

Lecture 7 Recap

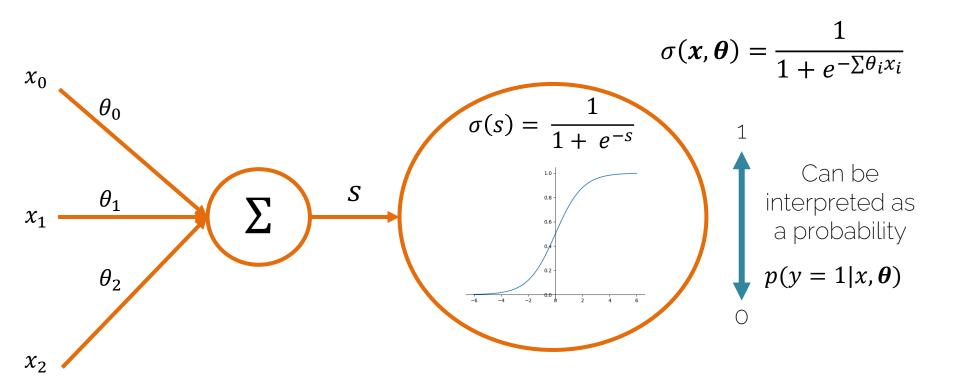
Regression Losses: L2 vs L1

- L2 Loss:
 - $-L^{2} = \sum_{i=1}^{n} (y_{i} f(x_{i}))^{2}$
 - Sum of squared differences (SSD)
 - Prone to outliers
 - Compute-efficient (optimization)
 - Optimum is the mean

- L1 Loss:
 - $-L^{1} = \sum_{i=1}^{n} |y_{i} f(x_{i})|$
 - Sum of absolute differences
 - Robust
 - Costly to compute

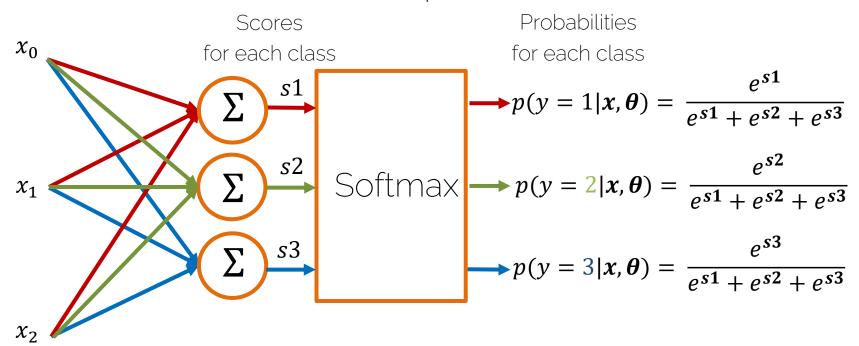
Optimum is the median

Binary Classification: Sigmoid



Softmax Formulation

What if we have multiple classes?



Example: Hinge vs Cross-Entropy

Hinge Loss:
$$L_i = \sum_{k \neq y_i} \max(0, s_k - s_{y_i} + 1)$$

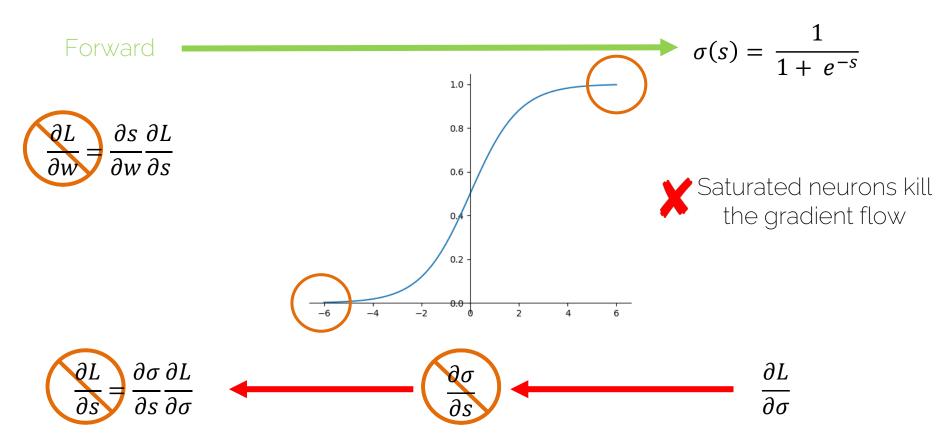
Cross Entropy: $L_i = -\log(\frac{e^{s_{y_i}}}{\sum_k e^{s_k}})$

