/

Congratulations! You passed!

Next Item



1/1 point

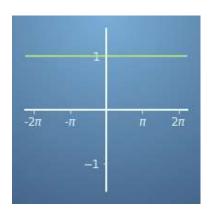
1

As mentioned in the previous video, the Taylor series approximation can also be viewed as a power series, in which these approximations are used to build functions that are often simpler and easier to evaluate, particularly when using numerical methods. In the following questions, we are looking at developing our understanding of how the increasing order of a power series allows us to develop further information of a function.

Below are three graphs highlighting the zeroth, second and fourth order approximations of a common trigonometric function. Observe how increasing the number of approximations in the power series begins to build a better approximation, and determine which function these approximations represent.

Zeroth order approximation:

$$f_0(x)=1$$



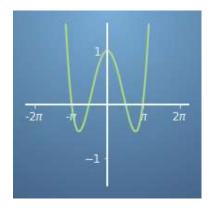
Second order approximation:

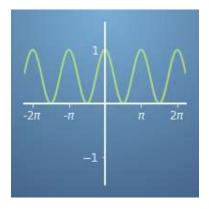
$$f_2(x)=1-\frac{x^2}{2}$$



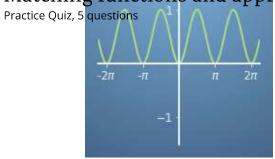
Fourth order approximation:

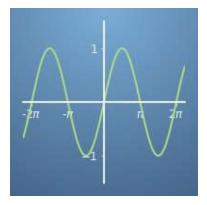
$$f_4(x) = 1 - \frac{x^2}{2} + \frac{x^4}{24}$$

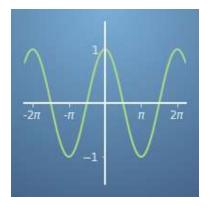




$$\bigcirc \quad f(x) = \sin^2(x)$$







Correct

The function $f(x)=\cos(x)$ is symmetric about the line x=0. Furthermore our approximation of this function is when x=0, known as a Maclaurin series. At the point x=0, f(0)=1 which is shown in the zeroth order approximation.

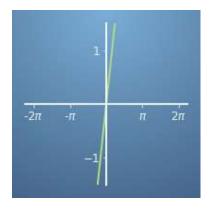
5/5 points (100%)

2.

Below are three graphs highlighting the first, third and fifth order approximations of a common trigonometric Matching dunction shapped approximations the function, and determine which function, these practice principles in the processing of the process of the

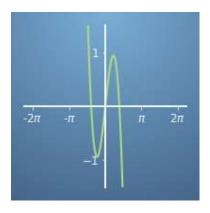
First Order:

$$f_1(x)=2x$$



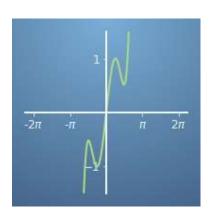
Third Order:

$$f_3(x)=2x-rac{4x^3}{3}$$

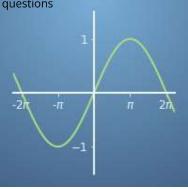


Fifth Order:

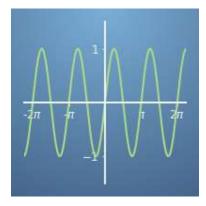
$$f_5(x)=2x-rac{4x^3}{3}+rac{4x^5}{15}$$



Practice Quiz, 5 questions

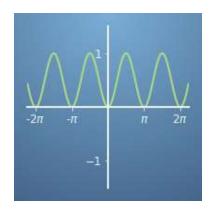


$$f(x) = \sin(2x)$$

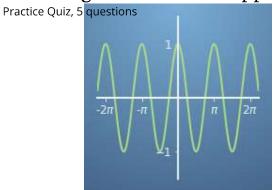


Correct

The function $f(x)=\sin(2x)$ has rotational symmetry about the origin. Furthermore, we can see that the period is much shorter, also evident from the three approximations shown.



