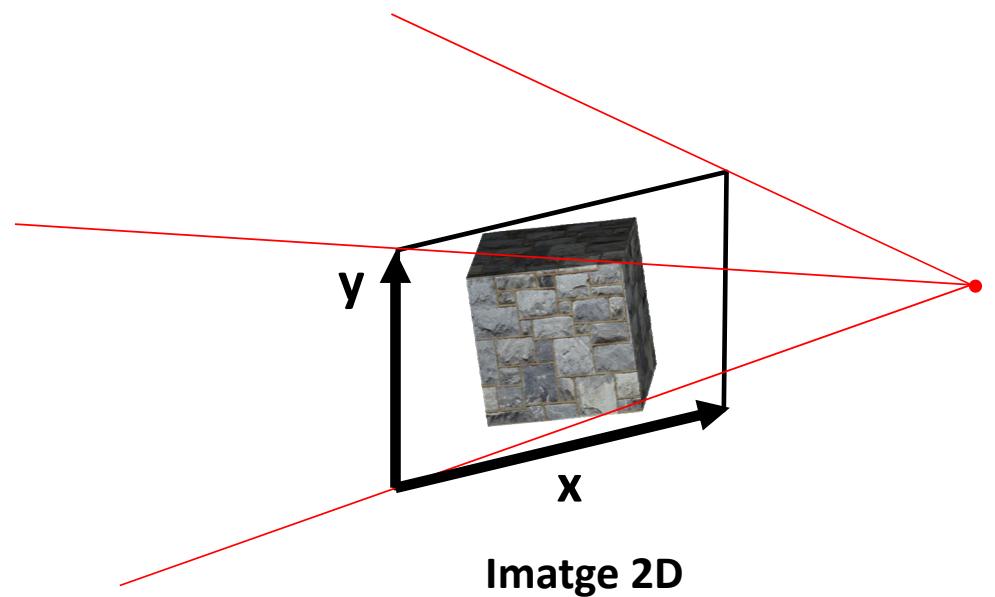
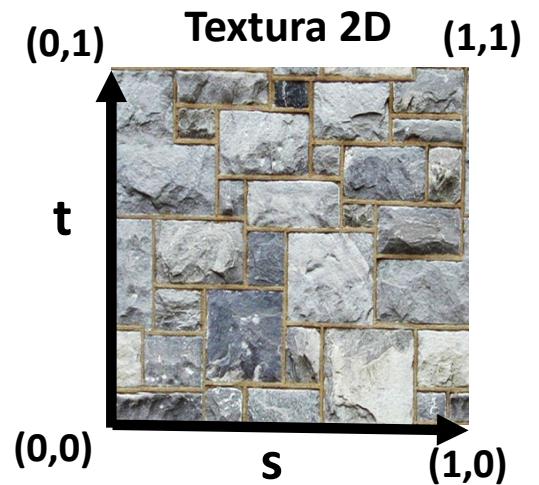
```
y = h;
```

```
z = cos(Θ);
```

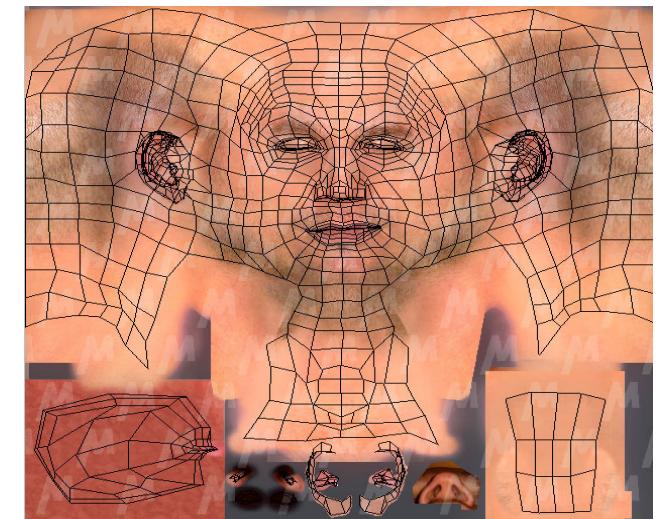
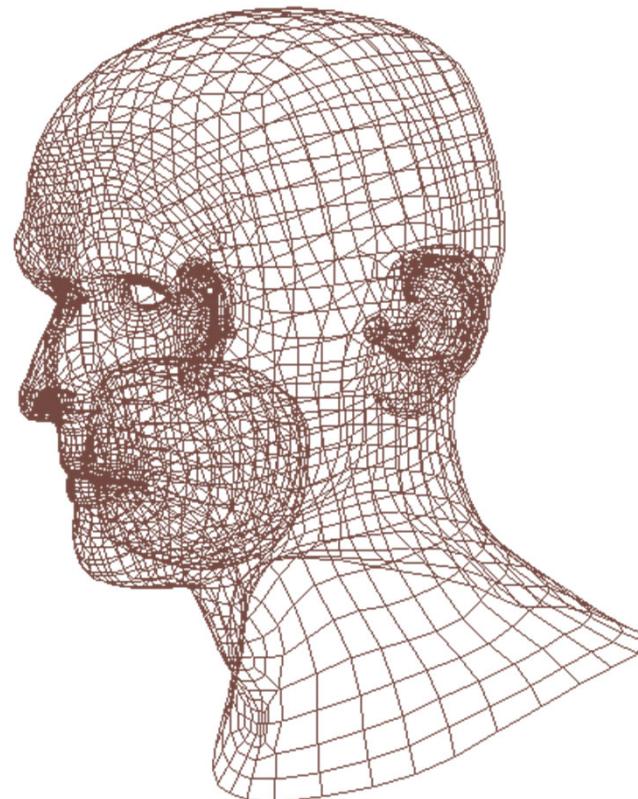


MAPPING EN OPENGL

En gràfics, habitualment



En gràfics, habitualment

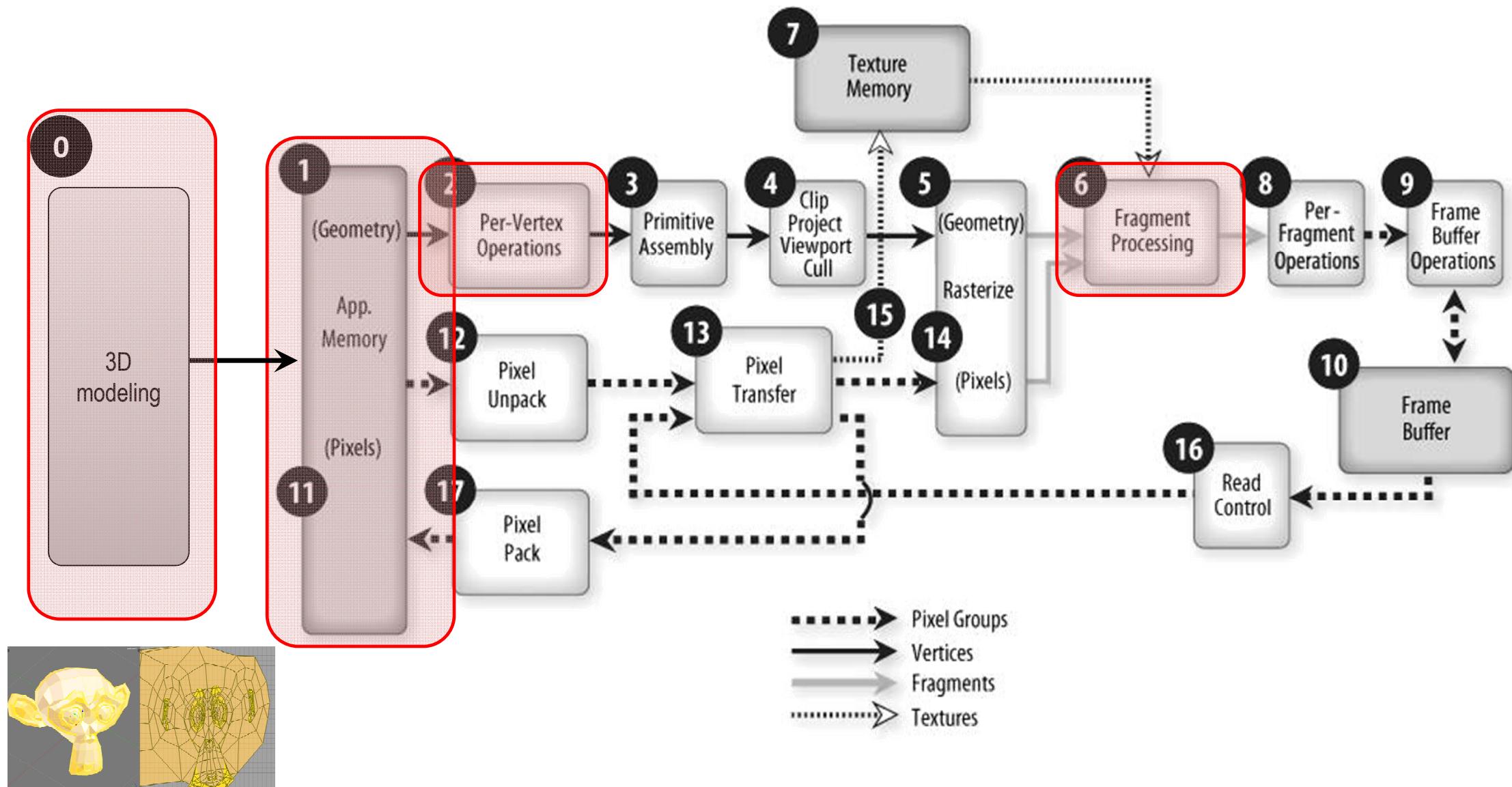


DEMO (TEXTURE MAPPING AMB BLENDER)

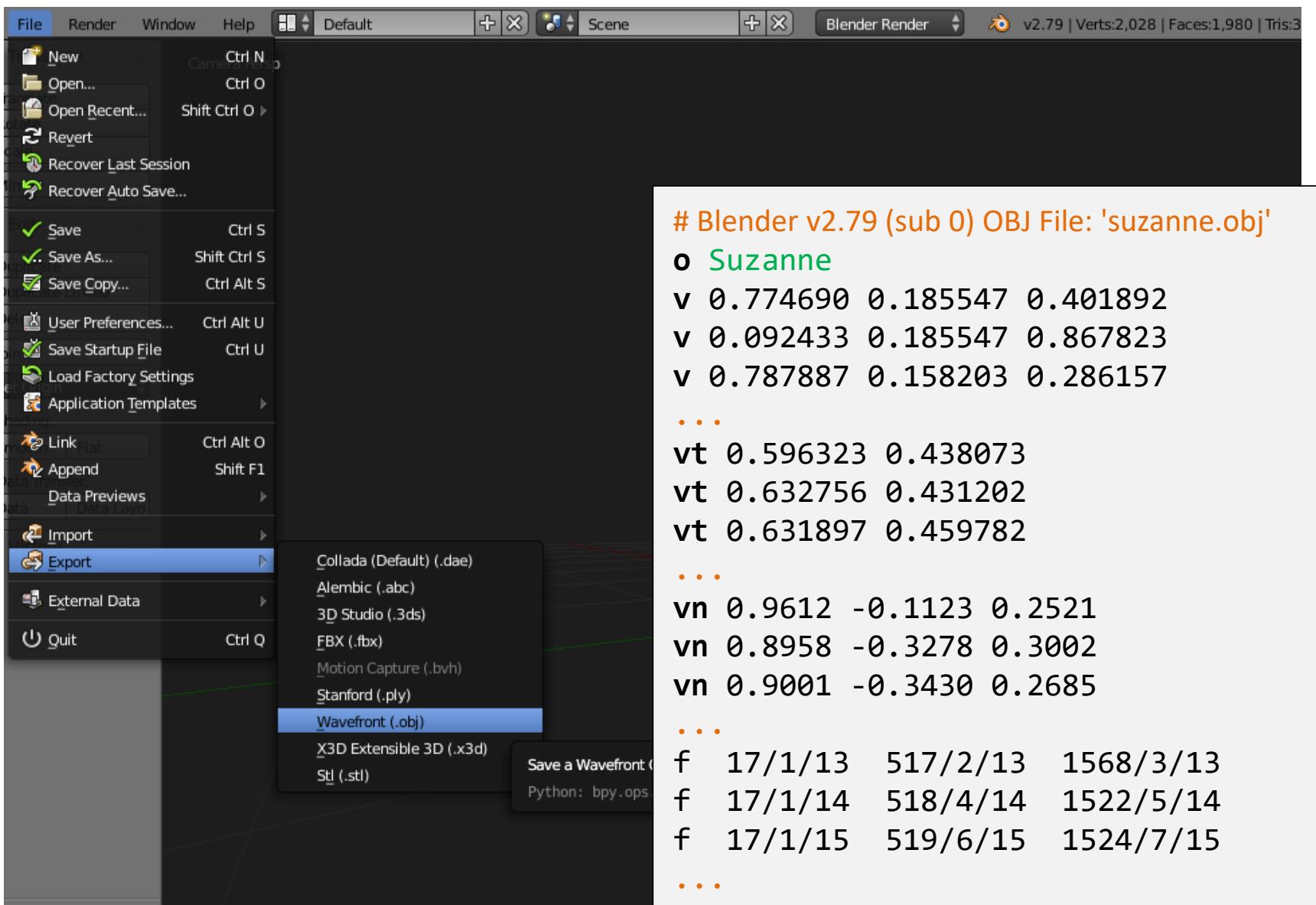
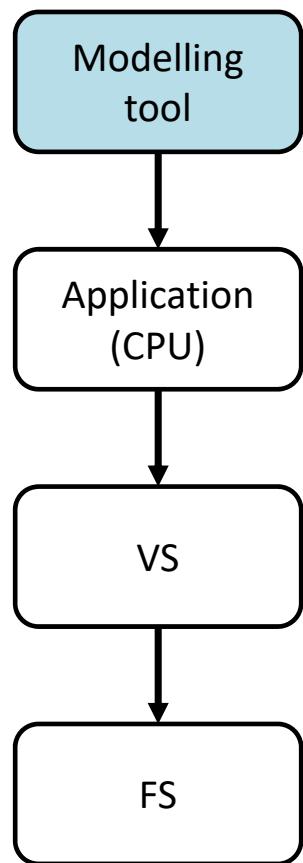
DEMO (TEXTURE MAPPING AMB OPENGL)

En quina etapa es generen les coordenades de textura?

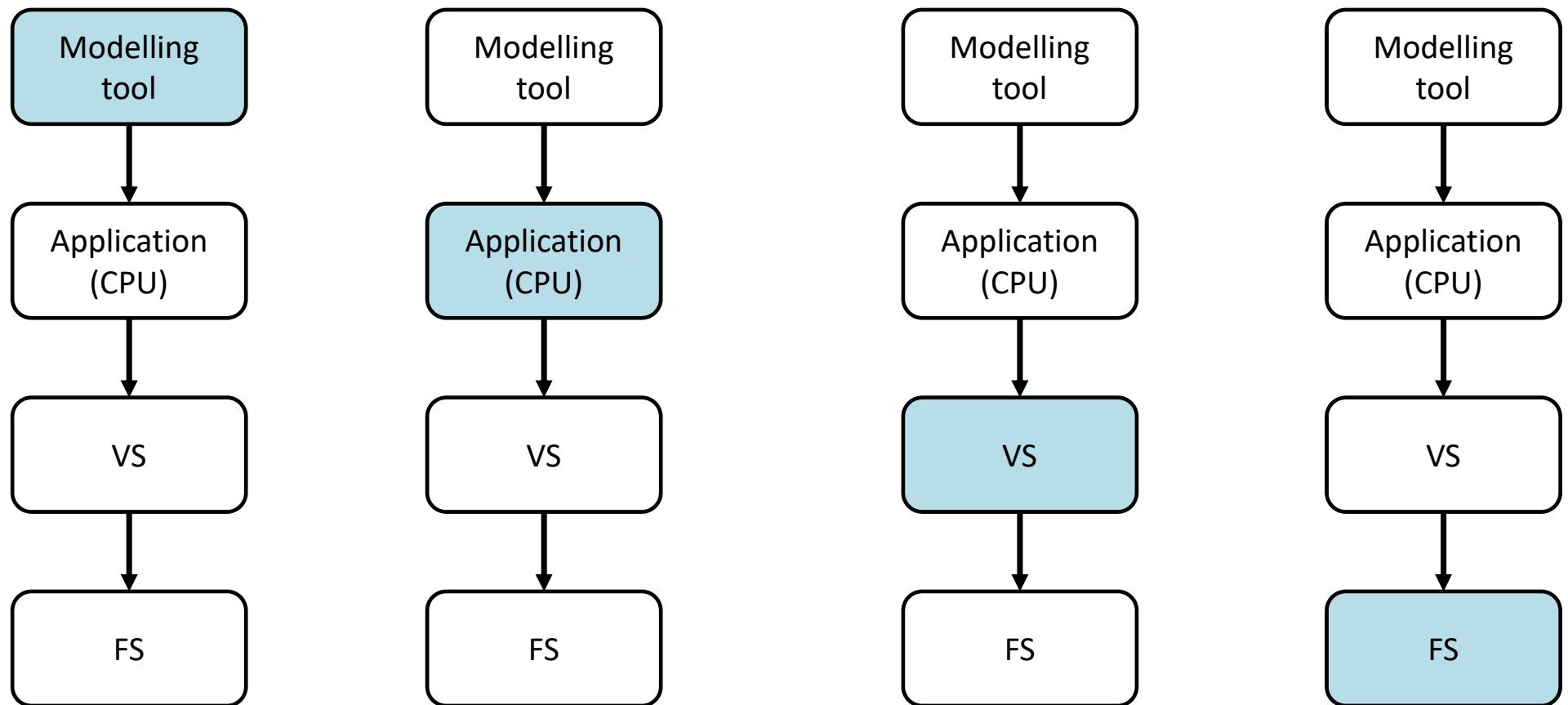
COORDENADES DE TEXTURA AL PIPELINE



Opcion



Opcions per a generar coords de textura



MÈTODES PER GENERAR COORDS DE TEXTURA

Generació de coordenades de textura

- Bàsics
 - Amb plans S, T
 - Amb superfície auxiliar (S-mapping, O-mapping)
- Avançats (mesh parameterization)
 - Mesh partition
 - Area-preserving, Angle-preserving, Stretch-preserving...

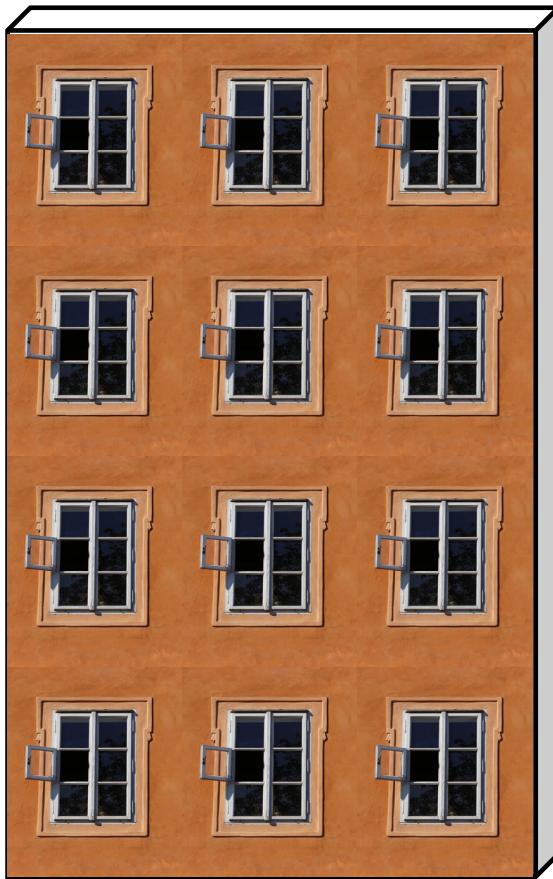
Plans S,T

Paràmetres:

- plans S,T

Càlcul s, t:

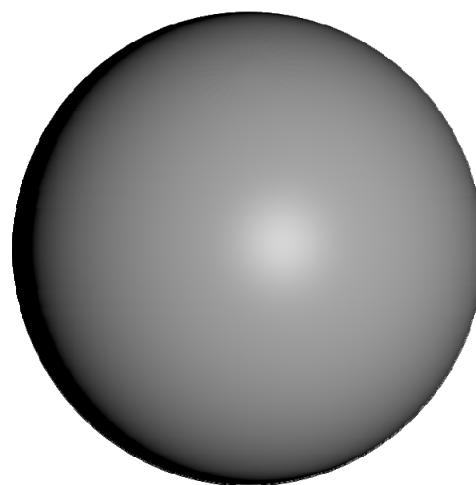
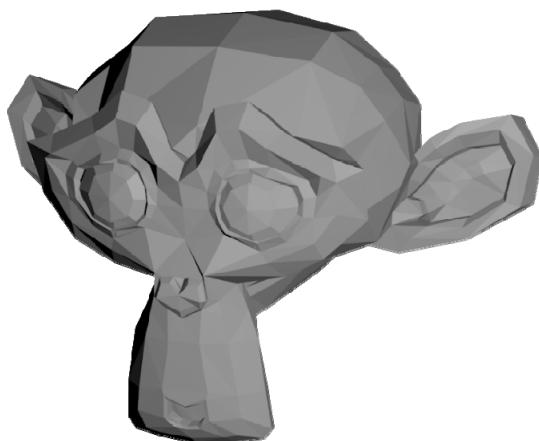
Plans S,T (exemple)



Generació de coordenades de textura

- Bàsics
 - Amb plans S, T
 - Amb superfície auxiliar (S-mapping, O-mapping)
- Avançats (mesh parameterization)
 - Mesh partition
 - Area-preserving, Angle-preserving, Stretch-preserving...

Parametrització amb superfície auxiliar



H1	H2	H3	H4	H5	H6	H7	H8
G1	G2	G3	G4	G5	G6	G7	G8
F1	F2	F3	F4	F5	F6	F7	F8
E1	E2	E3	E4	E5	E6	E7	E8
D1	D2	D3	D4	D5	D6	D7	D8
C1	C2	C3	C4	C5	C6	C7	C8
B1	B2	B3	B4	B5	B6	B7	B8
A1	A2	A3	A4	A5	A6	A7	A8



Exemples: S^{-1} mappings

Input: $s \in [0,1]$, $t \in [0,1]$

Output: $x,y,z \in$ esfera unitat

```
// pas (s, t) → (θ, ψ)
```

```
θ = 2πs;
```

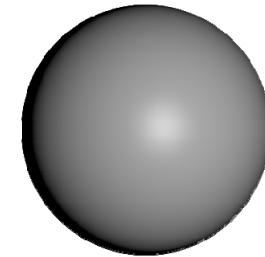
```
ψ = π(t-0.5);
```

```
// pas esfèriques → (x,y,z)
```

```
x = sin(θ)cos(ψ);
```

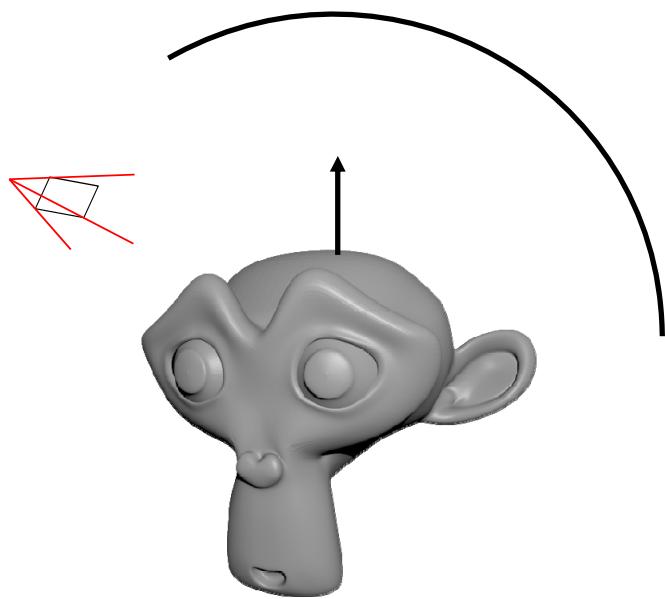
```
y = sin(ψ);
```

```
z = cos(θ)cos(ψ);
```

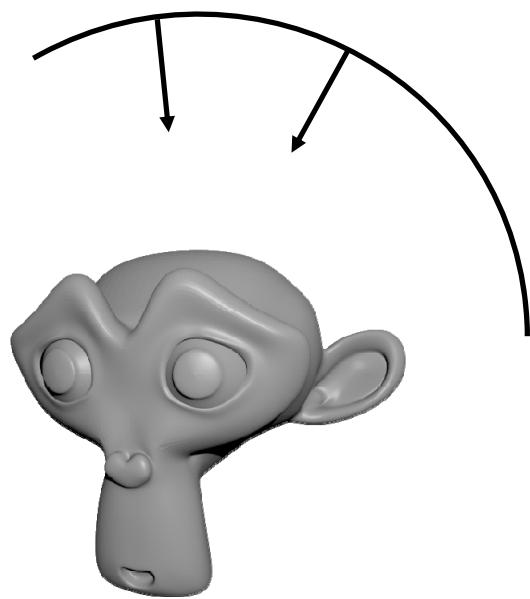


H1	H2	H3	H4	H5	H6	H7	H8
G1	G2	G3	G4	G5	G6	G7	G8
F1	F2	F3	F4	F5	F6	F7	F8
E1	E2	E3	E4	E5	E6	E7	E8
D1	D2	D3	D4	D5	D6	D7	D8
C1	C2	C3	C4	C5	C6	C7	C8
B1	B2	B3	B4	B5	B6	B7	B8
A1	A2	A3	A4	A5	A6	A7	A8

