

# Lecture 13

## Neural Networks: Part I

GEOL 4397: Data analytics and machine learning for geoscientists

Jiajia Sun, Ph.D.

April. 9th, 2019

UNIVERSITY of  
**HOUSTON**

YOU ARE THE PRIDE

EARTH AND ATMOSPHERIC SCIENCES

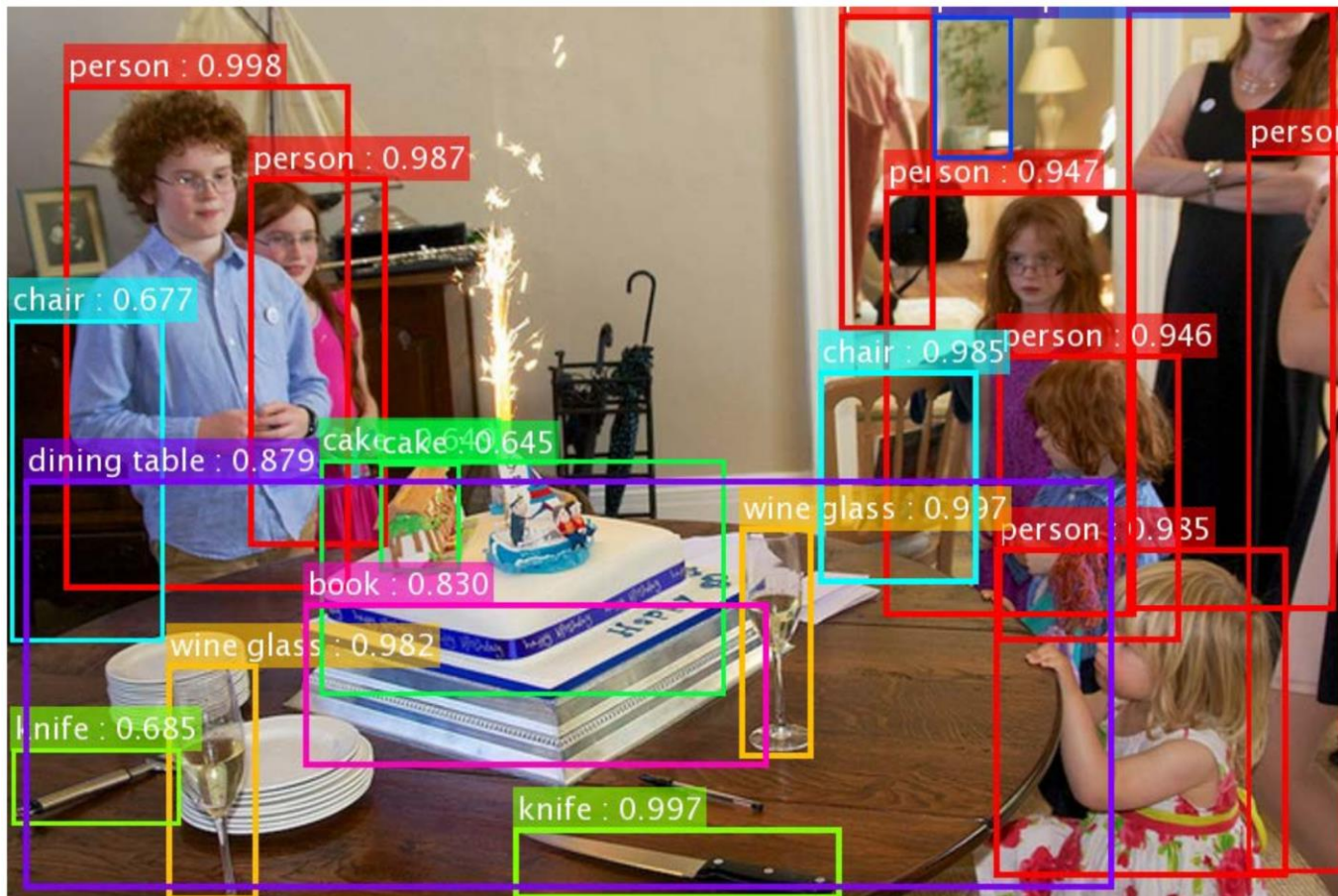


Week	Date	Topics	Comments
1	01/15 Tues 01/17 Thur	Overview of syllabus Lecture: Introduction to Machine learning: applications Lecture: Review of linear algebra	
2	01/22 Tues 01/24 Thur	Lab: Linear algebra in Python Lecture: Introduction to optimization	Not graded
3	01/29 Tues 01/31 Thur	Lab: Gradient descent + Linear regression Lecture: Introduction to machine learning: concepts	Report due on 02/05 at 5:30 pm
4	02/05 Tues 02/07 Thur	Lecture: Logistic regression Lab: Logistic regression	Report due on 02/14 at 5:30 pm
5	02/12 Tues 02/14 Thur	Lecture: Support vector machine Lab: Support vector machine	Report due on 02/21 at 5:30 pm
6	02/19 Tues 02/21 Thur	Lecture: Decision trees Lab: Decision trees	Report due on 02/28 at 5:30 pm
7	02/26 Tues 02/28 Thur	Lecture: Random Forest Lab: Random forest	Report due on 03/07 at 5:30 pm
8	03/05 Tues 03/07 Thur	Lecture: Ensemble learning Lab: Ensemble learning	Report due on 03/19 at 5:30 pm
9	03/12 Tues 03/14 Thur	No class due to spring break No class due to spring break	
10	03/19 Tues 03/21 Thur	Review & Recap Exam	
11	03/26 Tues 03/28 Thur	Lecture: Clustering Lab: Clustering	Report due on 04/04 at 5:30 pm
12	04/02 Tues 04/04 Thur	Lecture: Introduction to TensorFlow Lab: TensorFlow	Not graded
13	04/09 Tues 04/11 Thur	Lecture: Introduction to neural networks 1 Lecture: Introduction to neural networks 2	
14	04/16 Tues 04/18 Thur	Lab: Deep learning Lecture: Convolutional neural networks 1	Report due on 04/23 at 5:30pm
15	04/23 Tues 04/25 Thur	Guest lecture: Convolutional neural networks 2 Lab: CNN (optional)	Report due on 05/02 at 5:30 pm
16	04/30 Tues 05/02 Thur	final presentation?? final presentation??	
Note	28 class meetings		04/29 last day of class

# Outline

- What is neural networks?
- Forward propagation
- Backward propagation

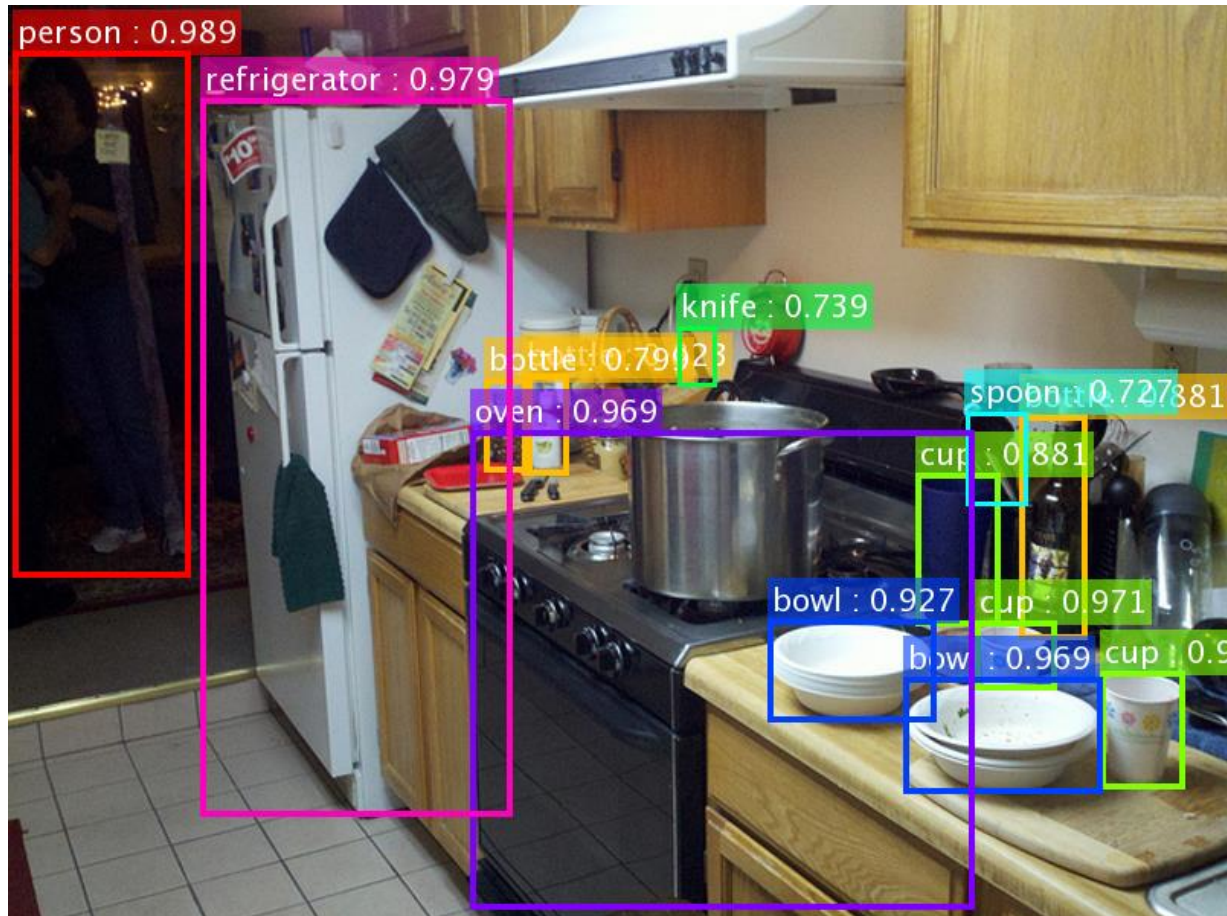
# Object detection



ResNet applied to COCO dataset.

