Lecture 11 Unsupervised learning

GEOL 4397: Data analytics and machine learning for geoscientists

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March. 26th, 2019





	Week	Date	Topics	Comments
			Overview of syllabus	
	1	01/15 Tues	Lecture: Introduction to Machine learning: applications	
		01/17 Thur	Lecture: Review of linear algebra	
	2	01/22 Tues	Lab: Linear algebra in Python	Not graded
		01/24 Thur	Lecture: Introduction to optimization	
	3	01/29 Tues	Lab: Gradient descent + Linear regression	Report due on 02/05 at 5:30 pm
		01/31 Thur	Lecture: Introduction to machine learning: concepts	
	4	02/05 Tues	Lecture: Logistic regression	
		02/07 Thur	Lab: Logistic regression	Report due on 02/14 at 5:30 pm
	5	02/12 Tues	Lecture: Support vector machine	
		02/14 Thur	Lab: Support vector machine	Report due on 02/21 at 5:30 pm
	6	02/19 Tues	Lecture: Decision trees	
		02/21 Thur	Lab: Decision trees	Report due on 02/28 at 5:30 pm
	7	02/26 Tues	Lecture: Random Forest	
		02/28 Thur	Lab: Random forest	Report due on 03/07 at 5:30 pm
	8	03/05 Tues	Lecture: Ensemble learning	
		03/07 Thur	Lab: Ensemble learning	Reprot due on 03/19 at 5:30 pm
	9	03/12 Tues	No class due to spring break	
		03/14 Thur	No class due to spring break	
	10	03/19 Tues	Review & Recap	
		03/21 Thur	Exam	
	11	03/26 Tues	Lecture: Clustering	
		03/28 Thur	Lab: Clustering	Report due on 04/04 at 5:30 pm
	12	04/02 Tues	Lecture: Introduction to TensorFlow	
		04/04 Thur	Lab: TensorFlow	Not graded
	13	04/09 Tues	Lecture: Introduction to neural networks 1	
		04/11 Thur	Lecture: Introduction to neural networks 2	
	14	04/16 Tues	Lab: Deep learning	Report due on 04/23 at 5:30pm
		04/18 Thur	Lecture: Convolutional neural networks 1	
	15	04/23 Tues	Guest lecture: Convolutional neural networks 2	
		04/25 Thur	Lab: CNN (optional)	Report due on 05/02 at 5:30 pm
	16	04/30 Tues	final presentation??	
lia		05/02 Thur	final presentation??	2
Jia	Note	28 class meetings		04/29 last day of class

