

# CS61B Lecture #4: Simple Pointer Manipulation

**Recreation** Prove that for every acute angle  $\alpha > 0$ ,

$$\tan \alpha + \cot \alpha \geq 2$$

## Announcements

- Today: More pointer hacking.
- Handing in labs and homework: We'll be lenient about accepting late homework and labs for lab1, lab2, and hw0. Just get it done: part of the point is getting to understand the tools involved. We will **not** accept submissions by email.
- We will feel free to interpret the absence of a central repository for you or a lack of a lab1 submission from you as indicating that you intend to drop the course.
- HW1 to be released tonight (roughly).
- Project 0 to be released Friday.

# Small Test of Understanding

- In Java, the keyword `final` in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {  
  
    private final IntList aList = new IntList(0, null);  
  
    public void modify(int k) {  
        this.aList.head = k;  
    }  
}
```

Why or why not?

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Why or why not?

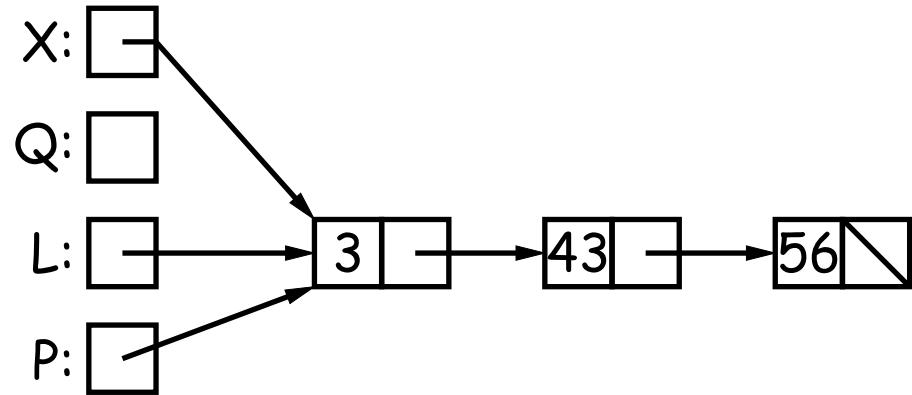
**Answer:** This is *valid*. Although `modify` changes the `head` variable of the object pointed to by `aList`, it does *not* modify the contents of `aList` itself (which is a pointer).

# Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
        p.head += n;
    return L;
}
```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```

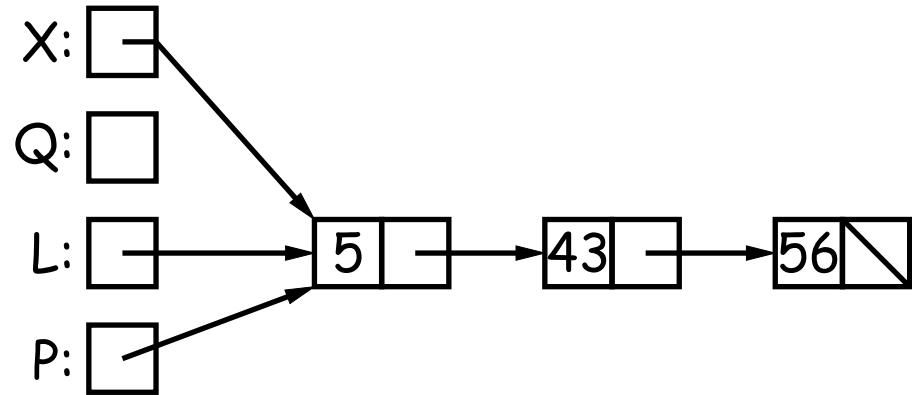


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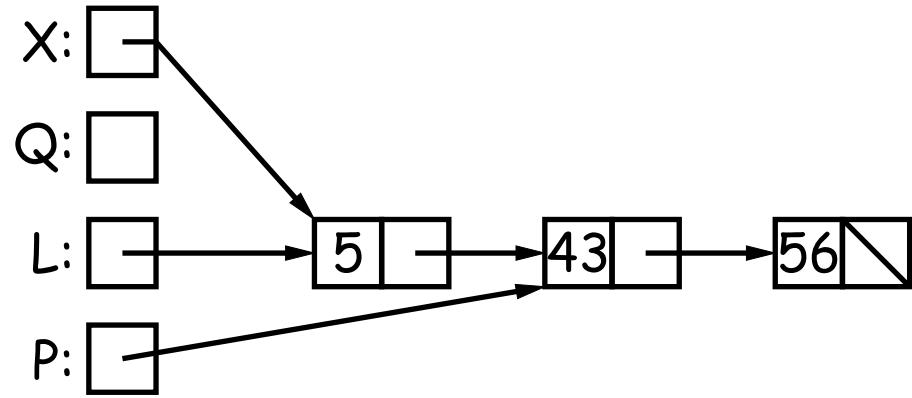


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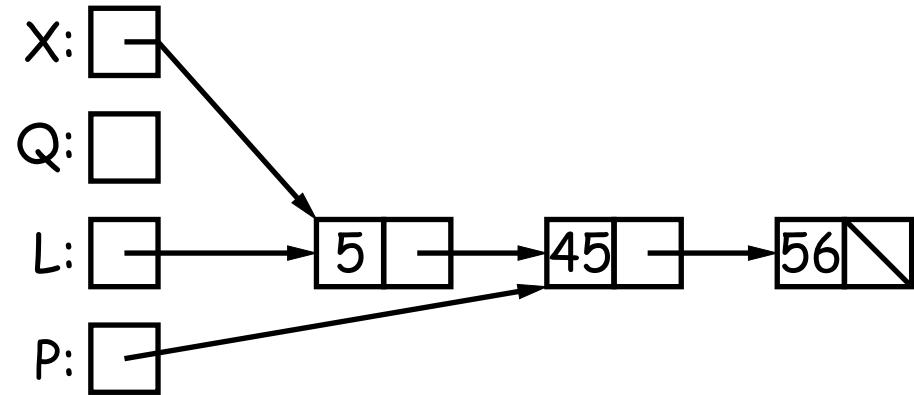