Source: He et al., Deep residual learning for image recognition, CVPR, 2016

# Object detection



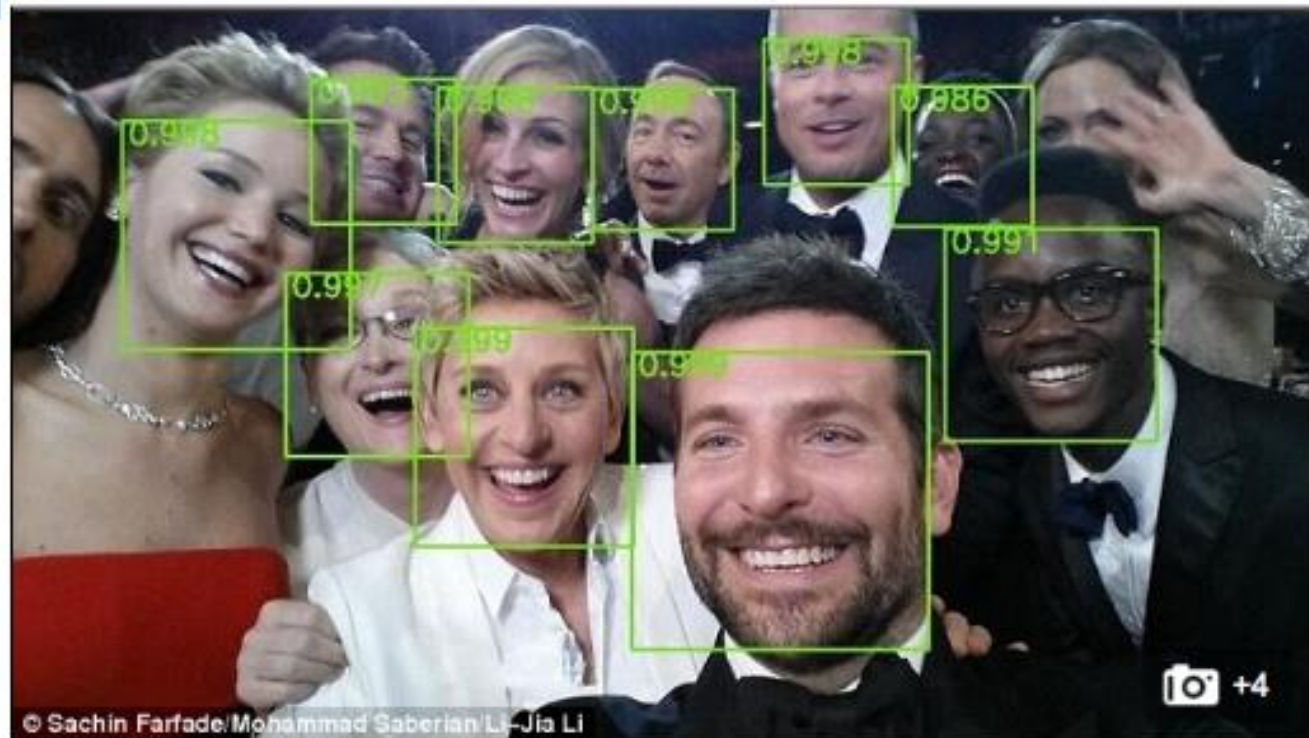
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# Face detection

## Convolution Neural Net (CNN)

Yahoo + Stanford example — find a face in a pic, even upside down

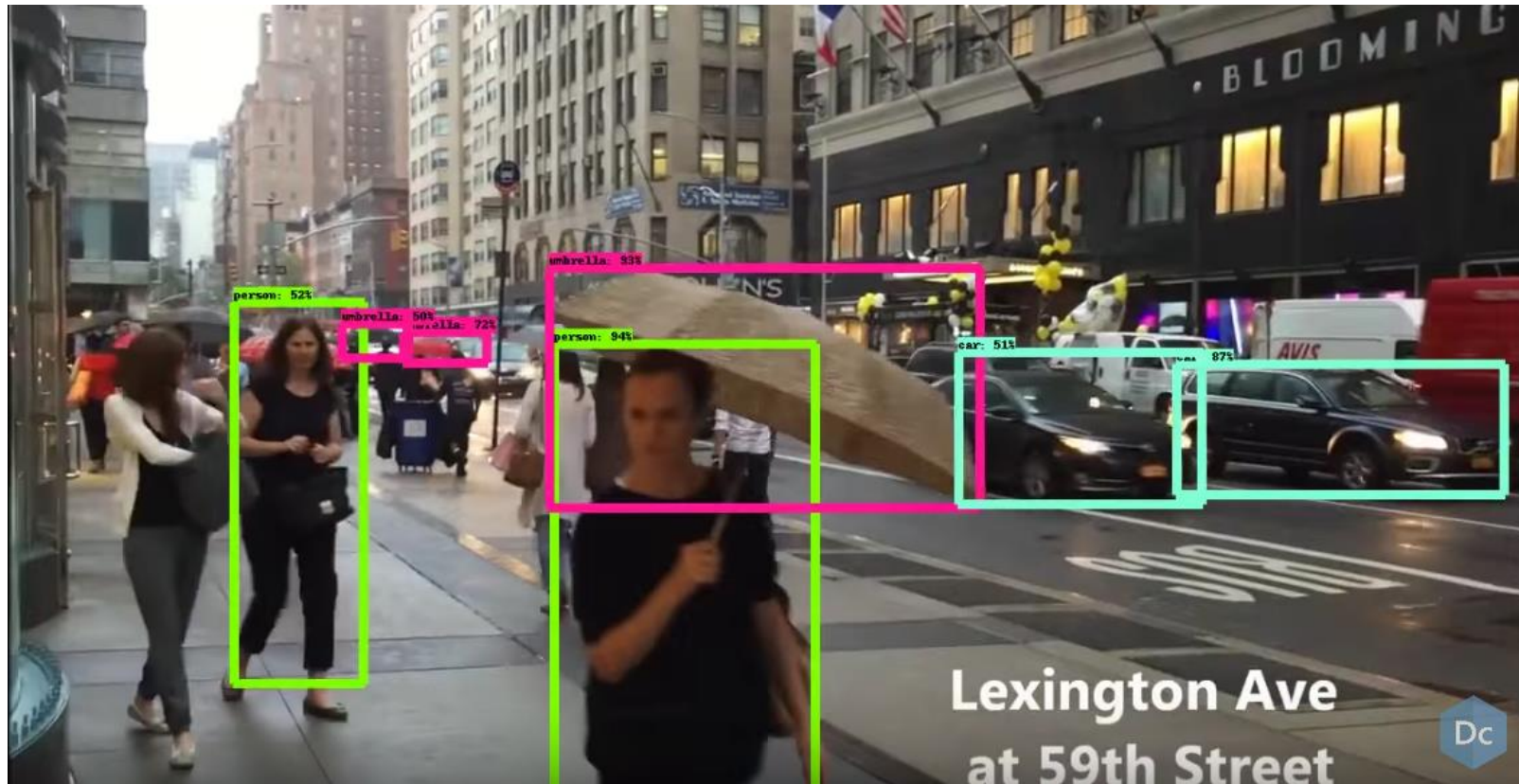


The Deep Dense Face Detector algorithm was built by Yahoo Labs in California and Stanford University. The researchers used a form of machine learning known as a deep convolutional neural network to train a computer to spot facial features (pictured) in a database of images

<http://www.cia>

At the moment, the so-called Deep Dense Face Detector doesn't recognise who the individual faces belong to, just that there is a face.

# Real time object detection



Video online: <https://www.youtube.com/watch?v=zZe27JYi8Y>

# Real time object detection



YOLO V2 achieves better results at very high FPS

Video online: <https://www.youtube.com/watch?v=VOC3huqHrss&list=RDVOC3huqHrss>



# Go game



Image credit: Nature



Image credit: theverge.com

# Deep learning applications

- Google images
  - Classifying billions of images



# Deep learning applications




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cat in the hat  



**Search by image** 

Search Google with an image instead of text. Try dragging an image here.

**Paste image URL**  **Upload an image**

**Search by image**



About 25,270,000,000 results (0.78 seconds)



Image size:  
900 × 790

Find other sizes of this image:  
[All sizes](#) - [Small](#) - [Medium](#)

Best guess for this image: **Cat**

**Cat - Wikipedia**  
<https://en.wikipedia.org/wiki/Cat> ▼  
The domestic **cat** is a small, typically furry, carnivorous mammal. They are often called house cats when kept as indoor pets or simply cats when there is no need to distinguish them from other felids and felines. They are often valued by humans for companionship and for their ability to hunt vermin. There are more than ...


**Cat | global-selector | Caterpillar**  
<https://www.cat.com/> ▼  
Genuine enabler of sustainable world progress and opportunity, defined by the brand attributes of global leadership, innovation and sustainability. Africa, Middle-East. English · Français · 简体中文 · العربية · Turkish. Asia. 简体中文 · 日本語 · 한글 · 繁體漢字 · English. Australia, New Zealand. English. Eurasia. Русский. Europe.