 $f(x) = \cos(2x)$ Matching functions and approximations

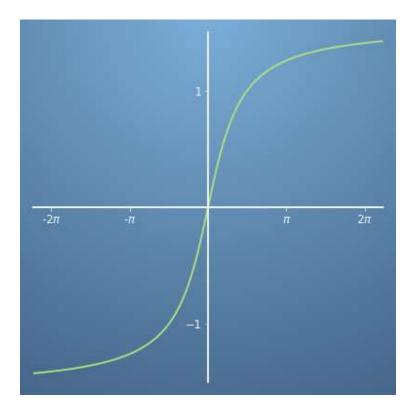


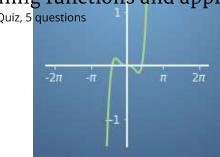
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1/1 point

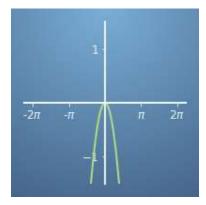
3.

The graph below shows the function $f(x) = \tan^{-1}(x)$, select all the power series approximations that can be used to obtain an approximation for this function.

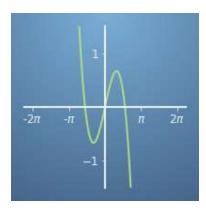




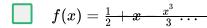
Un-selected is correct

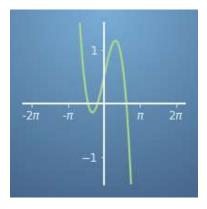


Un-selected is correct



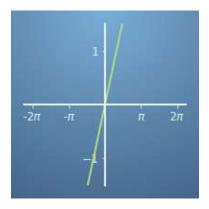
Matching functions and approximations practice We, same this approximation goes through the origin and also looks as if it fits the function we points (100%) between -0.5 < x < 0.5.





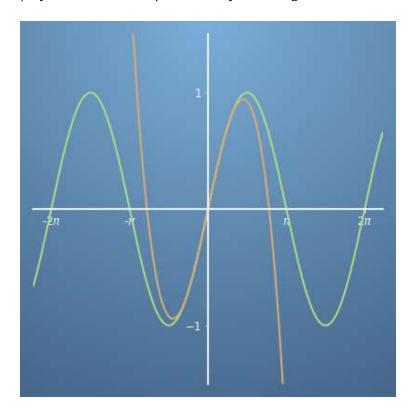
Un-selected is correct

$$f(x) = x \dots$$



We can see this approximation goes through the origin and also looks as if it fits the function well between -0.5 < x < 0.5. As this is a linear function, this is a first-order approximation.

The sinusoidal function $f(x)=\sin(x)$ (green line) centered at x=0 is shown in the graph below. The Matching function of a province for the province of the p



- Zeroth Order
- First Order
- Third Order

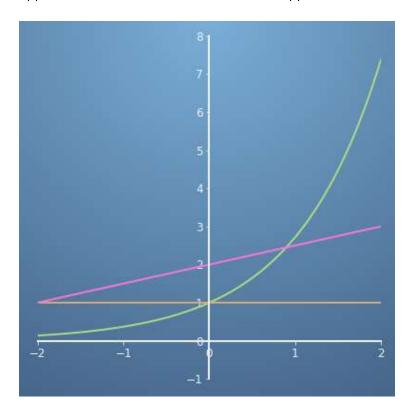
Correct

The highest power of x in the approximation is 3, therefore this approximation is a third order approximation.

- Fifth Order
- None of the above



1/1 point The graph below shows the function $f(x)=e^x$ (green line), the exponential function so widely used in Matciples and x approximation for the points (100%) Practices with function, centred at x=0. Determine if the pink line shown on the graph is, in fact, an approximation and if so, what order is this approximation.



First Order

Second Order

Third Order

Not a correct approximation

Correct

The approximation shown is not tangent to this point and is, therefore, a poor approximation of the function.



Matching functions and approximations Practice Quiz, 5 questions

5/5 points (100%)