Outline

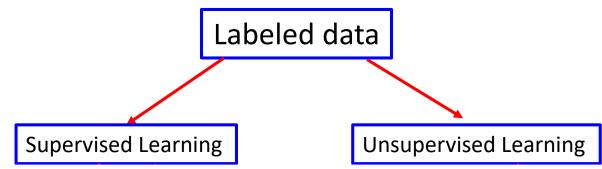
Dimensionality reduction

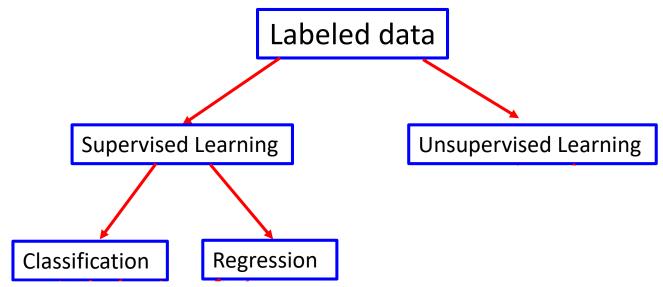
K-means Clustering

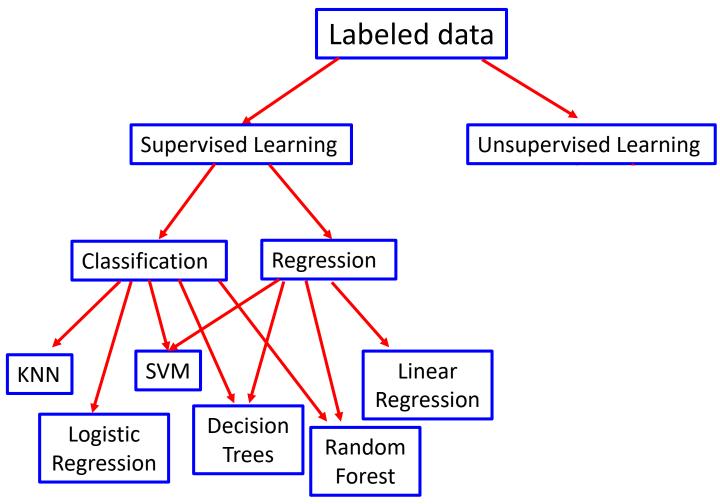
Implementation in Scikit-Learn

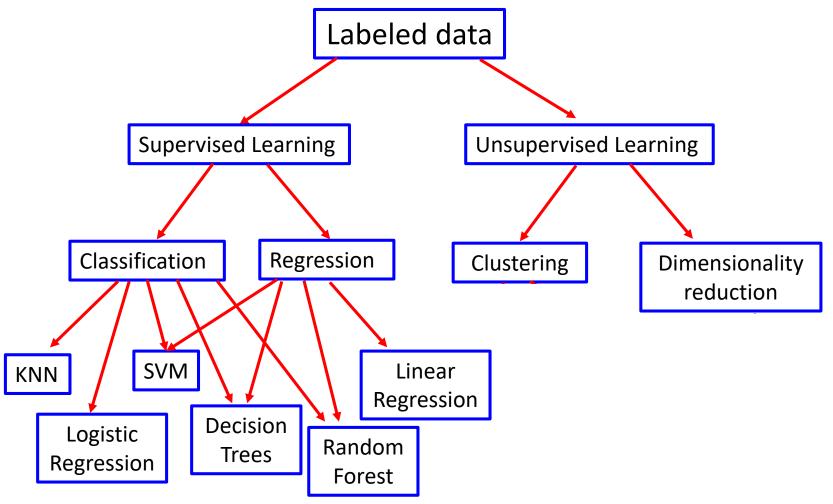
Acknowledgments

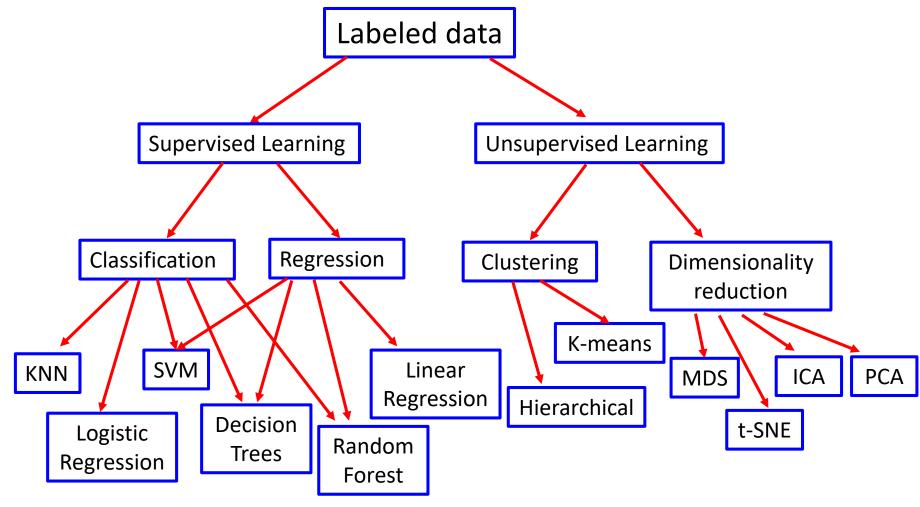
- Youtube video by Joshua Starmer: https://goo.gl/RDMb4P
- Youtube video by Luis Serrano: https://goo.gl/wuSYXK









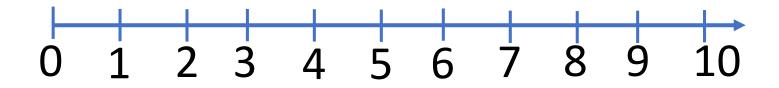


Dimensionality reduction

 Reduces high-dimensional data into 2D (or 3D) space for better visualization and analysis

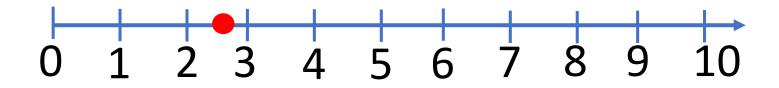
Introduction to dimensions

Fundamental yet important concepts



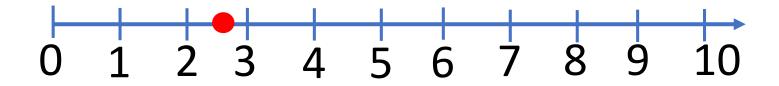
1-Dimension (1D) = a number line

1-Dimension (1D) = a number line



Suppose I measure the average density of some crustal rocks: 2.67 g/cc

1-Dimension (1D) = a number line



Suppose I measured densities on several different rocks:

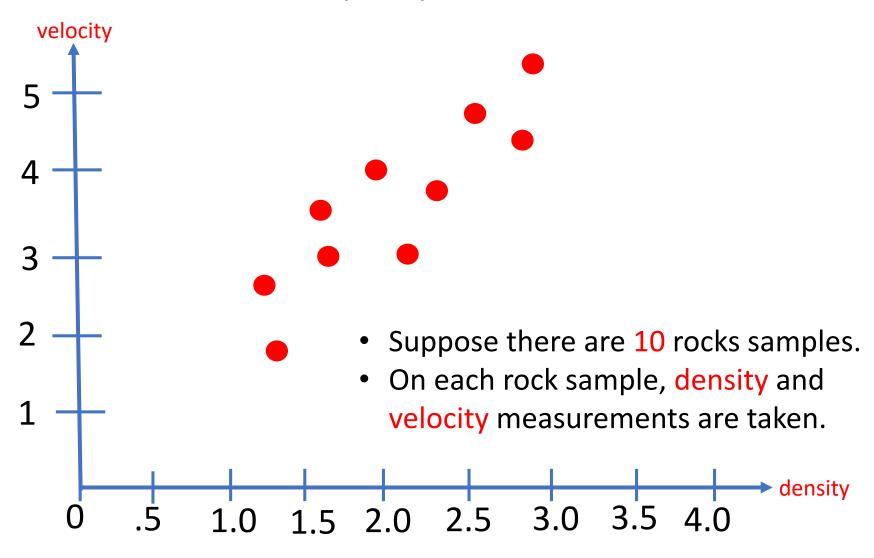
2.14 g/cc, 2.67 g/cc, 3.25 g/cc, 3.86 g/cc

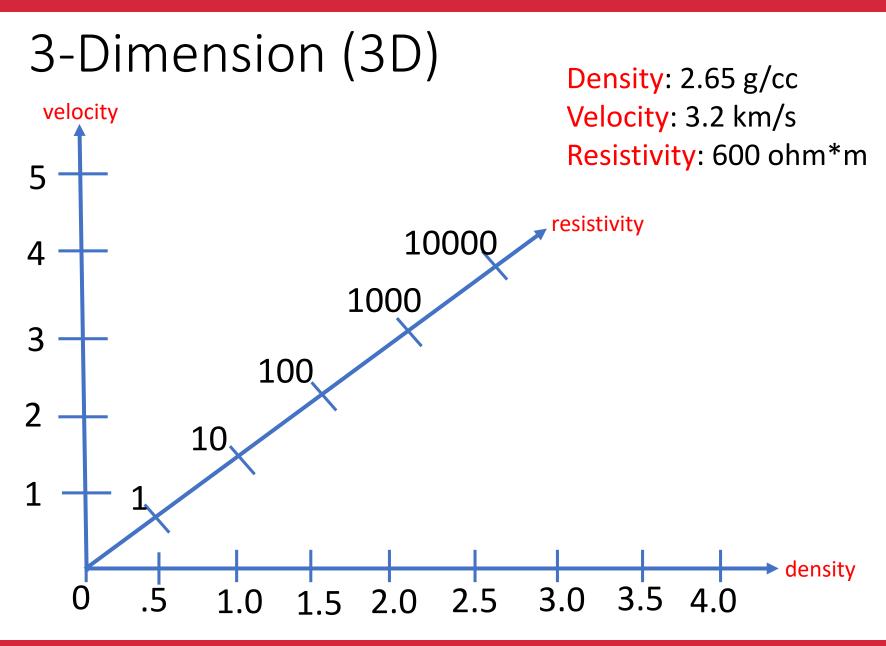
1-Dimension (1D) = a number line



Suppose I measured densities on several different rocks:

2.14 g/cc, 2.67 g/cc, 3.25 g/cc, 3.86 g/cc





- 1 measurement = 1D graph
- 2 measurements = 2D graph
- 3 measurements = 3D graph

- 1 measurement = 1D graph
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- 3 measurements = 3D graph
- 4 measurements = 4D graph (you cannot draw it)

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- 4 measurements = 4D graph (you cannot draw it)
- 200 measurements = 200D graph

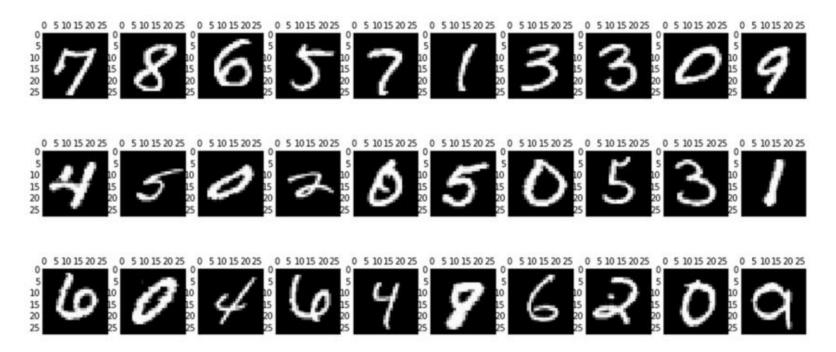
- 1 measurement = 1D graph
- 2 measurements = 2D graph
- 3 measurements = 3D graph
- 4 measurements = 4D graph (you cannot draw it)
- 200 measurements = 200D graph

Each more physical property measurement we make on one rock sample adds one more dimension.

In-class quiz

- Geochemical facies analysis
- Data consists of XRF measurements of cuttings from the lateral section of an unconventional well
- Measurements made at approximately 10 m intervals
- For each cutting sample, there were 22 measurements.
- A total of 269 cutting samples
- Question: If we plot up the measurements, what is the dimension of the space? How many points are there in this high dimensional space?

In-class quiz 2



Some examples of MNIST handwritten digits

Each image is a 28 X 28 pixel images

A total of 70,000 images

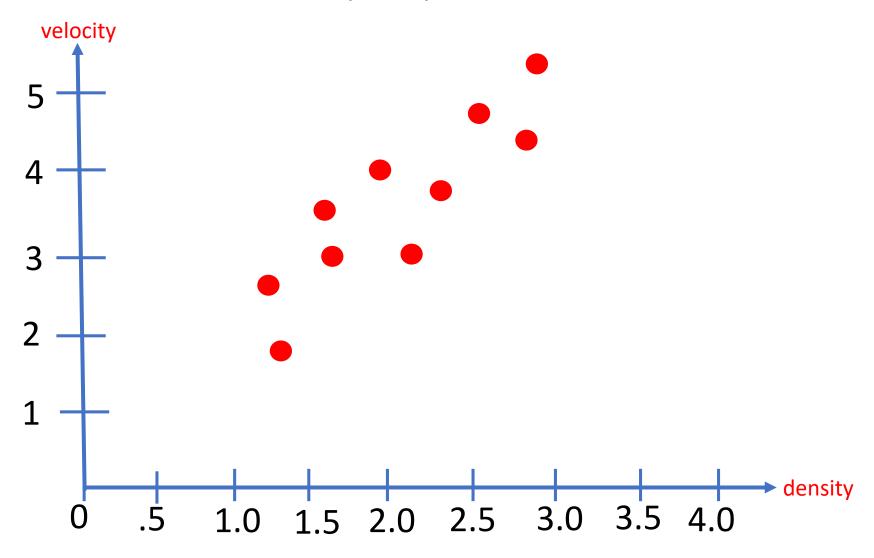
Question: Suppose we want to plot up all 70,000 images in a high dimensional space, what should the dimension of this space be?

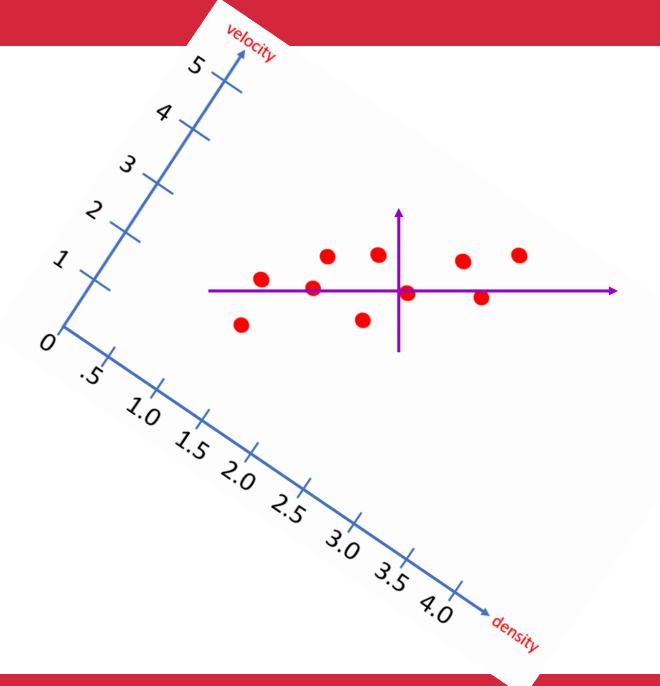
Questions

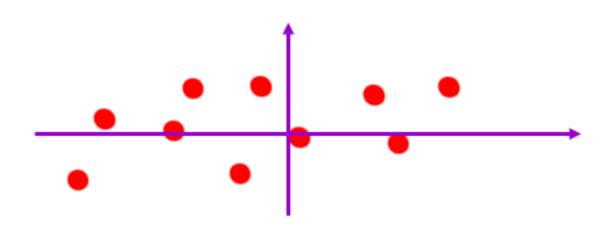
- How to visualize high-dimensional data?
- Are all those dimensional equally important? Or some more important than others?