Visually similar images



Cat

Animal



The domestic cat is a small, typically furry, carnivorous mammal. They are often called house cats when kept as indoor pets or simply cats when there is no need to distinguish them from other felids and felines. [Wikipedia](#)

**Lifespan:** 4 – 5 years (In the wild)

**Gestation period:** 64 – 67 days

**Scientific name:** Felis catus

**Daily sleep:** 12 – 16 hours


**Mass:** 7.9 – 9.9 lbs (Adult)


**Did you know:** The outer ear of cat has 32 muscles which allows the cat the rotate each ear 180 degrees - and independently from one another. [care2.com](#)

Breeds


View 20+ more

  
British Shorthair

  
Siamese cat

  
Persian cat

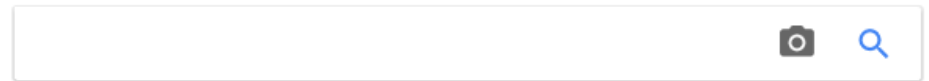
  
Ragdoll

  
Maine Coon

[Feedback](#)

# Deep learning applications

- Google images
  - Classifying billions of images



- Apple's Siri
  - Powering speech recognition
- Recommending the best videos to watch (e.g., YouTube)
- Beat world champion at the game of GO

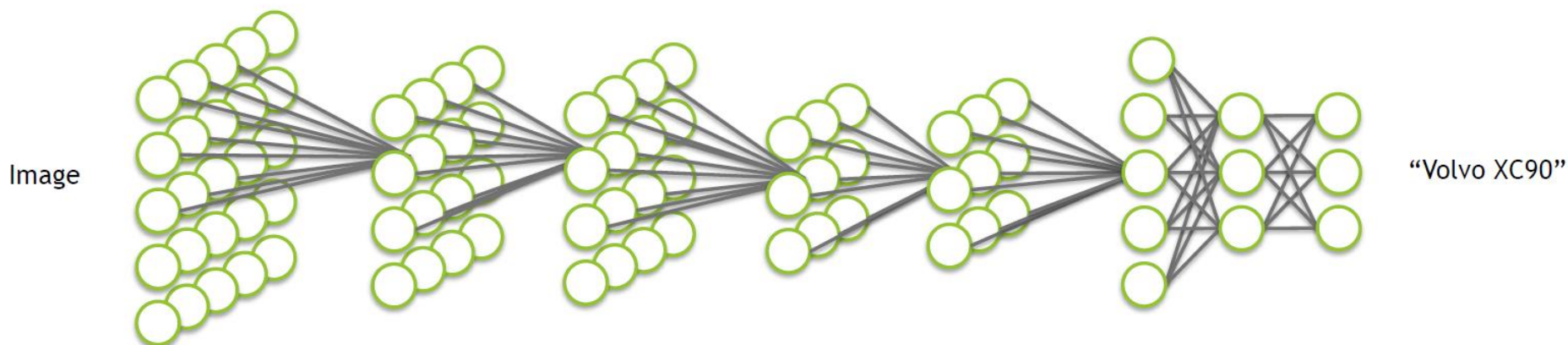
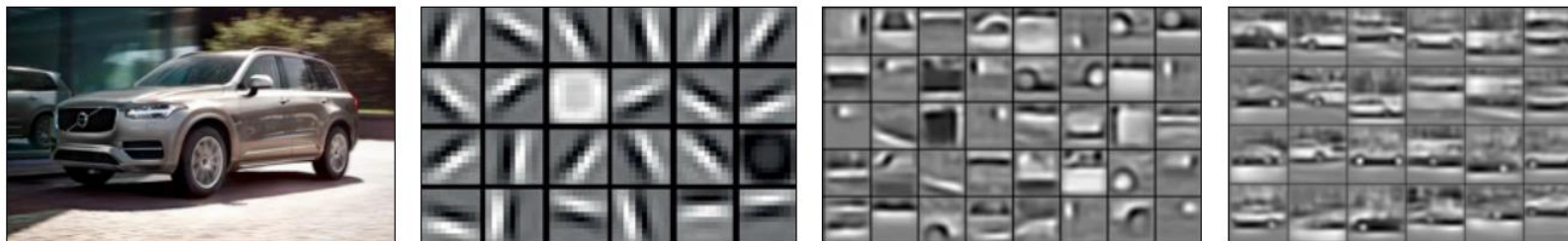
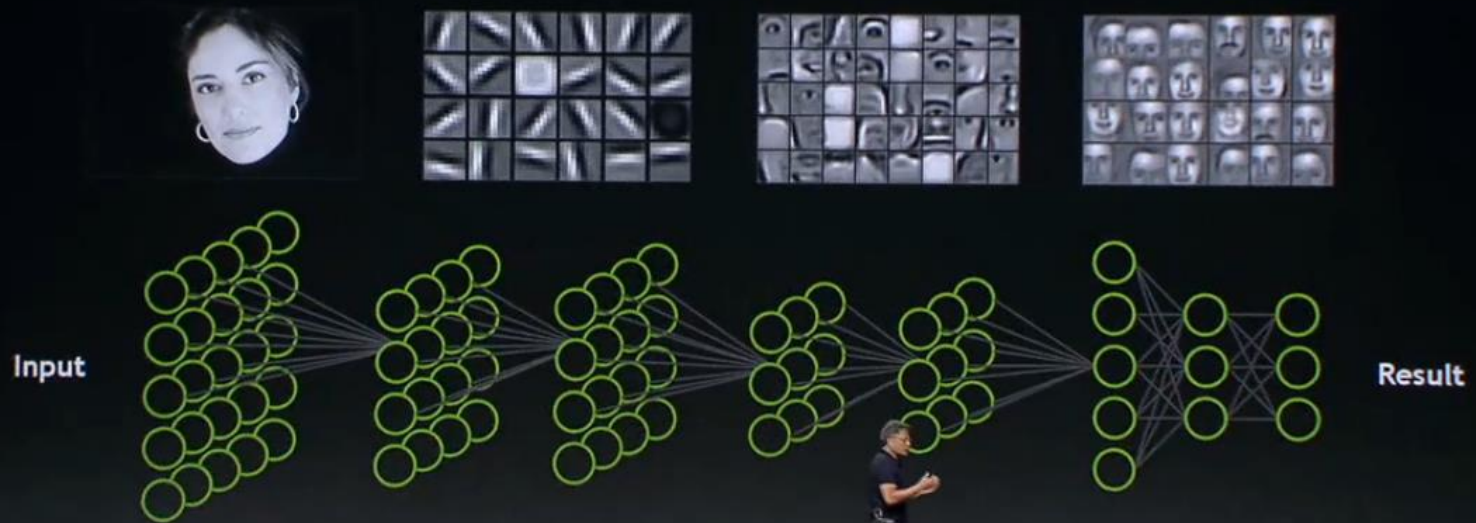


Image source: *"Unsupervised Learning of Hierarchical Representations with Convolutional Deep Belief Networks"* ICML 2009 & Comm. ACM 2011. Honglak Lee, Roger Grosse, Rajesh Ranganath, and Andrew Ng.

# Machine Learning using Deep Neural Networks





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Aurelien Geron, 2017, Hands-on Machine Learning with Scikit-Learn & TensorFlow, pp 254

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- 1990s, alternative ML algorithms such as SVM were favored
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- Around 2010, another wave of interest

Aurelien Geron, 2017, Hands-on Machine Learning with Scikit-Learn & TensorFlow, pp 254

# 2012

- Breakthrough in solving the ImageNet competition by AlexNet (achieved a top-5 error of 15.3%, more than 10.8% lower than that of the runner up, thanks to GPU and very deep neural networks).
- Often considered as the beginning of the deep learning revolution of the 2010s.
- Google brain (a deep learning team at Google): in 2012, trained a neural network to recognize cat images based on 10 million images from YouTube (used 16,000 processors)
- New York Times, National Public Radio and SmartPlanet covered the story.

# Why is machine learning taking off?

- Huge amount of labeled data available
  - Internet, social media, mobile devices, etc...

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- Better understanding of the ANNs
  - Theoretical proof that existence of local minima is not a problem
- A healthy circle of funding and progress
  - Amazing products regularly make headline news
  - Draws more attention and funding to ANN R&D
  - Resulting in more progress and better products

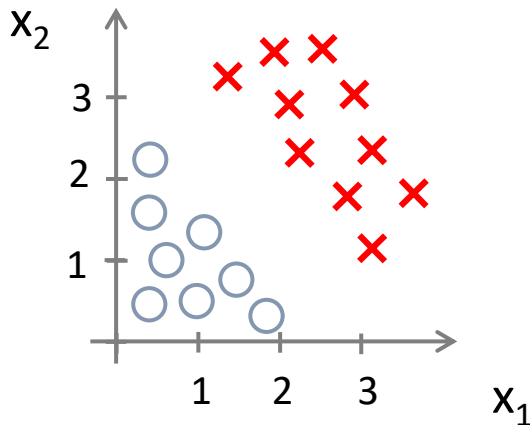
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# Neural networks

- Feedforward Neural networks
  - Most classical
- Convolutional Neural Networks
  - Extremely powerful at computer vision tasks
- Recurrent Neural Networks
  - Analyze time series and make predictions
  - E.g., analyze stock prices, and tell you when to buy or sell
  - E.g., natural language processing (NLP)

# Understanding logistic regression

## Decision Boundary



$$h_w(x) = g(w_0 + w_1x_1 + w_2x_2)$$

Predict “ $y = 1$ ” if  $-3 + x_1 + x_2 \geq 0$

This slide is taken from Andrew Ng’s ML class on coursera

# Logistic function

$$g(x) = \frac{1}{1 + e^{-x}}$$

Also called **sigmoid function**

- Map any real number in  $[-\infty, +\infty]$  to a real number within  $[0, 1]$