Exemples: O mappings

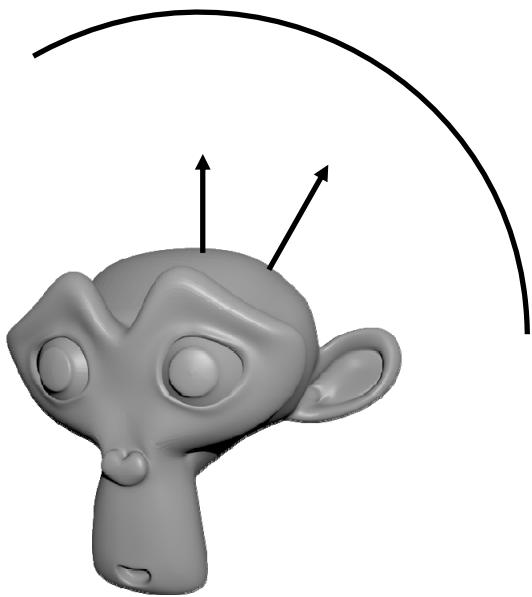


Reflected view ray

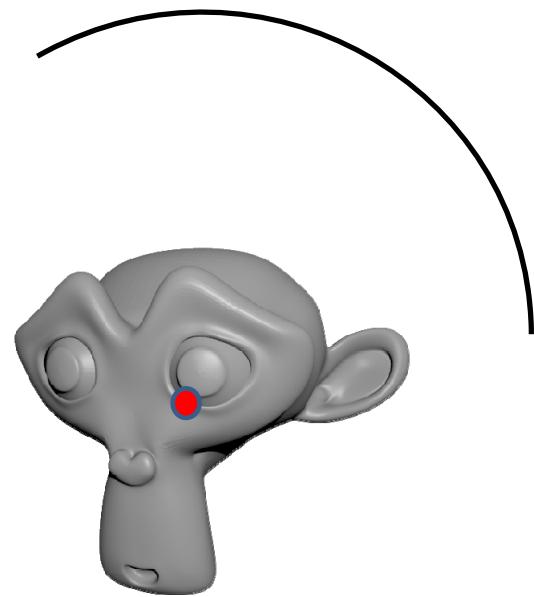


Intermediate surface normal

Exemples: O mappings

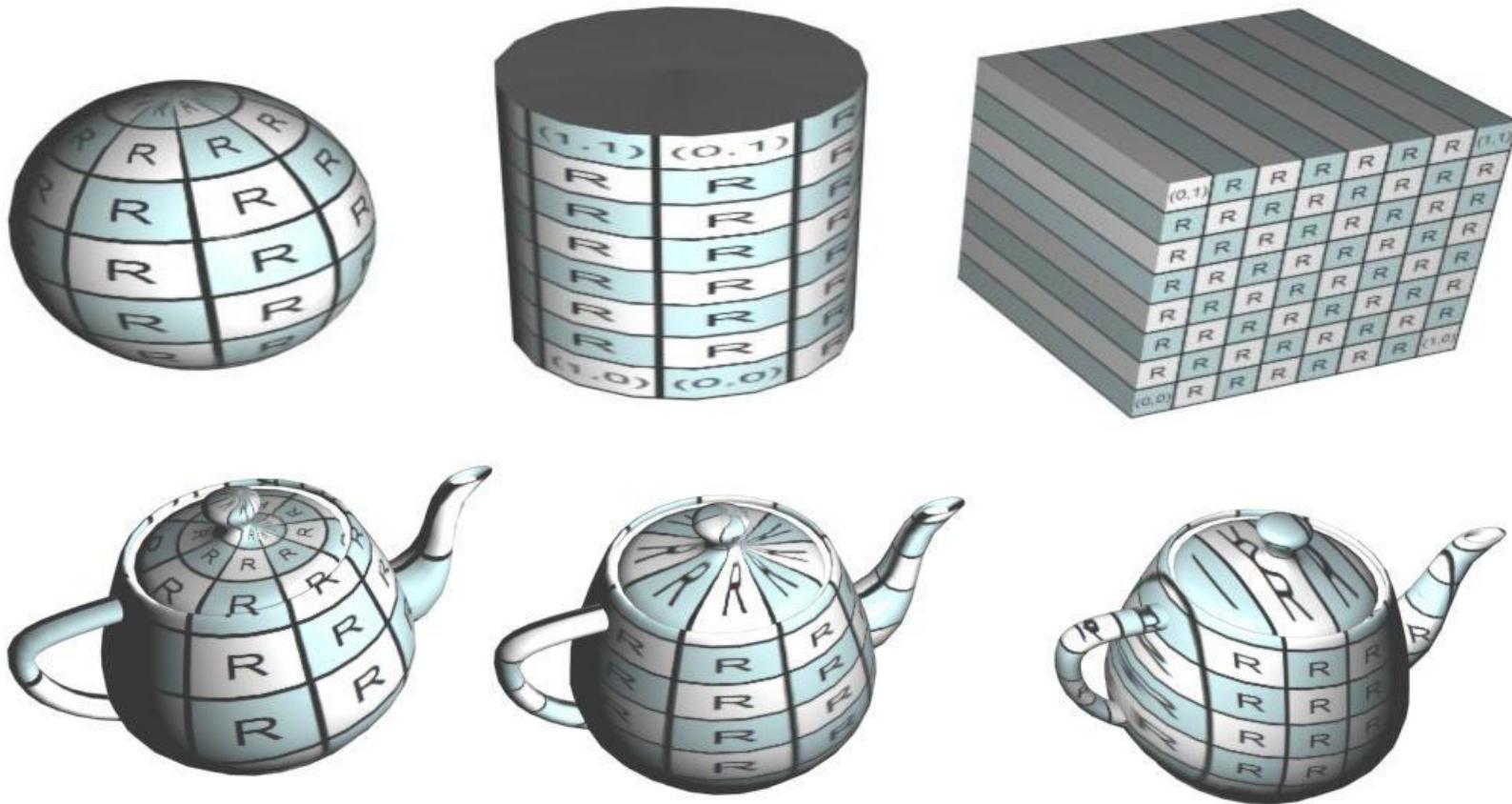


Object Normal

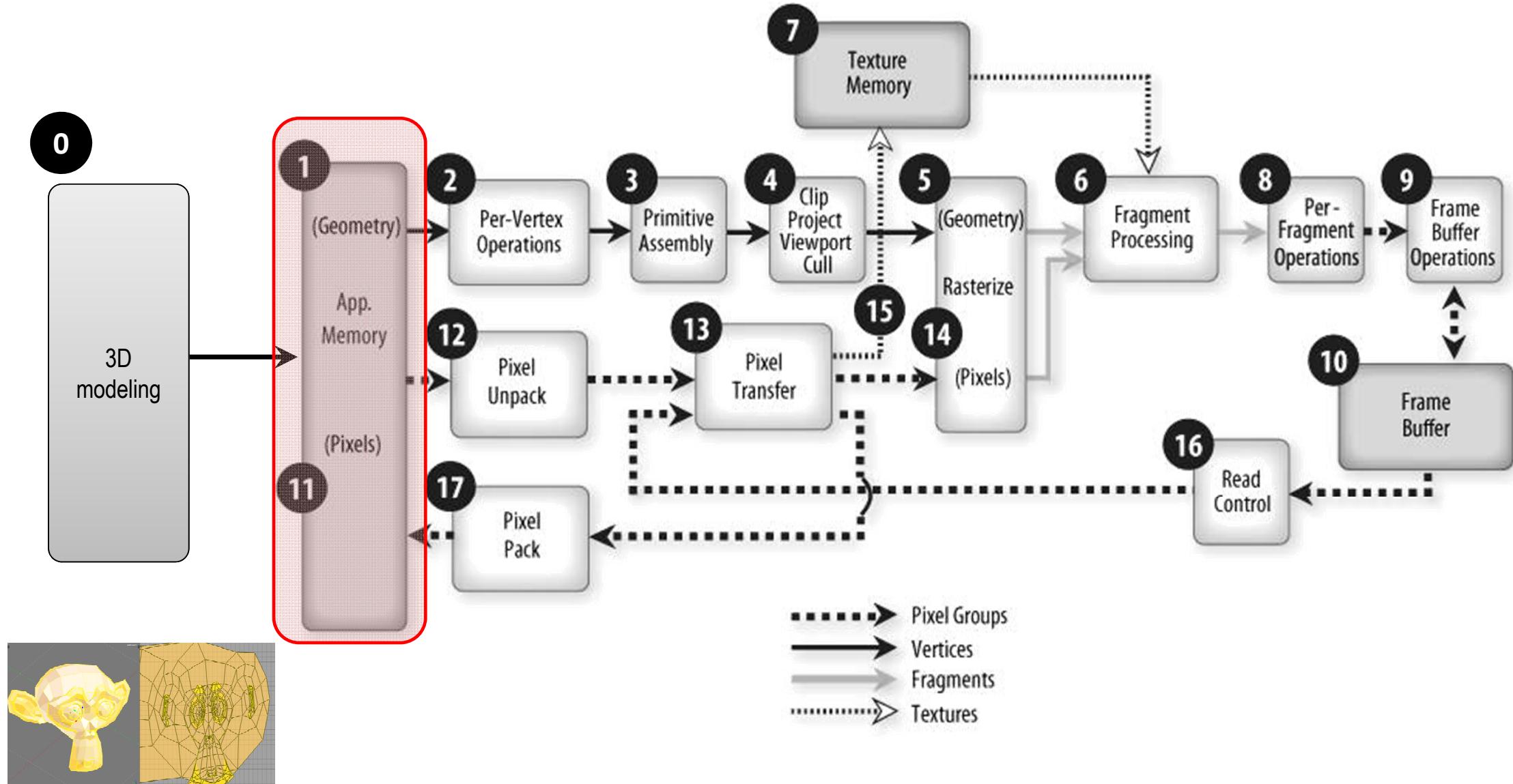


Object centroid

Projeccions esfèrica, cilíndrica i plana

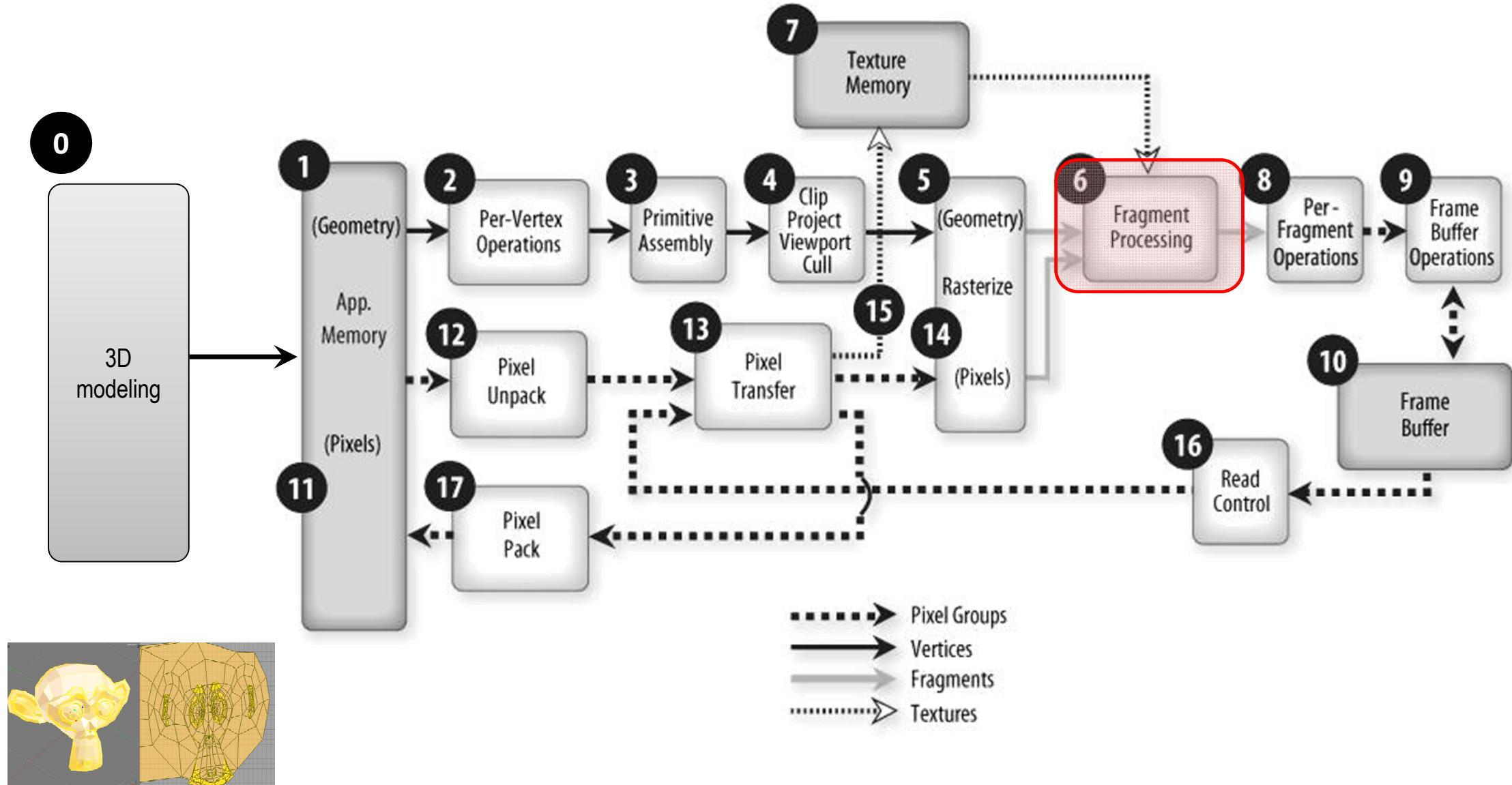


CREACIÓ DE LA TEXTURA



```
// Load Texture (once)
QImage img0("fieldstone.png");
QImage T = img0.convertToFormat(QImage::Format_ARGB32);
glGenTextures( 1, &textureId0);
glBindTexture(GL_TEXTURE_2D, textureId0);
glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, T.width(), T.height(), 0,
             GL_RGBA, GL_UNSIGNED_BYTE, T.bits());
...
// Bind textures, set uniforms...
g.glActiveTexture(GL_TEXTURE0);
g glBindTexture(GL_TEXTURE_2D, textureId0);
program->bind();
program->setUniformValue("colorMap", 0);
...
```

ÚS DE TEXTURA AL FRAGMENT SHADER



FS – exemple

```
uniform sampler2D colorMap;  
in vec2 vtexcoord;
```

...

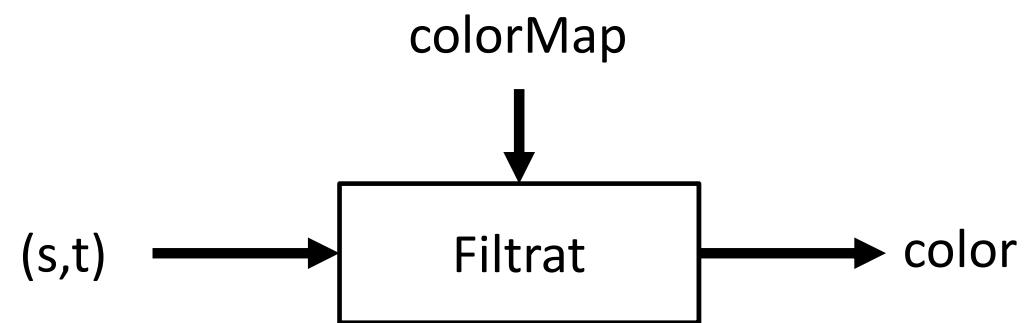
```
vec4 color = texture(colorMap, vtexcoord);
```

...

Magnification filters, Minification filters, Mipmapping

FILTRAT

Accés a textura



Necessitat del filtrat



Objeto texturado



Textura

Necessitat del filtrat



Textura



Magnification \approx upsampling

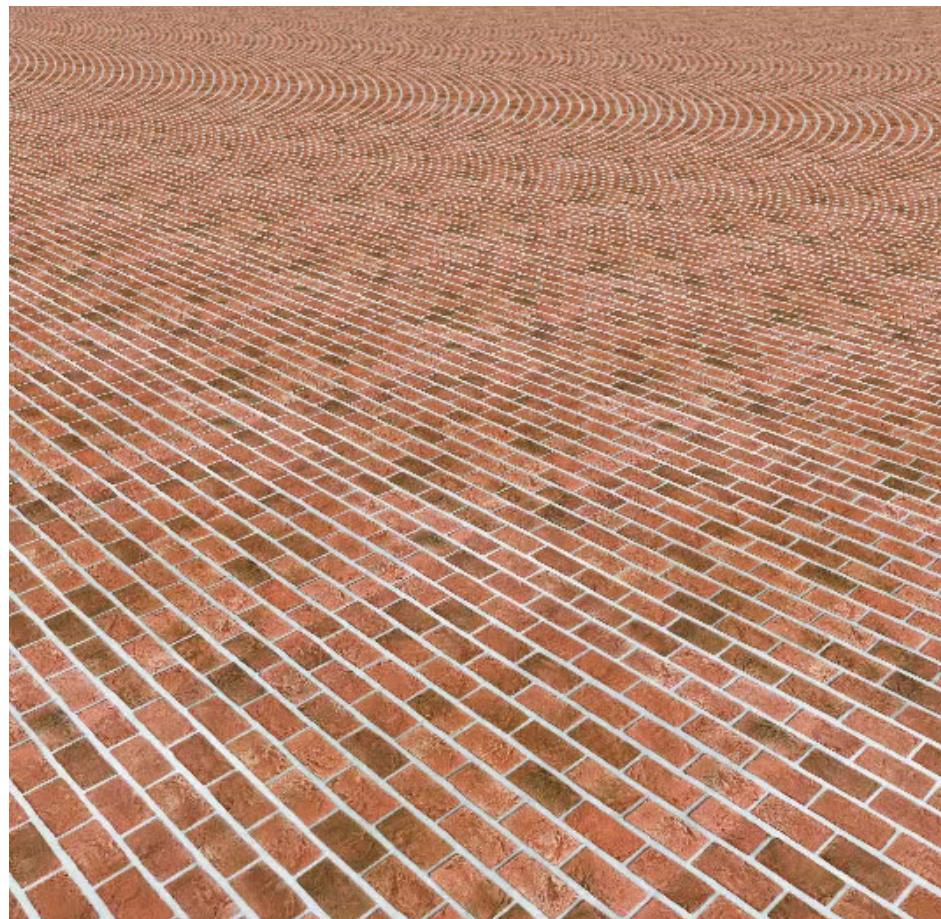


Minification \approx downsampling

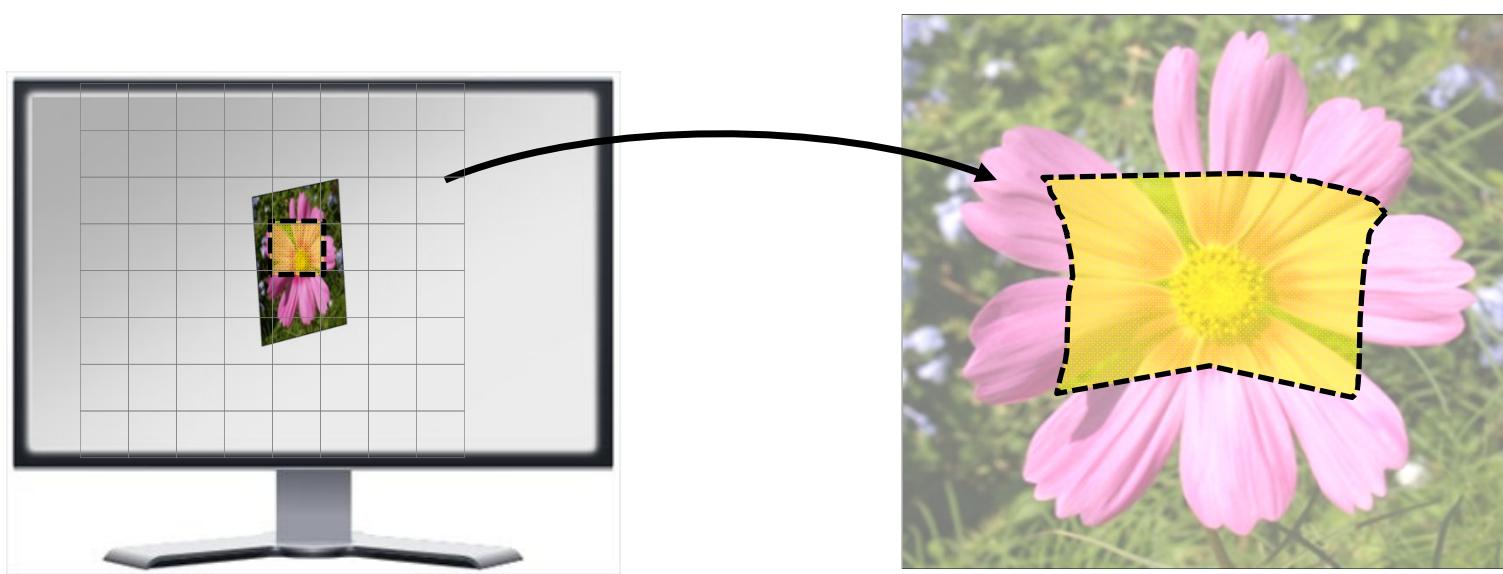
Magnification (naïve)



Minification (naïve)

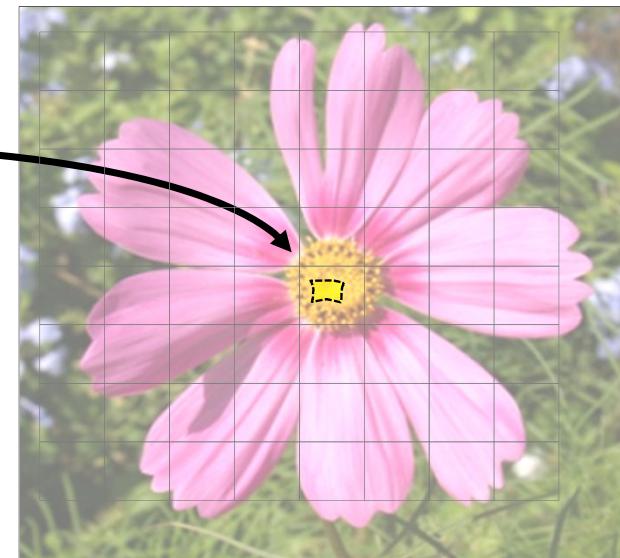
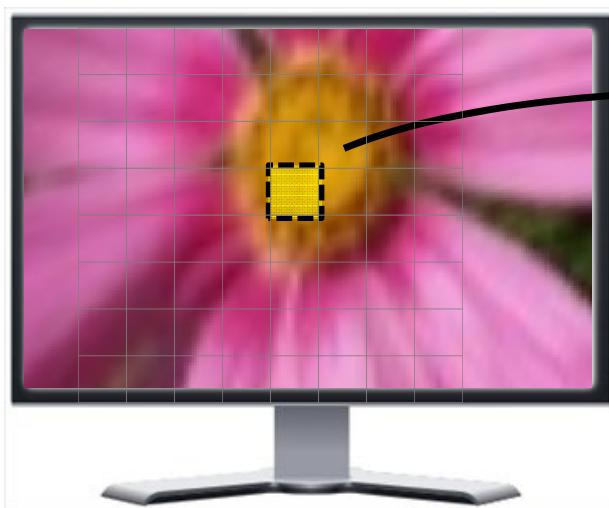


Preimatge d'un fragment



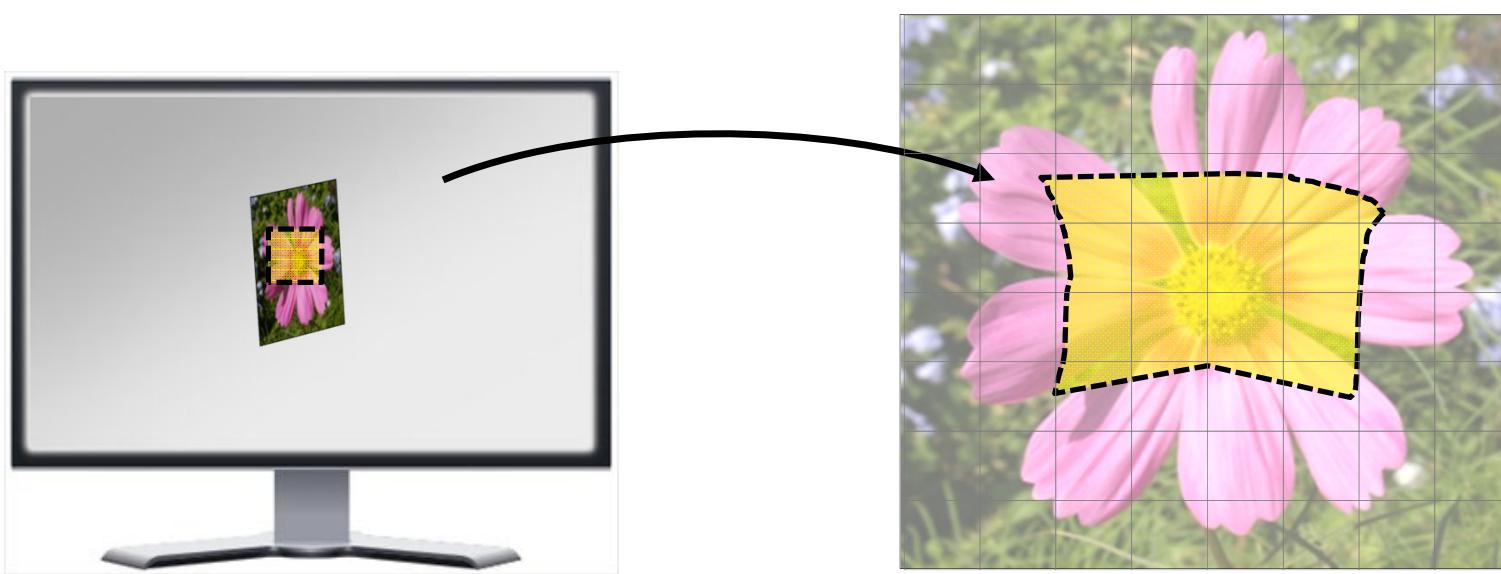
Ideal: color d'un pixel → color de la seva *preimatge* a la textura