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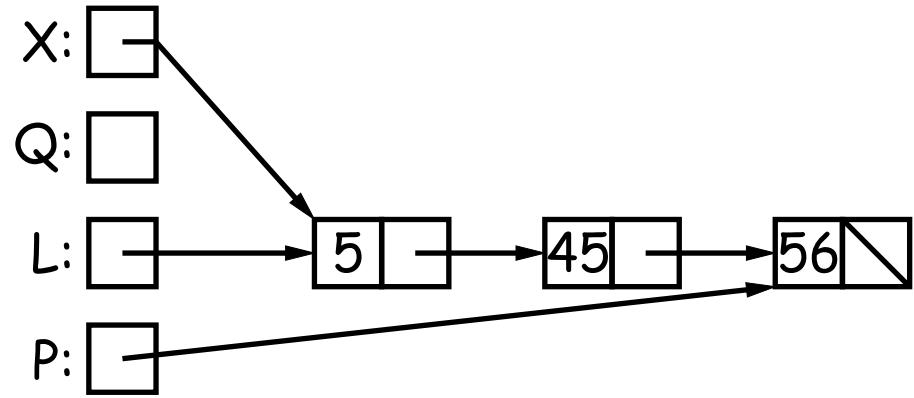


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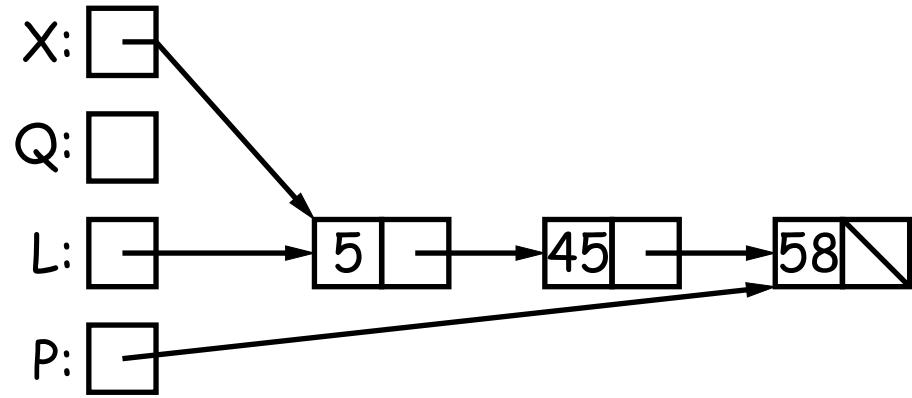


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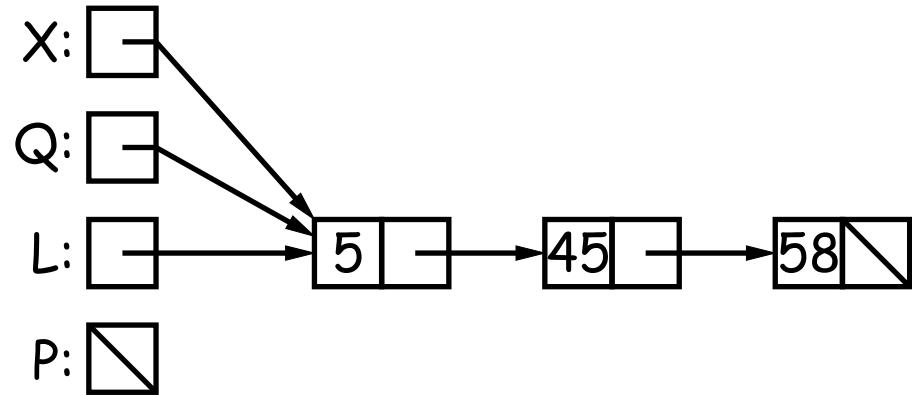


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static IntList dincrList(IntList L, int n)
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    return L;
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## Another Example: Non-destructive List Deletion

If  $L$  is the list  $[2, 1, 2, 9, 2]$ , we want  $\text{removeAll}(L, 2)$  to be the new list  $[1, 9]$ .

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L!=null, L.head==x) )*/;
    else
        return /*( L with all x's removed (L!=null, L.head!=x) )*/;
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        return removeAll(L.tail, x);
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If L is the list [2, 1, 2, 9, 2], we want removeAll(L, 2) to be the new list [1, 9].