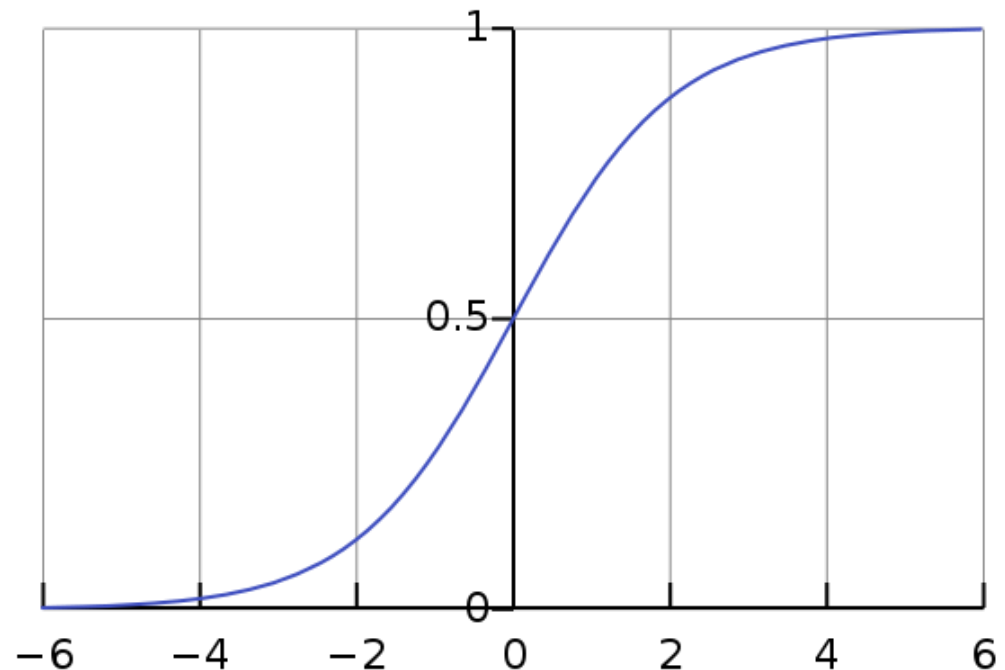
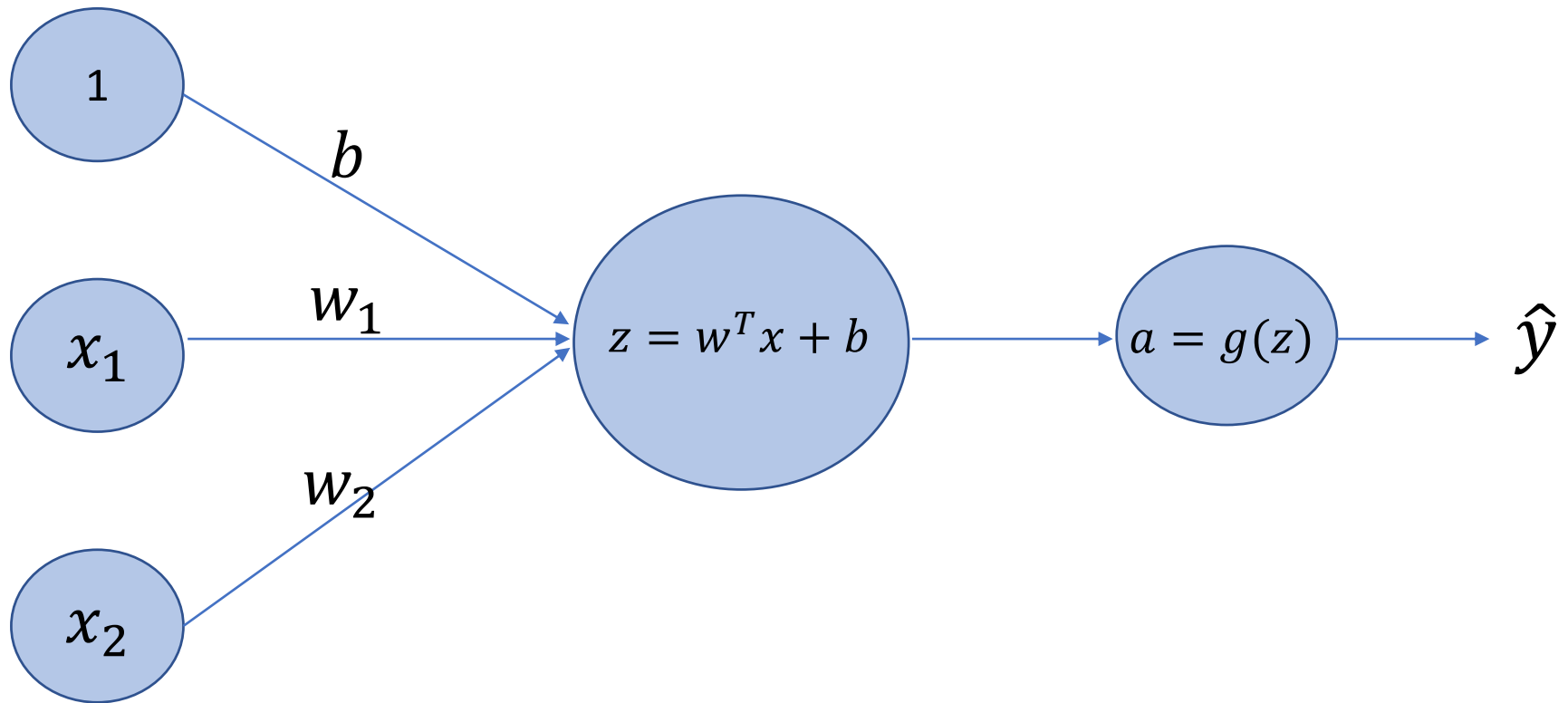


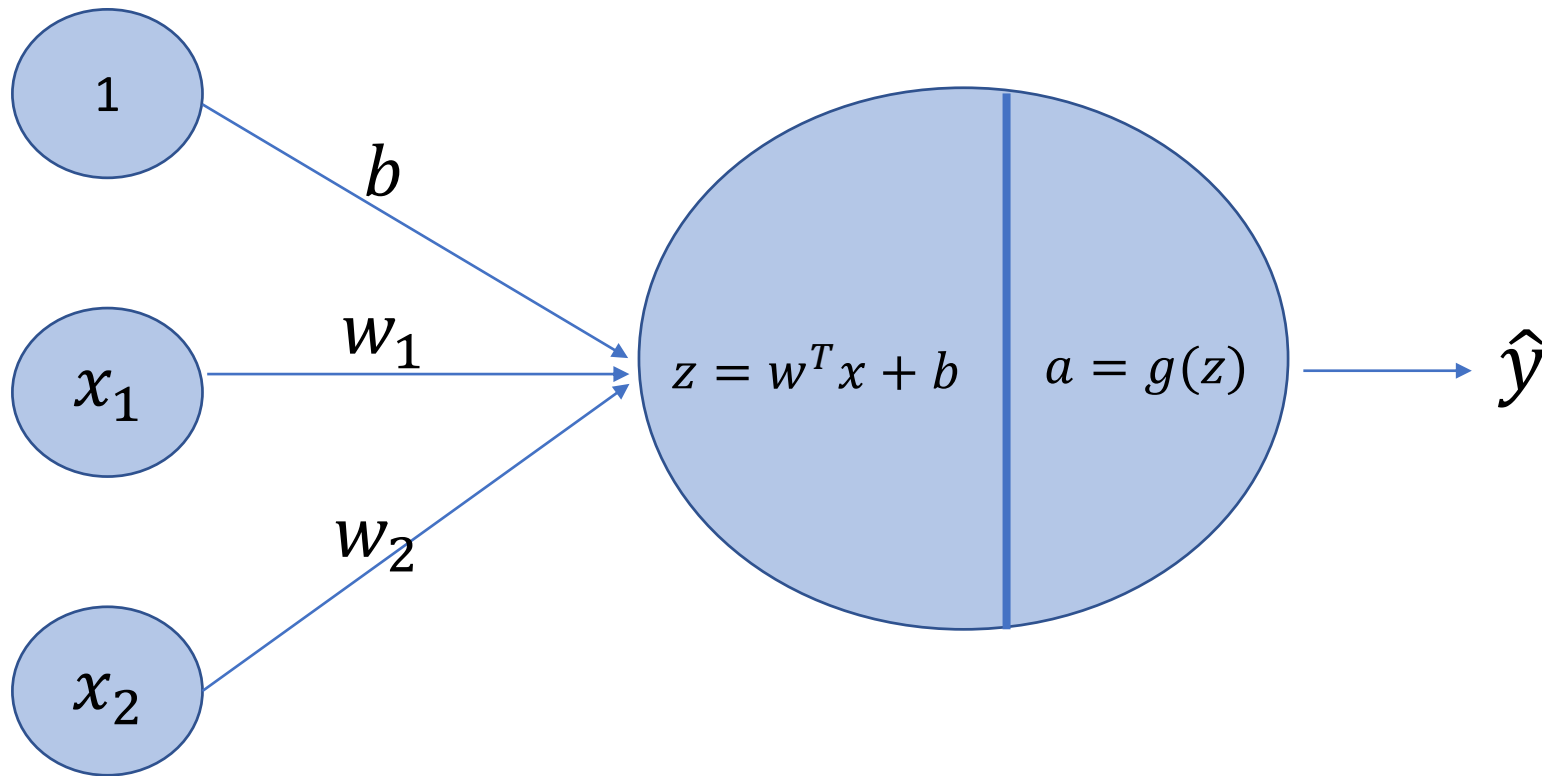
Image source: [https://en.wikipedia.org/wiki/Logistic\\_function](https://en.wikipedia.org/wiki/Logistic_function)