Magnification



Magnification → la preimatge és < texel

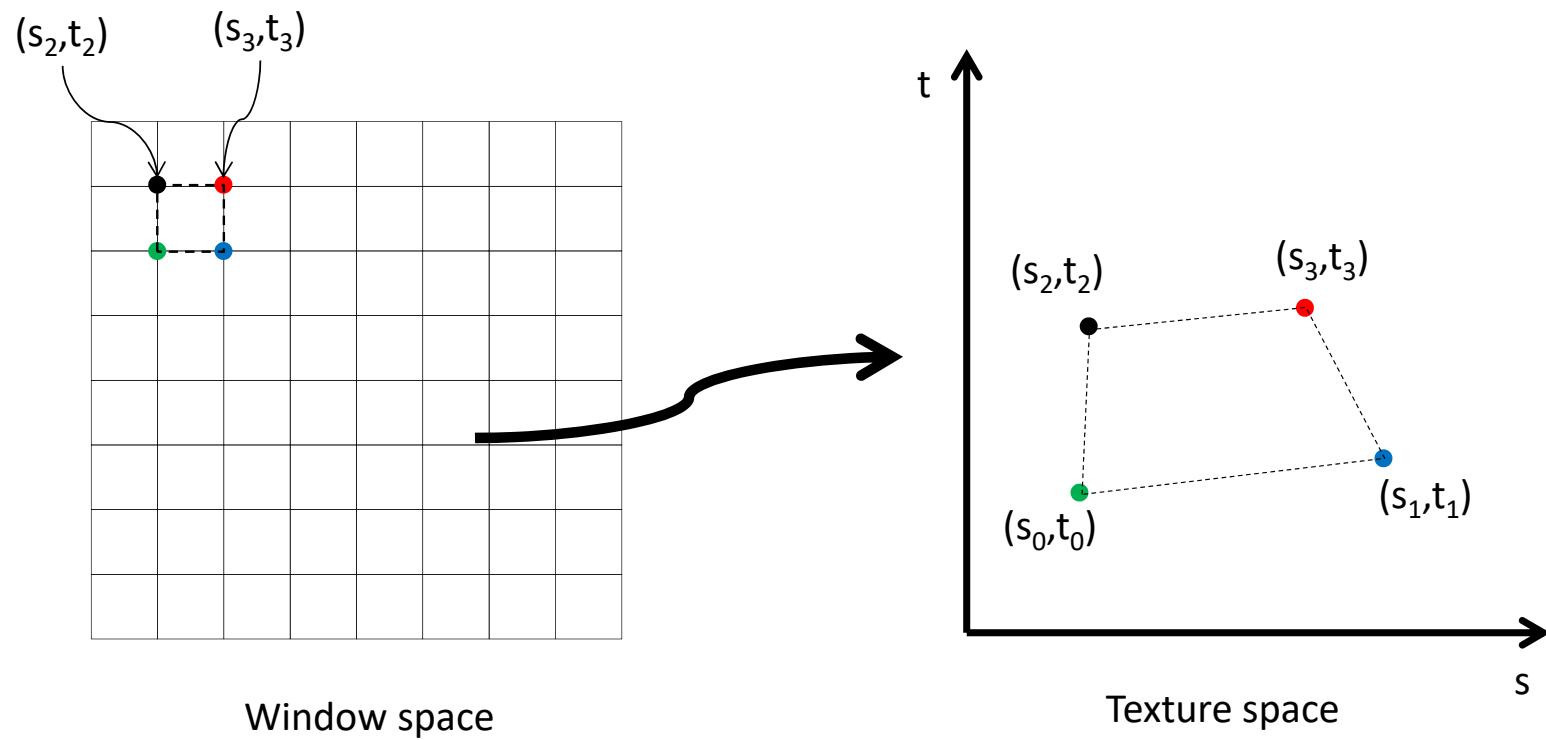
Minification



Minification → la preimatge és > texel

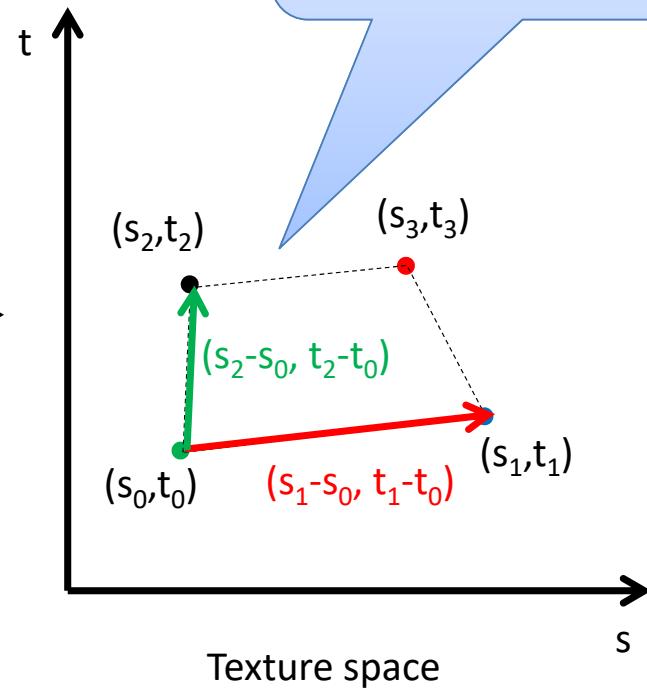
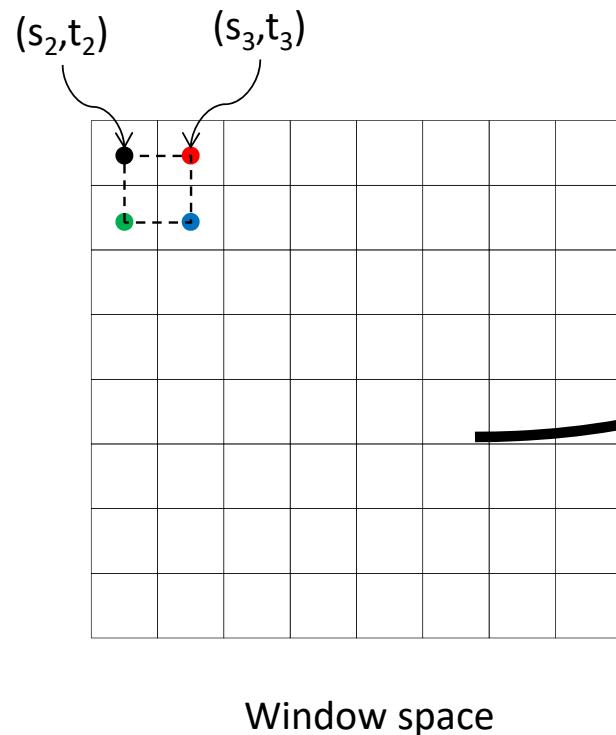
MAGNIFICATION O MINIFICATION?

Idealment



Aproximació que fa OpenGL

Usem les coords (s, t) del centre de cada fragment



Aproximació que fa OpenGL

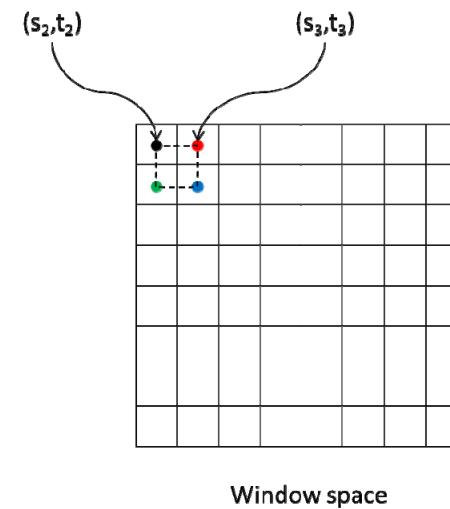
- Siguin $s(x,y)$, $t(x,y)$ les coordenades s,t del fragment (x,y)
- Derivades parcials de $s(x,y)$:

$$\begin{aligned}\frac{\partial s}{\partial x} &\approx s(x+1, y) - s(x, y) \\ \frac{\partial s}{\partial y} &\approx s(x, y+1) - s(x, y)\end{aligned}$$

- En GLSL es poden calcular amb $dFdx$, $dFdy$:

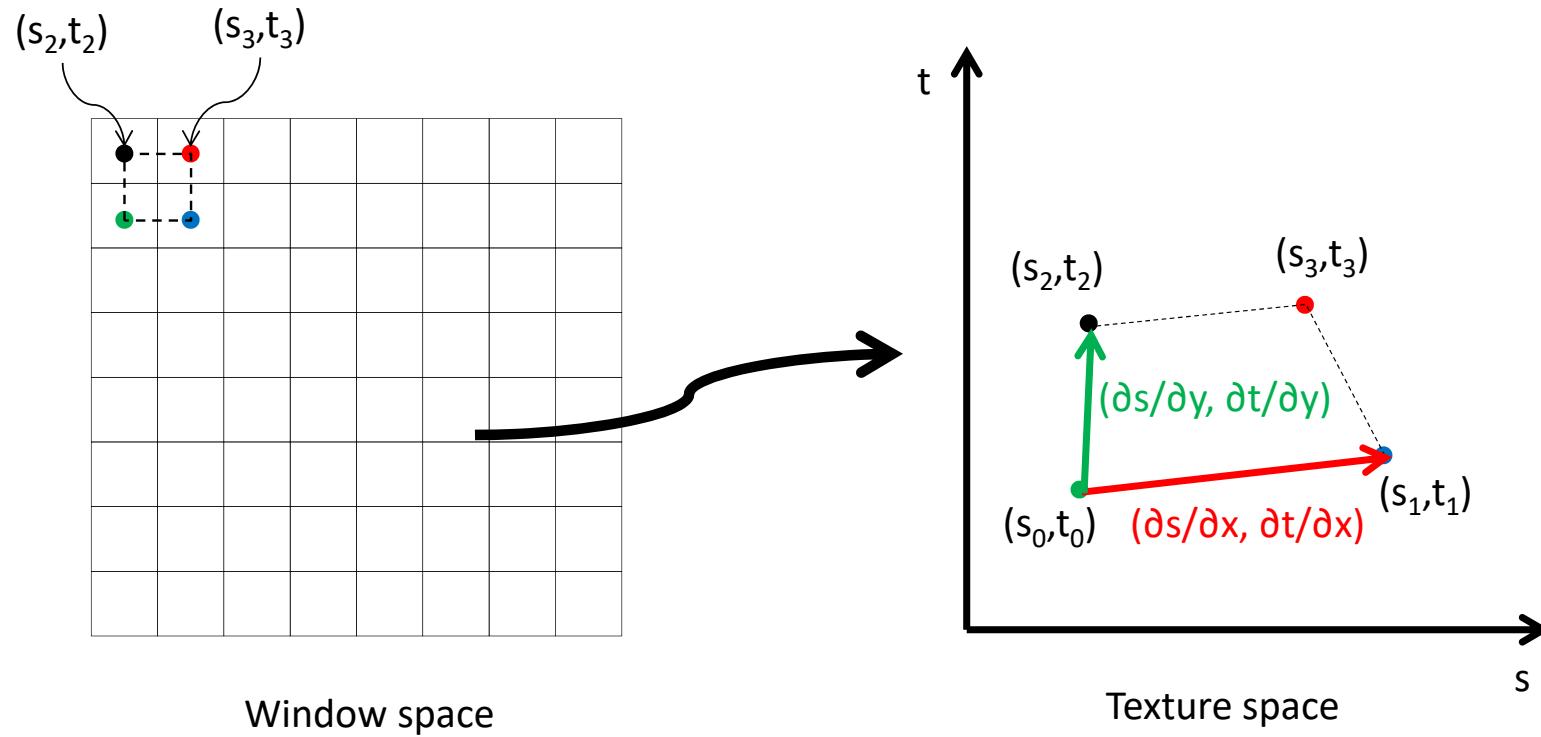
$$\begin{aligned}\frac{\partial s}{\partial x} &\approx dFdx(\text{texCoord}.s) \\ \frac{\partial s}{\partial y} &\approx dFdy(\text{texCoord}.s)\end{aligned}$$

(anàlogament per t)



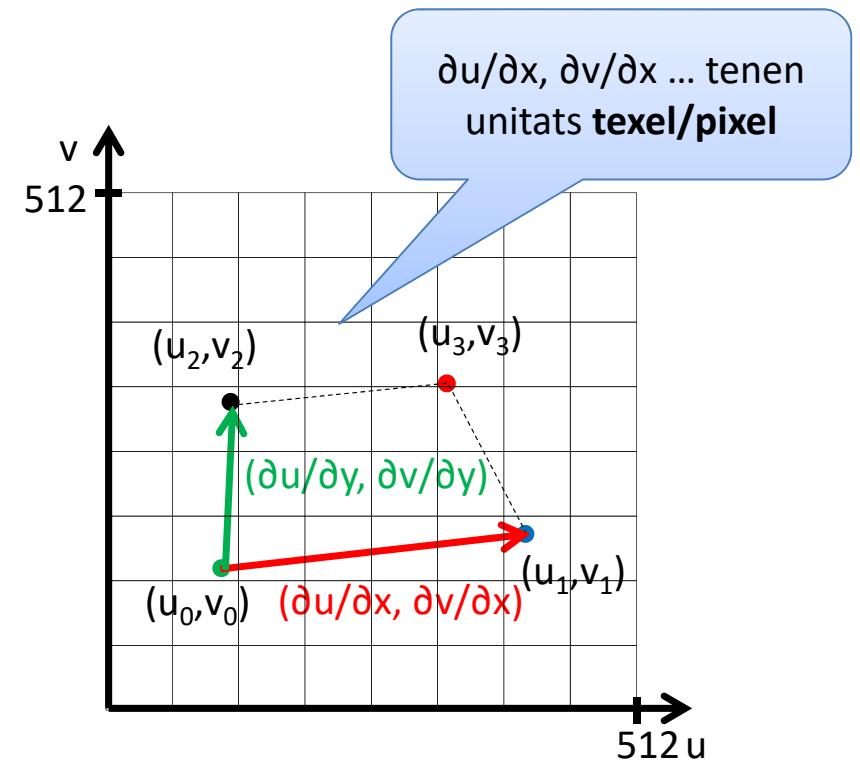
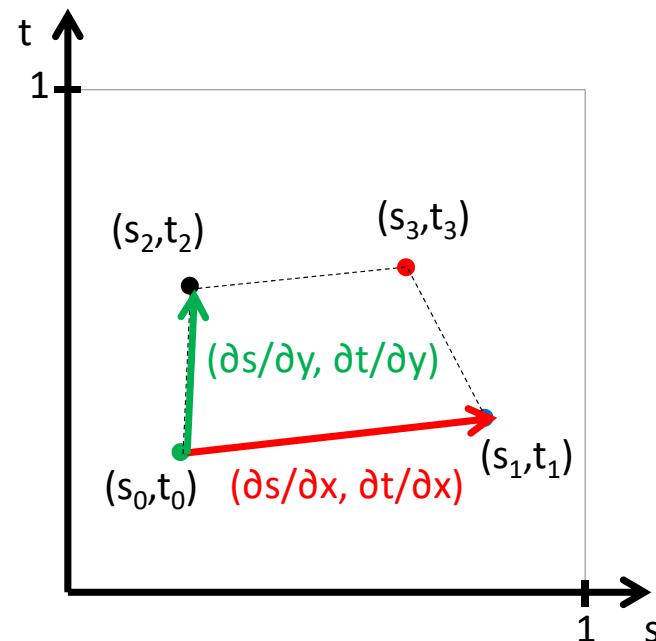
Aproximació que fa OpenGL

Aproximació de la mida de la pre-imatge (**en espai normalitzat de textura**)



Aproximació que fa OpenGL

Mida de la pre-imatge (**en texels**) amb una textura 512x512



Exemple 1 (mapping 1:1)



Polígon projectat en WxH pixels



Textura WxH texels

En aquest cas un pixel correspon a un texel:

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} = 1 \quad \frac{\partial v}{\partial x} = \frac{\partial u}{\partial y} = 0$$

Exemple 2 (magnification x2)



Fragments veïns
tenen coordenades
(u,v) properes

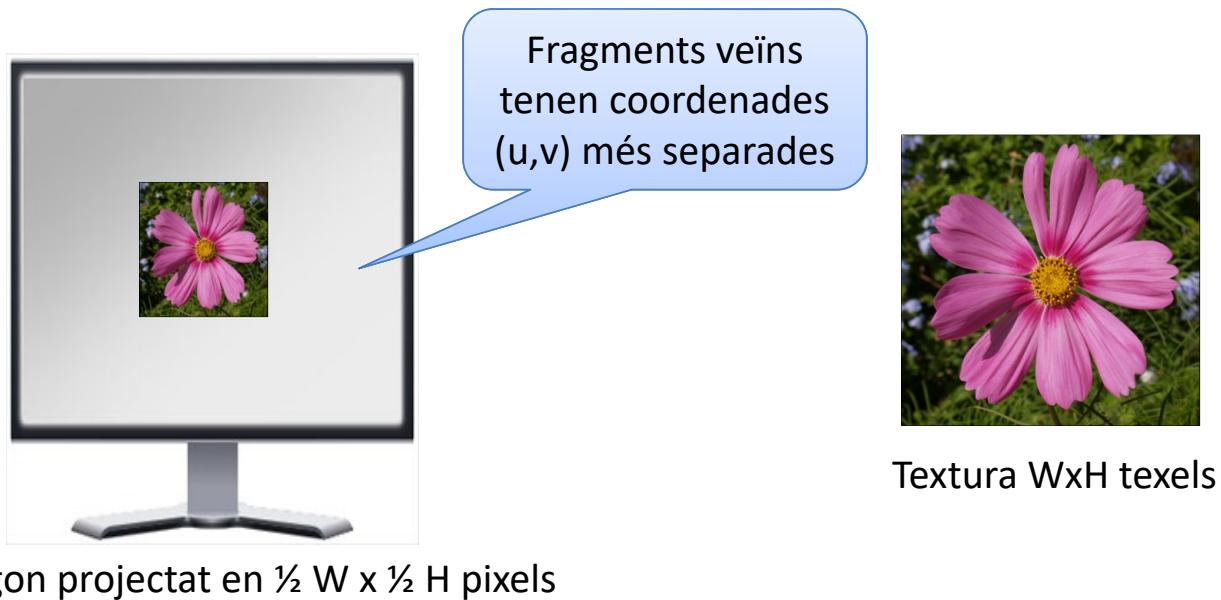


Polígon projectat en $2W \times 2H$ pixels

En aquest cas un pixel correspon a mig texel:

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} = \frac{1}{2} \quad \frac{\partial v}{\partial x} = \frac{\partial u}{\partial y} = 0$$

Exemple 3 (minification x2)



En aquest cas un pixel correspon a dos texels:

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} = 2 \quad \frac{\partial v}{\partial x} = \frac{\partial u}{\partial y} = 0$$

Exemple 4 (anisotròpic)



Textura WxH texels

En direcció horitzontal → magnification
En direcció vertical → minification

Exemple 4 (anisotròpic)



Textura WxH texels

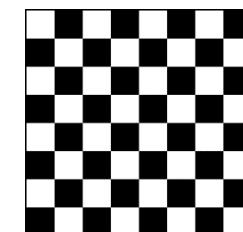
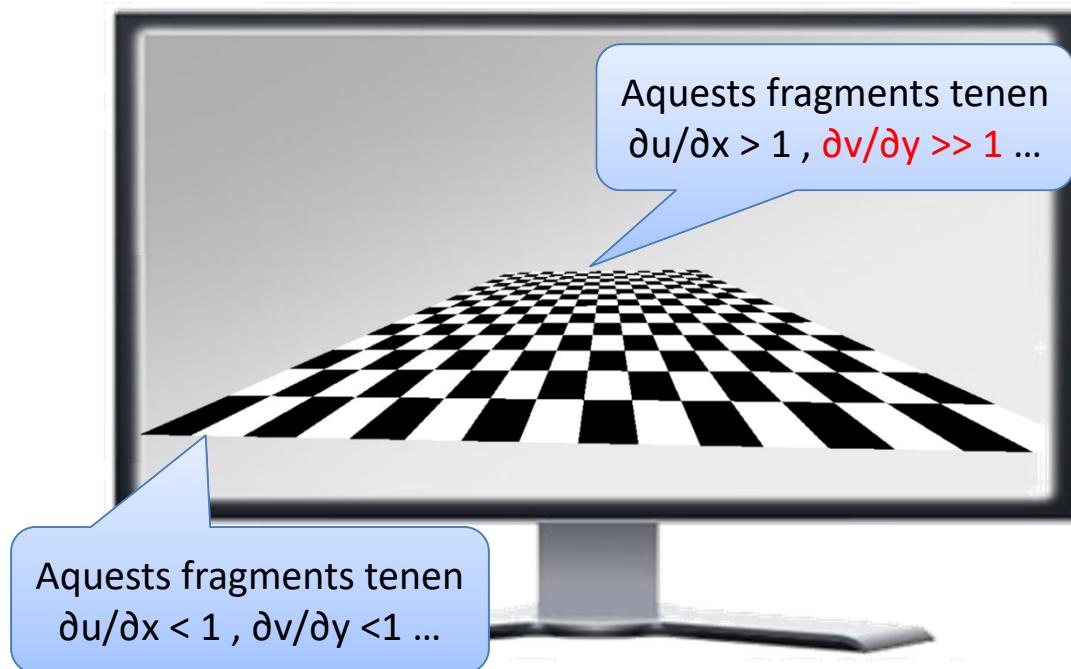
En direcció horitzontal → magnification

En direcció vertical → minification

$$\frac{\partial u}{\partial x} = \frac{1}{2} \quad \frac{\partial v}{\partial x} = 0$$

$$\frac{\partial u}{\partial y} = 0 \quad \frac{\partial v}{\partial y} = 2$$

Exemple 5

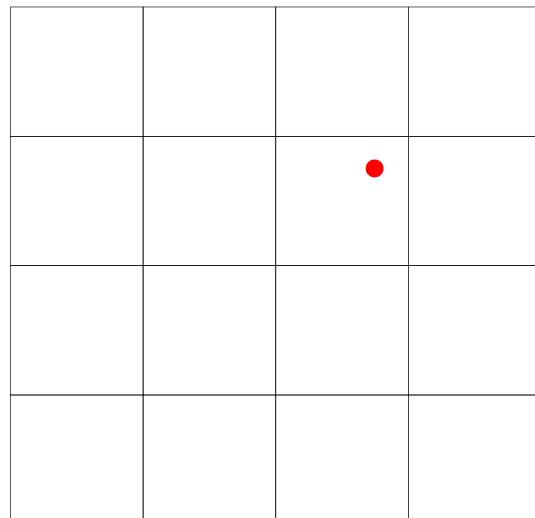


Textura

TEXTURE FILTERS

Texture filters

Determinen com s'avalua **texture(sampler, texCoord)**



Textura WxH texels

MAGNIFICATION

Magnification filters

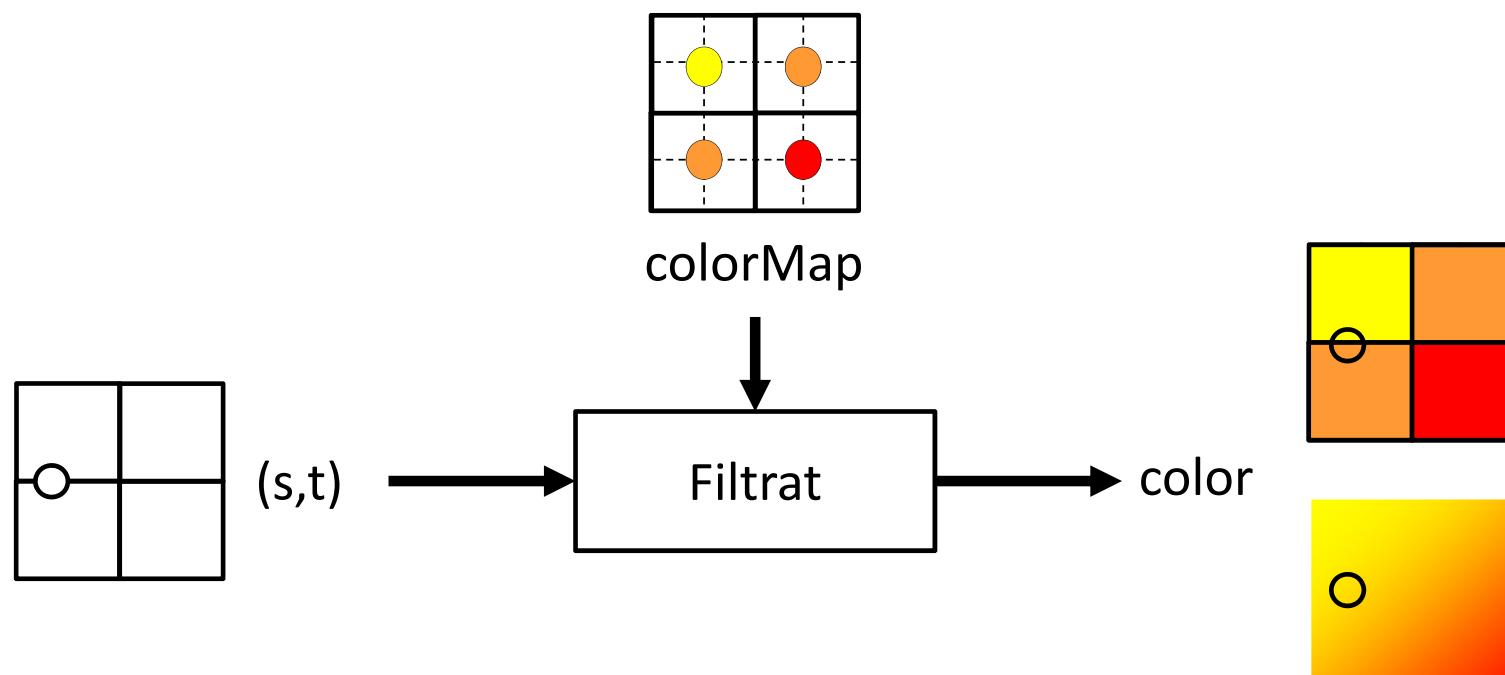
- GL_NEAREST
glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_NEAREST);
- GL_LINEAR
glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_LINEAR);

```
// Load Texture (once)
QImage img0("fieldstone.png");
QImage T = img0.convertToFormat(QImage::Format_ARGB32);
glGenTextures( 1, &textureId0);
 glBindTexture(GL_TEXTURE_2D, textureId0);
glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, T.width(), T.height(), 0,
             GL_RGBA, GL_UNSIGNED_BYTE, T.bits());
glTexParameterf(...)

// Bind textures, set uniforms...
g.glActiveTexture(GL_TEXTURE0);
g glBindTexture(GL_TEXTURE_2D, textureId0);
program->bind();
program->setUniformValue("colorMap", 0);

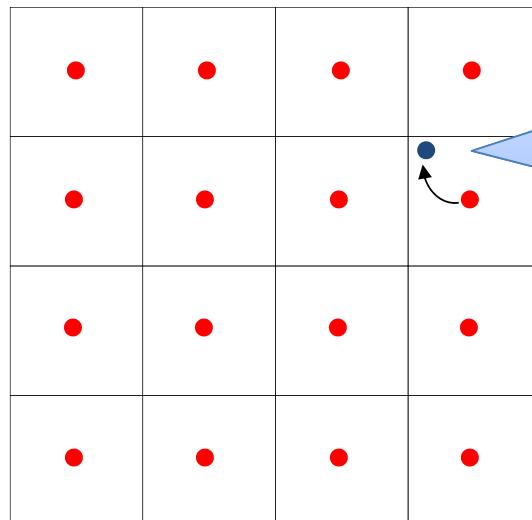
...
```