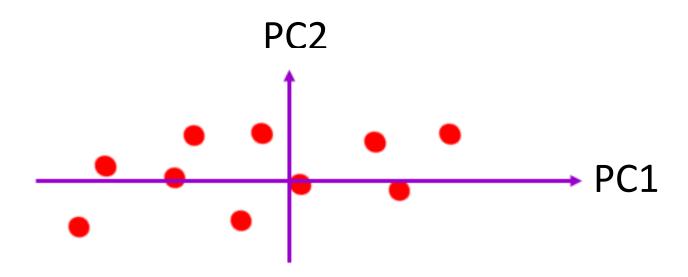
PCA

 Reduces a high-dimensional dataset (e.g., 22-D dimensional) to 2 or 3 dimensions for better visualization



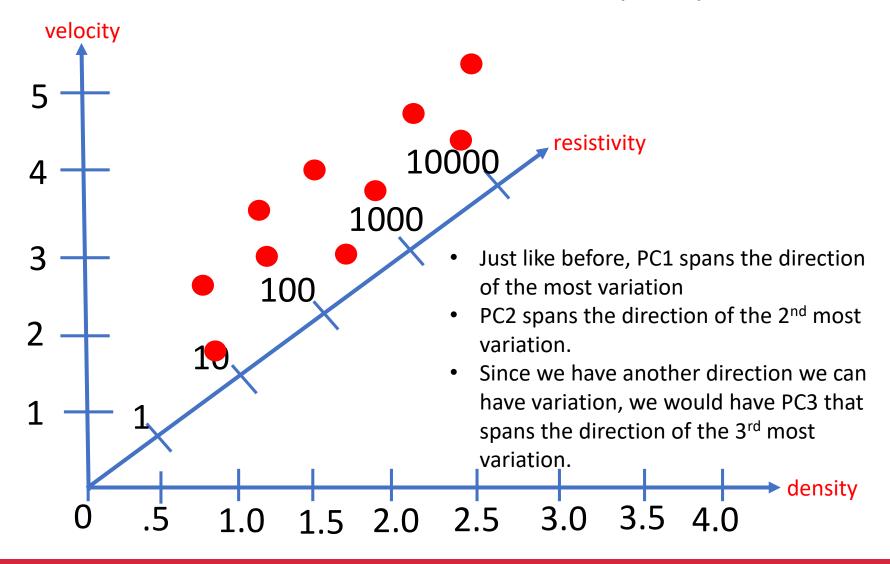






- PC1 (the first component) is the axis that spans the most variation
- PC2 (the second component) is the axis that spans the second most variation

What if we 3-Dimension (3D) data?



What if we had 4-D data?

- PC1 would span the direction of the most variation.
- PC2 would span the direction of the 2nd most variation.
- PC3 would span the direction of the 3rd most variation.
- PC4 would span the direction of the 4th most variation.

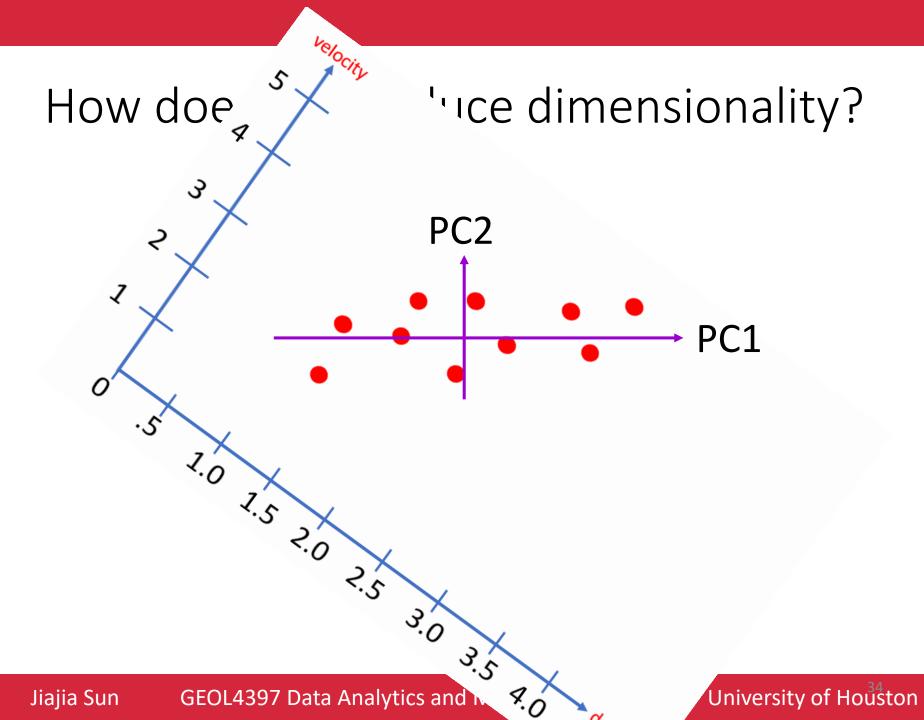
What if we had 4-D data?