# Logistic regression as a neural network

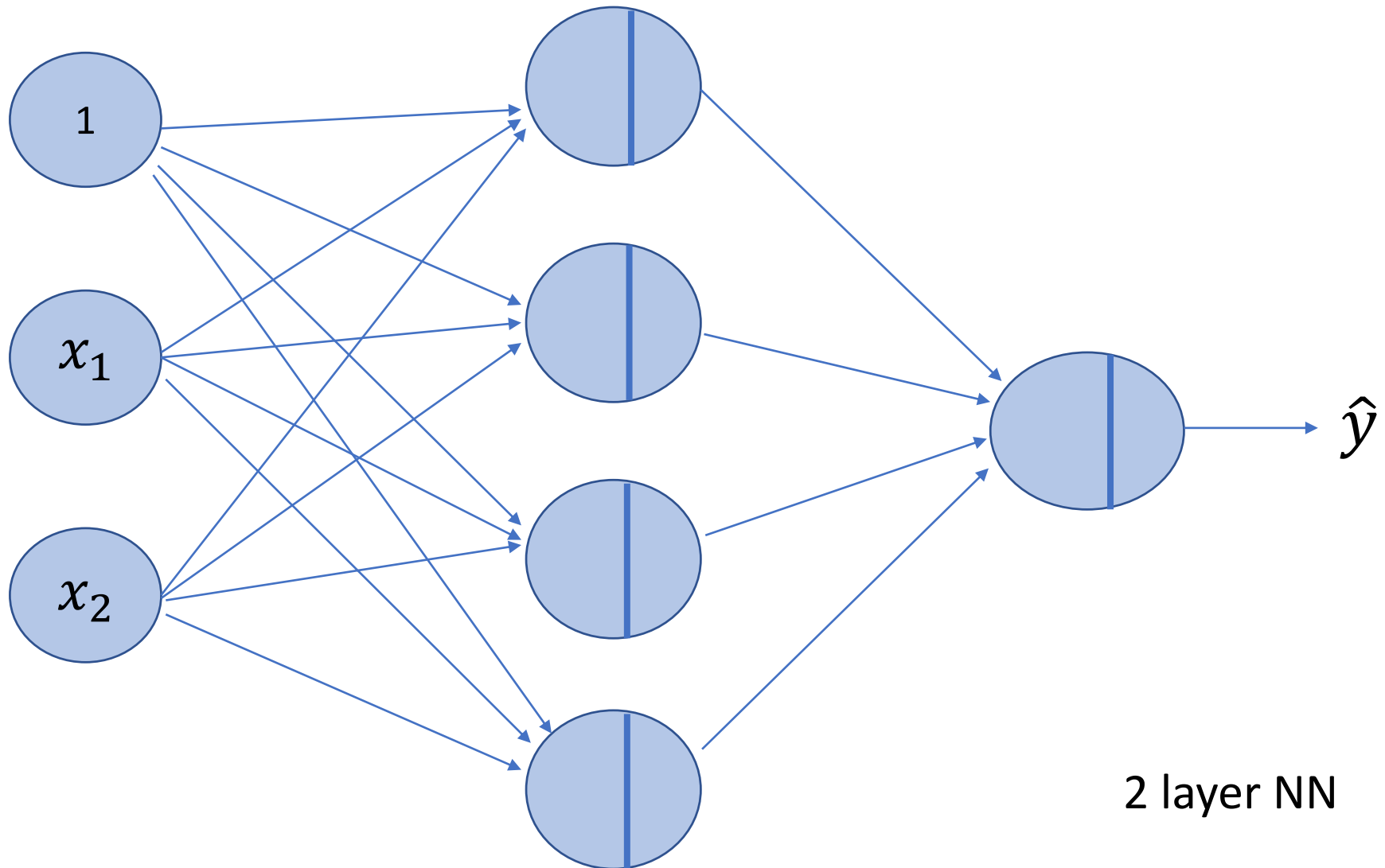




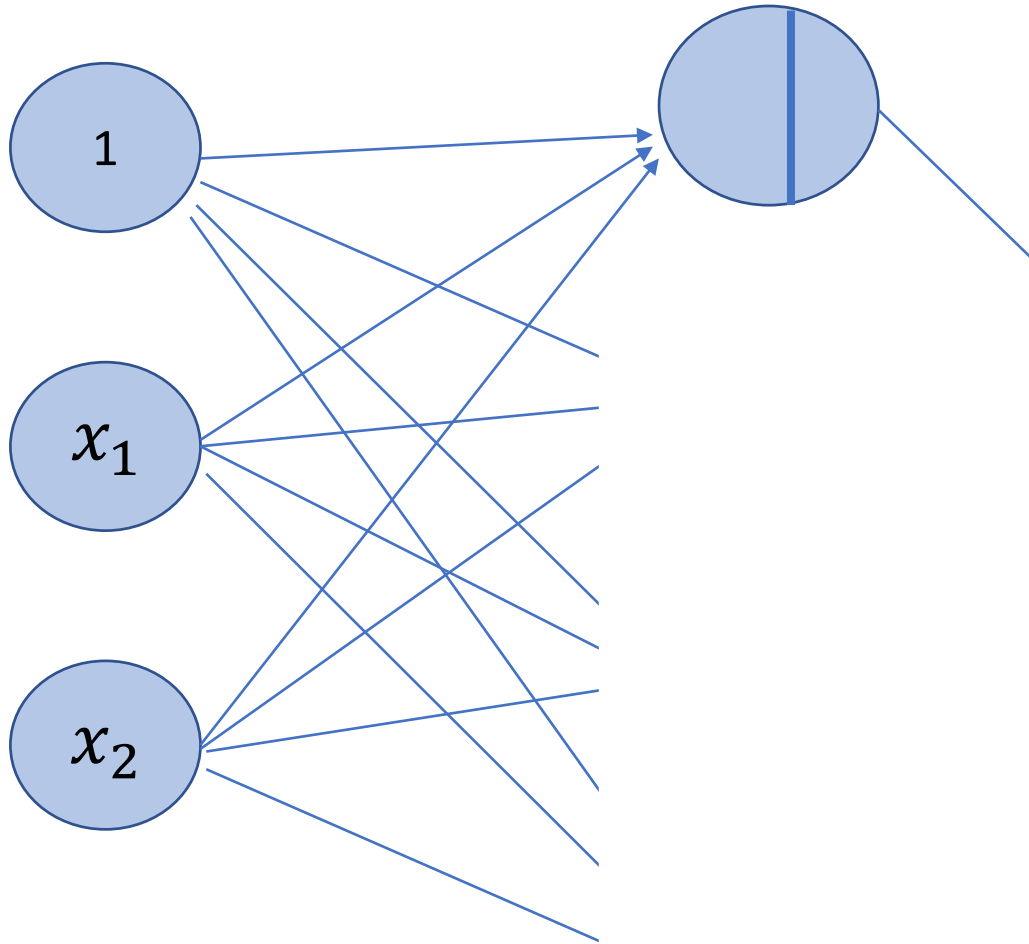
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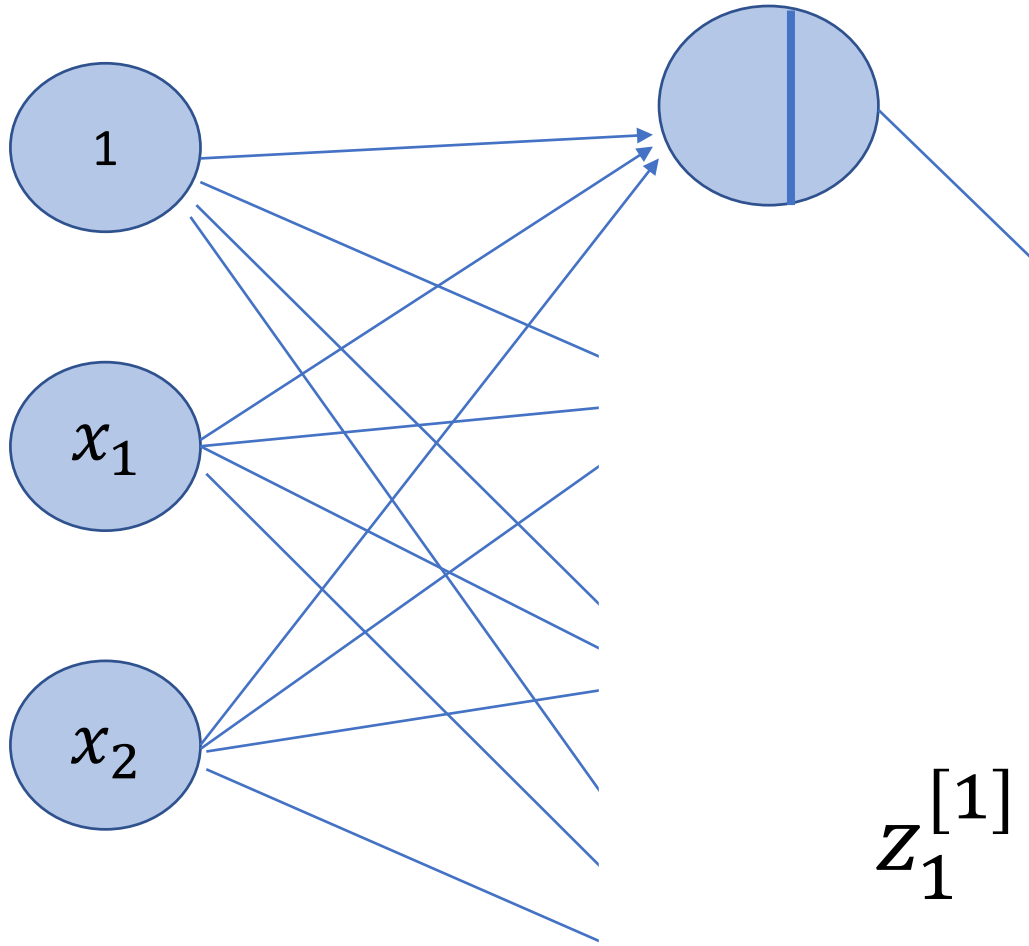
# A more general neural network