Cross Entropy :
$$L_i = -\log(\frac{e^{-y_i}}{\sum_k e^{s_k}})$$

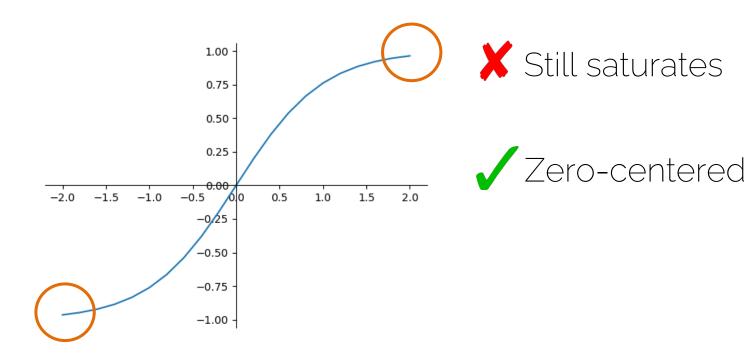
Given the following scores for x_i :		Hinge loss:	Cross Entropy loss:
Model 1	s = [5, -3, 2]	$\max(0, -3 - 5 + 1) + \max(0, 2 - 5 + 1) = 0$	$-\ln\left(\frac{e^5}{e^5 + e^{-3} + e^2}\right) = 0.05$
Model 2	s = [5, 10, 10]	max(0, 10 - 5 + 1) + max(0, 10 - 5 + 1) = 12	$-\ln\left(\frac{e^5}{e^5 + e^{10} + e^{10}}\right) = 5.70$
Model 3	$s = [5, -20, -20]$ $y_i = 0$ - Cross	max(0, -20 - 5 + 1) + max(0, -20 - 5 + 1) = 0 s Entropy *always* wants t	$-\ln\left(\frac{e^5}{e^5+e^{-20}+e^{-20}}\right)$ = 2 * 10 ⁻¹¹ to improve! (loss never 0)

- Hinge Loss saturates.

Sigmoid Activation

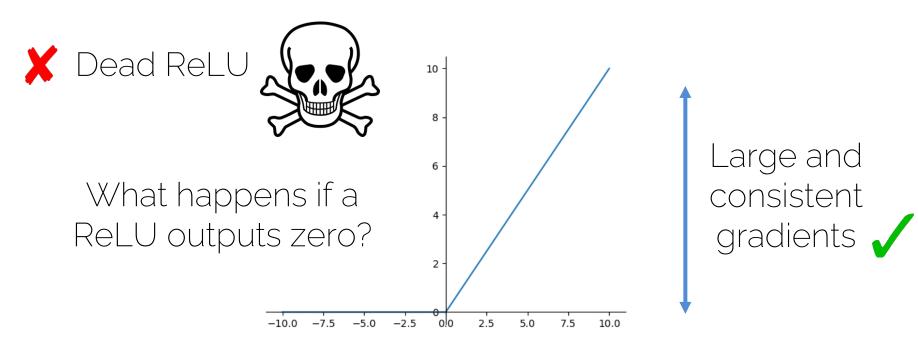


TanH Activation



[LeCun et al. 1991] Improving Generalization Performance in Character Recognition

Rectified Linear Units (ReLU)







[Krizhevsky et al. NeurlPS 2012] ImageNet Classification with Deep Convolutional Neural Networks

Quick Guide

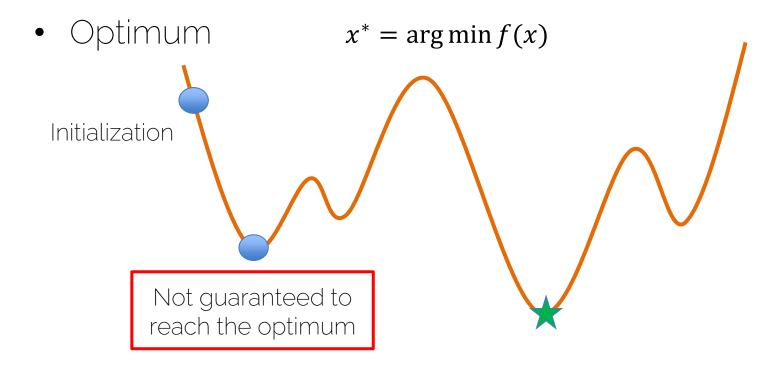
• Sigmoid is not really used.

ReLU is the standard choice.

Second choice are the variants of ReLU or Maxout.

Recurrent nets will require TanH or similar.

Initialization is Extremely Important!



Xavier/Kaiming Initialization

 How to ensure the variance of the output is the same as the input?

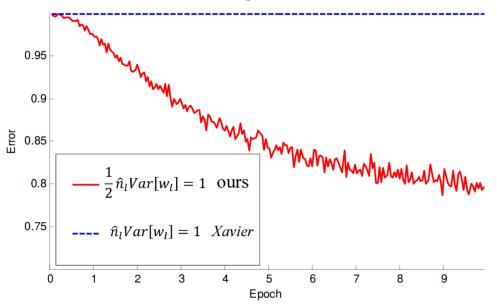
$$(nVar(w)Var(x)) = 1$$

$$Var(w) = \frac{1}{n}$$

ReLU Kills Half of the Data

$$Var(w) = \frac{2}{n}$$

It makes a huge difference!