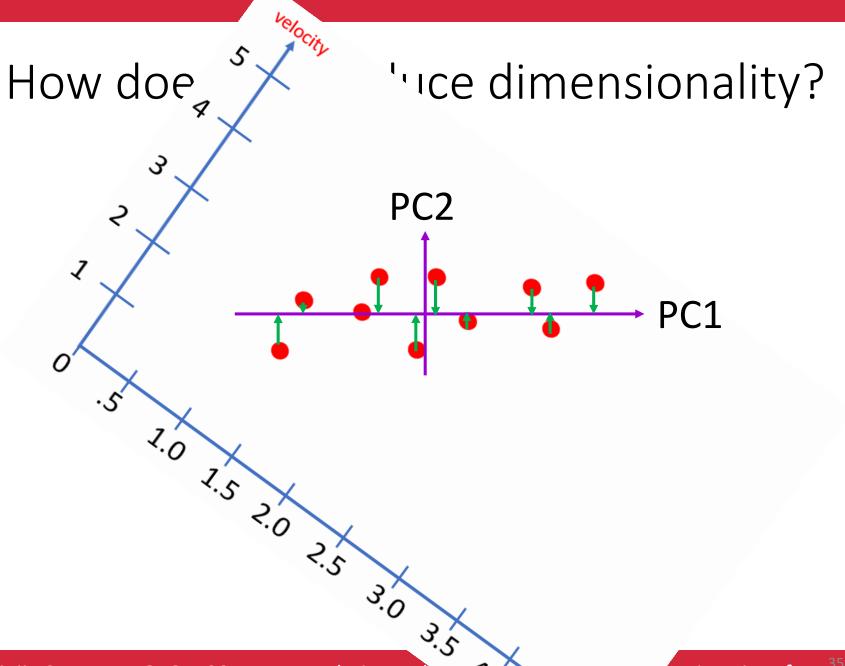
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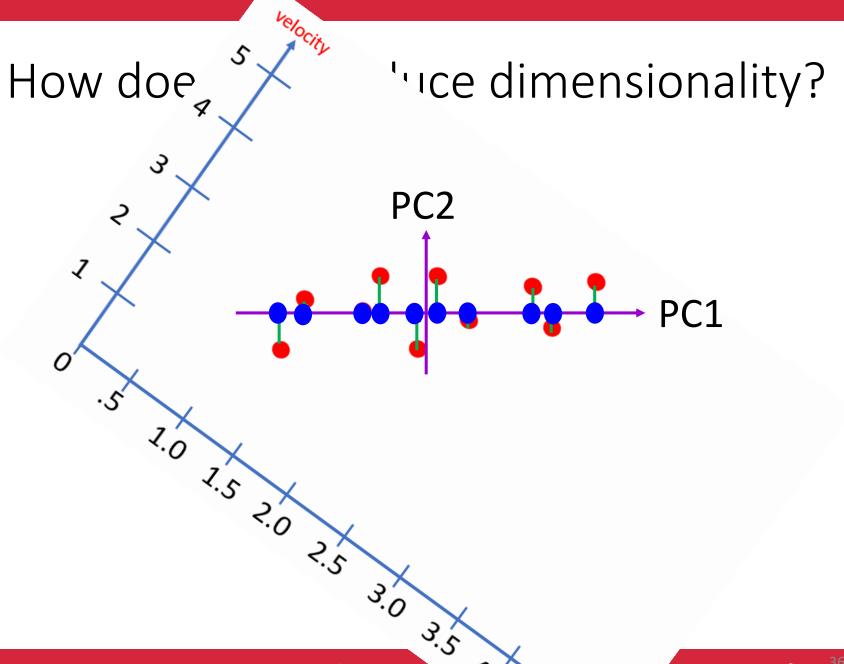
In general,

- There is a PC for each physical property measurement.
- If we had 22 measurements on each cutting sample, we would have 22 PCs.
- PC22 would span the direction of the 22nd most variation.

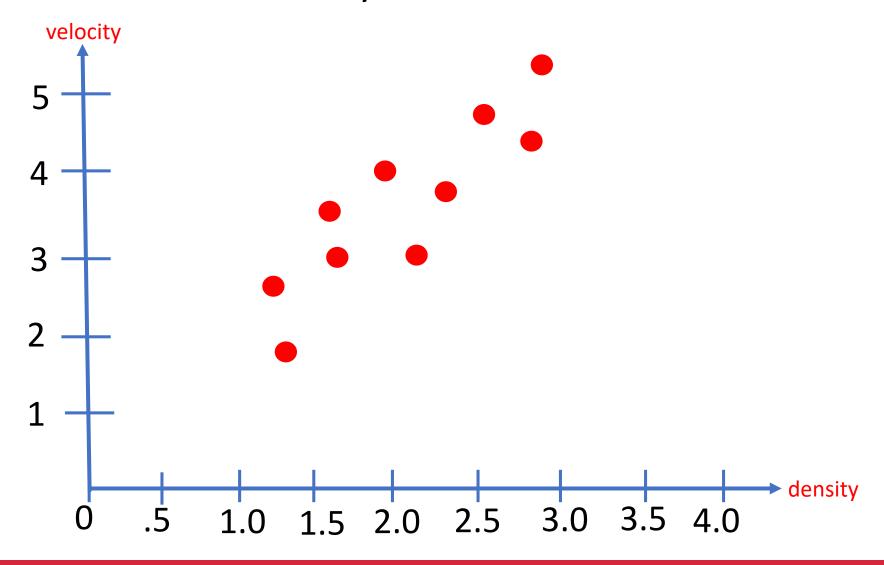
How does PCA reduce dimensionality?







Dimensionality reduction



MNIST dataset: PCA

Original data in 784 dimensional space

First and Second Principal Components colored by digit

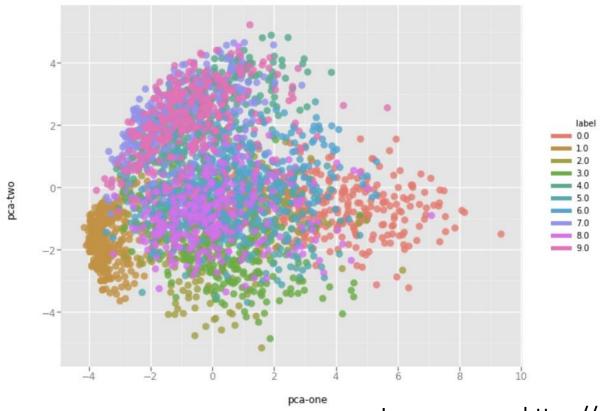


Image source: https://goo.gl/Dj97T7

MNIST dataset: t-SNE

Original data in 784 dimensional space

tSNE dimensions colored by digit

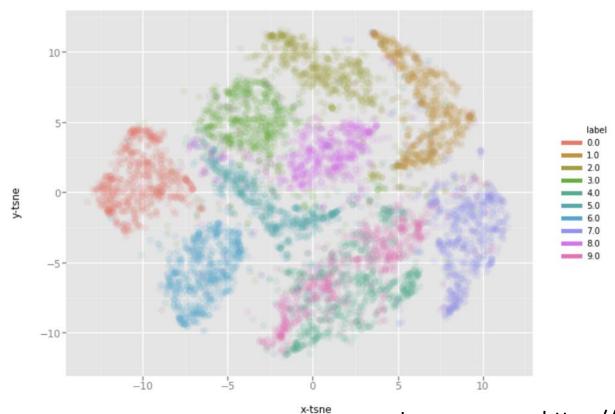


Image source: https://goo.gl/Dj97T7

Example: PCA for high-dimensional data

500,000 DNA sites in human genome projected to 2 dimensions with PCA

Principal components correspond to geography \rightarrow ancestry

Characterize genetic variations in a sample of 3,000 European individuals genotyped at over half a million variable DNA sites in the human genome. They find a close correspondence between genetic and geographic distances. → genetic ancestry testing an individual's DNA can be used to infer their geographic origin with surprising accuracy—often to within a few hundred kilometers.