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/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return new IntList(L.head, removeAll(L.tail, x));
}
```

# Iterative Non-destructive List Deletion

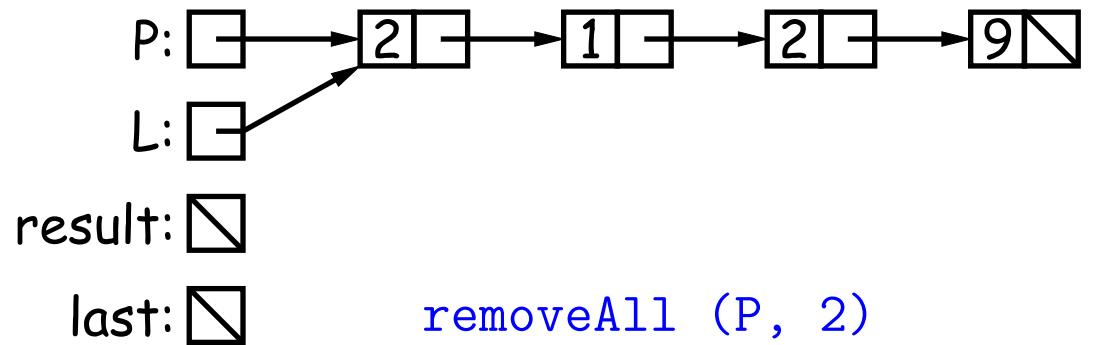
Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 *  of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    for ( ; L != null; L = L.tail) {
        if (x == L.head)
            continue;
        else if (last == null)
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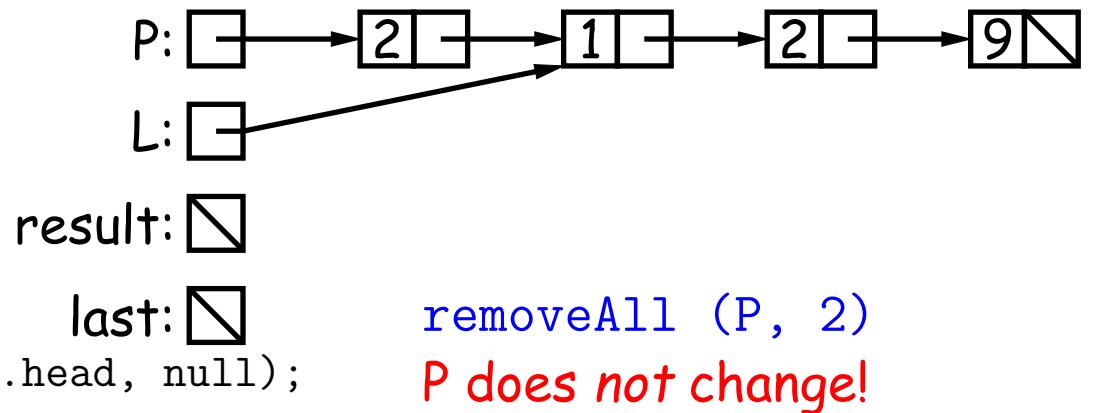
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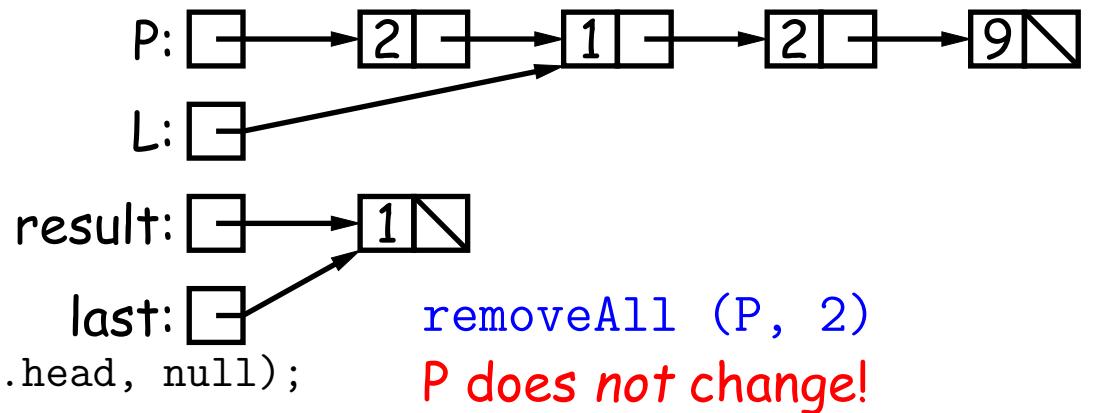
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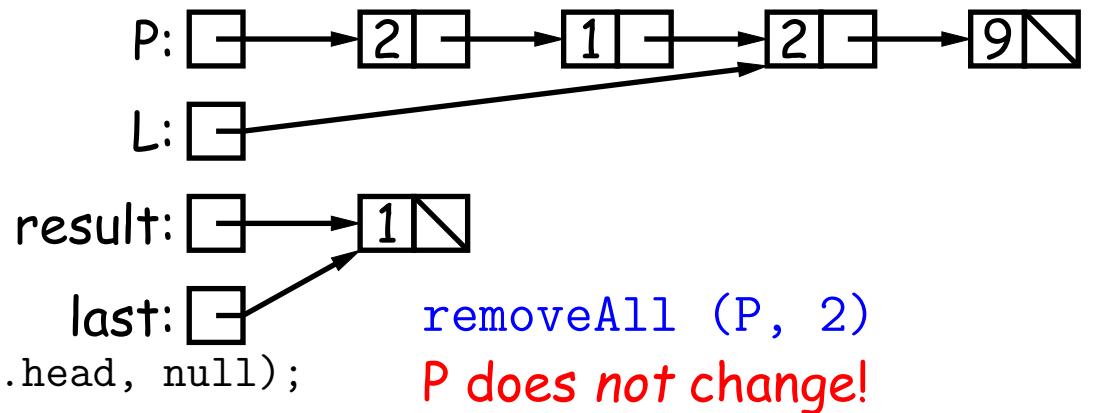
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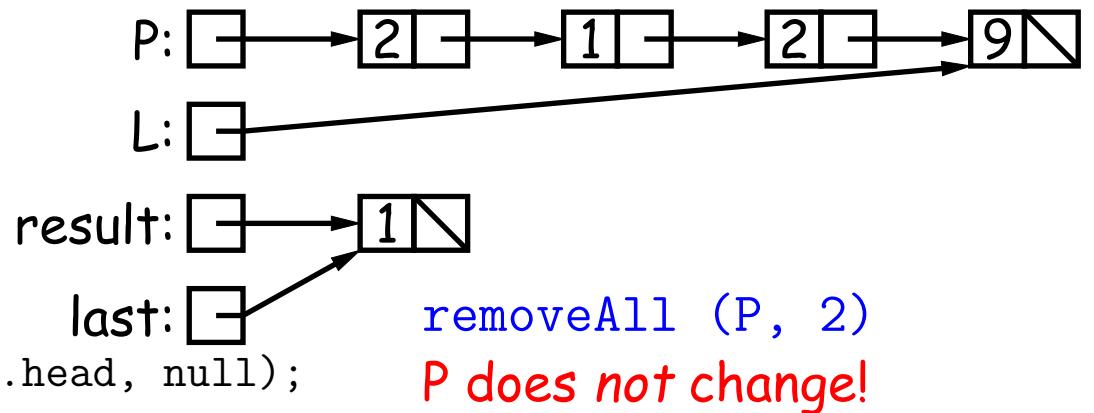
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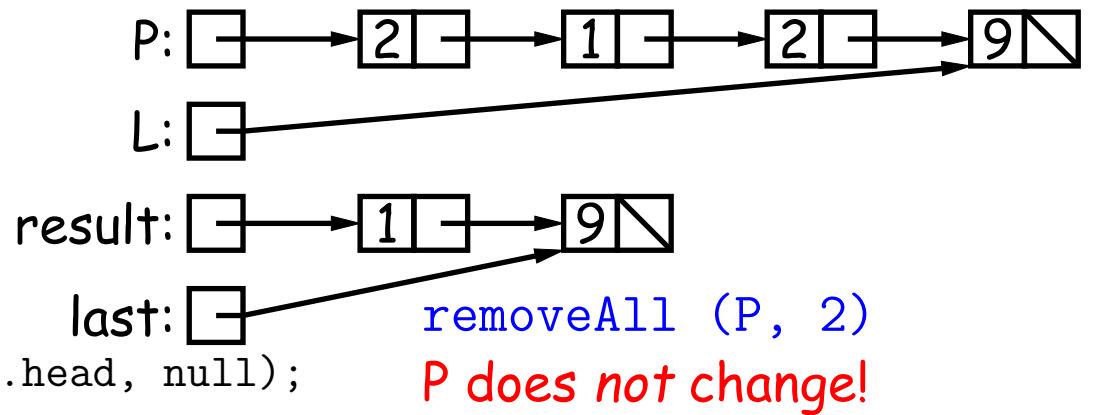
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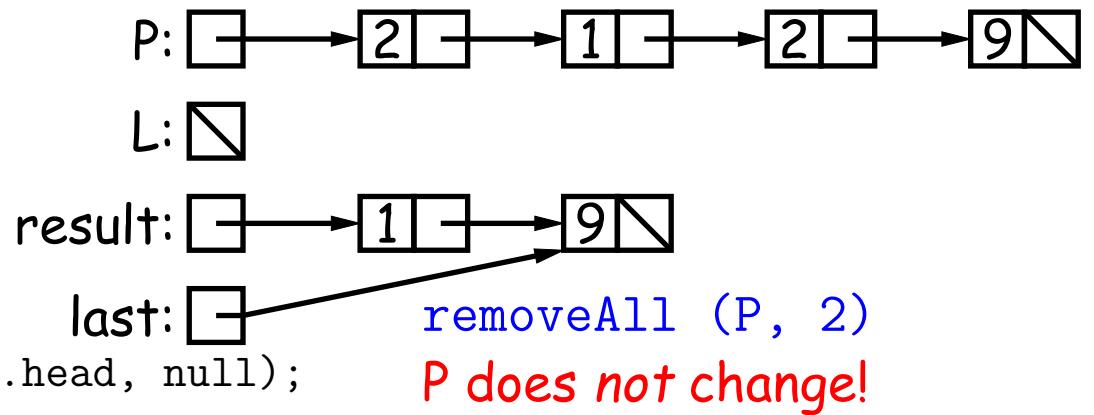
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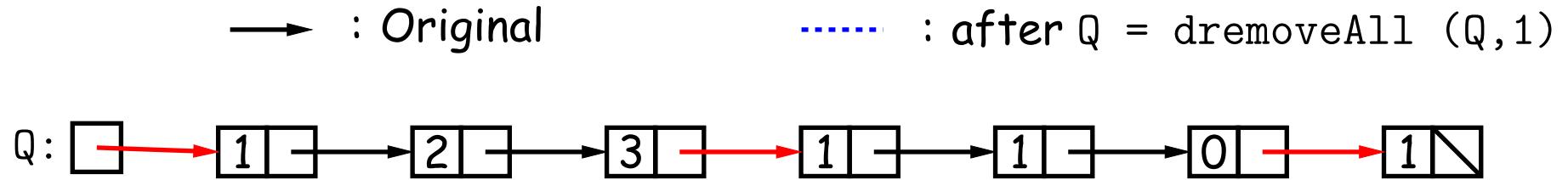
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 * The original list may be destroyed. */  
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    else {  
        /*{ Remove all x's from L's tail. }*/;  
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→ : Original

----- : after Q = dremoveAll (Q,1)



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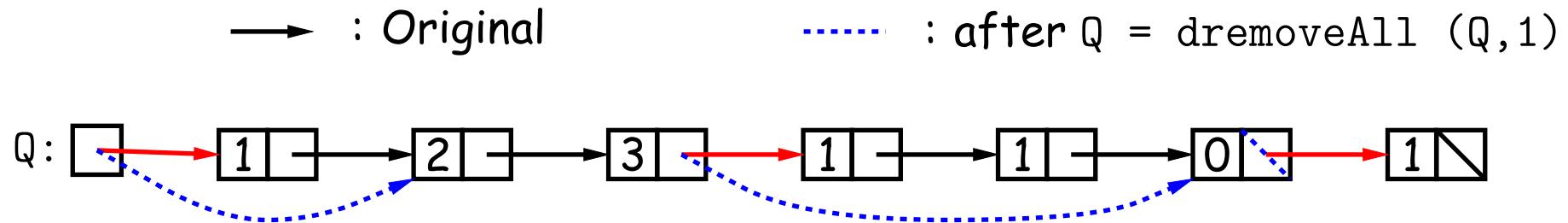
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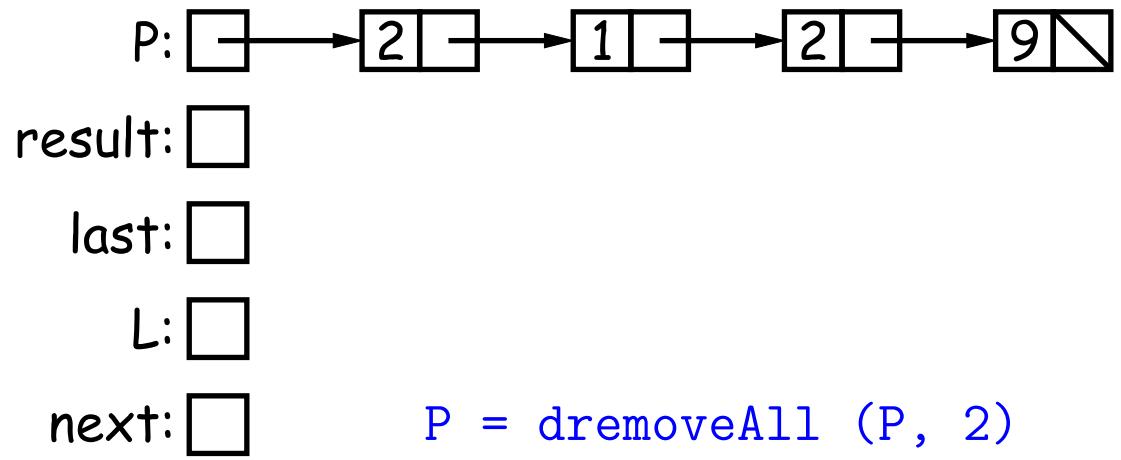
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        L.tail = dremoveAll(L.tail, x);  
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# Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
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            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
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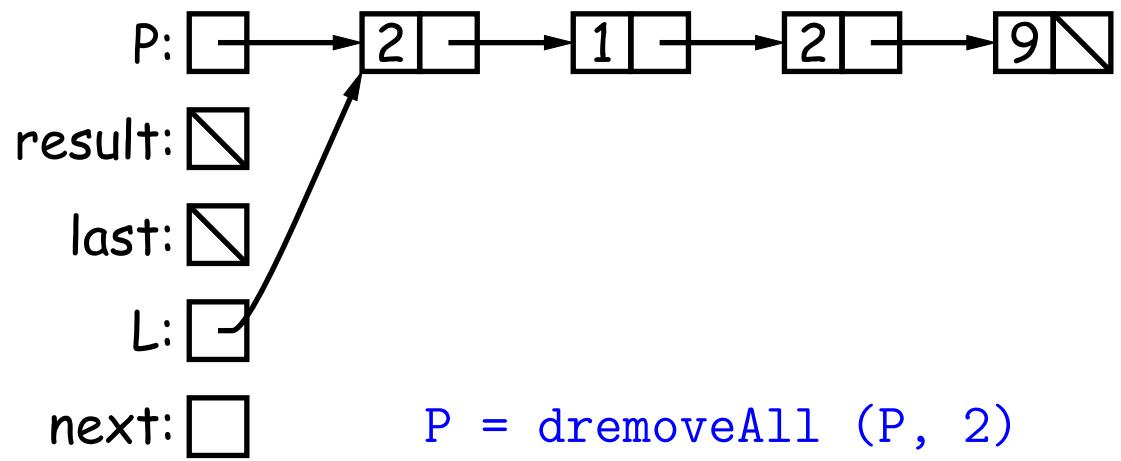
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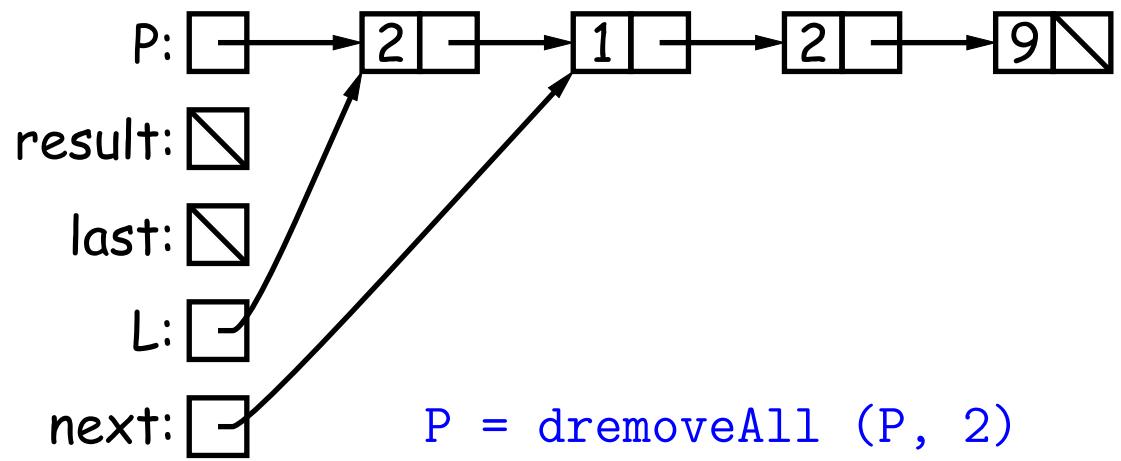
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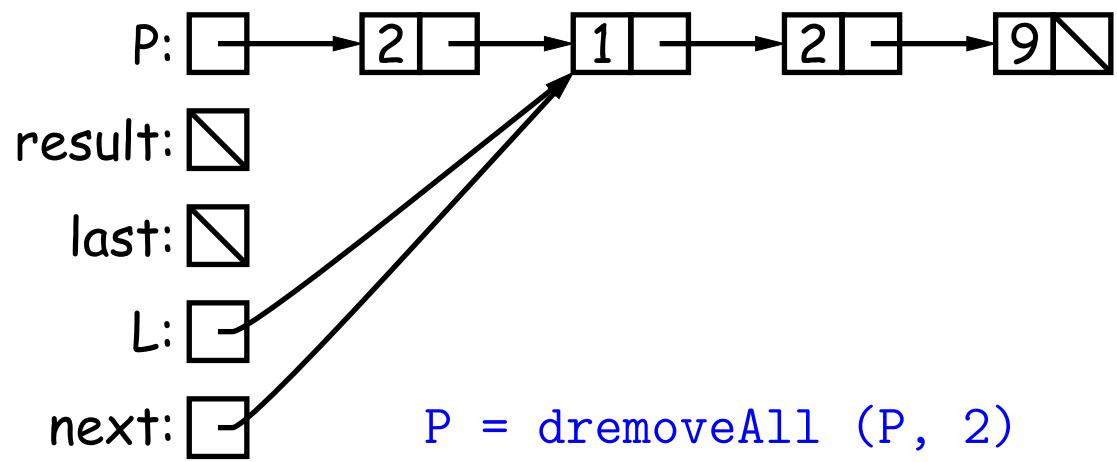
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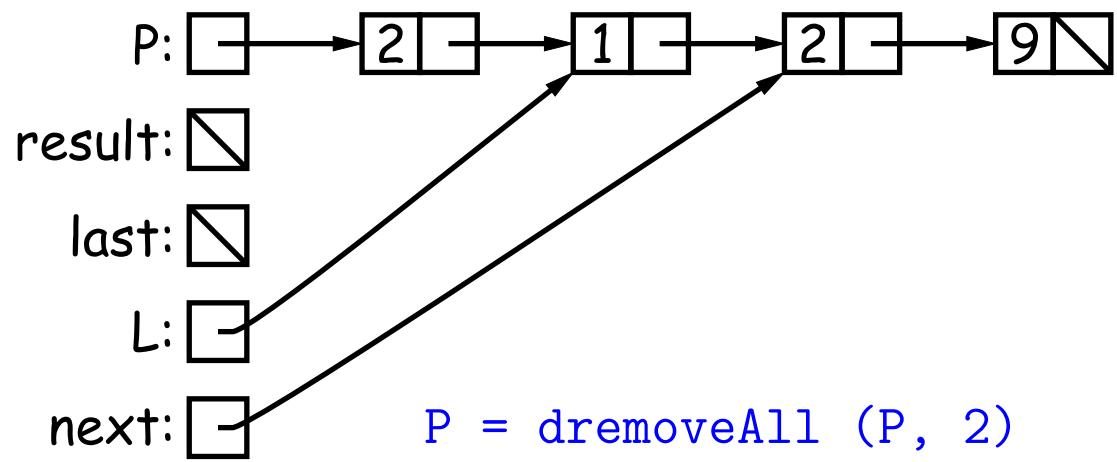
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        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



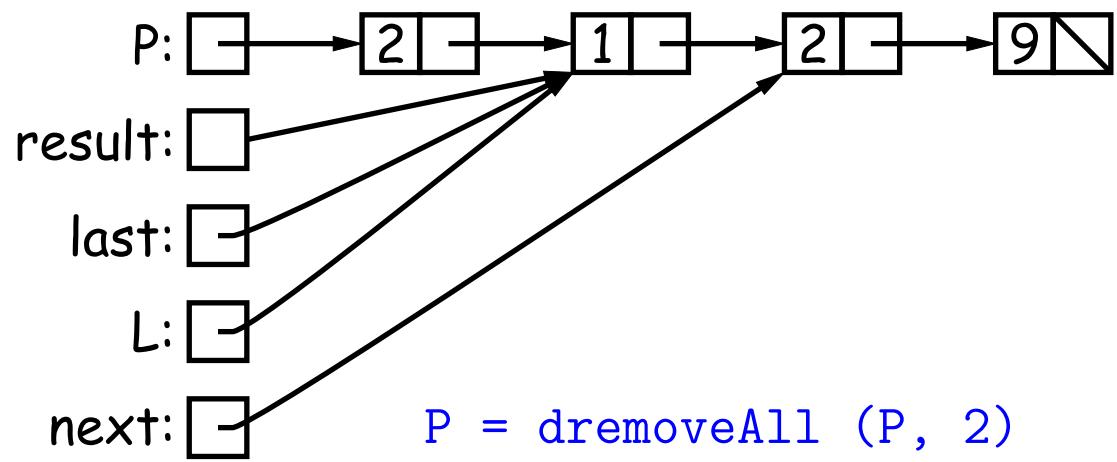
# Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
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            else
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            L.tail = null;
        }
        L = next;
    }
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}
```