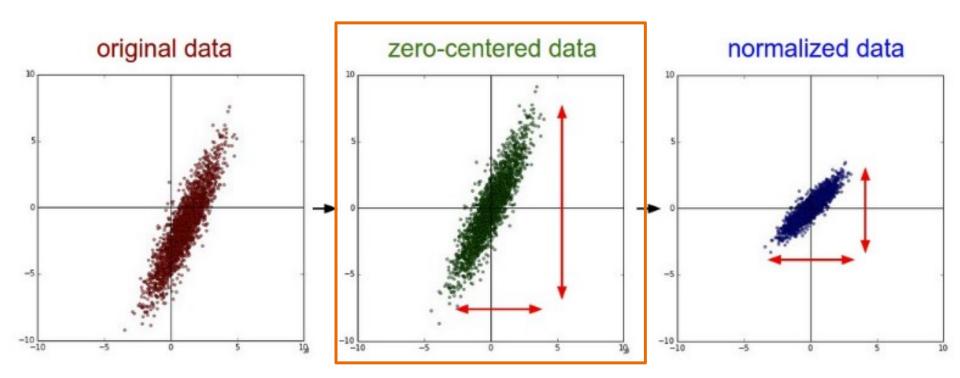




Lecture 8

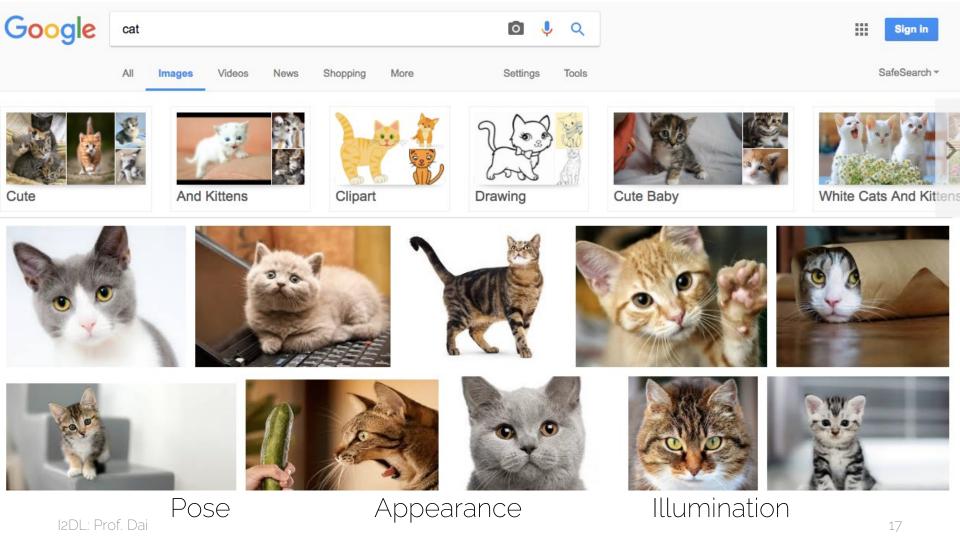


Data Pre-Processing



For images subtract the mean image (AlexNet) or per-channel mean (VGG-Net)

 A classifier has to be invariant to a wide variety of transformations



 A classifier has to be invariant to a wide variety of transformations

 Helping the classifier: synthesize data simulating plausible transformations

a. No augmentation (= 1 image)



224x224



b. Flip augmentation (= 2 images)



224x224



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c. Crop+Flip augmentation (= 10 images)



224x224







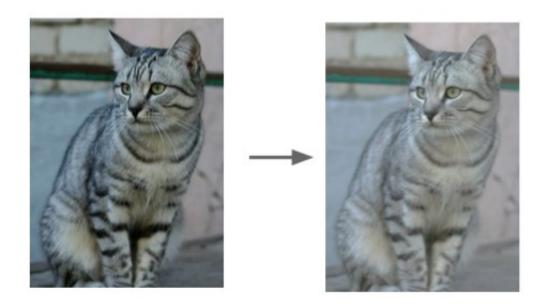




+ flips

Data Augmentation: Brightness

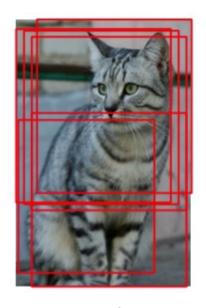
Random brightness and contrast changes



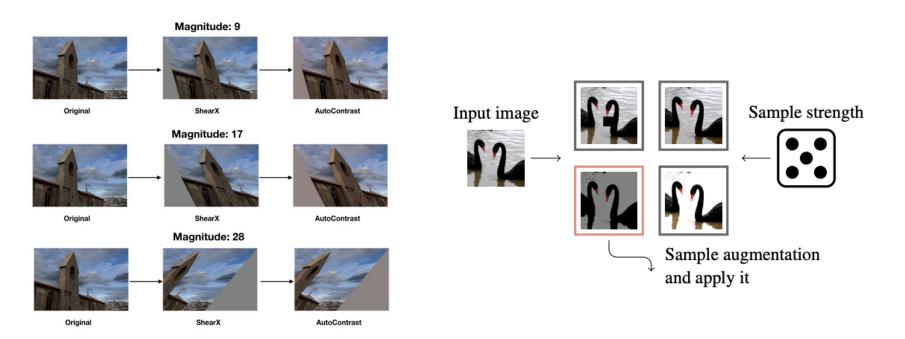
Data Augmentation: Random Crops

- Training: random crops
 - Pick a random L in [256,480]
 - Resize training image, short side L
 - Randomly sample crops of 224x224