Novembre et al. (2008), Nature

Thanks to Karianne Bergen

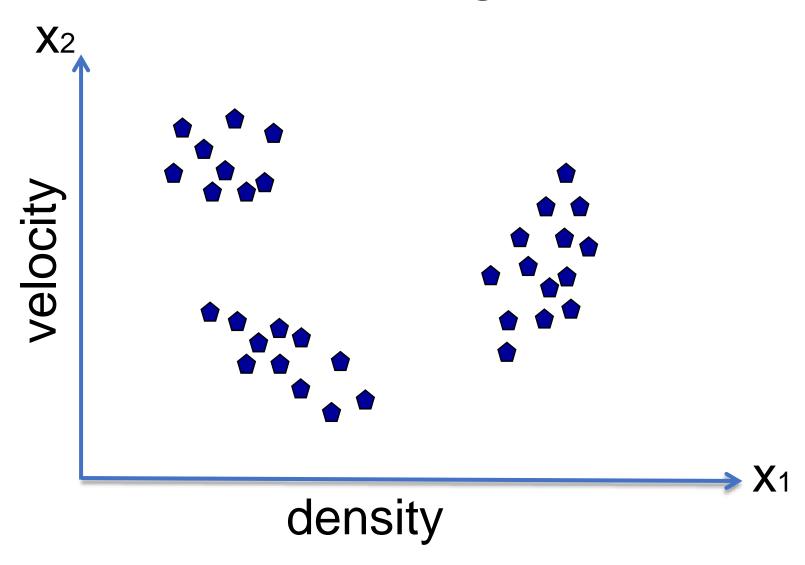
Outline

Dimensionality reduction

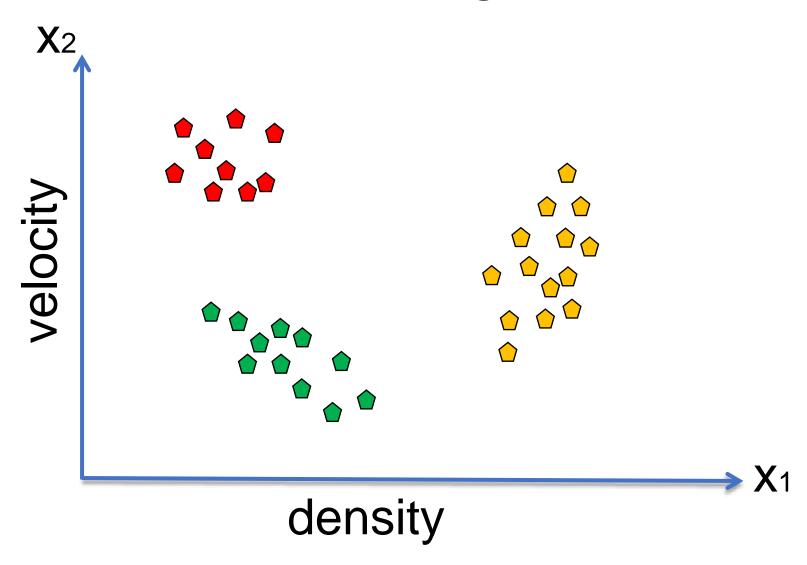
K-means Clustering

Implementation in Scikit-Learn

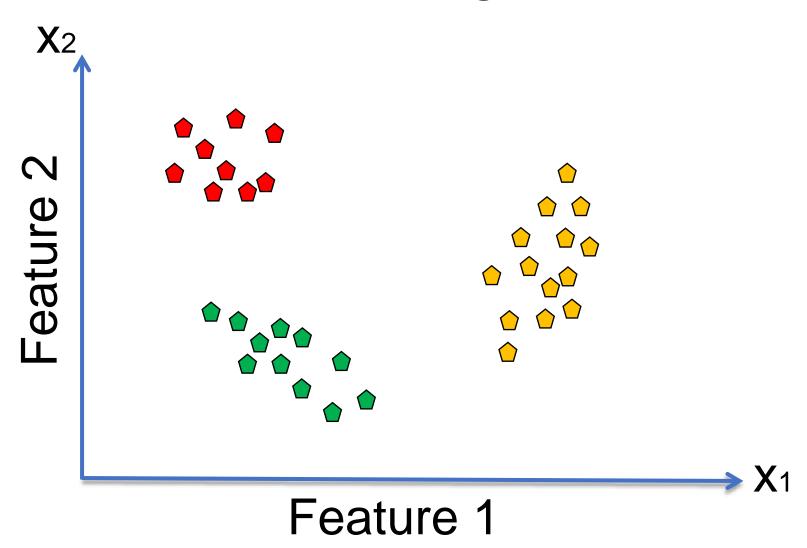
Clustering

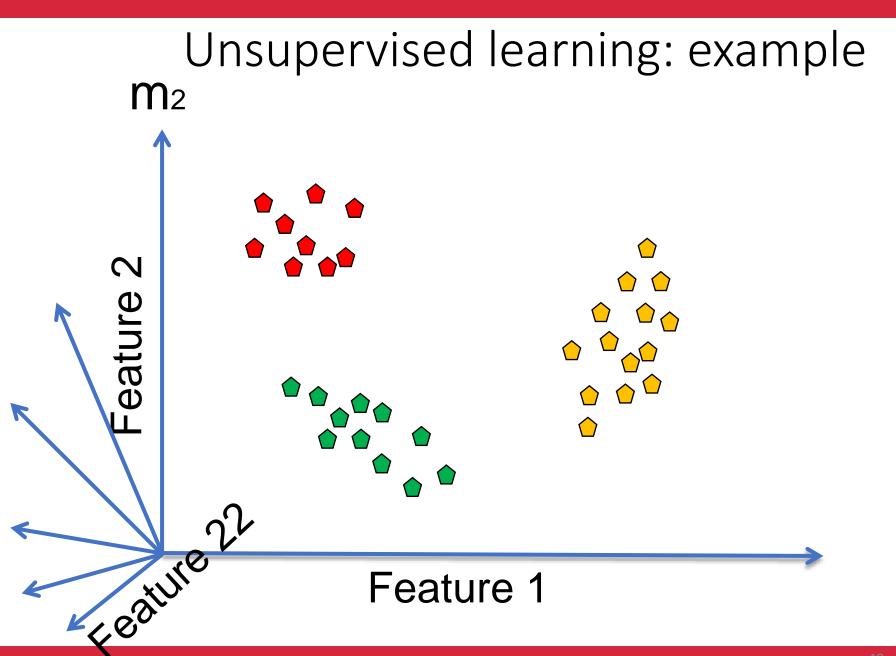


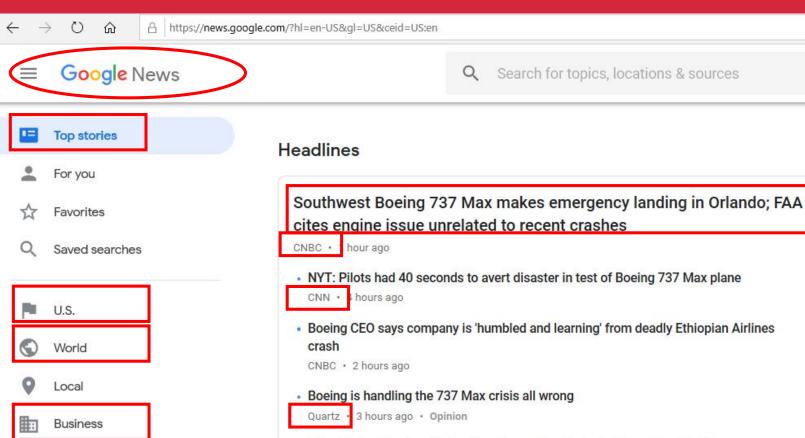
Clustering



Clustering





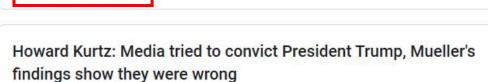


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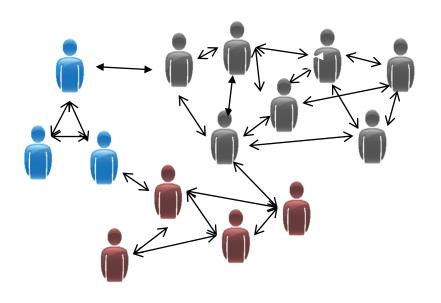
Entertainment

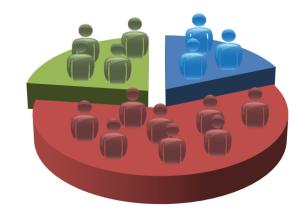




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Unsupervised learning: applications