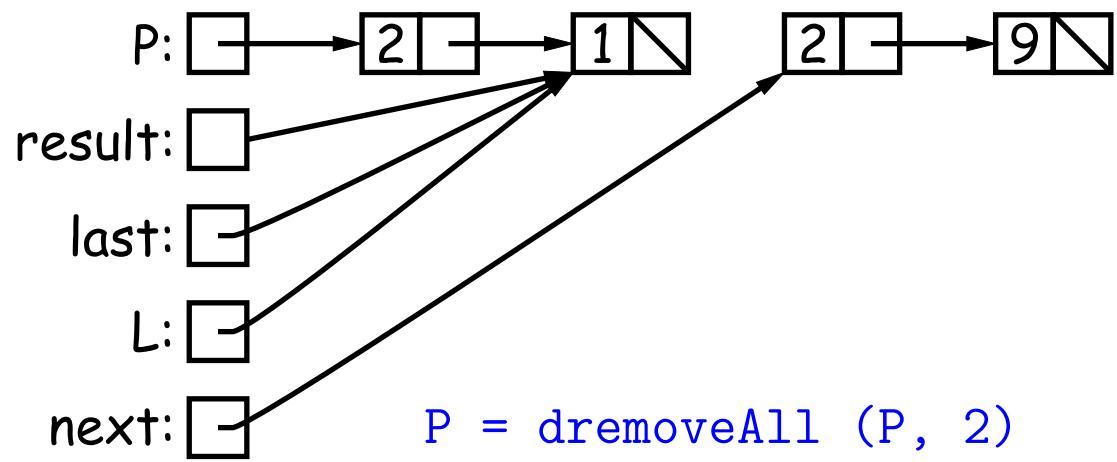
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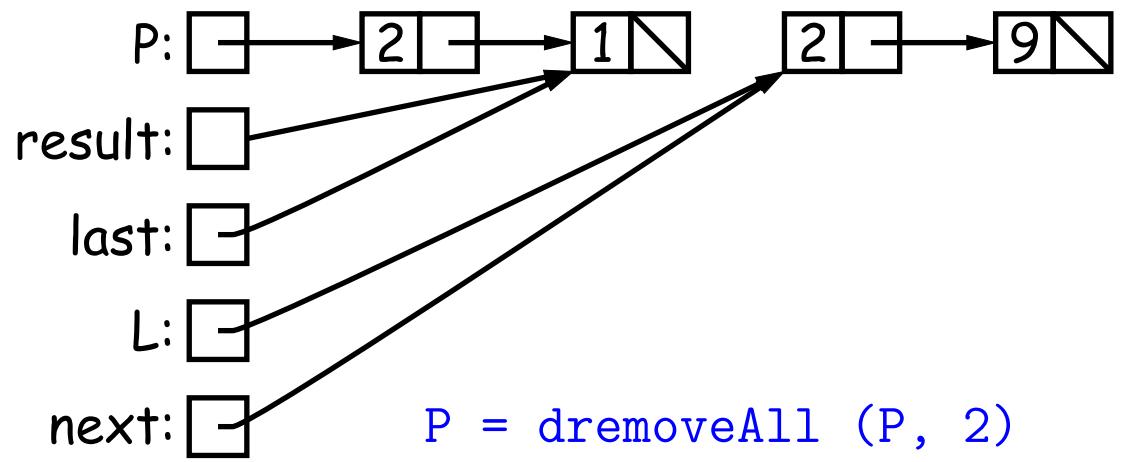
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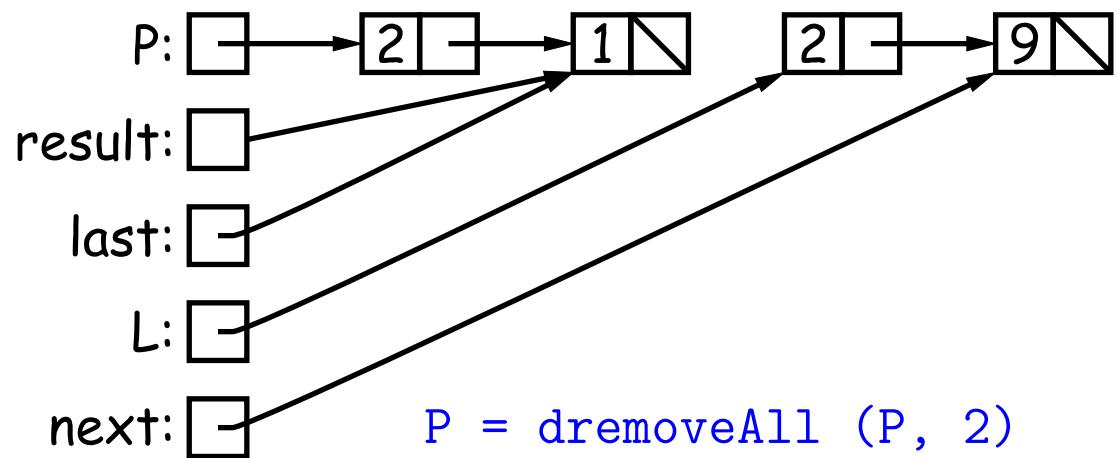
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        }
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}
```



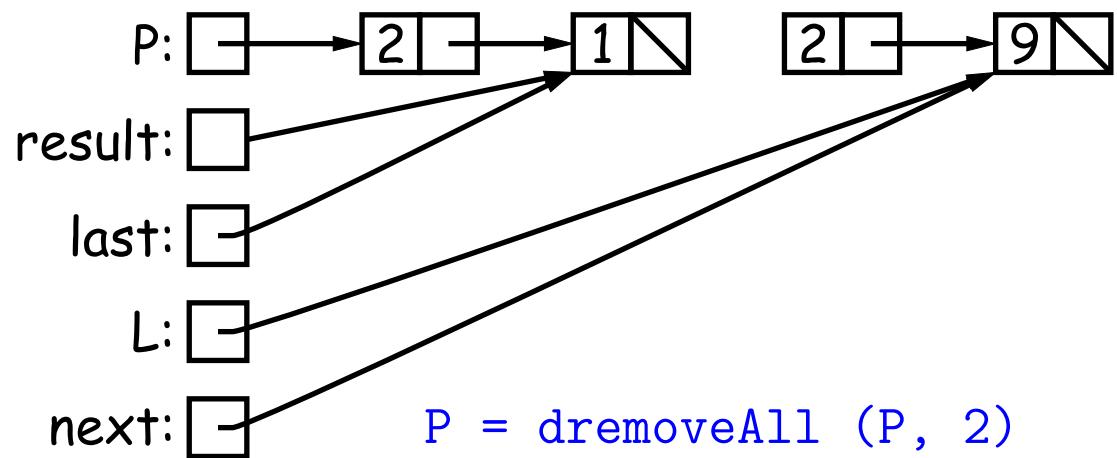
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}
```