- Testing: fixed set of crops
 - Resize image at N scales
 - 10 fixed crops of 224x224: (4 corners + 1 center) × 2 flips



Data Augmentation: Advanced



Cubuk et al., RandAugment, CVPRW 2020

Muller et al., Trivial Augment, ICCV 2021

• When comparing two networks make sure to use the same data augmentation!

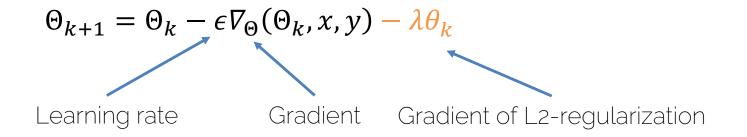
Consider data augmentation a part of your network design



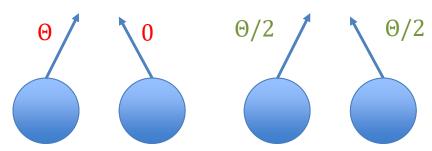
Advanced Regularization

L2 regularization, also (wrongly) called weight decay

L2 regularization

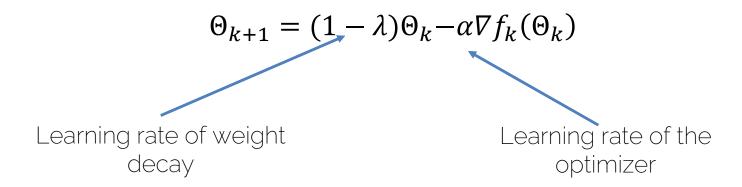


- Penalizes large weights
- Improves generalization



L2 regularization, also (wrongly) called weight decay

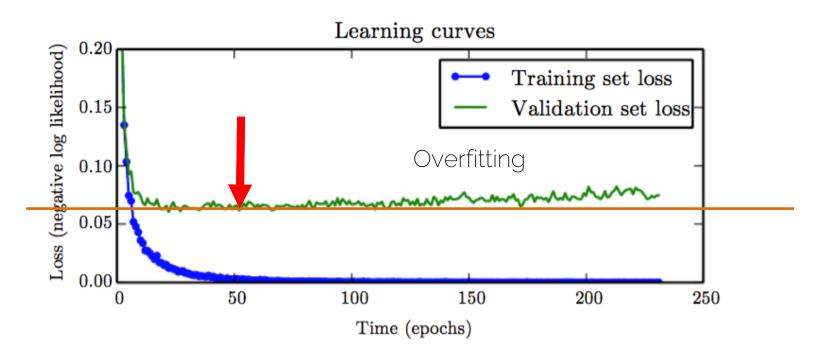
Weight decay regularization



• Equivalent to L2 regularization in GD, but not in Adam.

Loshchilov and Hutter, Decoupled Weight Decay Regularization, ICLR 2019

Early Stopping



27

Bagging and Ensemble Methods

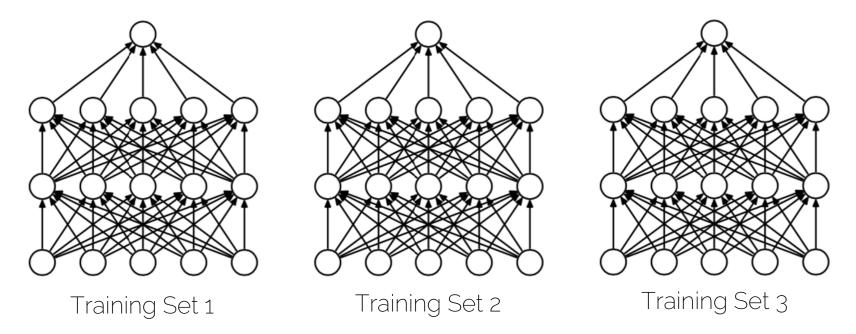
Train multiple models and average their results

 E.g., use a different algorithm for optimization or change the objective function / loss function.