Magnification filters



Magnification filters

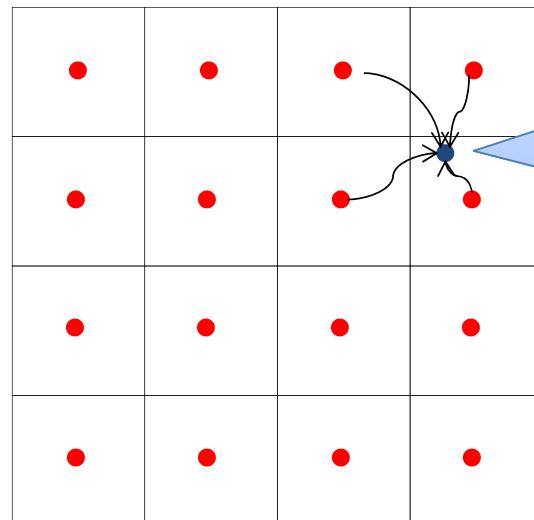
GL_NEAREST: nearest neighbor sampling



Amb nearest neighbor sampling, el color d'aquesta mostra és el color del veí més proper

Magnification filters

GL_LINEAR: bilinear interpolation

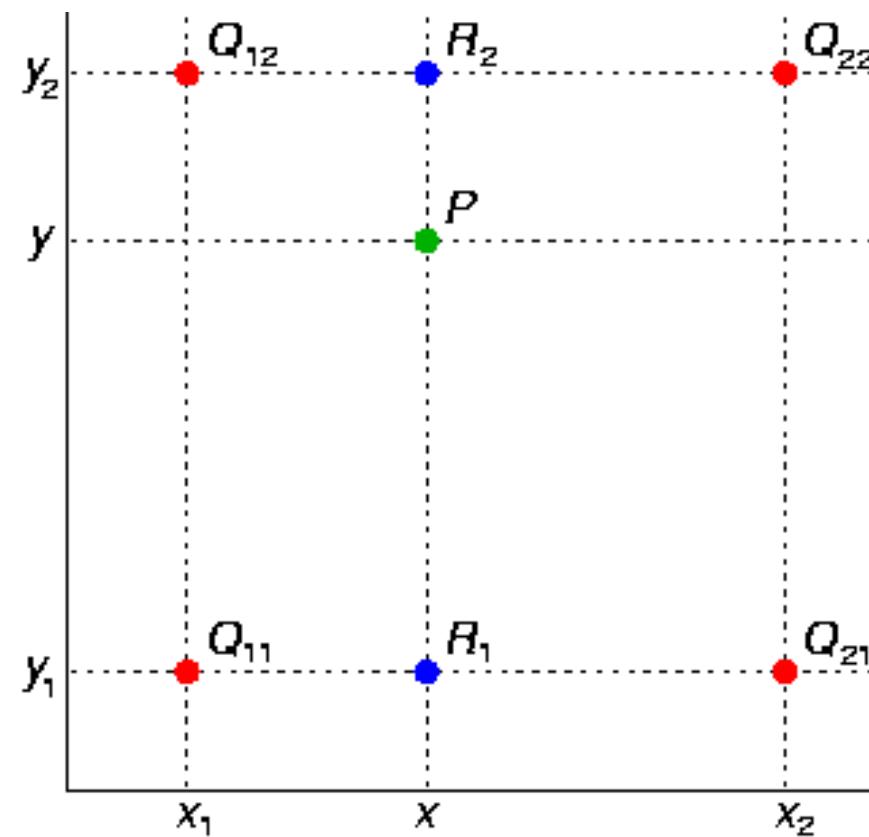
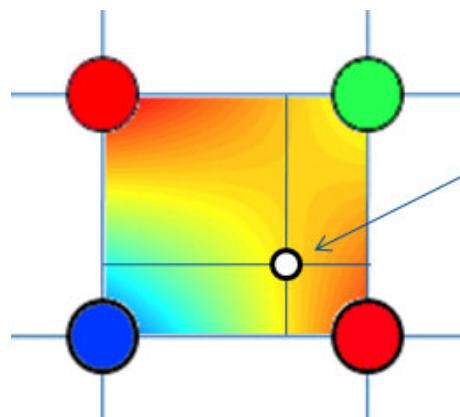


Amb interpolació bilineal,
el color d'aquesta mostra
és una mitjana ponderada
dels colors dels quatre
veïns més propers

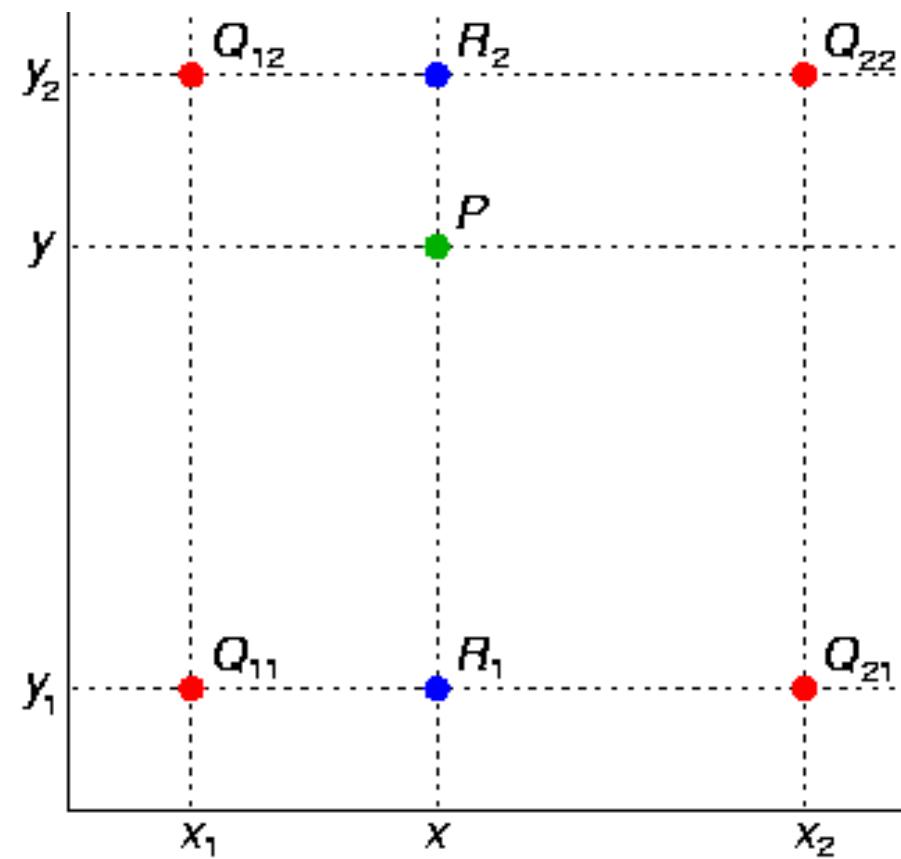
Comparació



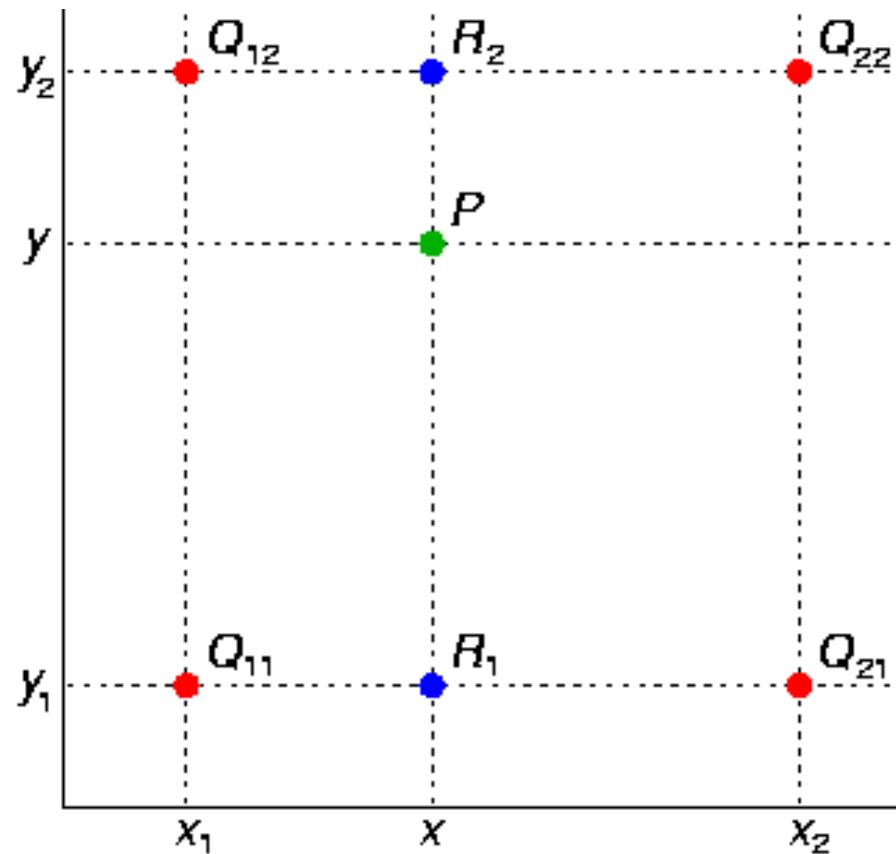
Bilinear interpolation



Bilinear interpolation



Bilinear interpolation



$$\begin{aligned} f(x, y) \approx & \frac{f(Q_{11})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y_2 - y) \\ & + \frac{f(Q_{21})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y_2 - y) \\ & + \frac{f(Q_{12})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y - y_1) \\ & + \frac{f(Q_{22})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y - y_1). \end{aligned}$$

MINIFICATION

Minification filters

- **Magnification** → la preimatge d'un pixel en espai textura és petita → n'hi ha prou filtrant amb 2x2 texels.
- **Minification** → la preimatge d'un pixel és arbitràriament gran → no n'hi ha prou amb 2x2 texels!



Minification x16

Minification x8

Minification x4

Minification x2



Textura

Mipmapping

Idea bàsica: cada textura està representada amb diferents resolucions (level-of-details, LODs)

1x1 (LOD 8)

:

:



16x16 (LOD 4)



32x32 (LOD 3)



64x64 (LOD 2)



128x128 (LOD 1)



256x256 (LOD 0)

Mipmapping

En alguns casos el LOD més adient λ és fàcil de calcular

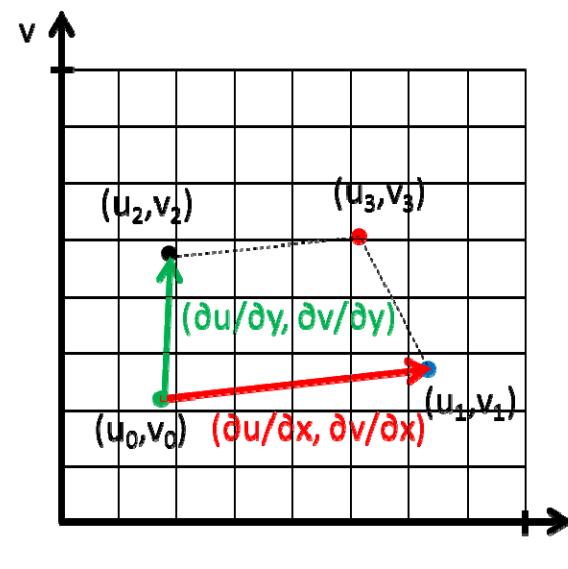
Minification	$\partial u / \partial x, \partial v / \partial y$	LOD
	1x	1
	2x	2
	4x	4
	8x	8
	$2^\lambda x$	2^λ

En aquest cas $2^\lambda = \partial u / \partial x$
Per tant: $\lambda = \log_2(\partial u / \partial x)$

Mipmapping

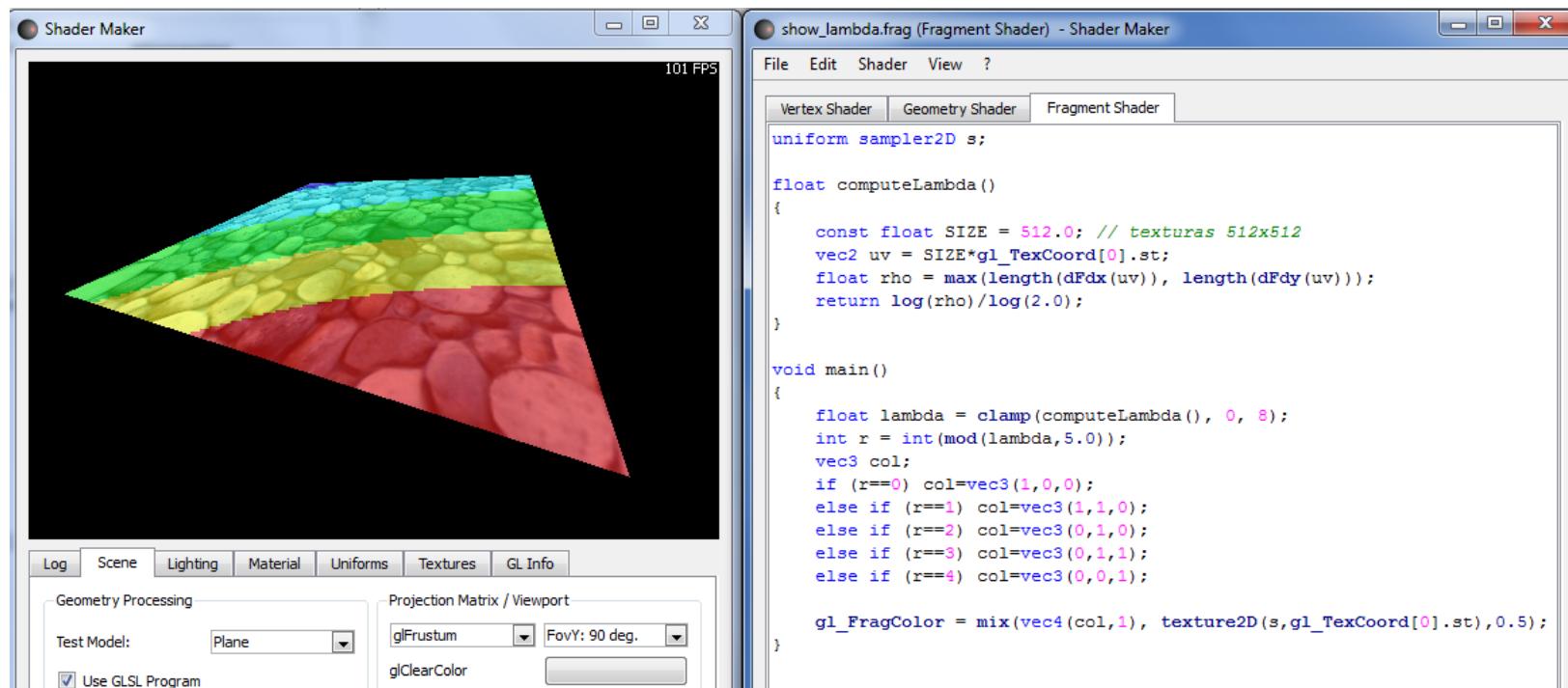
En general:

- Es calcula un valor $\rho = f(\partial u / \partial x, \partial v / \partial x, \partial u / \partial y, \partial v / \partial y)$
- Es calcula el $\lambda = \log_2(\rho)$



Mipmapping

Demo: show_lambda.frag



Minification filters

Without mipmapping

- GL_NEAREST // Nearest neighbor sampling on LOD 0
- GL_LINEAR // Bilinear interpolation on LOD 0

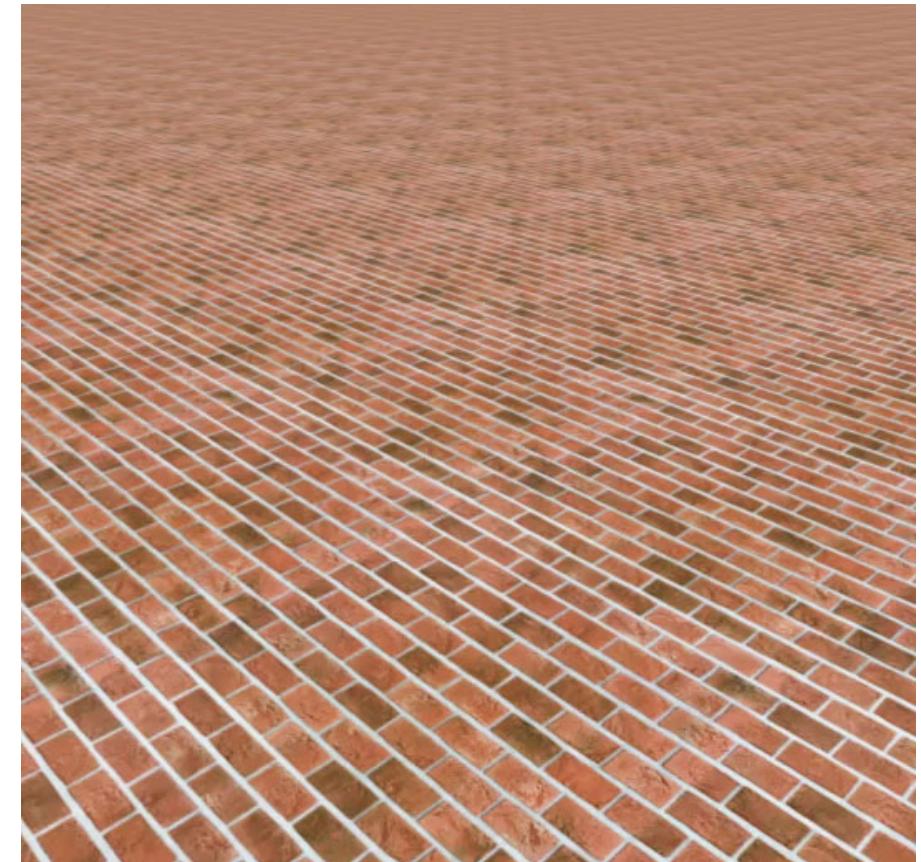
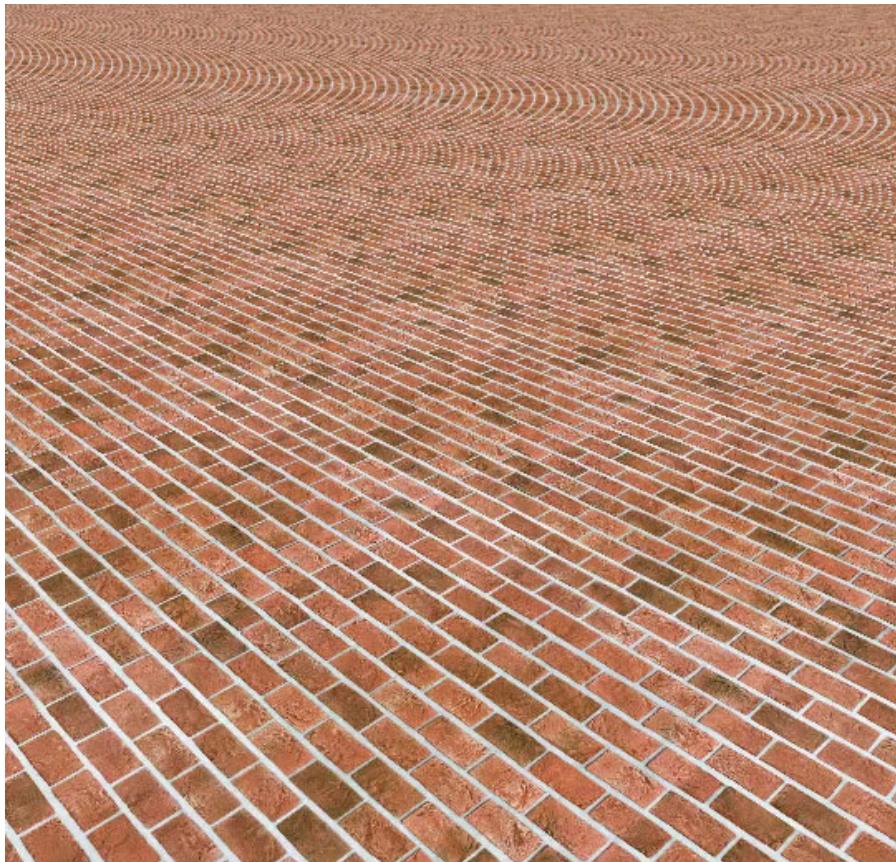
With mipmapping

- GL_NEAREST_MIPMAP_NEAREST // Nearest neighbor sampling on LOD $\text{int}(\lambda)$
- GL_LINEAR_MIPMAP_NEAREST // Bilinear sampling on LOD $\text{int}(\lambda)$
- GL_NEAREST_MIPMAP_LINEAR // c_0 = nearest neighbor on LOD $\text{int}(\lambda)$
// c_1 = nearest neighbor on LOD $\text{int}(\lambda+1)$
// mix($c_0, c_1, \text{fract}(\lambda)$)
- GL_LINEAR_MIPMAP_LINEAR // c_0 = bilinear sampling on LOD $\text{int}(\lambda)$
// c_1 = bilinear sampling on LOD $\text{int}(\lambda+1)$
// mix($c_0, c_1, \text{fract}(\lambda)$)

GL_<samplingWithinTheLODs>_MIPMAP_<oneOrTwoLODs>



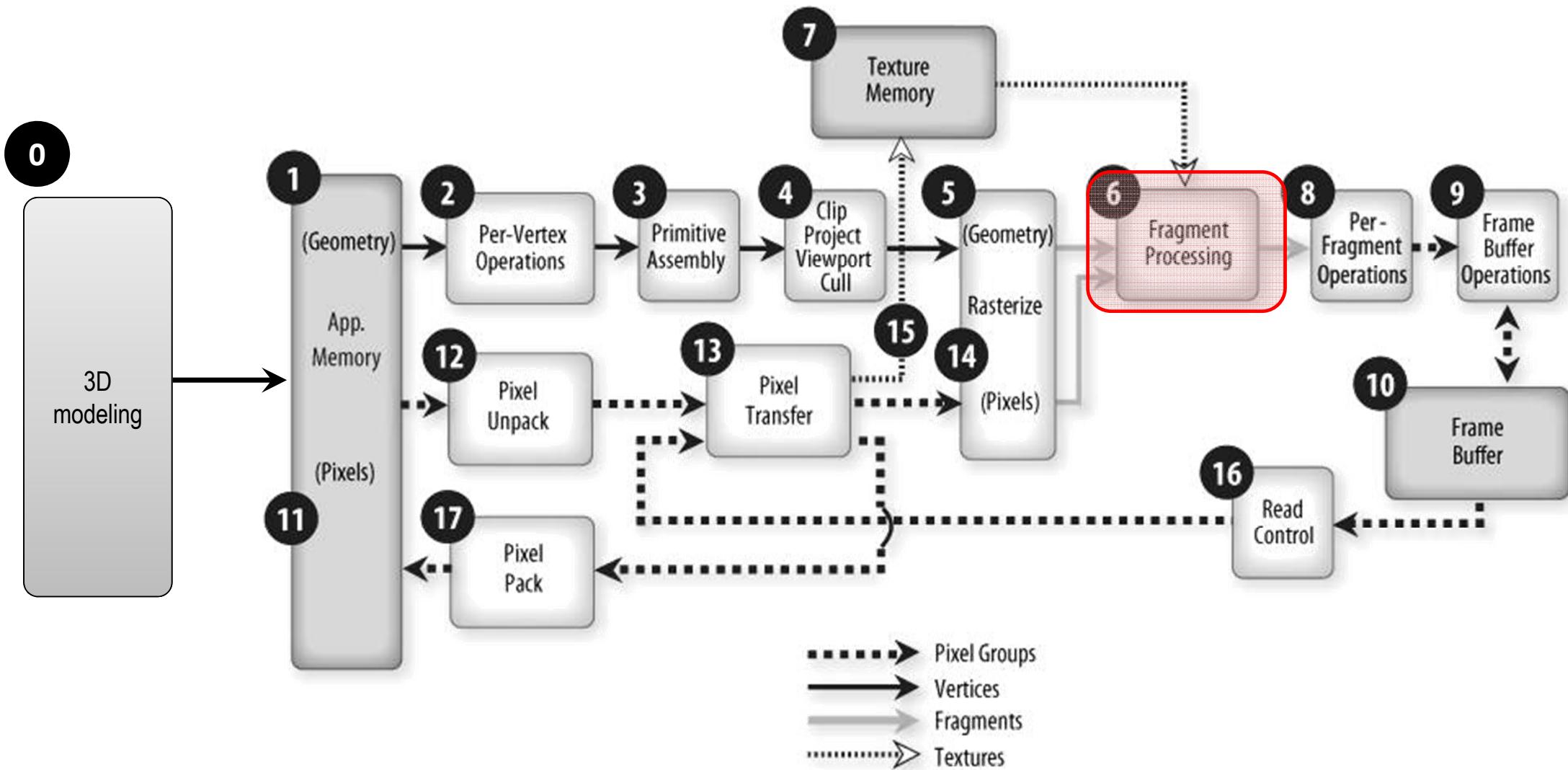
Comparació



Minification filters (2)

[Demo mipmapping]

COMBINACIÓ



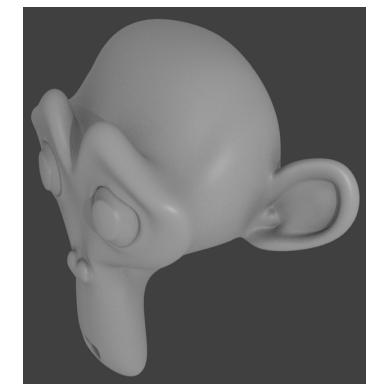
FS – exemple

```
uniform sampler2D colorMap;  
in vec2 vtexcoord;  
in vec4 frontColor;  
  
vec4 texColor = texture(colorMap, vtexcoord);  
...  
fragCoord = ???
```

Modes habituels

REPLACE: `fragColor = texColor;`

$$K_d I_d (N \cdot L) + K_s I_s (R \cdot V)^s$$



Modes habituels

MODULATE: `fragColor = texColor * frontColor;`

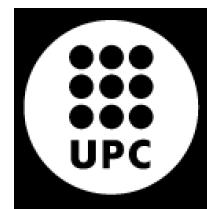
$$K_d I_d (N \cdot L) + K_s I_s (R \cdot V)^s$$



Modes habituels

DECAL:

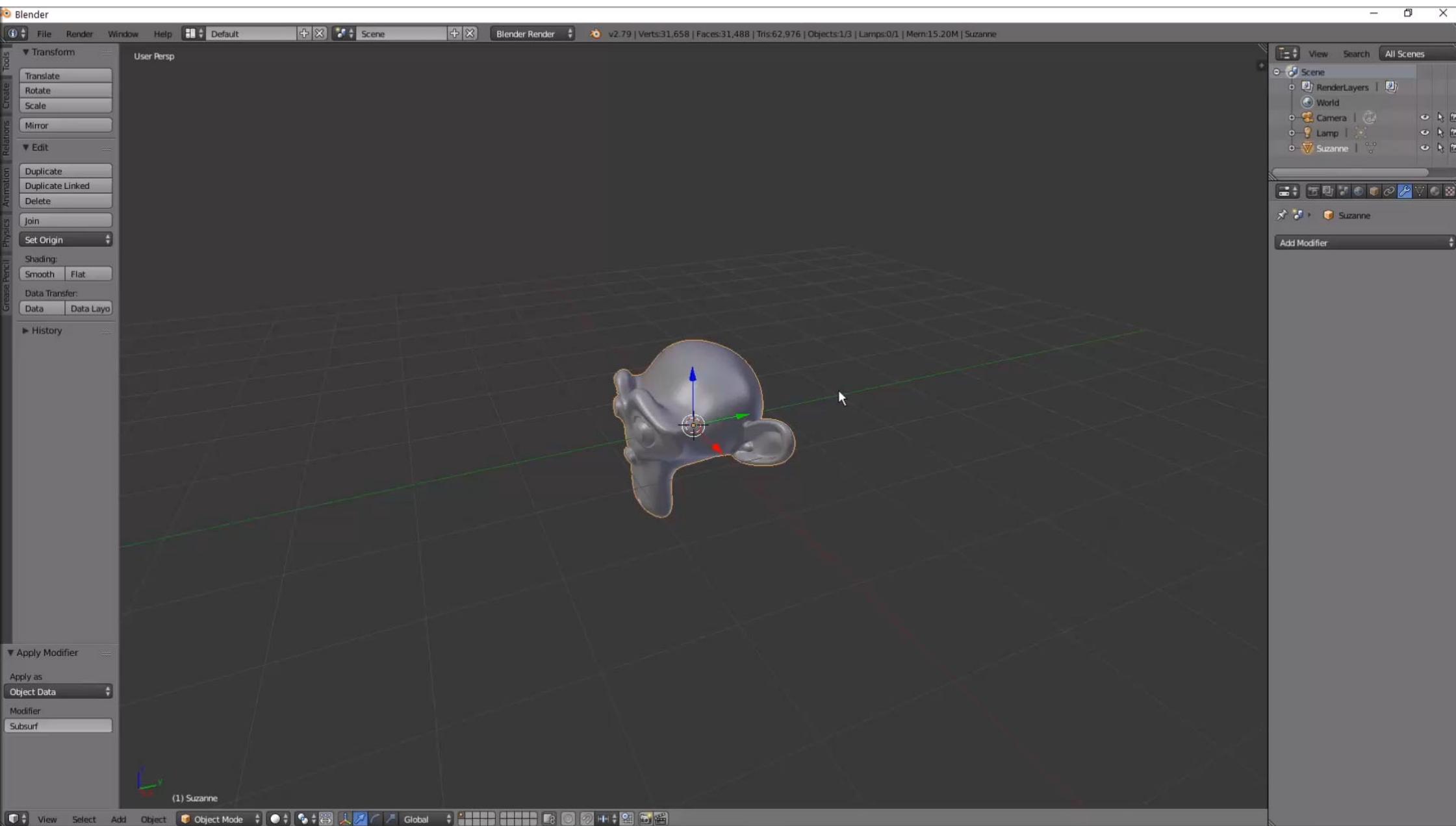
```
fragColor = mix(frontColor, texColor, texColor.a);
```



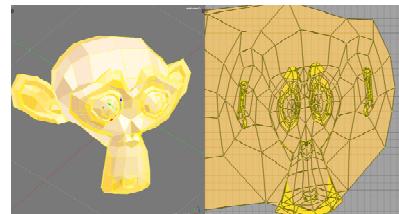
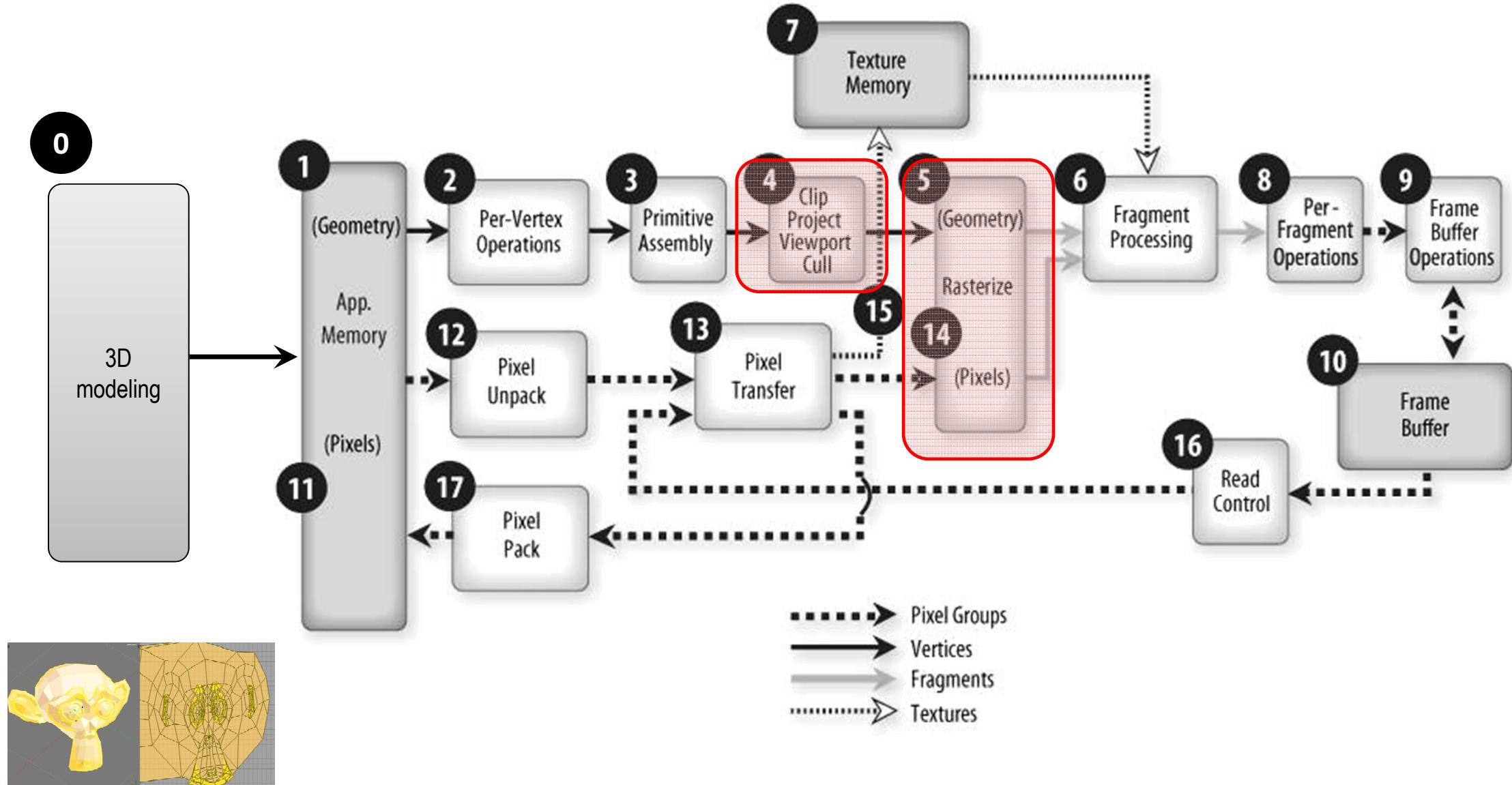
```
if (texColor.a < alphaThreshold)  
    discard;
```



GENERACIÓ D'UN LIGHT MAP



INTERPOLACIÓ DE COORDS DE TEXTURA

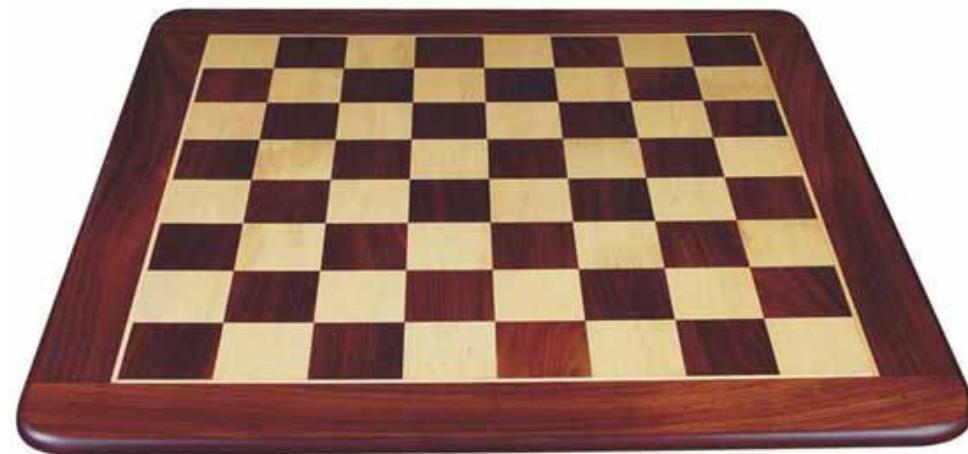
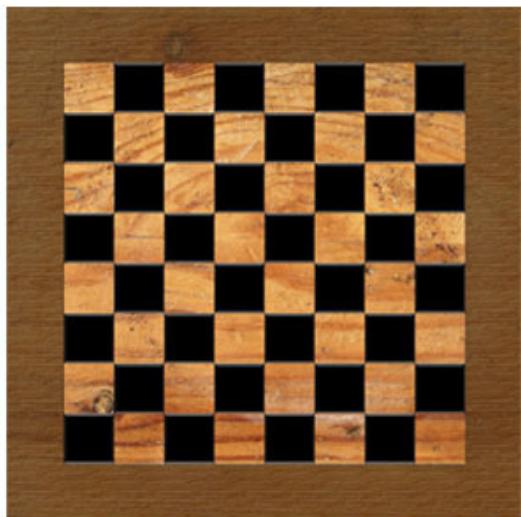


PERSPECTIVE-CORRECT INTERPOLATION

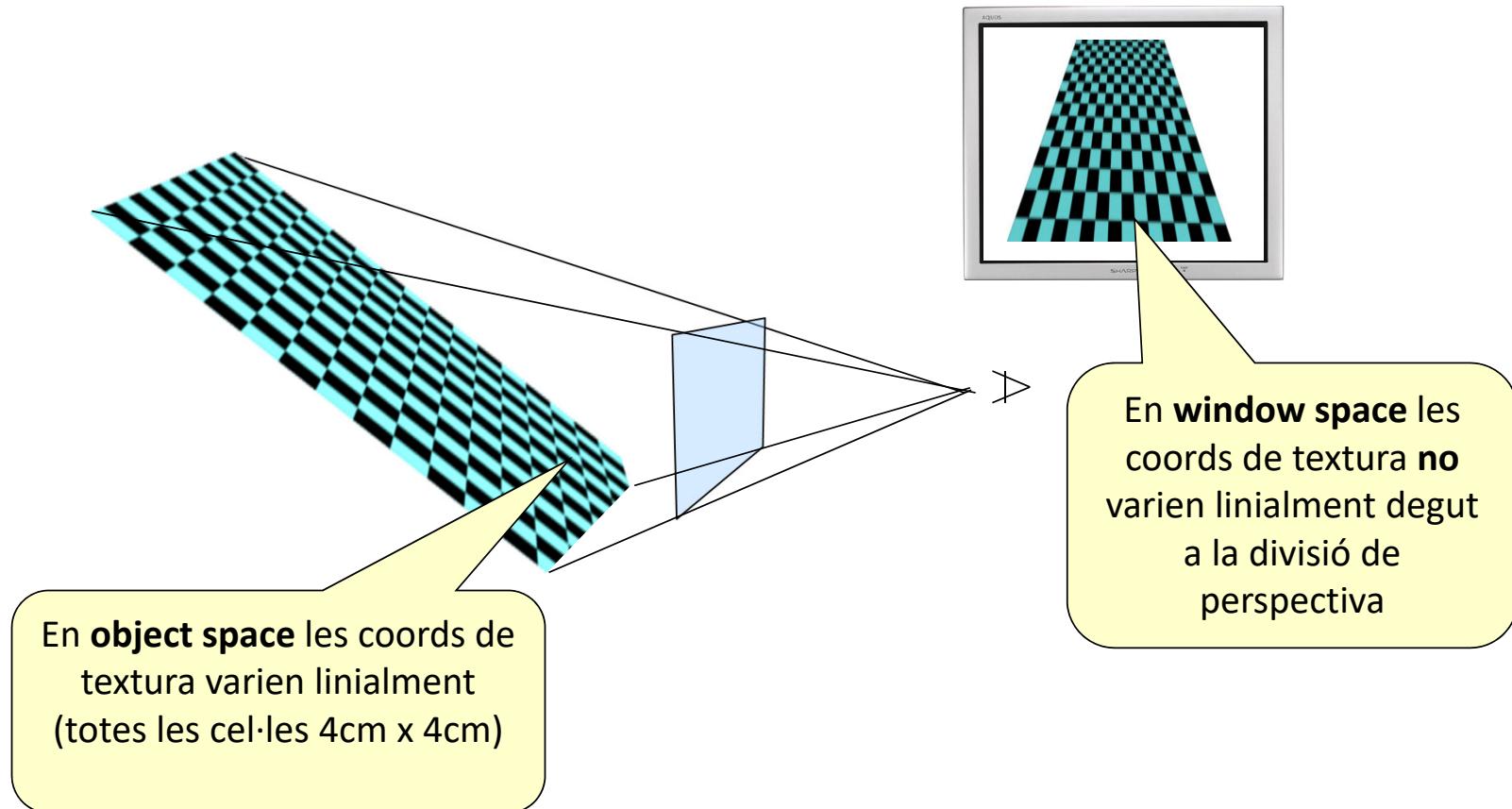
Perspective deformation



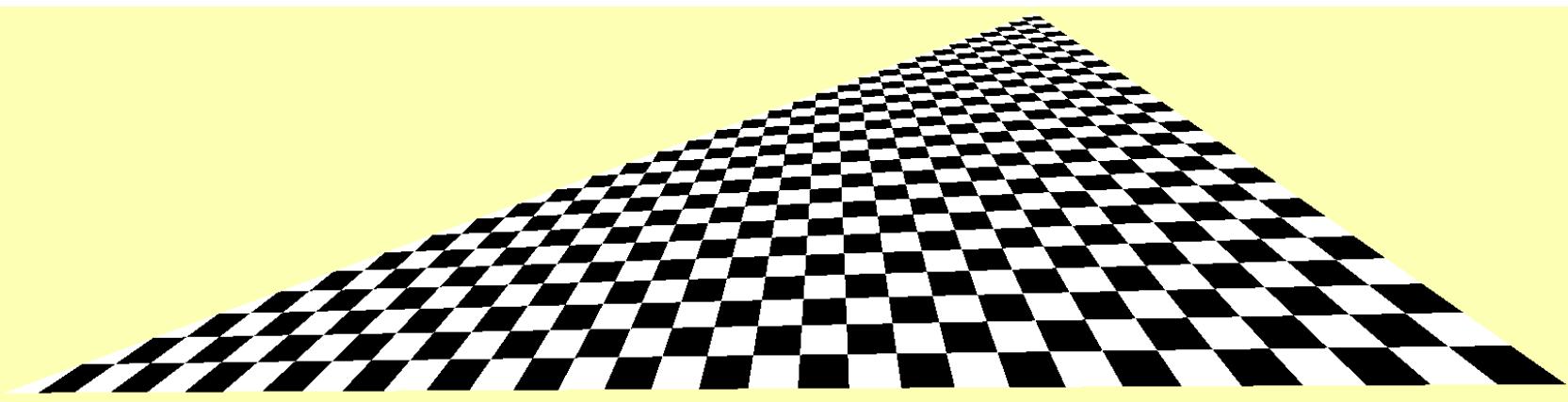
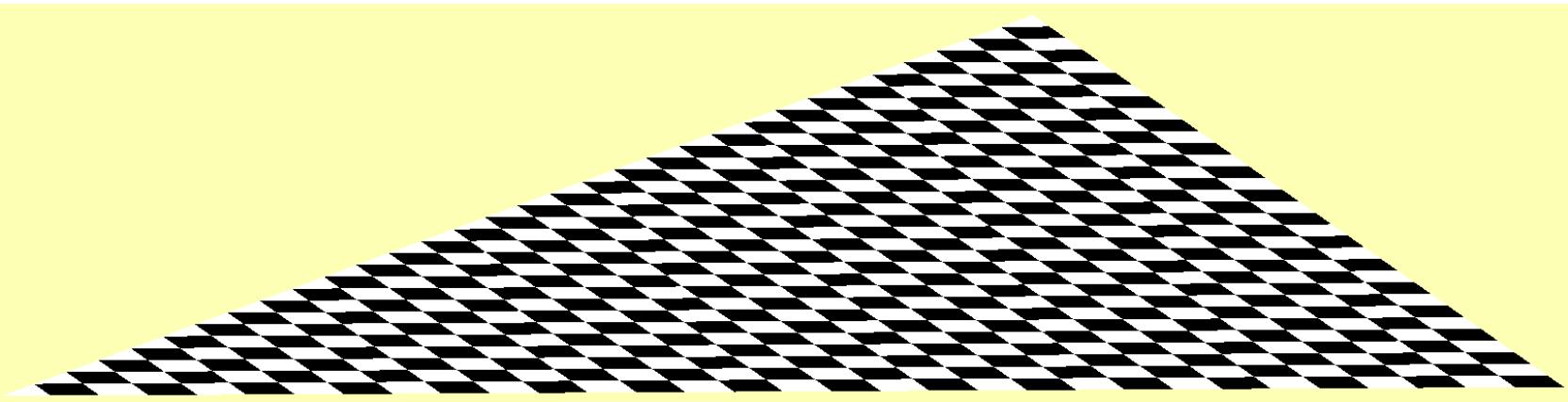
Perspective deformation



Perspective-correct interpolation



Perspective-correct interpolation



[Demo: pers.vert, pers.frag]

Perspective-correct interpolation

Solucions:

- a) Interpolem (s, t) en **object space** (també valdria en **world, eye i clip space**, perquè són abans de la div. de perspectiva)
- b) Interpolem (sw, tw, w) en **window space**, obtenint un texel (s, t, q) ; accedirem a la textura amb $(s/q, t/q)$

Recordeu que $w = 1/w_c = -1/z_e$

Perspective-Correct Interpolation

[Demostració de (b): consulteu per exemple l'article de Kok-Lim Low]

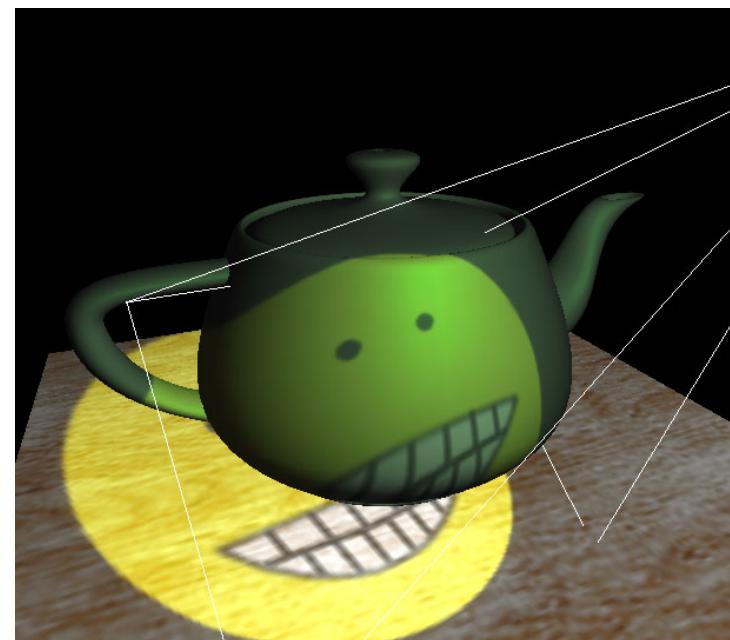
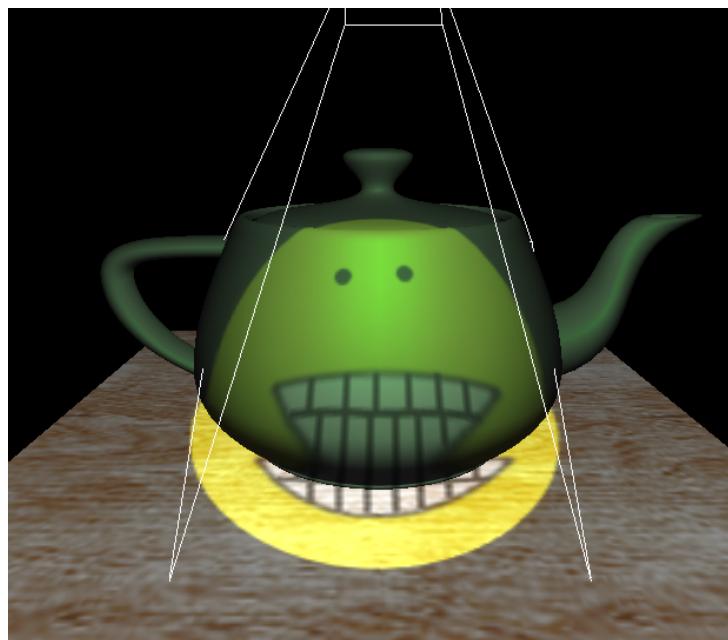
Kok-Lim Low

Department of Computer Science
University of North Carolina at Chapel Hill
Email: lowk@cs.unc.edu

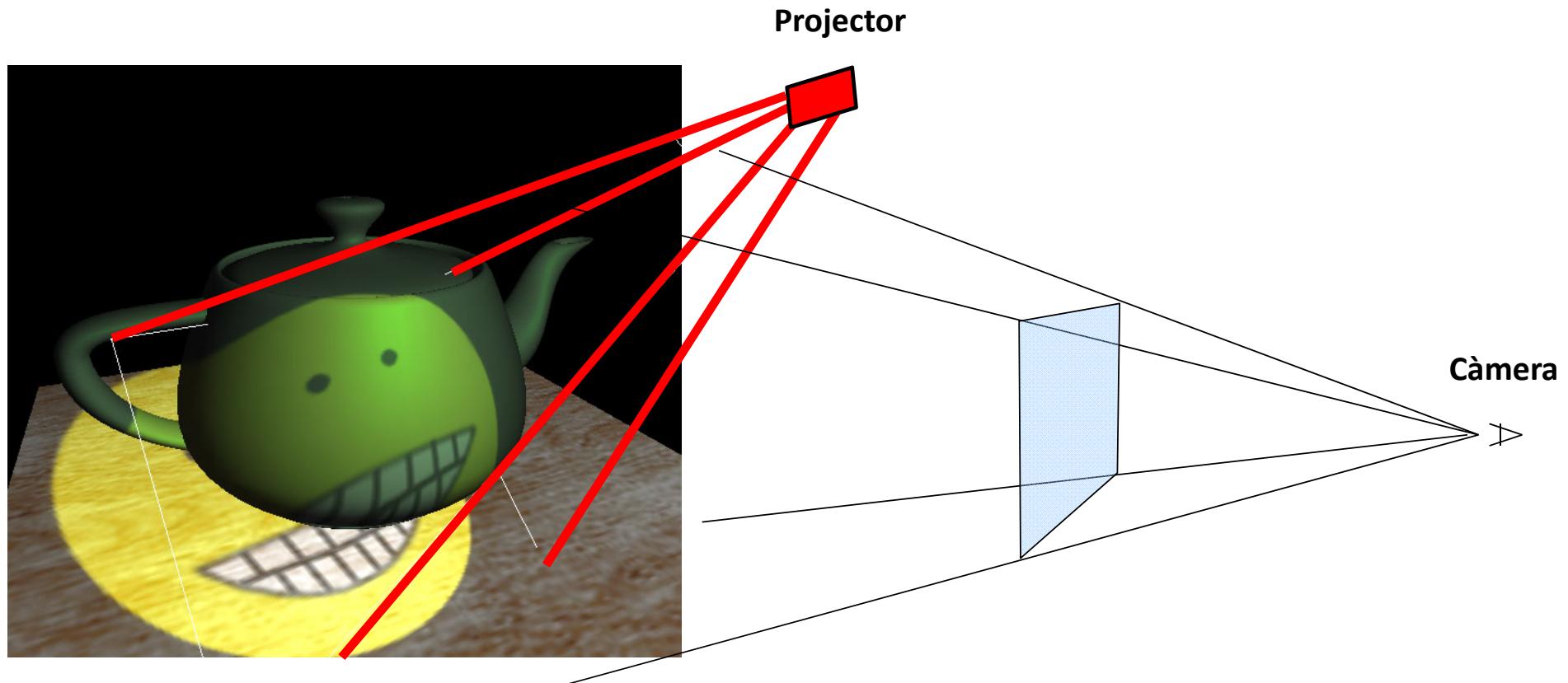
March 12, 2002

PROJECTIVE TEXTURE MAPPING

Projective texture mapping



Projective texture mapping



Opció 1 (incorrecta)