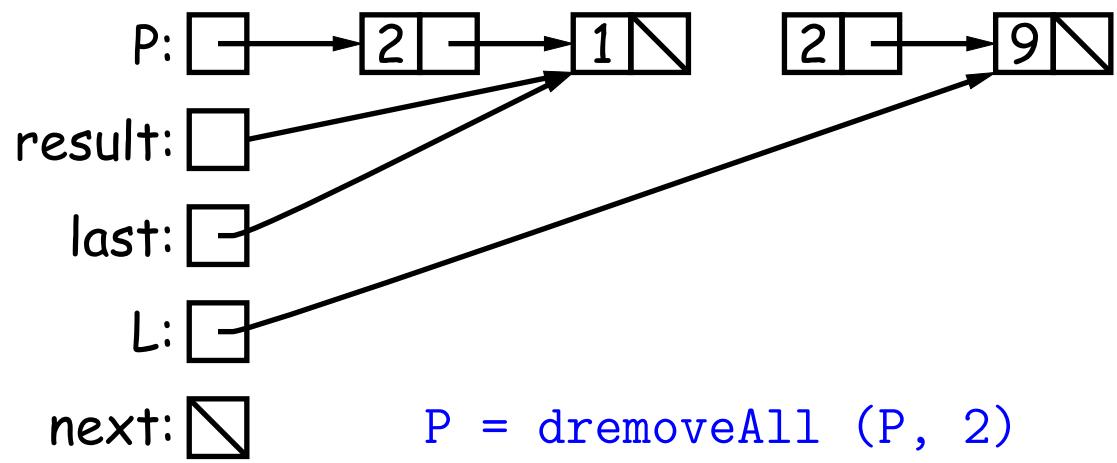
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        }
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}
```



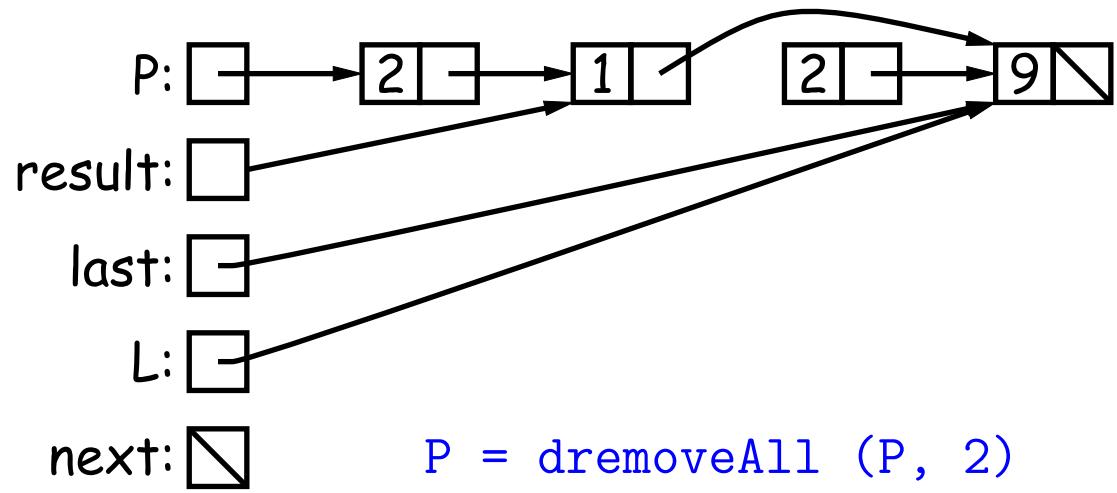
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            if (last == null)
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            else
                last = last.tail = L;
            L.tail = null;
        }
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    }
    return result;
}
```