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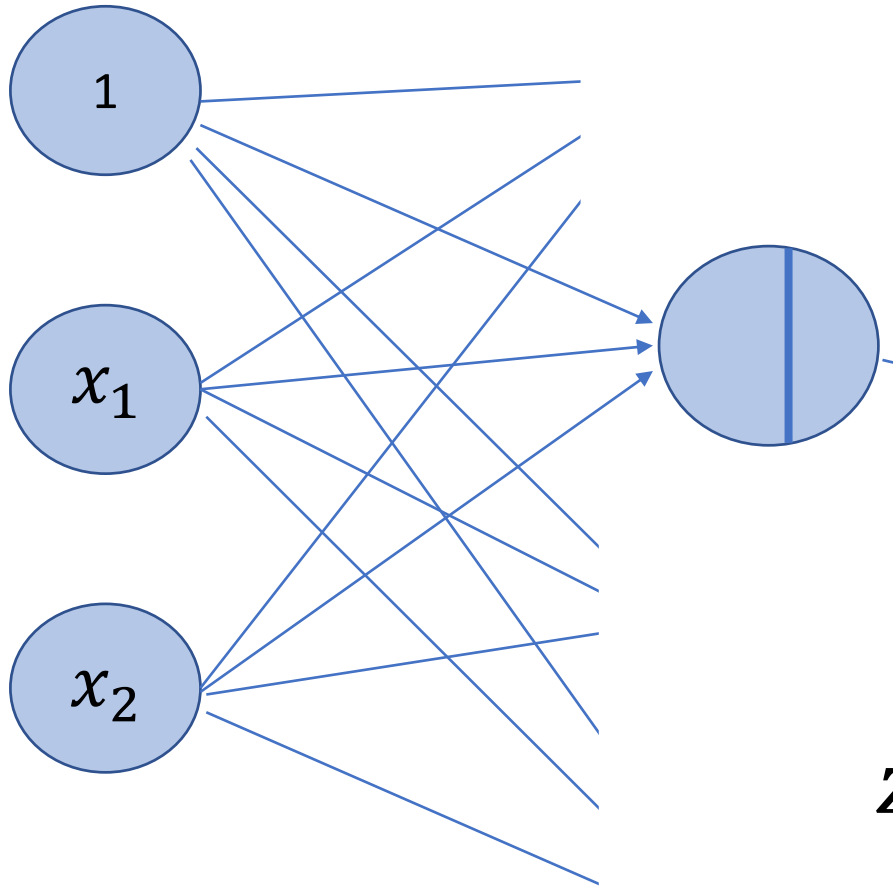


# A more general neural network

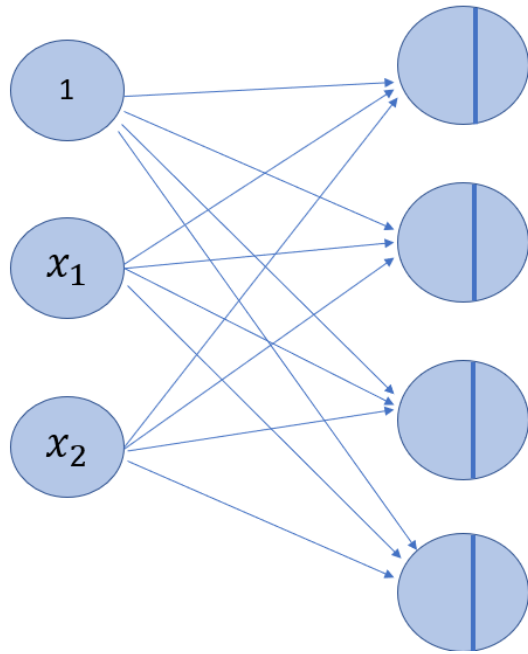


$$z_1^{[1]} = w_1^{[1]}x + b_1^{[1]}$$
$$a_1^{[1]} = g(z_1^{[1]})$$

# A more general neural network



$$z_2^{[1]} = w_2^{[1]}x + b_2^{[1]}$$
$$a_2^{[1]} = g(z_2^{[1]})$$



$$z_1^{[1]} = w_1^{[1]}x + b_1^{[1]}, a_1^{[1]} = g(z_1^{[1]})$$

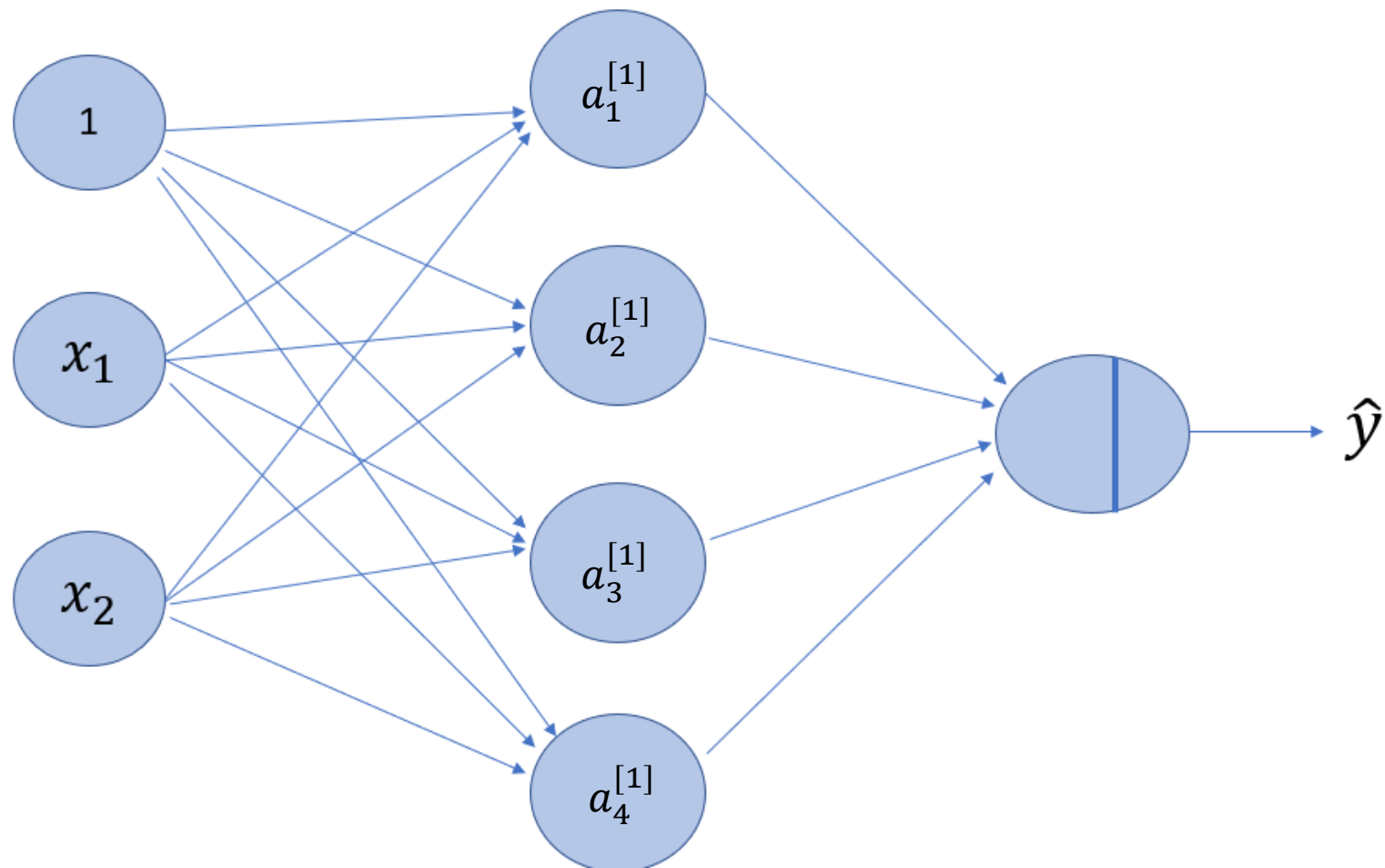
$$z_2^{[1]} = w_2^{[1]}x + b_2^{[1]}, a_2^{[1]} = g(z_2^{[1]})$$