• If errors are uncorrelated, the expected combined error will decrease linearly with the ensemble size

Bagging and Ensemble Methods

Bagging: uses k different datasets (or SGD/init noise)

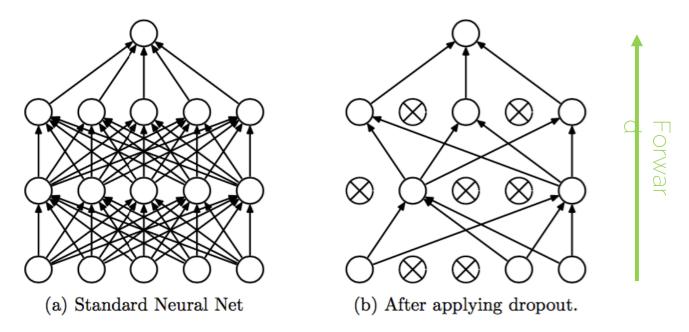




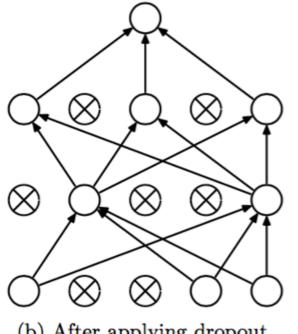
Dropout

Dropout

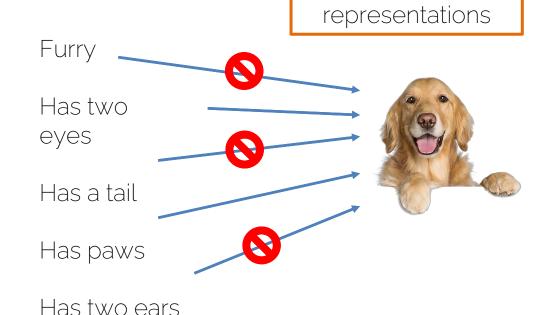
Disable a random set of neurons (typically 50%)



Using half the network = half capacity



(b) After applying dropout.

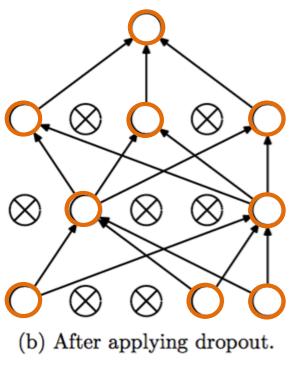


Redundant

- Using half the network = half capacity
 - Redundant representations
 - Base your scores on more features

• Consider it as a model ensemble

Two models in one



Model 1



Model 2





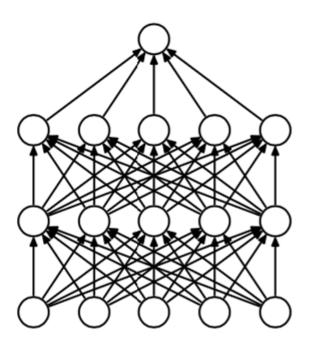
- Using half the network = half capacity
 - Redundant representations
 - Base your scores on more features

- Consider it as two models in one
 - Training a large ensemble of models, each on different set of data (mini-batch) and with SHARED parameters

Reducing co-adaptation between neurons

Dropout: Test Time

• All neurons are "turned on" - no dropout



Conditions at train and test time are not the same

PyTorch: model.train() and model.eval()

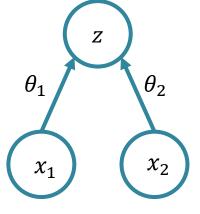
Dropout: Test Time

Dropout probability

Test:

 $z = (\theta_1 x_1 + \theta_2 x_2) \cdot p$

• Train:



Weight scaling inference rule

$$E[z] = \frac{1}{4}(\theta_1 0 + \theta_2 0) + \theta_1 x_1 + \theta_2 0 + \theta_1 0 + \theta_2 x_2 + \theta_1 x_1 + \theta_2 x_2)$$

$$= \frac{1}{2}(\theta_1 x_1 + \theta_2 x_2)$$

Dropout: Before

Efficient bagging method with parameter sharing

• Try it!

 Dropout reduces the effective capacity of a model, but needs more training time

• Efficient regularization method, can be used with L2

Dropout: Nowadays

- Usually does not work well when combined with batch-norm.
- Training takes a bit longer, usually 1.5x
- But, can be used for uncertainty estimation.
- Monte Carlo dropout (Yarin Gal and Zoubin Ghahramani series of papers).

Monte Carlo Dropout

- Neural networks are massively overconfident.
- We can use dropout to make the softmax probabilities more calibrated.
- Training: use dropout with a low p (0.1 or 0.2).
- Inference, run the same image multiple times (25-100), and average the results.