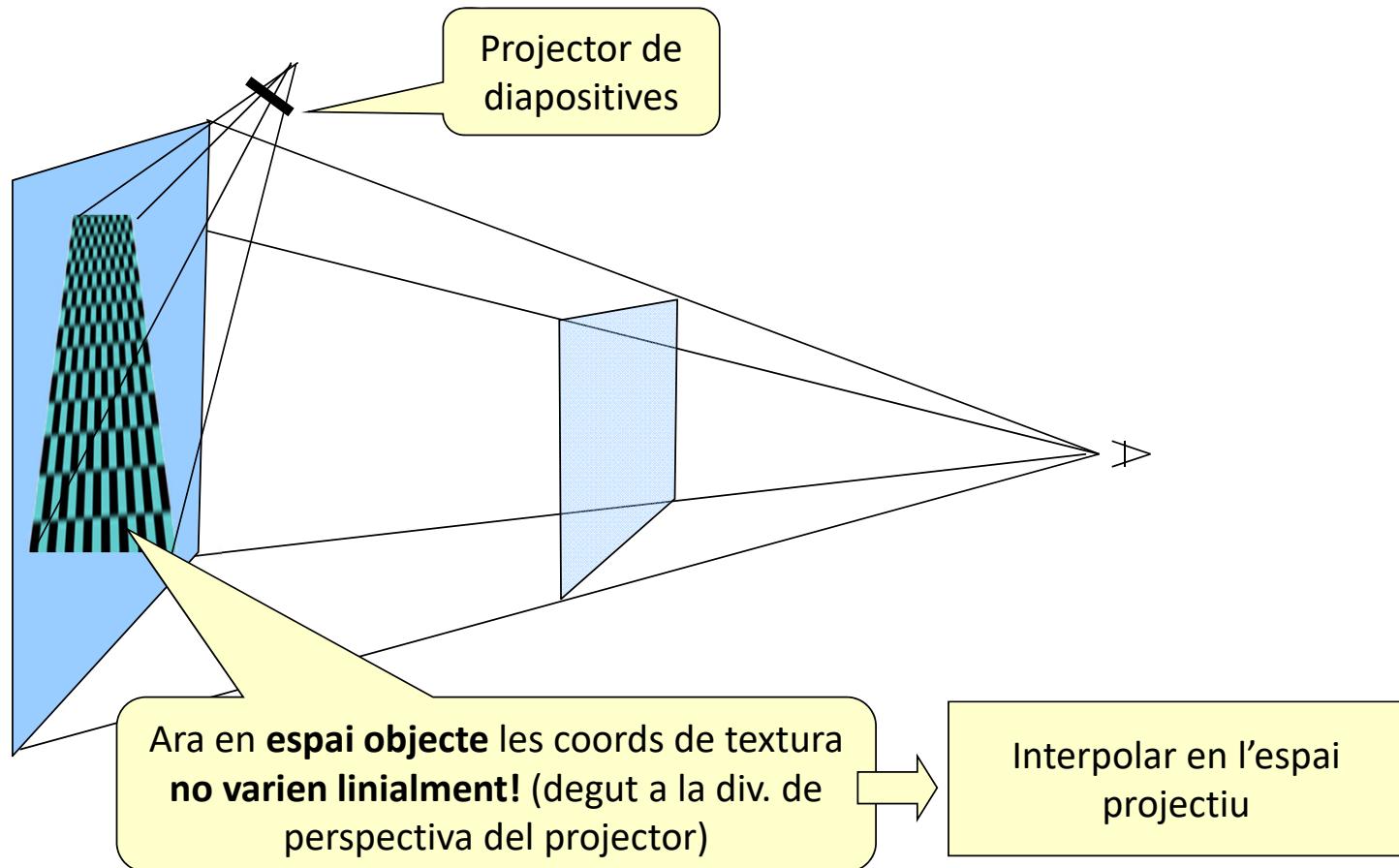
VS – generació coords de textura

Passa el vèrtex de *object space* a *window space* (viewport 1x1)
Calcula (s,t) com (x,y) del resultat

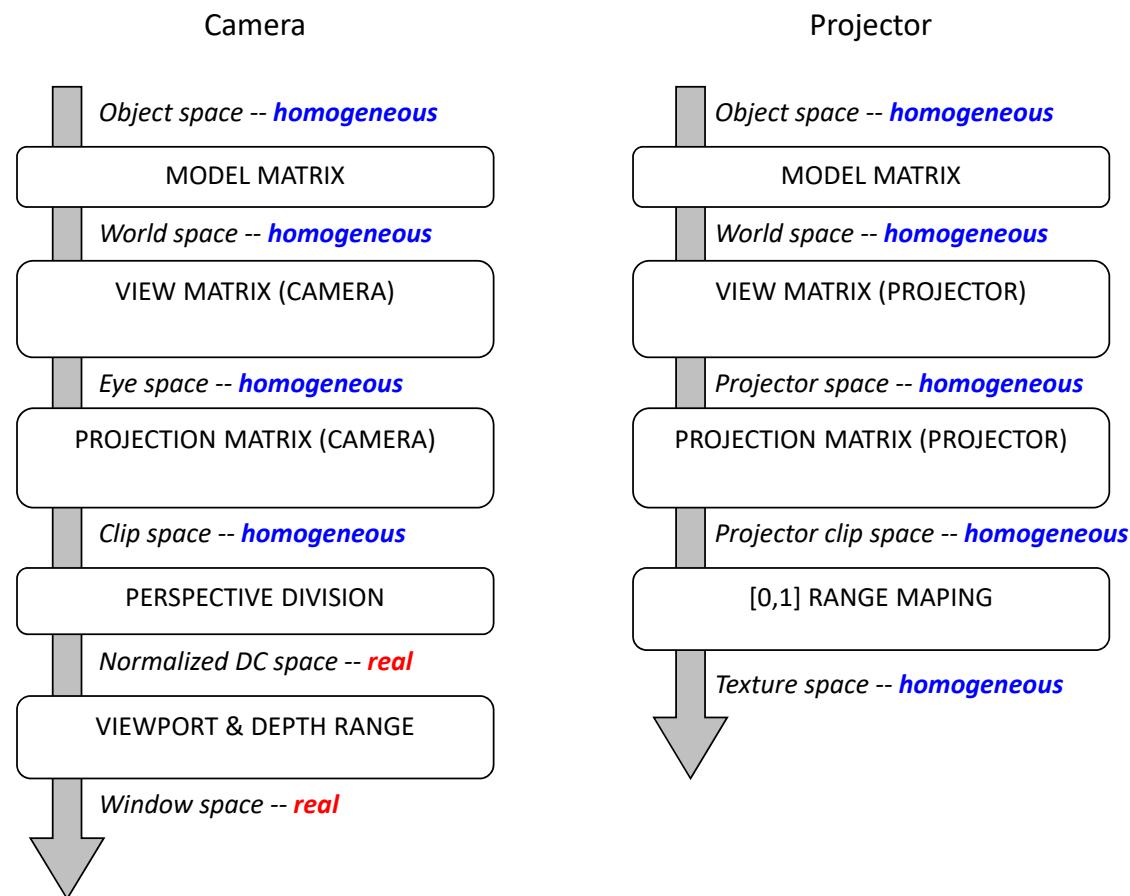
FS – accés a textura

Usa (s,t) per accedir a la textura

Projective-space interpolation



Projective texture mapping



Opció 2 (correcta)

VS – generació coords de textura

Passa el vèrtex de *object space* a *window space* (viewport 1x1)
però sense aplicar la div de perspectiva.

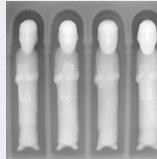
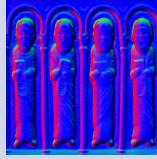
Calcula (s, t, p, q) com (x, y, z, w) del resultat

FS – accés a textura

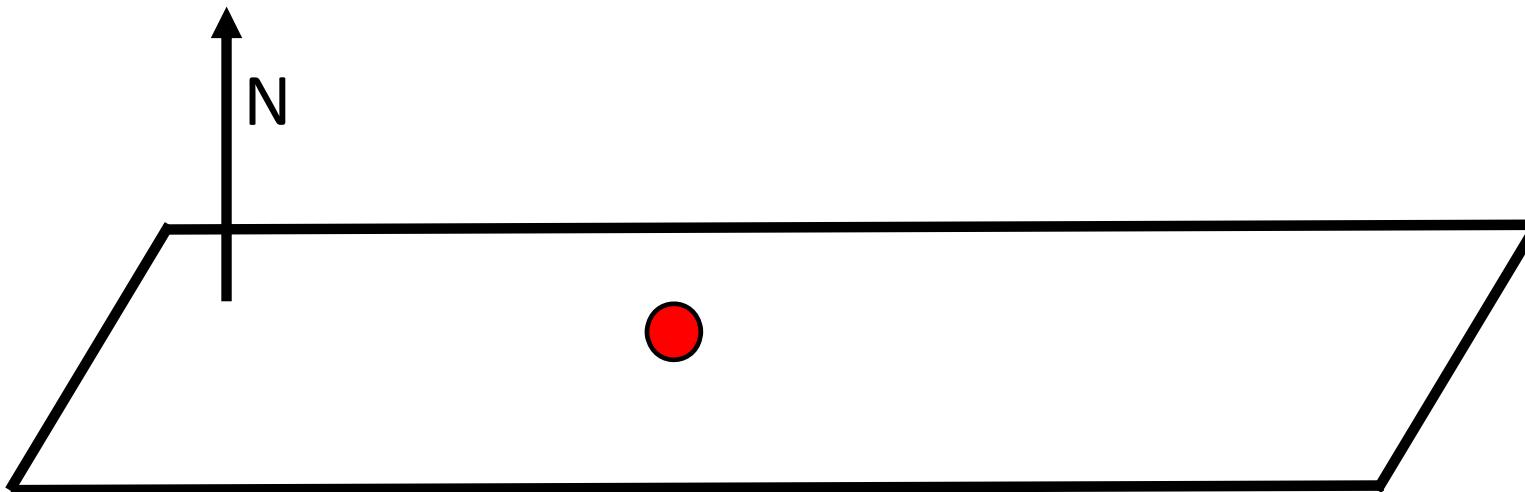
Usa $(s/q, t/q)$ per a accedir a la textura

Color, bump, parallax, relief i displacement mapping

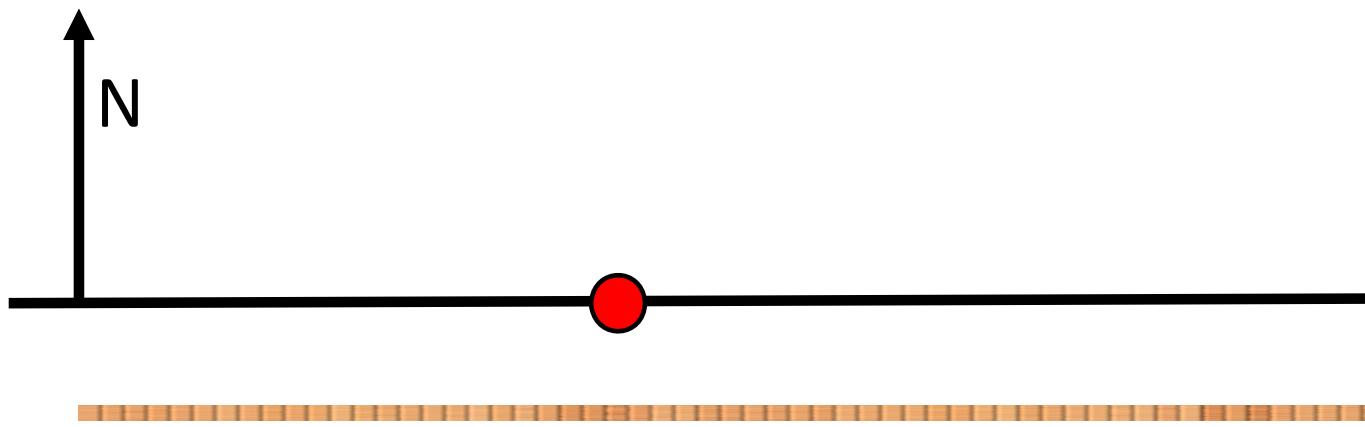
APLICACIONES

Tècnica	Info a la textura	Ús de la textura	Coords de textura	View parallax	Self-occlusion	Detailed silhouette	On s'aplica	
Color mapping	RGB 3	Kd del material	(s,t)	-	-	-	FS	
Bump mapping	D 1		Modificar la normal	(s,t)	N	N	N	FS
Normal mapping	Normal 3		Modificar la normal	(s,t)	N	N	N	FS
Parallax mapping	Normal + D 3+1 o 4	Modificar la normal	$(s+d_s, t+d_t)$	S	N	N	FS	
Relief mapping	Normal + D 3+1 o 4	Modificar la normal; descartar fragments	$(s+d_s, t+d_t)$	S	S	S	FS!!!	
Displacement mapping	D 1	Desplaçar els vèrtexs un cop subdividits els polígons.	(s,t)	S	S	S	CPU GS TCS+TES	

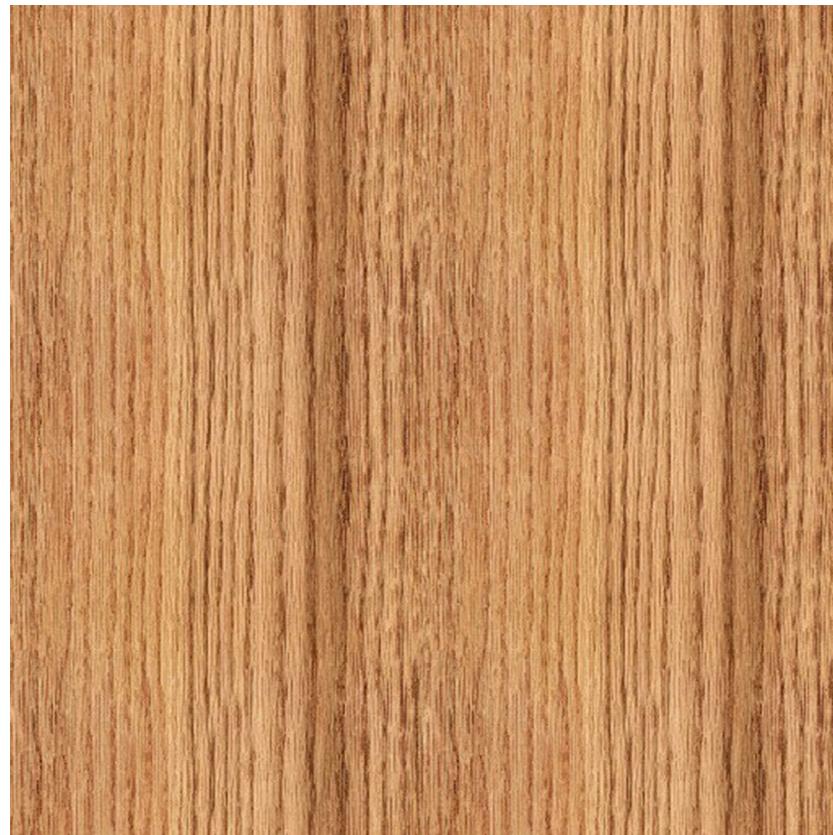
Color mapping

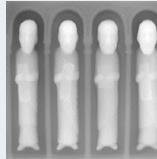
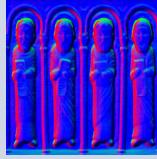


Color mapping

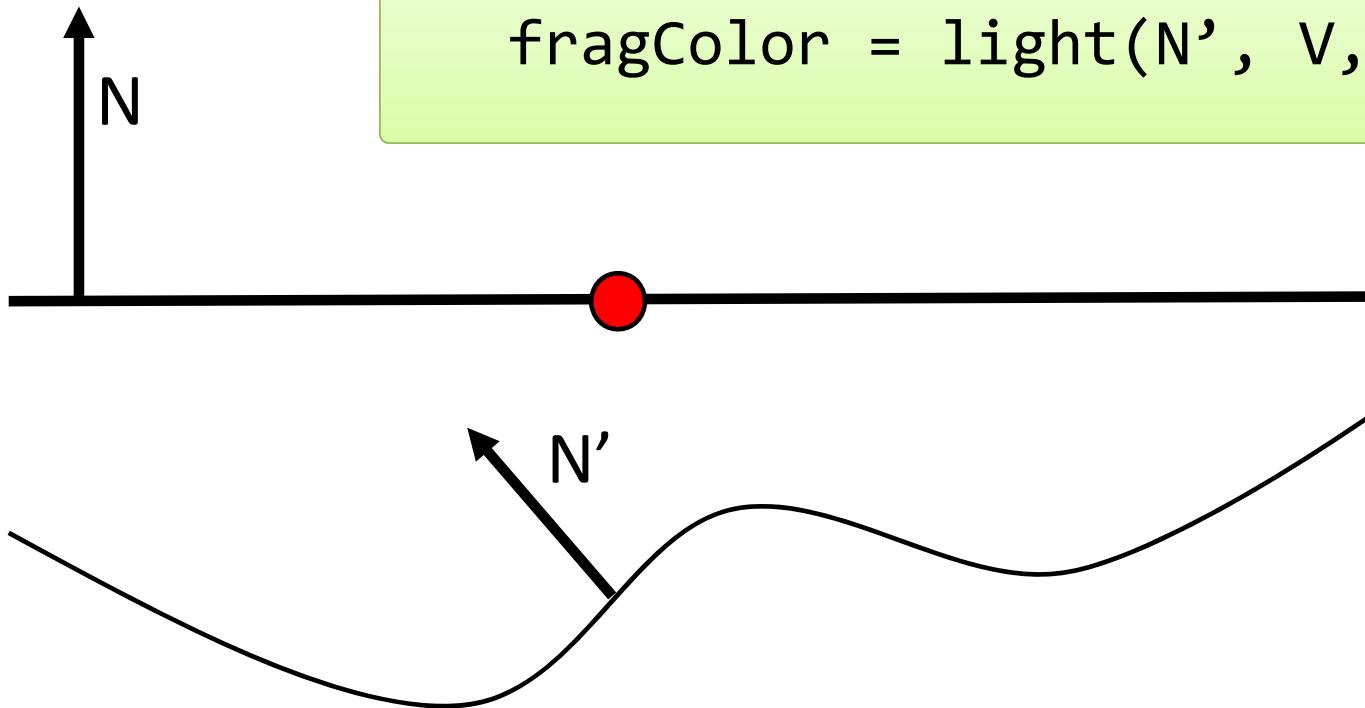


Color mapping

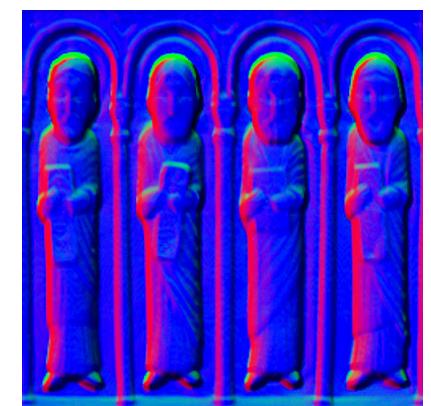
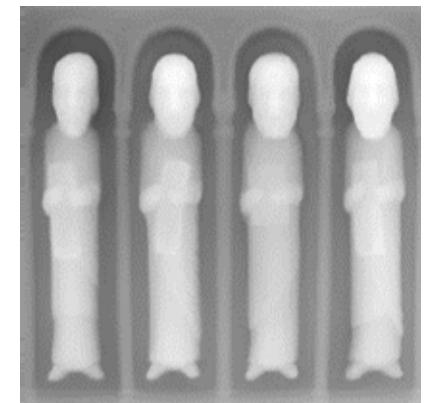


Tècnica	Info a la textura	Ús de la textura	Coords de textura	View parallax	Self-occlusion	Detailed silhouette	On s'aplica	
Color mapping	RGB 3	Kd del material	(s,t)	-	-	-	FS	
Bump mapping	D 1		Modificar la normal	(s,t)	N	N	N	FS
Normal mapping	Normal 3		Modificar la normal	(s,t)	N	N	N	FS
Parallax mapping	Normal + D 3+1 o 4	Modificar la normal	$(s+d_s, t+d_t)$	S	N	N	FS	
Relief mapping	Normal + D 3+1 o 4	Modificar la normal; descartar fragments	$(s+d_s, t+d_t)$	S	S	S	FS!!!	
Displacement mapping	D 1	Desplaçar els vèrtexs un cop subdividits els polígons.	(s,t)	S	S	S	CPU GS TCS+TES	

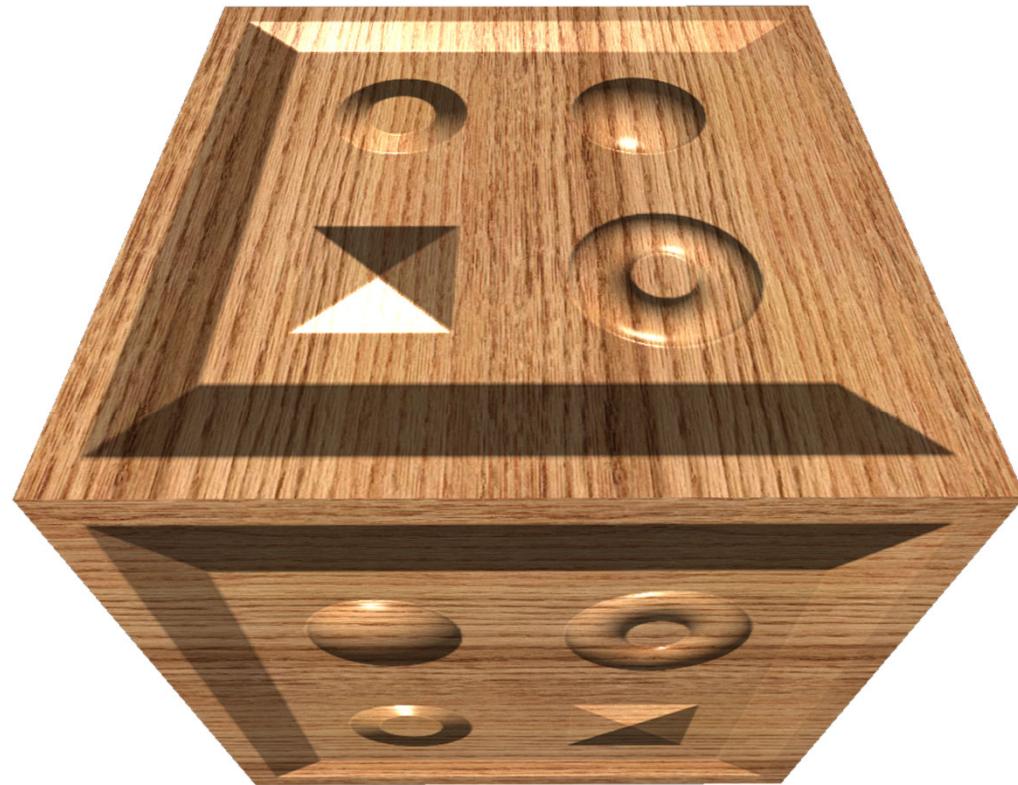
Bump mapping/Normal mapping



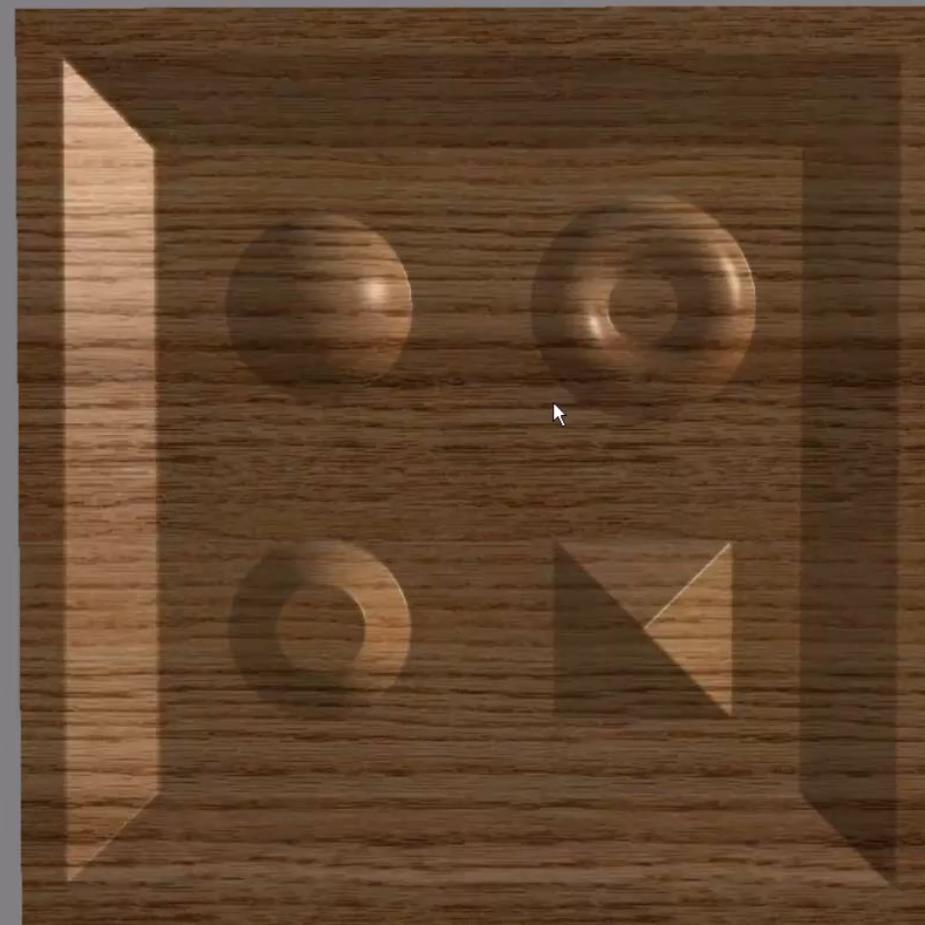
```
N' = computeNormal(s,t);  
fragColor = light(N', V, L);
```