$$z_3^{[1]} = w_3^{[1]}x + b_3^{[1]}, a_3^{[1]} = g(z_3^{[1]})$$

$$z_4^{[1]} = w_4^{[1]}x + b_4^{[1]}, a_4^{[1]} = g(z_4^{[1]})$$

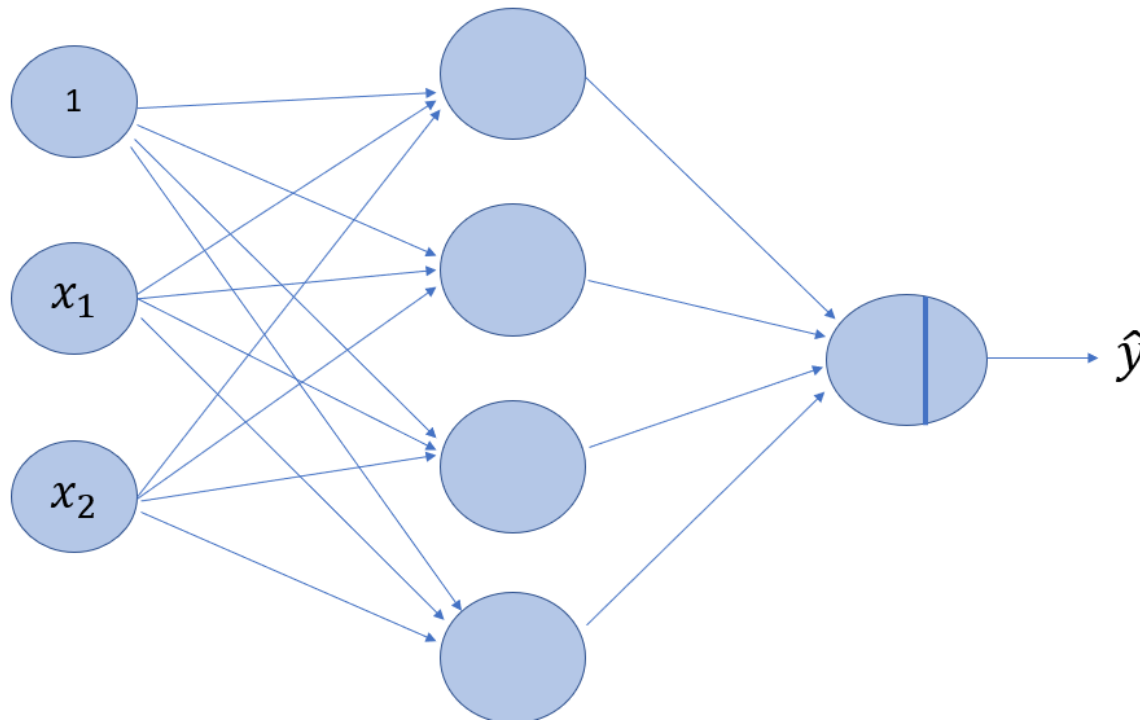
$$z^{[1]} = w^{[1]}x + b^{[1]}, a^{[1]} = g(z^{[1]})$$





$$z^{[2]} = w^{[2]} a^{[1]} + b^{[2]}, a^{[2]} = g(z^{[2]})$$

# Forward propagation



$$z^{[1]} = w^{[1]}x + b^{[1]}$$

$$a^{[1]} = g(z^{[1]})$$

$$z^{[2]} = w^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = g(z^{[2]})$$

$$L = \frac{1}{2} ||a^{[2]} - y||^2$$

# Training

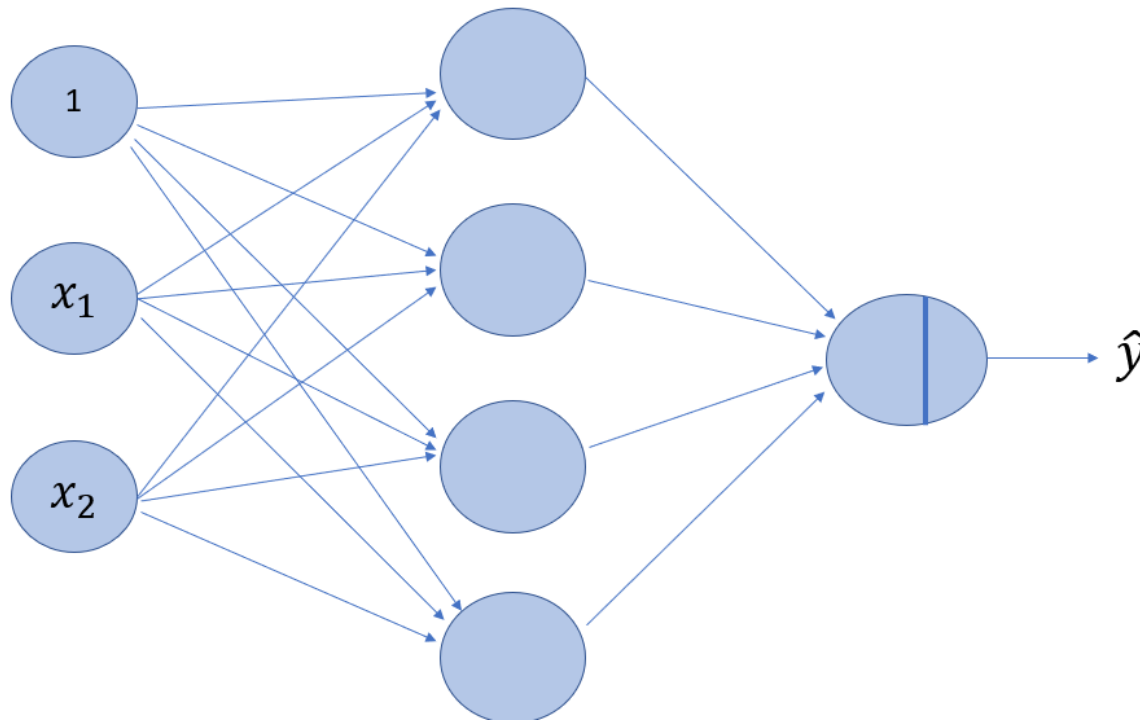
- Minimizing cost function with respect to all the weights:

$$L(w^{[1]}, b^{[1]}, w^{[2]}, b^{[2]}) = \frac{1}{2} ||a^{[2]} - y||^2$$

# Gradient descent

- Initialize  $w^{[1]}, b^{[1]}, w^{[2]}, b^{[2]}$
- While (not converge):
  - compute  $\frac{\partial L}{\partial w^{[1]}}, \frac{\partial L}{\partial b^{[1]}}, \frac{\partial L}{\partial w^{[2]}}, \frac{\partial L}{\partial b^{[2]}}$
  - $w^{[1]} = w^{[1]} - \alpha \frac{\partial L}{\partial w^{[1]}}$
  - $b^{[1]} = b^{[1]} - \alpha \frac{\partial L}{\partial b^{[1]}}$
  - $w^{[2]} = w^{[2]} - \alpha \frac{\partial L}{\partial w^{[2]}}$
  - $b^{[2]} = b^{[2]} - \alpha \frac{\partial L}{\partial b^{[2]}}$
- end

# Forward propagation



$$z^{[1]} = w^{[1]}x + b^{[1]}$$

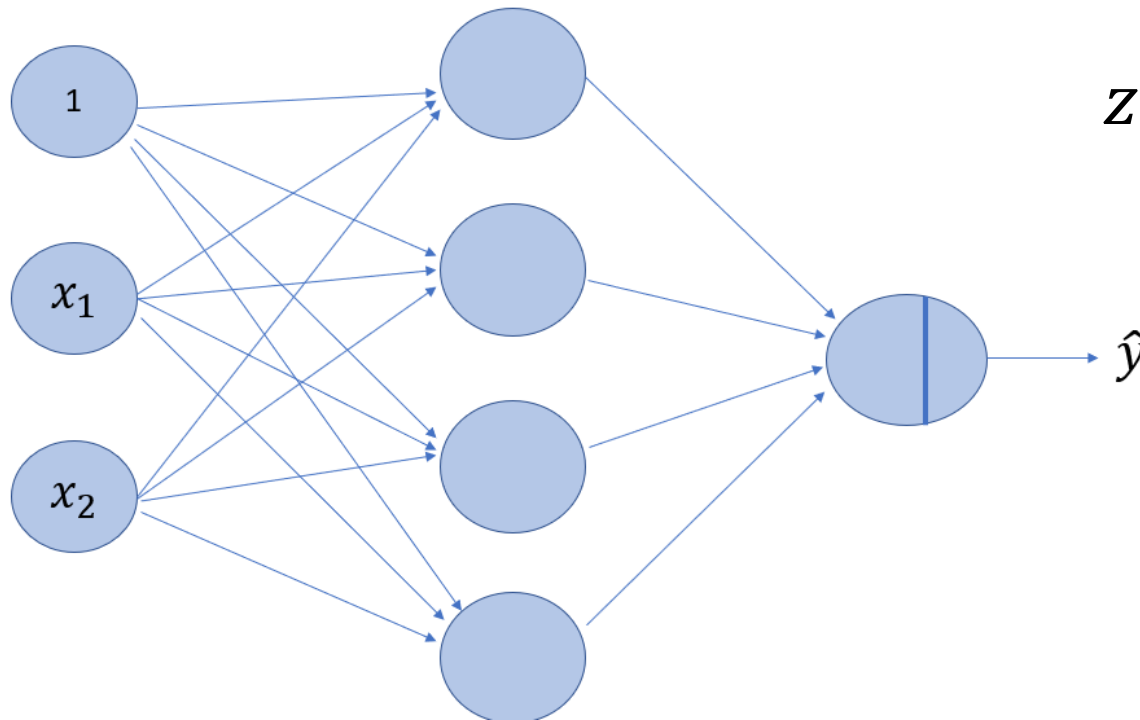
$$a^{[1]} = g(z^{[1]})$$

$$z^{[2]} = w^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = g(z^{[2]})$$