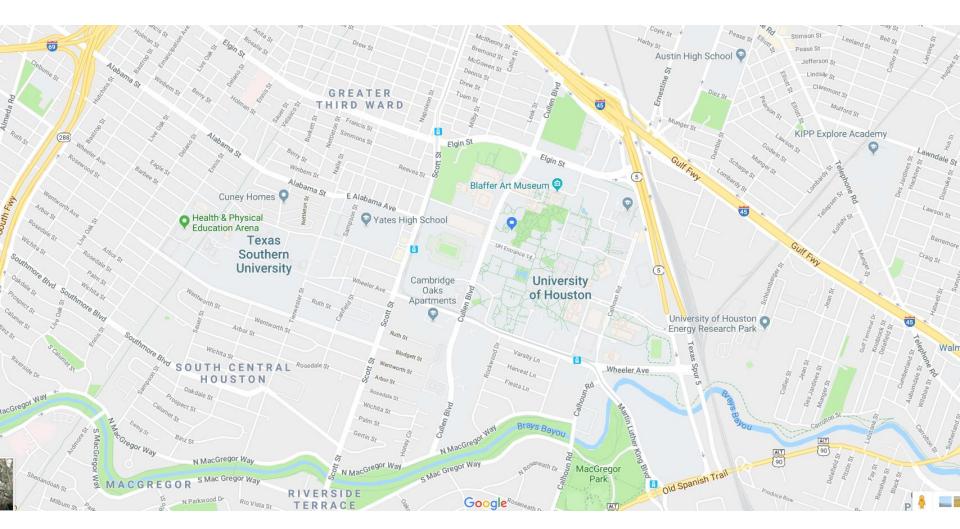




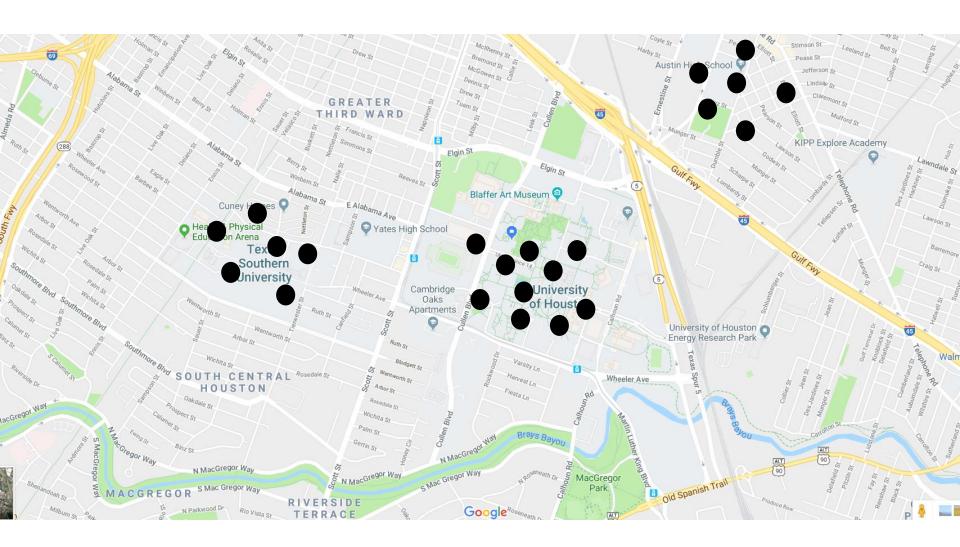
Social network analysis

Market segmentation

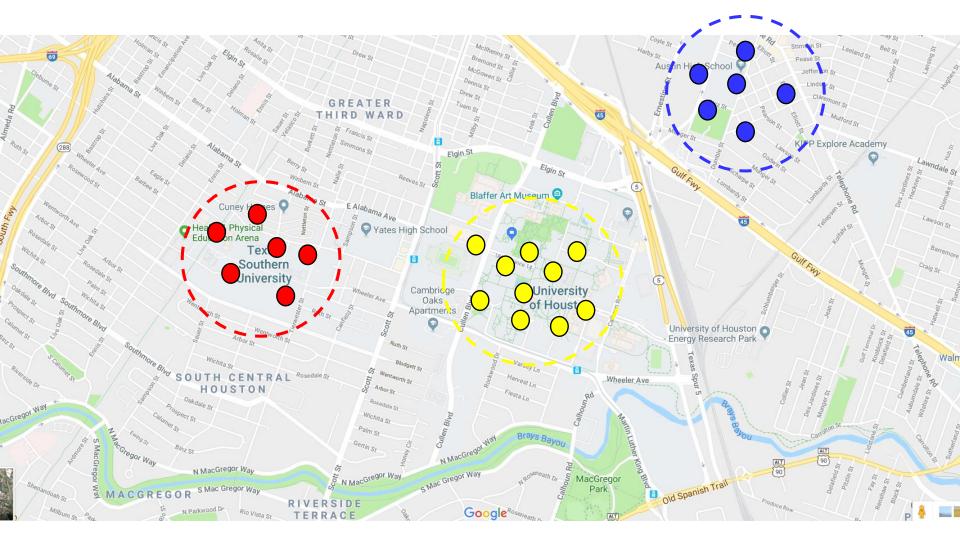
Investing in pizza stores in Houston