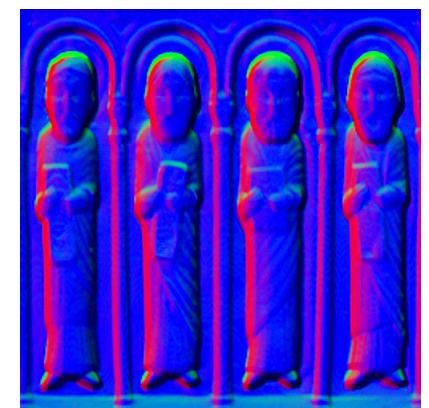
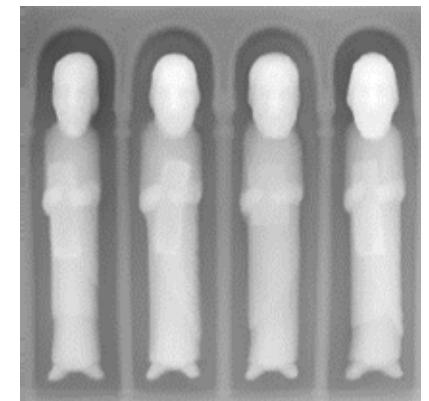
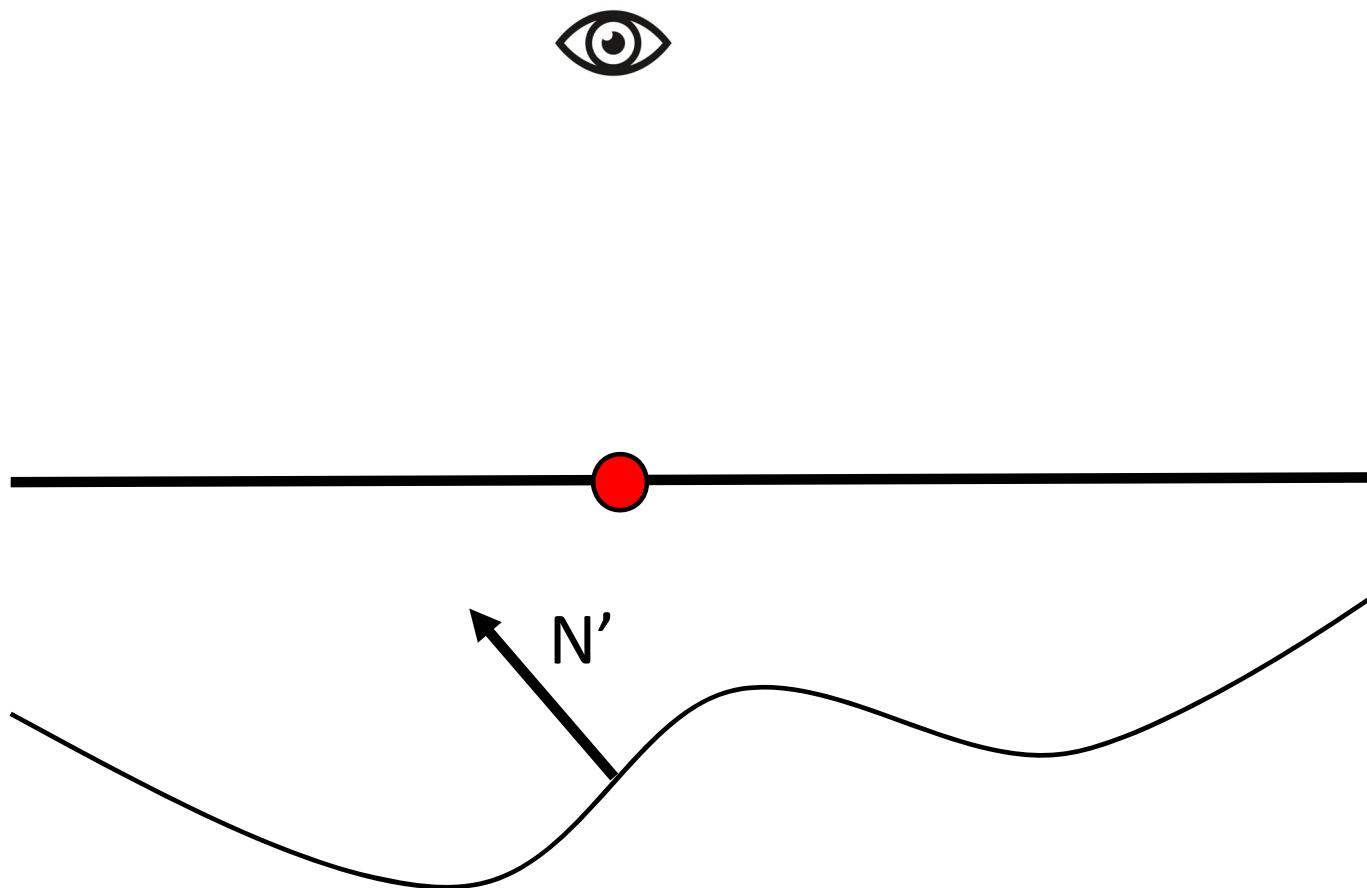
Bump mapping/Normal mapping



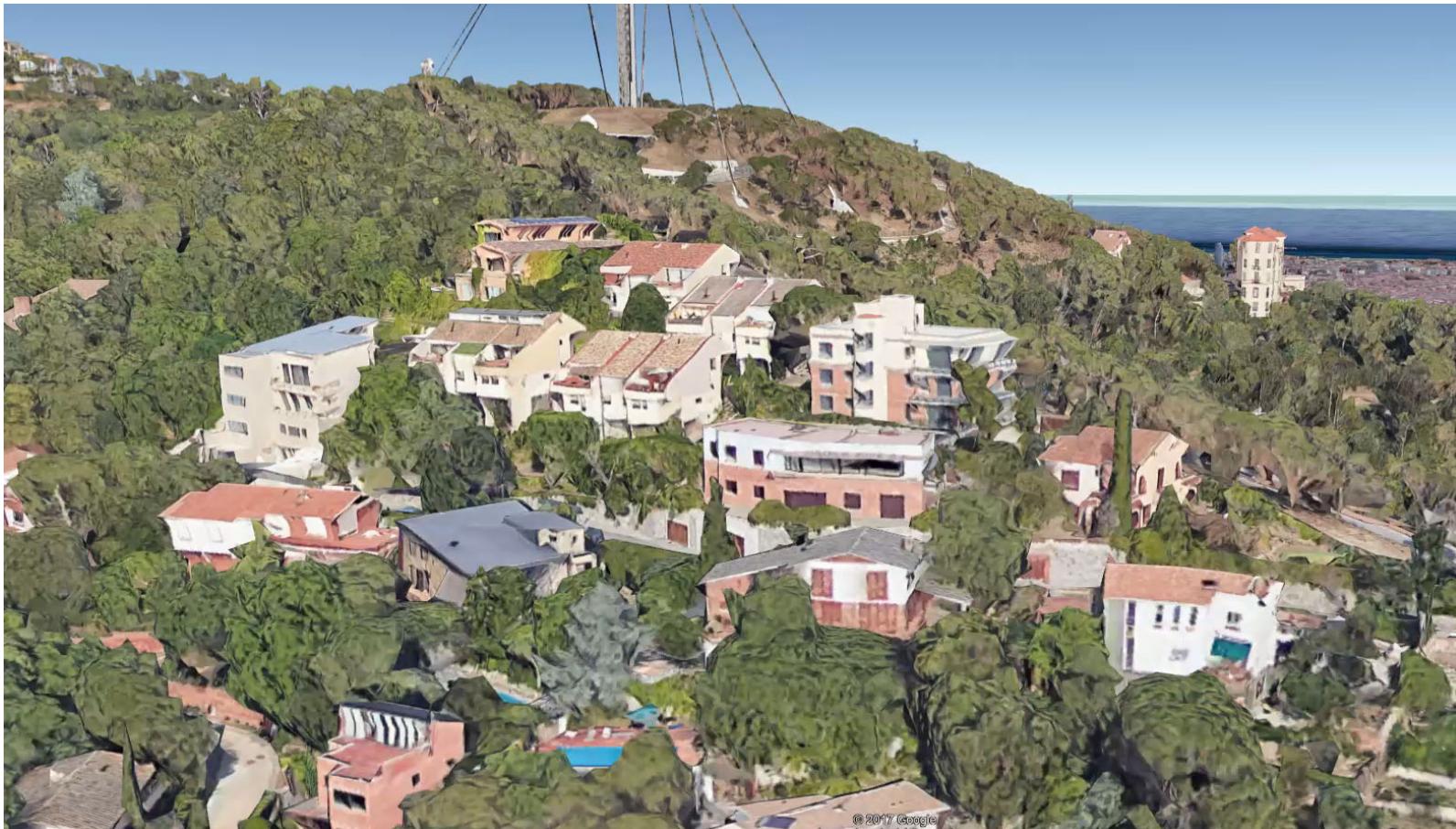
Relief Mapping
File View Render About...
Normal Mapping
Border Clamp
Depth Bias

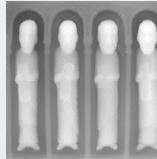
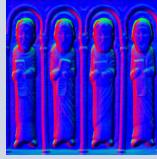


Problema Bump mapping/Normal mapping

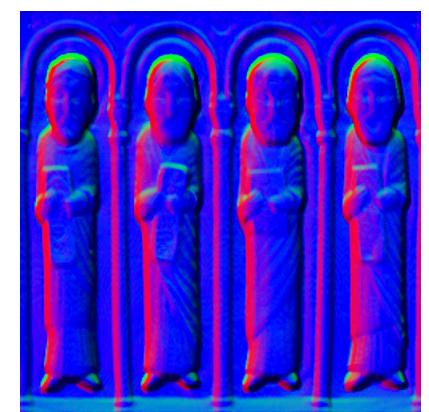
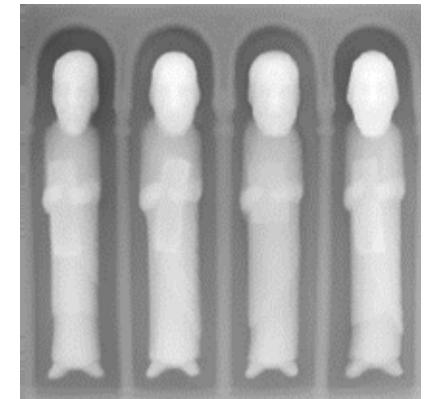
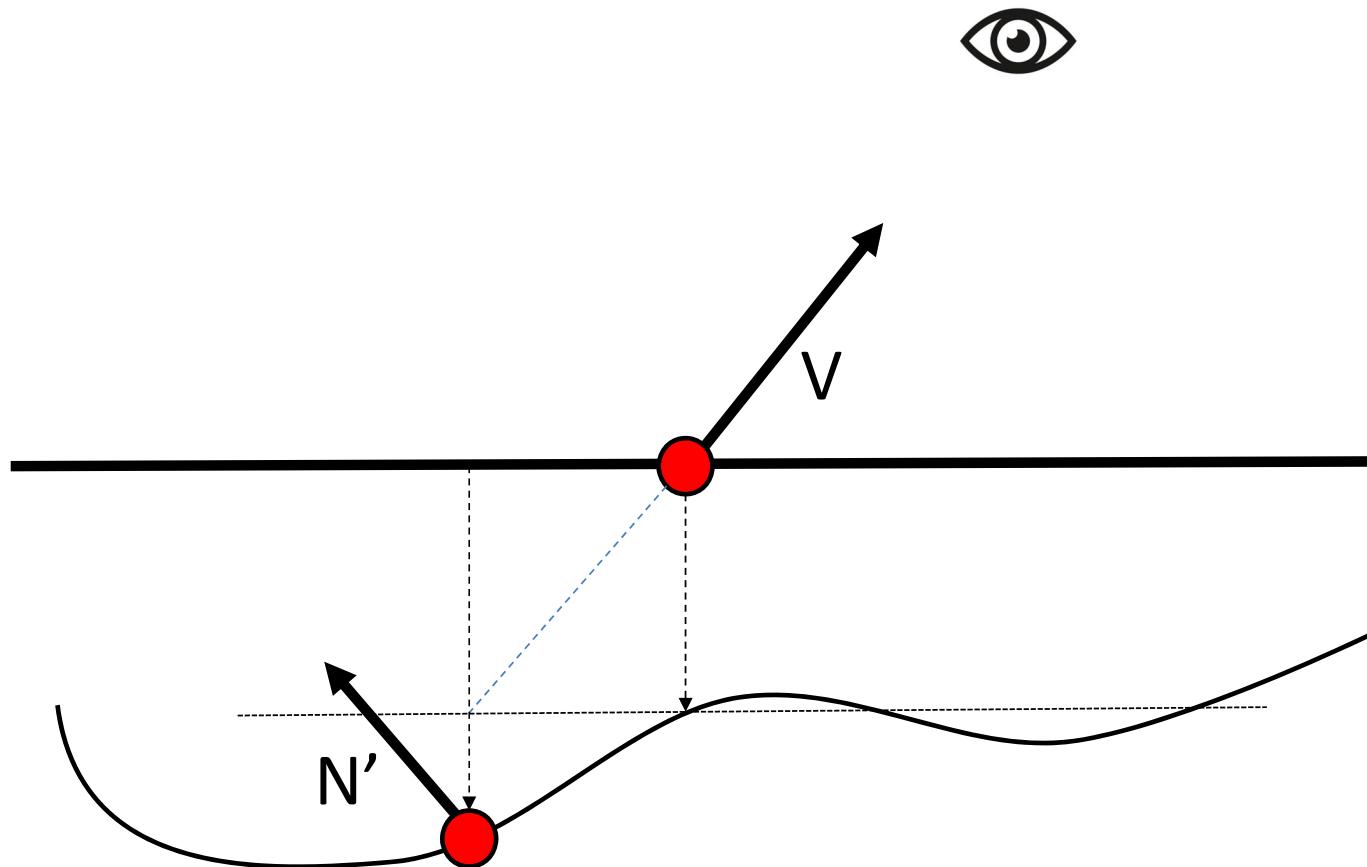


View-motion parallax

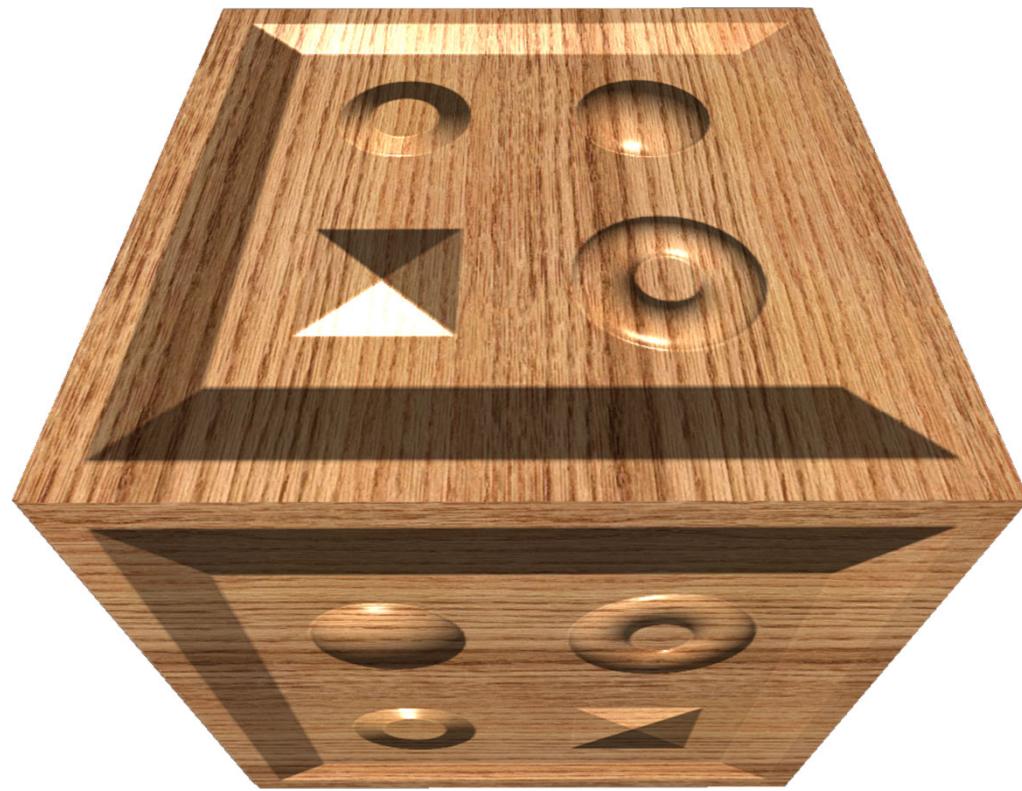


Tècnica	Info a la textura	Ús de la textura	Coords de textura	View parallax	Self-occlusion	Detailed silhouette	On s'aplica	
Color mapping	RGB 3	Kd del material	(s,t)	-	-	-	FS	
Bump mapping	D 1		Modificar la normal	(s,t)	N	N	N	FS
Normal mapping	Normal 3		Modificar la normal	(s,t)	N	N	N	FS
Parallax mapping	Normal + D 3+1 o 4	Modificar la normal	$(s+d_s, t+d_t)$	S	N	N	FS	
Relief mapping	Normal + D 3+1 o 4	Modificar la normal; descartar fragments	$(s+d_s, t+d_t)$	S	S	S	FS!!!	
Displacement mapping	D 1	Desplaçar els vèrtexs un cop subdividits els polígons.	(s,t)	S	S	S	CPU GS TCS+TES	

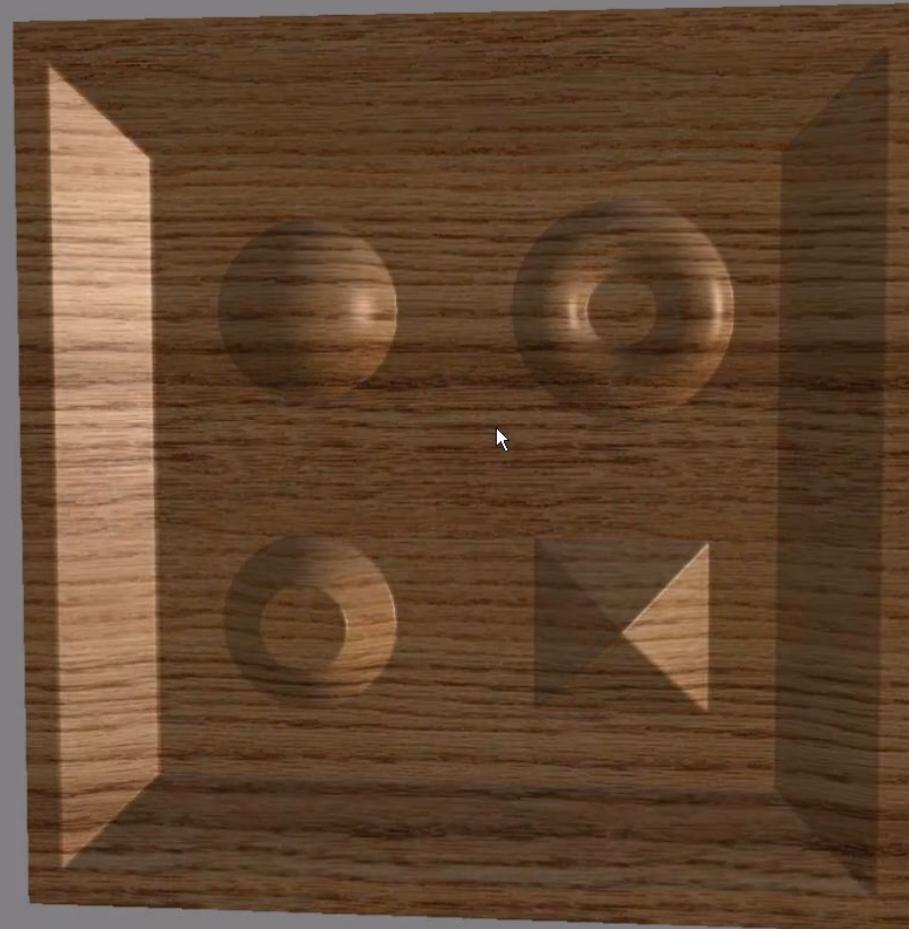
Parallax mapping



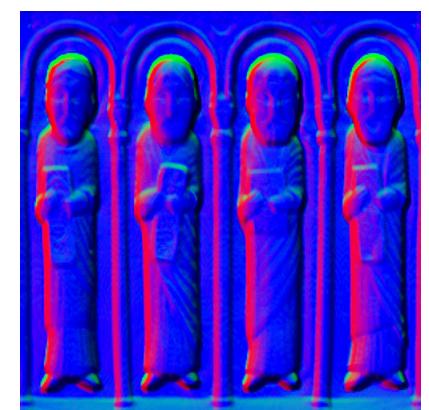
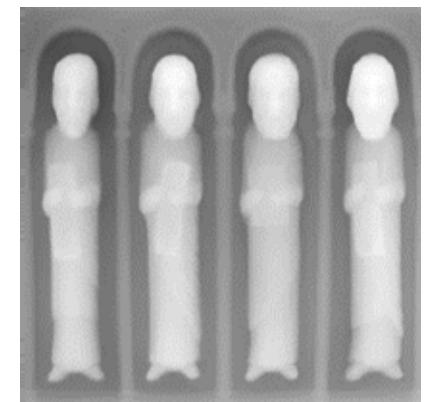
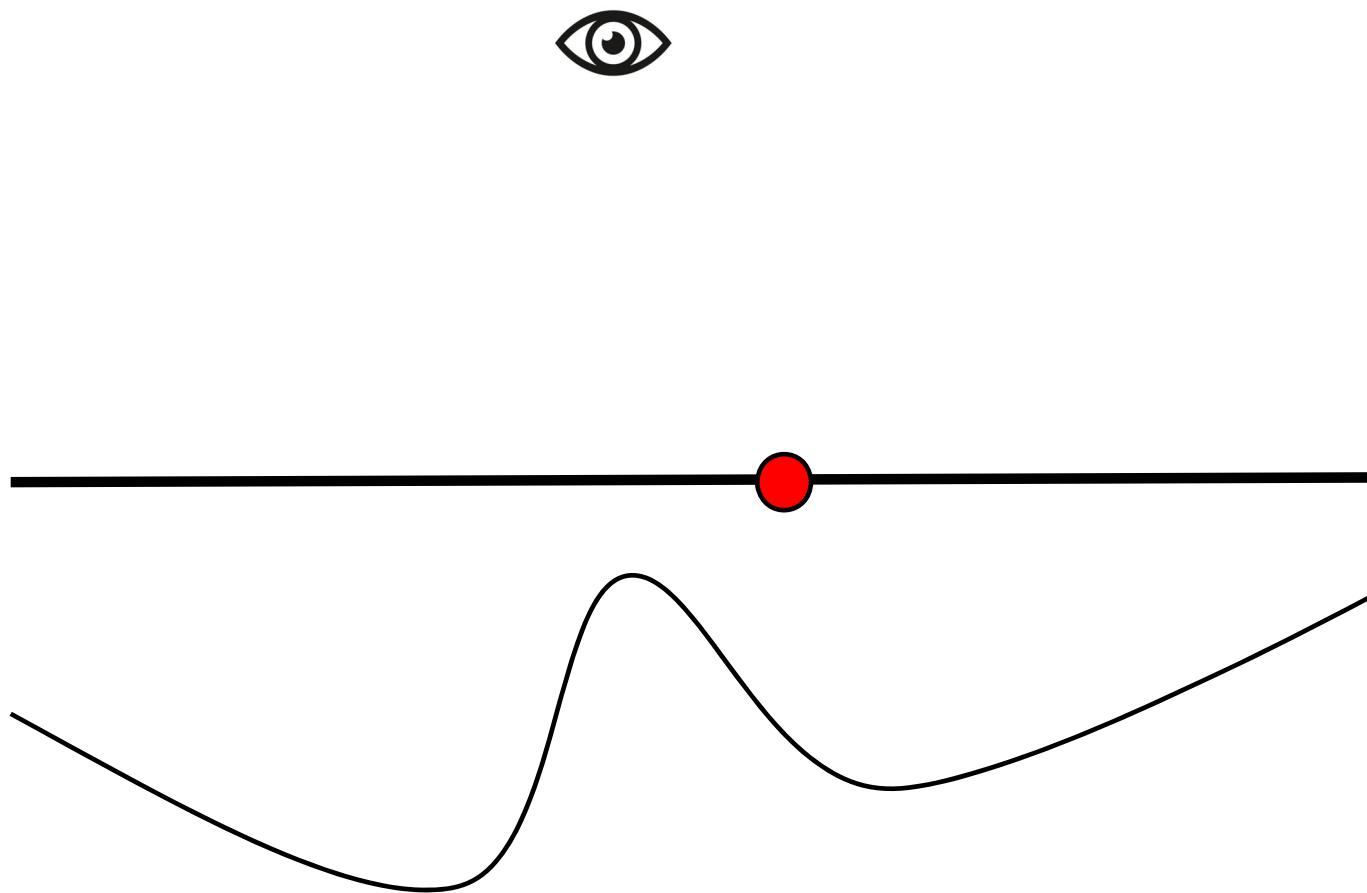
Parallax mapping

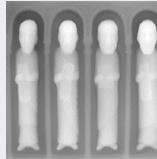
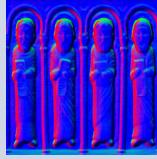


Relief Mapping
File View Render About...
Parallax Mapping
Border Clamp
Depth Bias

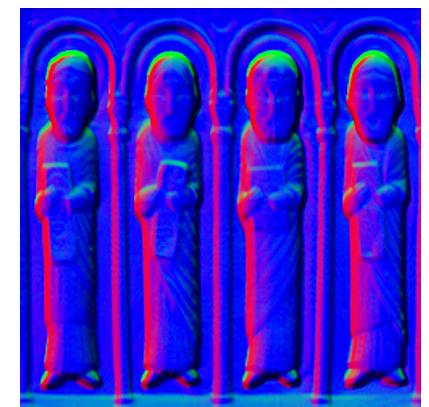
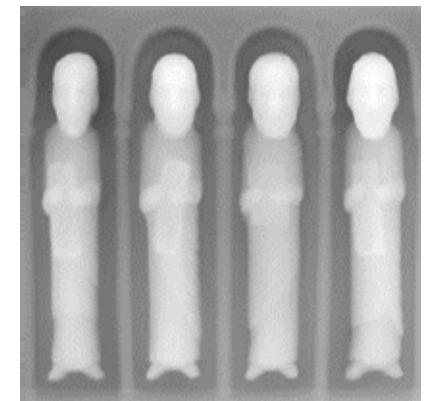
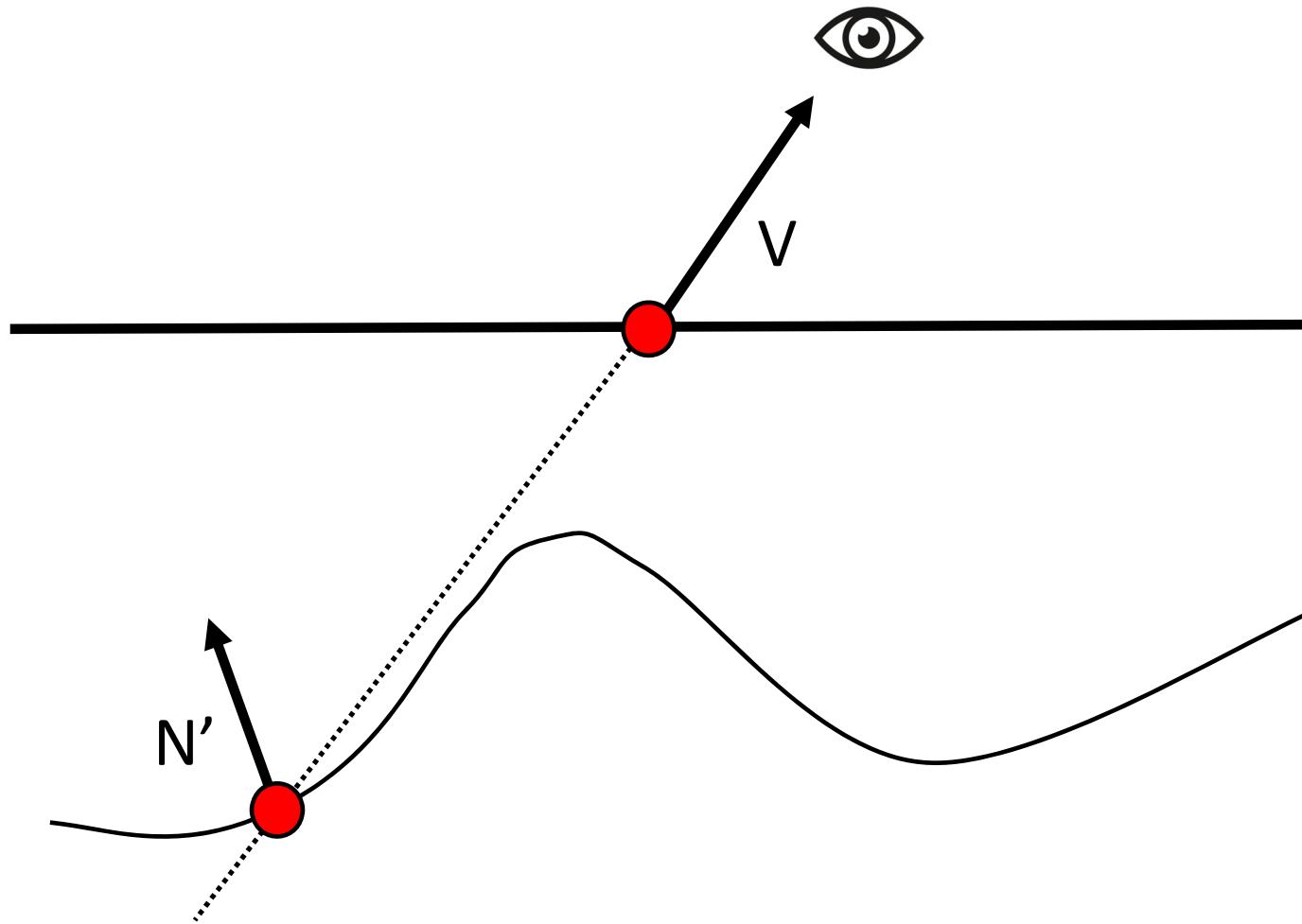