$$L = \frac{1}{2} ||a^{[2]} - y||^2$$

# A different representation



$$z^{[1]} = f_1(w^{[1]}, b^{[1]}, x)$$
$$a^{[1]} = g_1(z^{[1]})$$

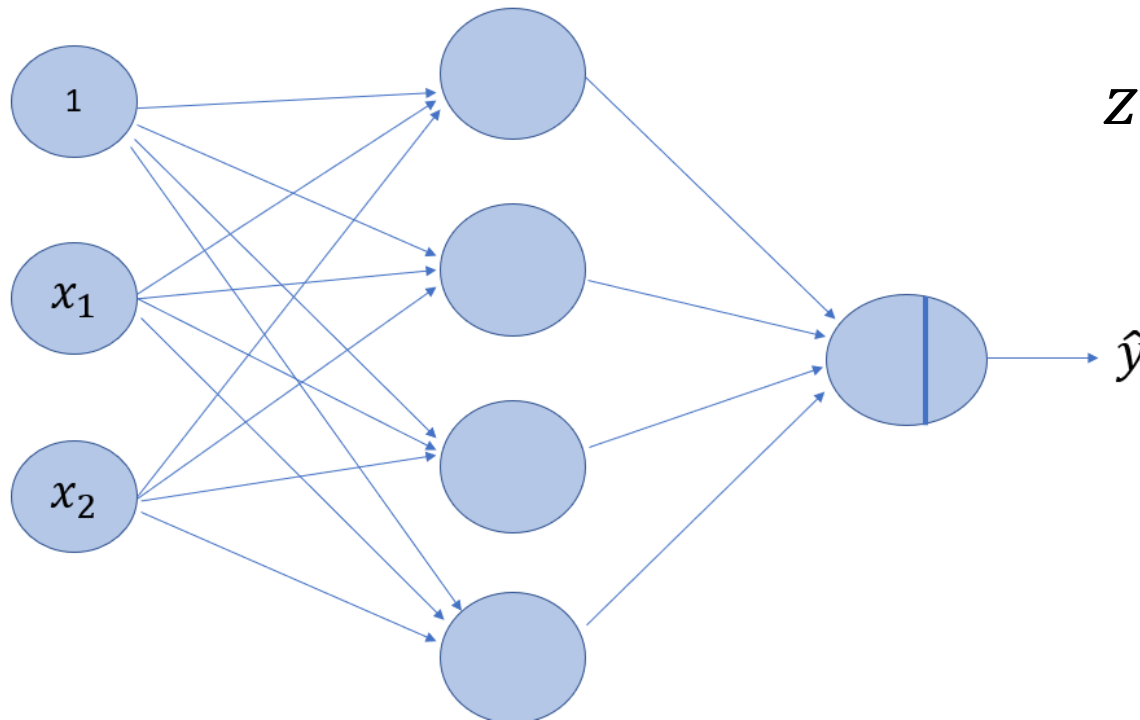
$$z^{[2]} = f_2(w^{[2]}, b^{[2]}, a^{[1]})$$
$$a^{[2]} = g_2(z^{[2]})$$
$$L = l(a^{[2]})$$



# How to calculate these gradients?

- Back propagation!

# Back propagation intuition



$$z^{[1]} = f_1(w^{[1]}, b^{[1]}, x)$$
$$a^{[1]} = g_1(z^{[1]})$$

$$z^{[2]} = f_2(w^{[2]}, b^{[2]}, a^{[1]})$$
$$a^{[2]} = g_2(z^{[2]})$$
$$L = l(a^{[2]})$$

# Back propagation intuition

$$\begin{aligned}z^{[1]} &= f_1(w^{[1]}, b^{[1]}, x) \\ a^{[1]} &= g_1(z^{[1]})\end{aligned}$$

$$\begin{aligned}z^{[2]} &= f_2(w^{[2]}, b^{[2]}, a^{[1]}) \\ a^{[2]} &= g_2(z^{[2]}) \\ L &= l(a^{[2]})\end{aligned}$$

$$\begin{aligned}L &= l(g_2(z^{[2]})) \\ &= l(g_2(f_2(w^{[2]}, b^{[2]}, a^{[1]}))) \\ &= l(g_2(f_2(w^{[2]}, b^{[2]}, g_1(z^{[1]})))) \\ &= l(g_2(f_2(w^{[2]}, b^{[2]}, g_1(f_1(w^{[1]}, b^{[1]}, x))))))\end{aligned}$$

# Compute gradients

$$L = l \left( g_2 \left( f_2(w^{[2]}, b^{[2]}, g_1(f_1(w^{[1]}, b^{[1]})) \right) \right)$$

How to compute  $\frac{\partial L}{\partial w^{[2]}}$  ?

$$z^{[1]} = f_1(w^{[1]}, b^{[1]})$$

$$a^{[1]} = g_1(z^{[1]})$$

Chain rule!

$$z^{[2]} = f_2(w^{[2]}, b^{[2]}, a^{[1]})$$

$$a^{[2]} = g_2(z^{[2]})$$

$$L = l(a^{[2]})$$

# Compute gradients

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How to compute  $\frac{\partial L}{\partial w^{[2]}}$  ?

Chain rule!

$$\frac{\partial L}{\partial w^{[2]}} = \frac{\partial L}{\partial g_2} \frac{\partial g_2}{\partial f_2} \frac{\partial f_2}{\partial w^{[2]}}$$



# Compute gradients

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$$a^{[2]} = g_2(z^{[2]})$$

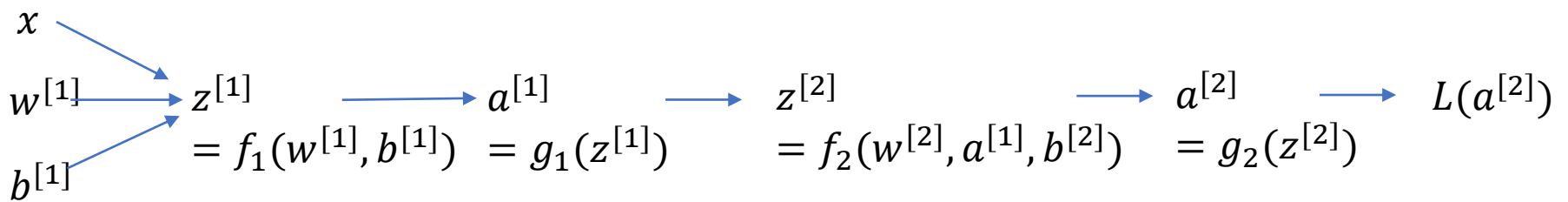
$$L = \frac{1}{2} ||a^{[2]} - y||^2$$

Similarly, for the other three

$$L = l \left( g_2 \left( f_2(w^{[2]}, b^{[2]}, g_1(f_1(w^{[1]}, b^{[1]})) \right) \right)$$

# Back Propagation

$$\frac{\partial L}{\partial w^{[1]}} = \frac{\partial L}{\partial g_2} \frac{\partial g_2}{\partial f_2} \frac{\partial f_2}{\partial g_1} \frac{\partial g_1}{\partial f_1} \frac{\partial f_1}{\partial w^{[1]}}$$



# 2018 Turing Award winners



From left to right: Yann LeCun | Photo: Facebook; Geoffrey Hinton | Photo: Google; Yoshua Bengio | Photo: Botler AI

Godfathers of AI

<https://www.theverge.com/2019/3/27/18280665/ai-godfathers-turing-award-2018-yoshua-bengio-geoffrey-hinton-yann-lecun>

<https://amturing.acm.org/>

## Geoffrey Hinton

**Backpropagation:** In a 1986 paper, “Learning Internal Representations by Error Propagation,” co-authored with David Rumelhart and Ronald Williams, Hinton demonstrated that the backpropagation algorithm allowed neural nets to discover their own internal representations of data, making it possible to use neural nets to solve problems that had previously been thought beyond their reach. The backpropagation algorithm is standard in most neural networks today.

**Boltzmann Machines:** In 1983, with Terrence Sejnowski, Hinton invented Boltzmann Machines, one of the first neural networks capable of learning internal representations in neurons that were not part of the input or output.

**Improvements to convolutional neural networks:** In 2012, with his students, Alex Krizhevsky and Ilya Sutskever, Hinton improved convolutional neural networks using rectified linear units and dropout regularization. In the prominent ImageNet competition, Hinton and his students almost halved the error for object recognition and reshaped the computer vision field.

## Yann LeCun

**Convolutional neural networks:** In the 1980s, LeCun developed convolutional neural networks, a foundational principle in the field, which, among other advantages, have been essential in making deep learning more efficient. In the late 1980s, while working at the University of Toronto and Bell Labs, LeCun was the first to train a convolutional neural network system on images of handwritten digits. Today, convolutional neural networks are an industry standard in computer vision, as well as in speech recognition, speech synthesis, image synthesis, and natural language processing. They are used in a wide variety of applications, including autonomous driving, medical image analysis, voice-activated assistants, and information filtering.

**Improving backpropagation algorithms:** LeCun proposed an early version of the backpropagation algorithm (backprop), and gave a clean derivation of it based on variational principles. His work to speed up backpropagation algorithms included describing two simple methods to accelerate learning time.

**Broadening the vision of neural networks:** LeCun is also credited with developing a broader vision for neural networks as a computational model for a wide range of tasks, introducing in early work a number of concepts now fundamental in AI. For example, in the context of recognizing images, he studied how hierarchical feature representation can be learned in neural networks—a concept that is now routinely used in many recognition tasks. Together with Léon Bottou, he proposed the idea, used in every modern deep learning software, that learning systems can be built as complex networks of modules where backpropagation is performed through automatic differentiation. They also proposed deep learning architectures that can manipulate structured data, such as graphs.

<https://amturing.acm.org/>