Gal et al., Bayesian Convolutional Neural Networks with Bernoulli Approximate Variational Inference, ICLRW 2015 Gal and Ghahramani, Dropout as a Bayesian approximation, ICML 2016 Gal et al., Deep Bayesian Active Learning with Image Data, ICML 2017 Gal, Uncertainty in Deep Learning, PhD thesis 2017



Batch Normalization: Reducing Internal Covariate Shift

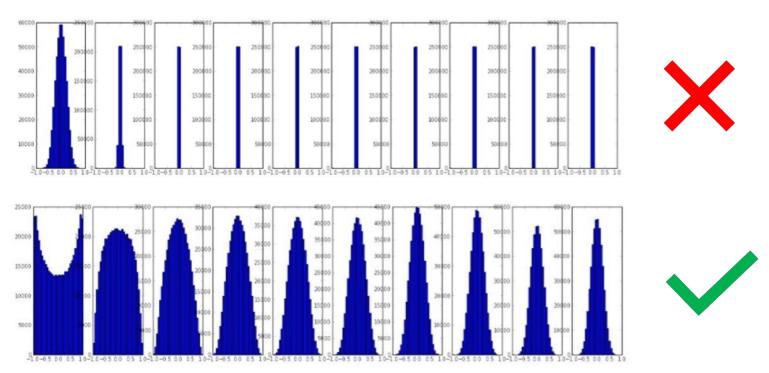


Batch Normalization: Reducing Internal Covariate Shift

What is internal covariate shift, by the way?

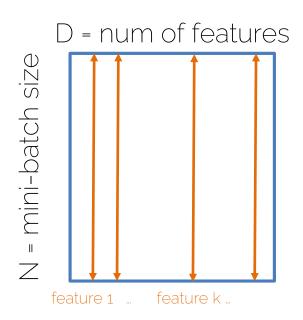
Our Goal

All we want is that our activations do not die out



Batch Normalization
Unit Gaussian as Input and Unit Gausian as Dutput

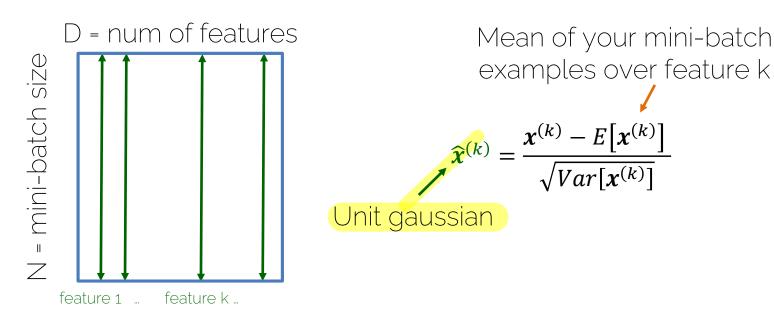
- Wish: Unit Gaussian activations (in our example)
- Solution: let's do it



Mean of your mini-batch examples over feature k

$$\widehat{\boldsymbol{x}}^{(k)} = \frac{\boldsymbol{x}^{(k)} - E[\boldsymbol{x}^{(k)}]}{\sqrt{Var[\boldsymbol{x}^{(k)}]}}$$

 In each dimension of the features, you have a unit gaussian (in our example)

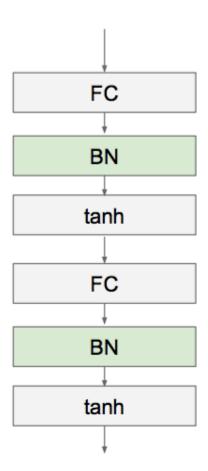


 In each dimension of the features, you have a unit gaussian (in our example)

 For NN in general, BN normalizes the mean and variance of the inputs to your activation functions

BN Layer

 A layer to be applied after Fully Connected (or Convolutional) layers and before non-linear activation functions



1. Normalize

$$\widehat{\boldsymbol{x}}^{(k)} = \frac{\boldsymbol{x}^{(k)} - E[\boldsymbol{x}^{(k)}]}{\sqrt{Var[\boldsymbol{x}^{(k)}]}}$$
 Differentiable function so we can backprop through it...

2. Allow the network to change the range

$$y^{(k)} = \gamma^{(k)} \widehat{x}^{(k)} + \beta^{(k)}$$
 These parameters will be optimized during backprop

1. Normalize

$$\widehat{\boldsymbol{x}}^{(k)} = \frac{\boldsymbol{x}^{(k)} - E[\boldsymbol{x}^{(k)}]}{\sqrt{Var[\boldsymbol{x}^{(k)}]}}$$

• 2. Allow the network to change the range

The network can learn to undo the normalization

$$\gamma^{(k)} = \sqrt{Var[\mathbf{x}^{(k)}]}$$
$$\beta^{(k)} = E[\mathbf{x}^{(k)}]$$



 Ok to treat dimensions separately? Shown empirically that even if features are not correlated, convergence is still faster with this method

BN: Train vs Test

 Train time: mean and variance is taken over the minibatch

$$\widehat{\boldsymbol{x}}^{(k)} = \frac{\boldsymbol{x}^{(k)} - E[\boldsymbol{x}^{(k)}]}{\sqrt{Var[\boldsymbol{x}^{(k)}]}}$$

- Test-time: what happens if we can just process one image at a time?
 - No chance to compute a meaningful mean and variance

BN: Train vs Test

Training: Compute mean and variance from mini-batch 1,2,3 ...