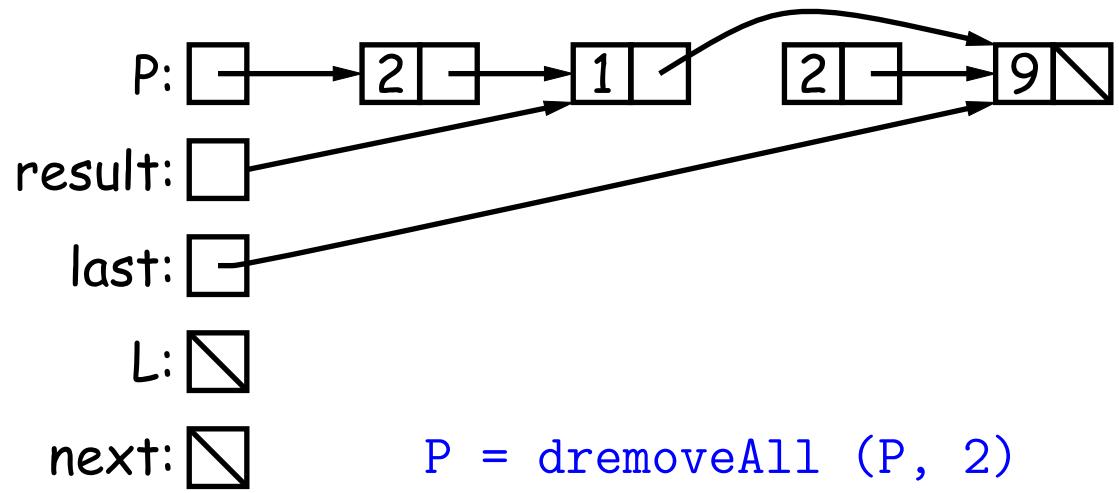
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        if (x != L.head) {
            if (last == null)
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            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