Problema Parallax mapping

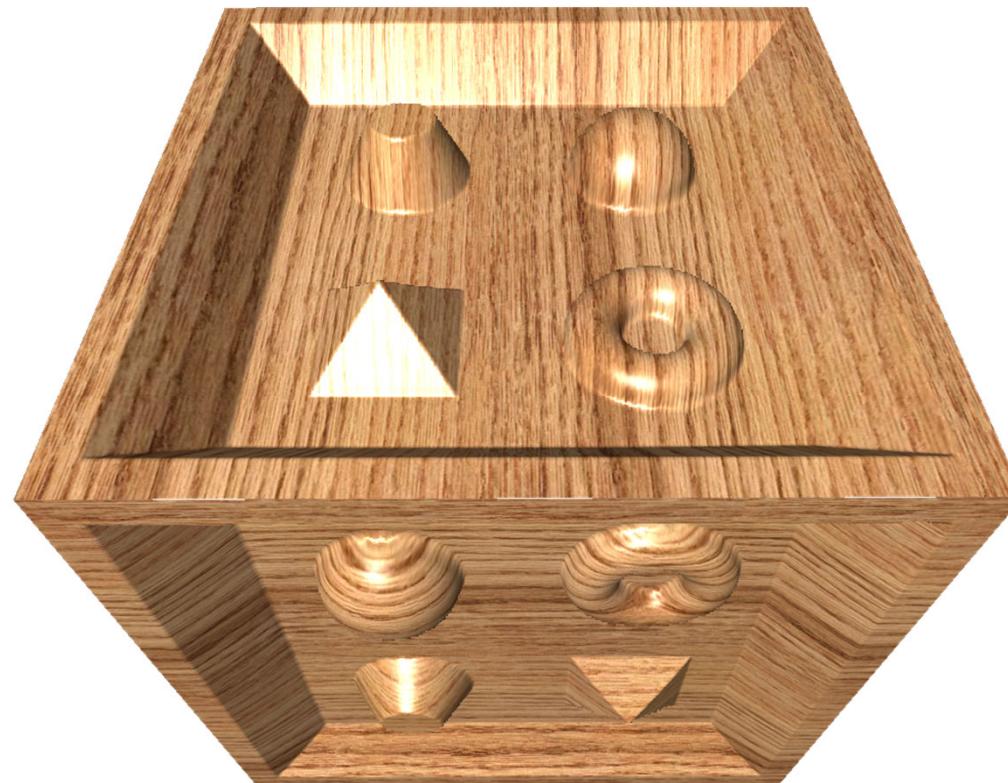


Tècnica	Info a la textura	Ús de la textura	Coords de textura	View parallax	Self-occlusion	Detailed silhouette	On s'aplica	
Color mapping	RGB 3	Kd del material	(s,t)	-	-	-	FS	
Bump mapping	D 1		Modificar la normal	(s,t)	N	N	N	FS
Normal mapping	Normal 3		Modificar la normal	(s,t)	N	N	N	FS
Parallax mapping	Normal + D 3+1 o 4	Modificar la normal	$(s+d_s, t+d_t)$	S	N	N	FS	
Relief mapping	Normal + D 3+1 o 4	Modificar la normal; descartar fragments	$(s+d_s, t+d_t)$	S	S	S	FS!!!	
Displacement mapping	D 1	Desplaçar els vèrtexs un cop subdividits els polígons.	(s,t)	S	S	S	CPU GS TCS+TES	

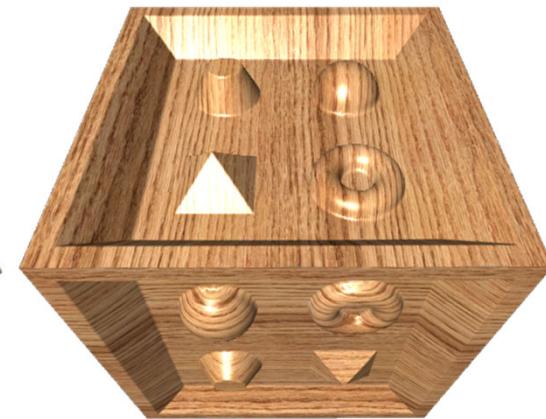
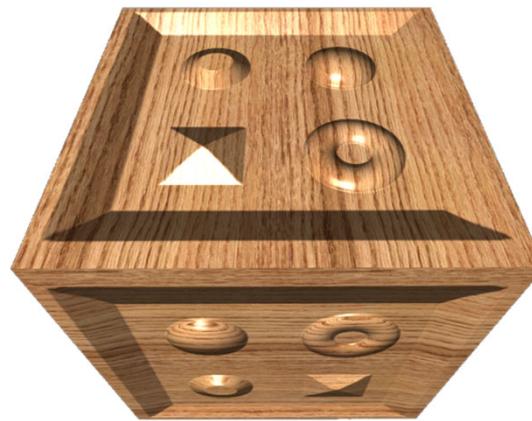
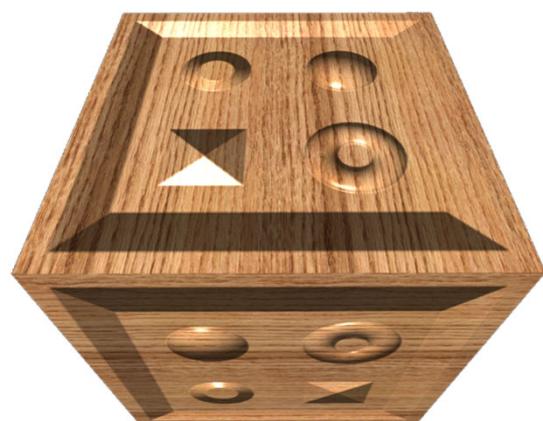
Relief mapping



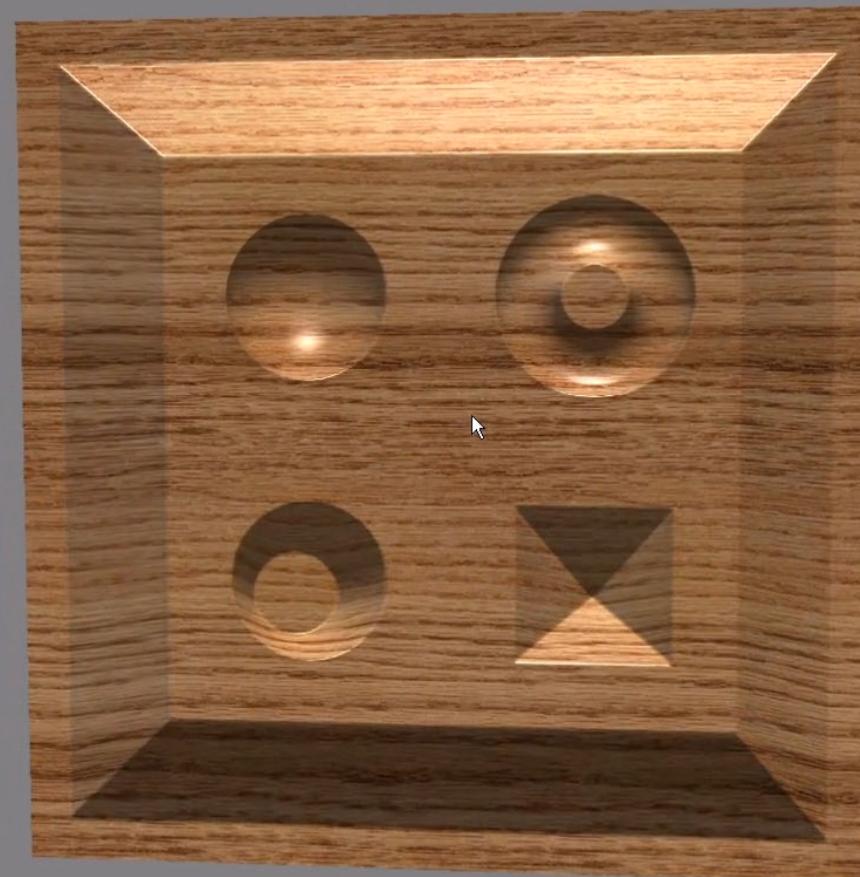
Relief mapping

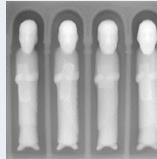
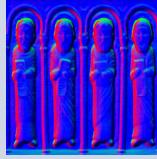


Comparació

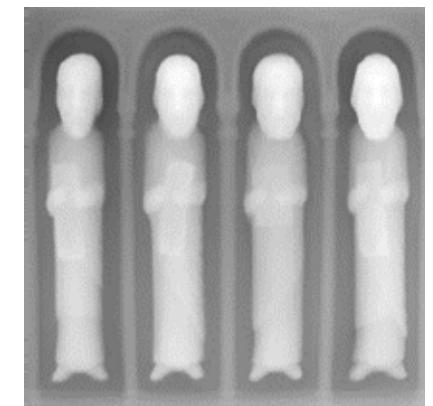
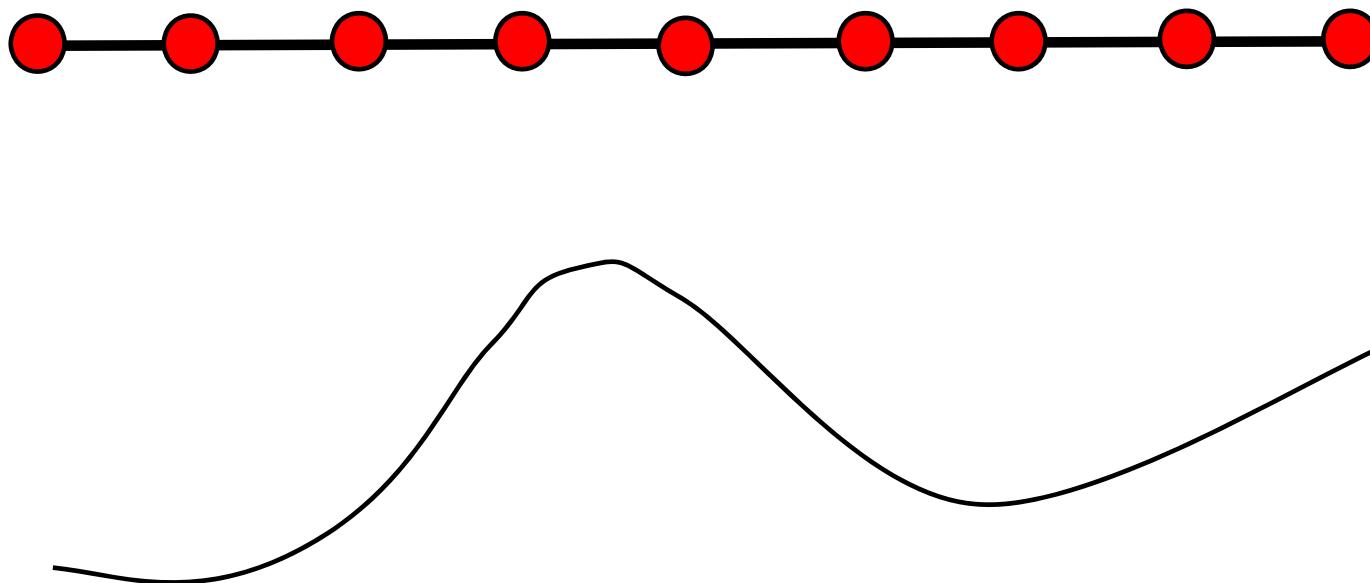


Relief Mapping
File View Render About...
Relief Mapping
Border Clamp
Depth Bias



Tècnica	Info a la textura	Ús de la textura	Coords de textura	View parallax	Self-occlusion	Detailed silhouette	On s'aplica	
Color mapping	RGB 3	Kd del material	(s,t)	-	-	-	FS	
Bump mapping	D 1		Modificar la normal	(s,t)	N	N	N	FS
Normal mapping	Normal 3		Modificar la normal	(s,t)	N	N	N	FS
Parallax mapping	Normal + D 3+1 o 4	Modificar la normal	$(s+d_s, t+d_t)$	S	N	N	FS	
Relief mapping	Normal + D 3+1 o 4	Modificar la normal; descartar fragments	$(s+d_s, t+d_t)$	S	S	S	FS!!!	
Displacement mapping	D 1	Desplaçar els vèrtexs un cop subdividits els polígons.	(s,t)	S	S	S	CPU GS TCS+TES	

Displacement mapping



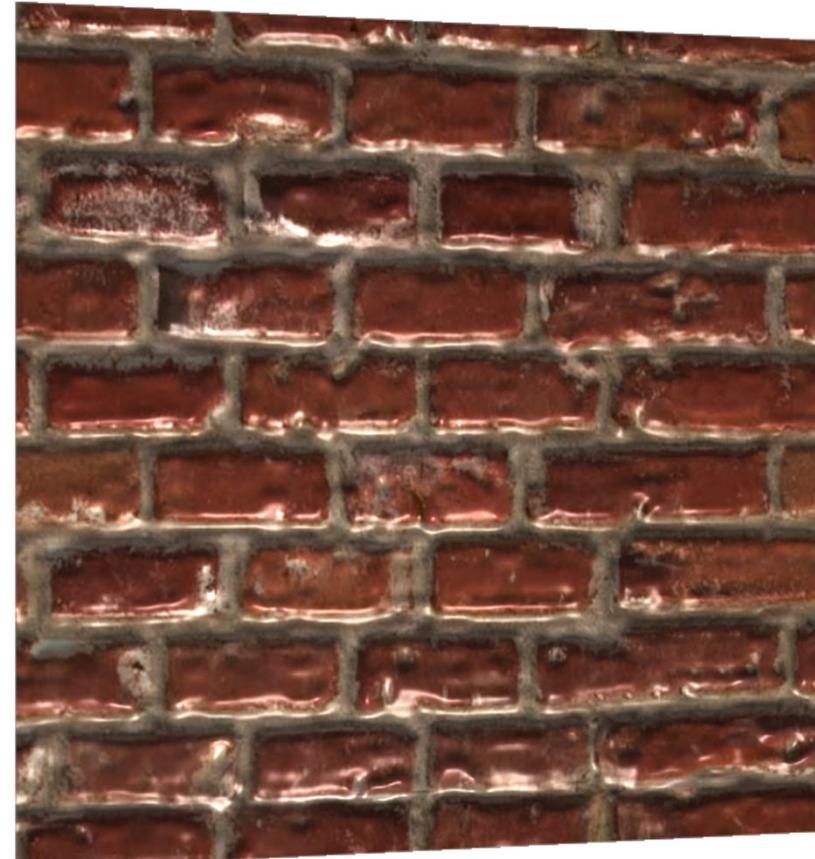
Comparació



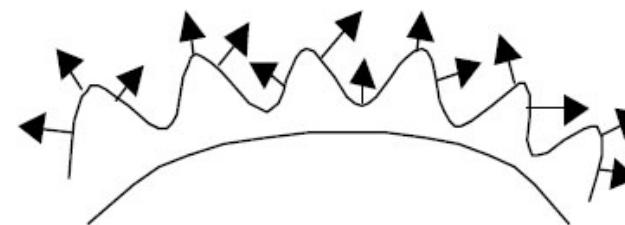
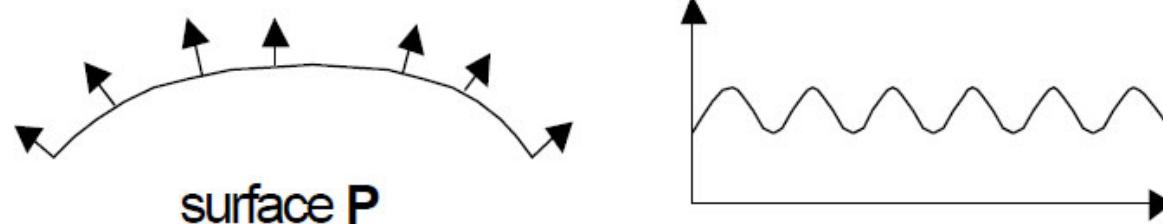
Mark Kilgard. A Practical and Robust Bump-mapping Technique for Today's GPUs. GDC 2000

BUMP MAPPING

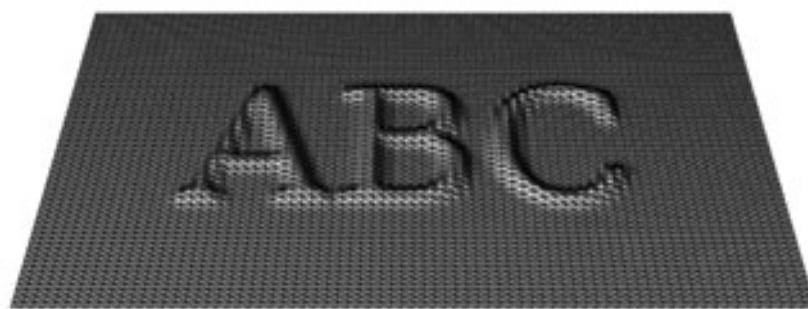
Bump mapping



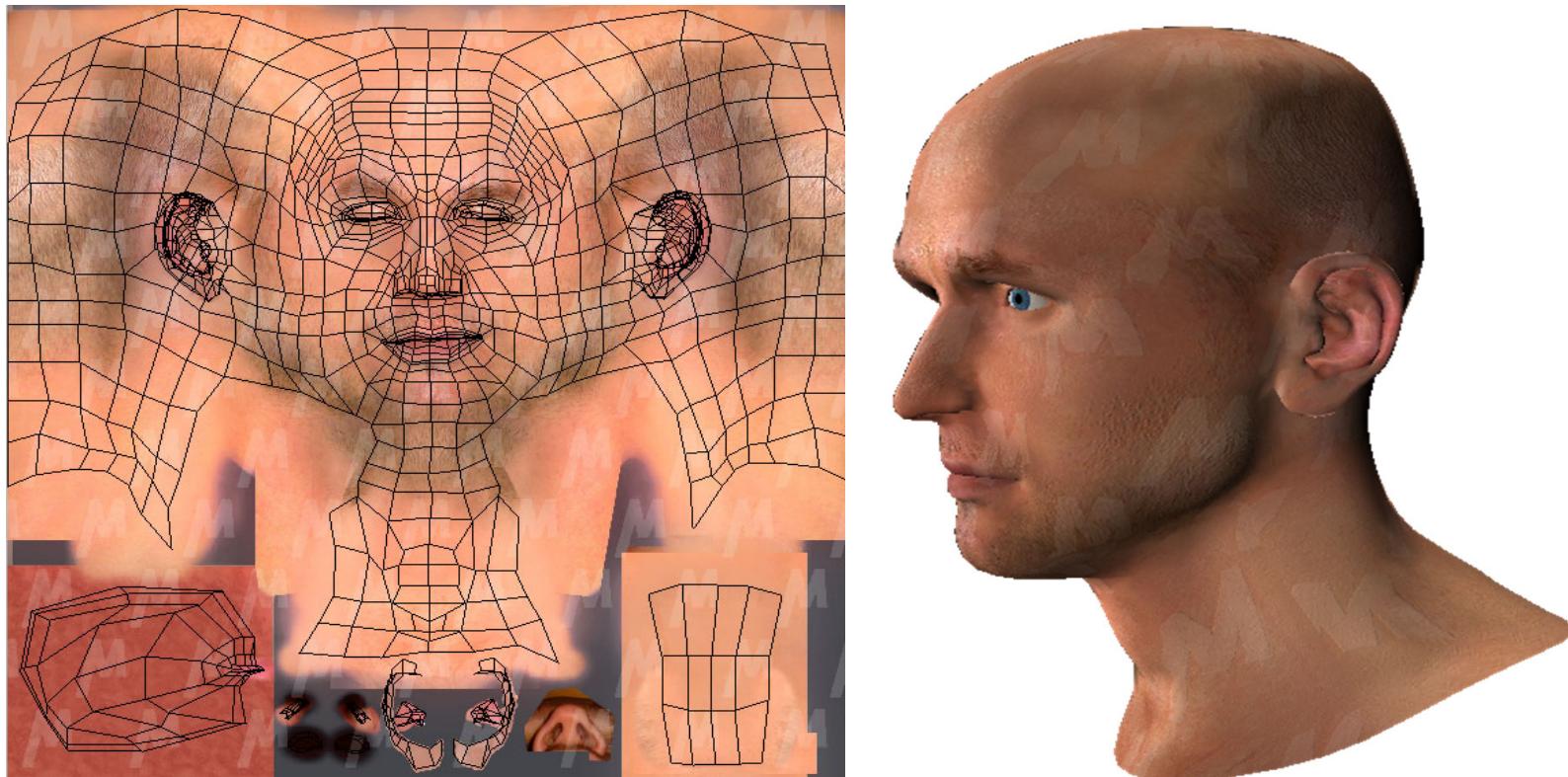
Elements bàsics



Height field



Malla amb coordenades de textura



Eqüacions

$$\mathbf{N}(u, v) = \frac{\partial \mathbf{P}(u, v)}{\partial u} \times \frac{\partial \mathbf{P}(u, v)}{\partial v}$$

$$\mathbf{N}'(u, v) = \frac{\partial \mathbf{P}'(u, v)}{\partial u} \times \frac{\partial \mathbf{P}'(u, v)}{\partial v}$$

$$\mathbf{P}'(u, v) = \mathbf{P}(u, v) + F(u, v) \frac{\mathbf{N}(u, v)}{|\mathbf{N}(u, v)|}$$

Eqüacions

$$\mathbf{N}'(u, v) = \frac{\partial \mathbf{P}'(u, v)}{\partial u} \times \frac{\partial \mathbf{P}'(u, v)}{\partial v} \quad \mathbf{P}'(u, v) = \mathbf{P}(u, v) + F(u, v) \frac{\mathbf{N}(u, v)}{|\mathbf{N}(u, v)|}$$

$$\mathbf{N}' = \left(\frac{\partial \mathbf{P}}{\partial u} + \frac{\partial F}{\partial u} \left(\frac{\mathbf{N}}{|\mathbf{N}|} \right) \right) \times \left(\frac{\partial \mathbf{P}}{\partial v} + \frac{\partial F}{\partial v} \left(\frac{\mathbf{N}}{|\mathbf{N}|} \right) \right) \quad \frac{\partial \mathbf{P}'}{\partial u} = \frac{\partial \mathbf{P}}{\partial u} + \frac{\partial F}{\partial u} \left(\frac{\mathbf{N}}{|\mathbf{N}|} \right) + F \left(\frac{\partial \frac{\mathbf{N}}{|\mathbf{N}|}}{\partial u} \right)$$

$$\mathbf{N}' = \frac{\partial \mathbf{P}}{\partial u} \times \frac{\partial \mathbf{P}}{\partial v} + \frac{\frac{\partial F}{\partial u} \left(\mathbf{N} \times \frac{\partial \mathbf{P}}{\partial v} \right)}{|\mathbf{N}|} + \frac{\frac{\partial F}{\partial v} \left(\frac{\partial \mathbf{P}}{\partial u} \times \mathbf{N} \right)}{|\mathbf{N}|} + \frac{\frac{\partial F}{\partial u} \frac{\partial F}{\partial v} (\mathbf{N} \times \mathbf{N})}{|\mathbf{N}|^2}$$

$$\mathbf{N}' = \mathbf{N} + \frac{\frac{\partial F}{\partial u} \left(\mathbf{N} \times \frac{\partial \mathbf{P}}{\partial v} \right) - \frac{\partial F}{\partial v} \left(\mathbf{N} \times \frac{\partial \mathbf{P}}{\partial u} \right)}{|\mathbf{N}|}$$

Eqüacions - resum

$$\mathbf{N}'(u, v) = \frac{\partial \mathbf{P}'(u, v)}{\partial u} \times \frac{\partial \mathbf{P}'(u, v)}{\partial v}$$

$$\mathbf{P}'(u, v) = \mathbf{P}(u, v) + F(u, v) \frac{\mathbf{N}(u, v)}{|\mathbf{N}(u, v)|}$$

$$\mathbf{N}' = \mathbf{N} + \frac{\frac{\partial F}{\partial u} \left(\mathbf{N} \times \frac{\partial \mathbf{P}}{\partial v} \right) - \frac{\partial F}{\partial v} \left(\mathbf{N} \times \frac{\partial \mathbf{P}}{\partial u} \right)}{|\mathbf{N}|}$$