Testing: Compute mean and variance by running an exponentially weighted averaged across training minibatches. Use them as σ_{test}^2 and μ_{test} .

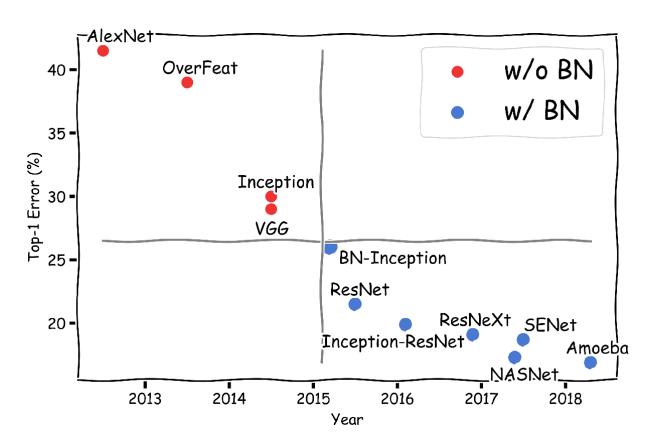
$$Var_{running} = \beta_m * Var_{running} + (1 - \beta_m) * Var_{minibatch}$$
 $\mu_{running} = \beta_m * \mu_{running} + (1 - \beta_m) * \mu_{minibatch}$
 β_m : momentum (hyperparameter)

BN: What do you get?

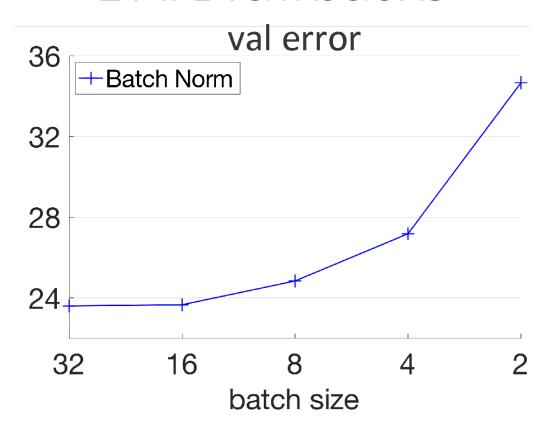
 Very deep nets are much easier to train, more stable gradients