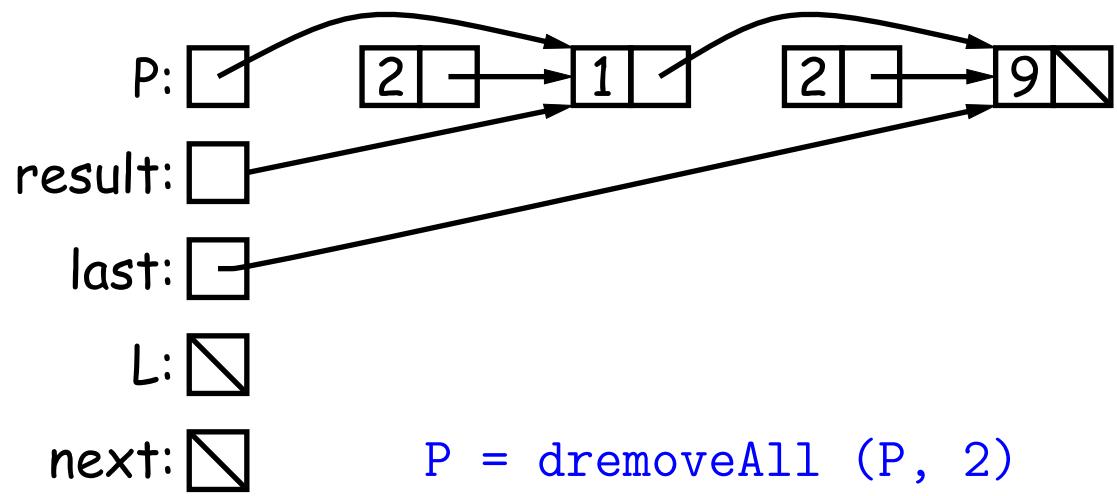
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                last = last.tail = L;
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        }
        L = next;
    }
    return result;
}
```



# Iterative Destructive Deletion

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static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
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    while (L != null) {
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        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



## Aside: How to Write a Loop (in Theory)

- Try to give a description of how things look on *any arbitrary iteration* of the loop.
- This description is known as a *loop invariant*, because it is always true at the start of each iteration.
- The loop body then must
  - Start from any situation consistent with the invariant and condition;
  - Make progress in such a way as to make the invariant true again.

```
// Invariant must be true here
while (condition) { // condition must not have side-effects.
    // (Invariant and condition are necessarily true here.)
    loop body
    // Invariant must again be true here
}
// Invariant true and condition false.
```

- So if our loop gets the desired answer whenever *Invariant* is true and *condition* false, our job is done!

# Relationship to Recursion

- Another way to see this is to consider an equivalent recursive procedure:

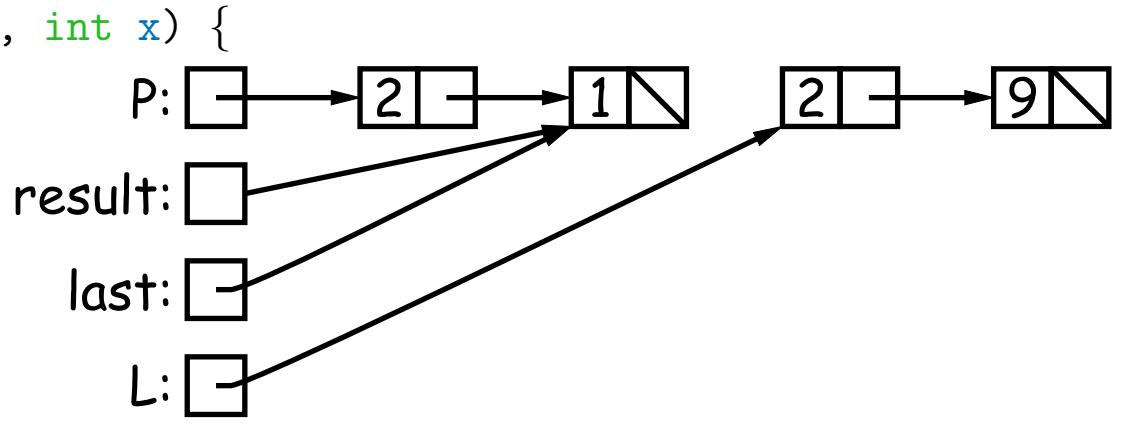
```
/** Assuming Invariant, produce a situation where Invariant
 * is true and condition is false. */
void loop() {
    // Invariant assumed true here.
    if (condition) {
        // Invariant and condition true here.
        loop body
        // Invariant must be true here.
        loop()
        // Invariant true here and condition false.
    } else { /* condition false here. */ }
}
```

- Here, the invariant is the precondition of the function `loop`.
- The loop maintains the invariant while making the condition false.
- Idea is to arrange that our actual goal is implied by this post-condition.

# Example: Loop Invariant for dremoveAll

```
/** The list resulting from removing all X's from L
 * destructively. */

static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while ** (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



P = dremoveAll (P, 2)

\*\* Invariant:

- **result** points to the list of items in the final result except for those from **L** onward.
- **L** points to an unchanged tail of the original list of items in **L**.
- **last** points to the last item in **result** or is null if **result** is null.