 A much larger range of hyperparameters works similarly when using BN

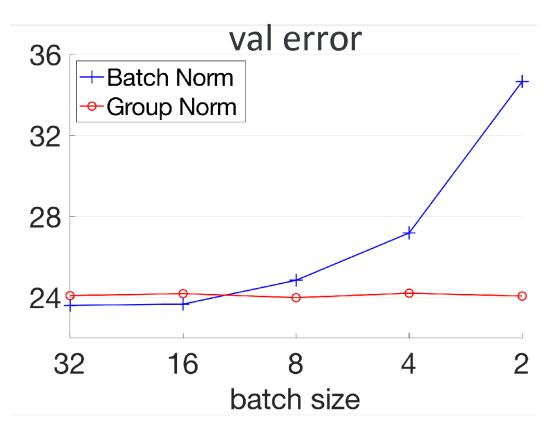
BN: A Milestone



BN: Drawbacks

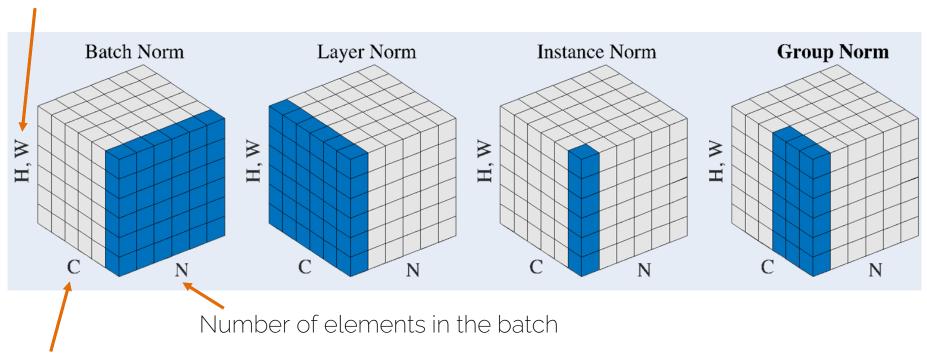


Other Normalizations



Other Normalizations

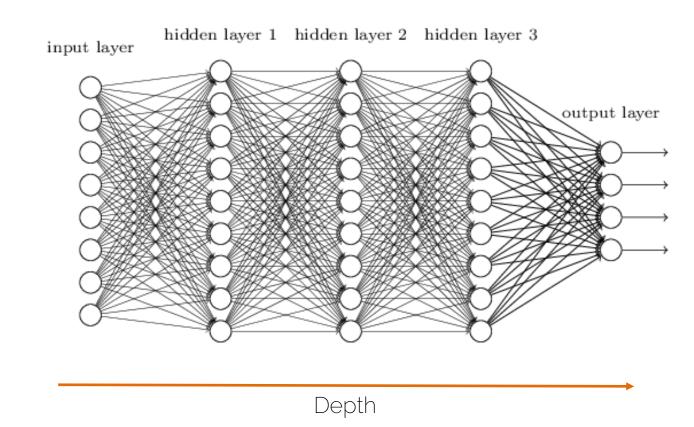
Image size



Number of channels



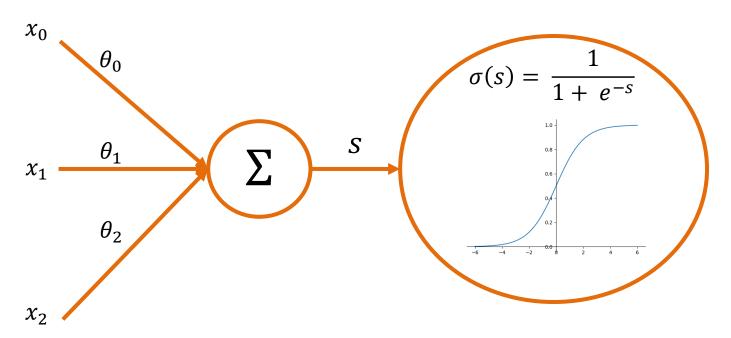
What We Know



I2DL: Prof. Dai

60

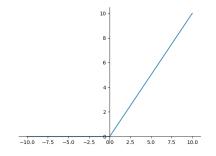
Concept of a 'Neuron'



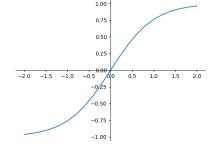
Activation Functions (non-linearities)

• Sigmoid: $\sigma(x) = \frac{1}{(1+e^{-x})^{\frac{0.8}{0.6}}}$

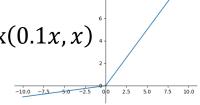
• ReLU: max(0, x)



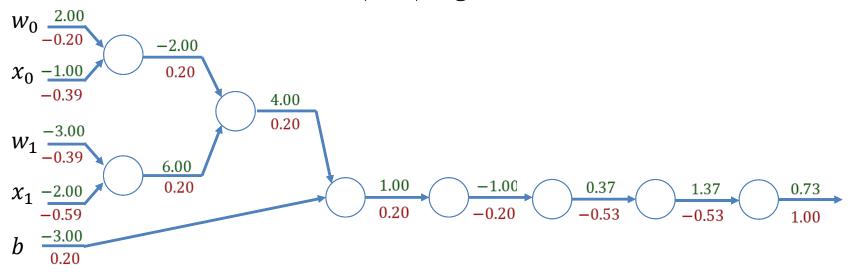
• TanH: tanh(x)



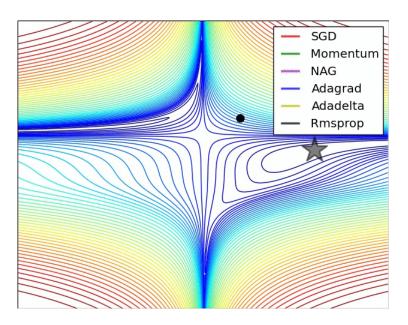
Leaky ReLU: max(0.1x, x)



Backpropagation



SGD Variations (Momentum, etc.)



Data Augmentation

a. No augmentation (= 1 image)







b. Flip augmentation (= 2 images)









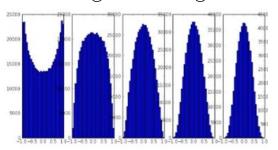
Weight Regularization

e.g.,
$$L^2$$
-reg: $R^2(\boldsymbol{W}) = \sum_{i=1}^N w_i^2$

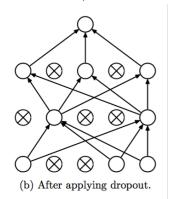
Batch-Norm

$$\widehat{\boldsymbol{x}}^{(k)} = \frac{\boldsymbol{x}^{(k)} - E[\boldsymbol{x}^{(k)}]}{\sqrt{Var[\boldsymbol{x}^{(k)}]}}$$

Weight Initialization (e.g., Kaiming)



Dropout



Why not simply more layers?

- Neural nets with at least one hidden layer are universal function approximators.
- But generalization is another issue.
- Why not just go deeper and get better?
 - No structure!!
 - It is just brute force!
 - Optimization becomes hard
 - Performance plateaus / drops!
- We need more! More means CNNs, RNNs and eventually Transformers.



See you next week!

References

- Goodfellow et al. "Deep Learning" (2016),
 - Chapter 6: Deep Feedforward Networks
- Bishop "Pattern Recognition and Machine Learning" (2006),
 - Chapter 5.5: Regularization in Network Nets
- http://cs231n.github.io/neural-networks-1/
- http://cs231n.github.io/neural-networks-2/
- http://cs231n.github.io/neural-networks-3/