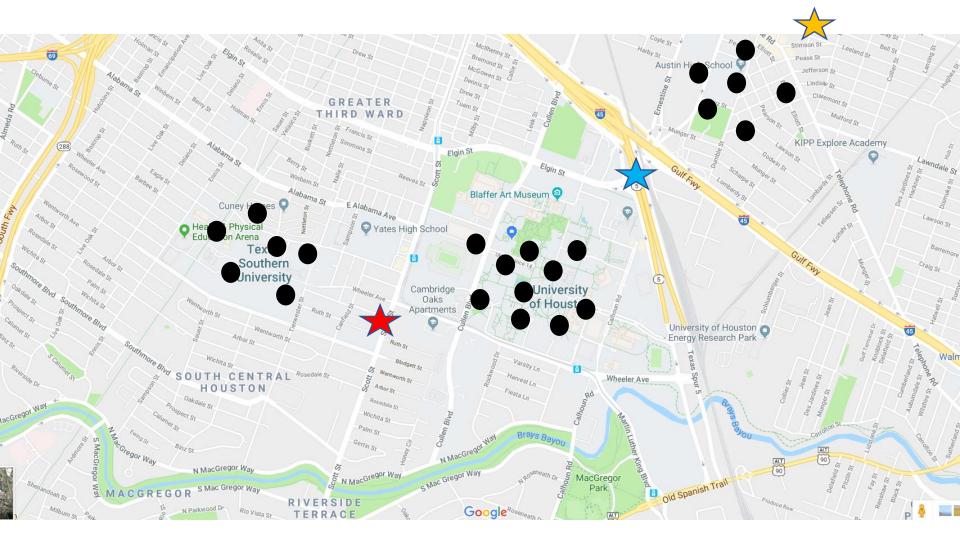
Customer data



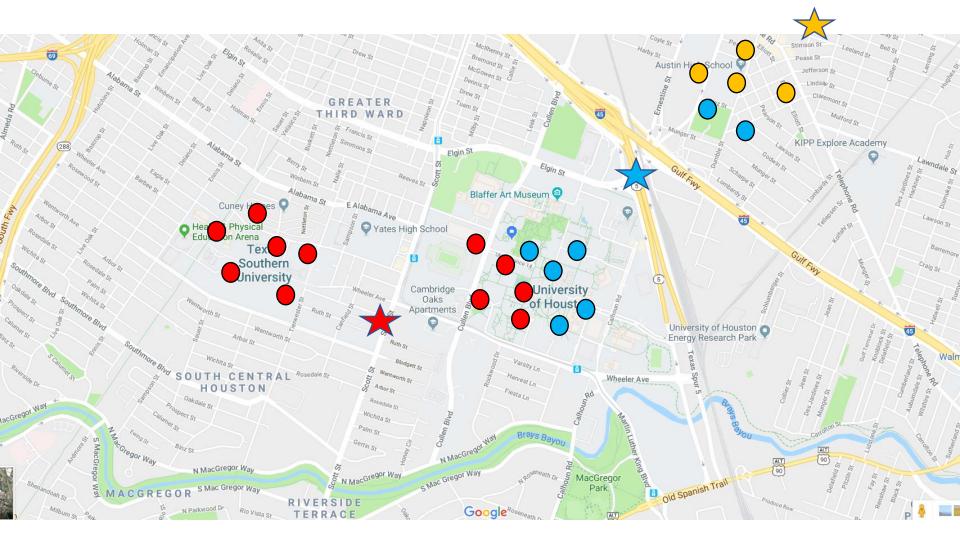
Human wisdom



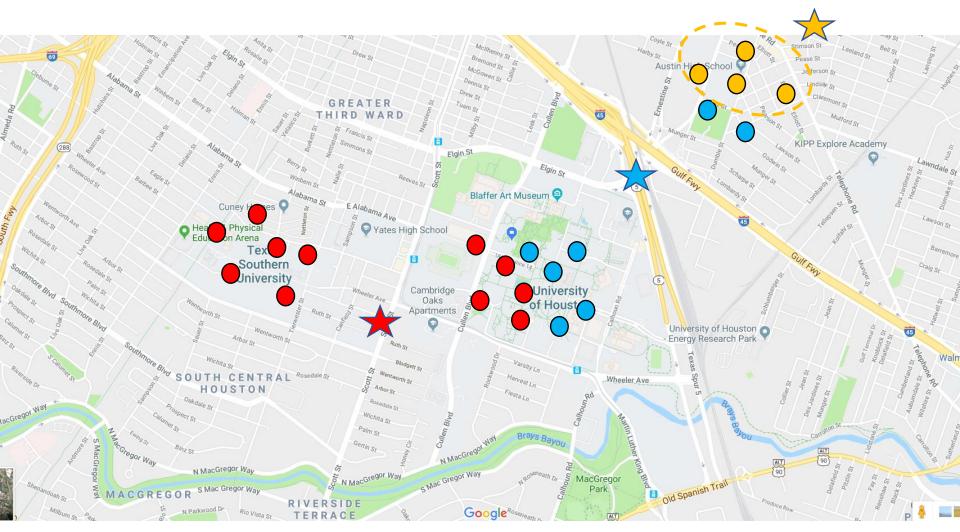
Start with random locations



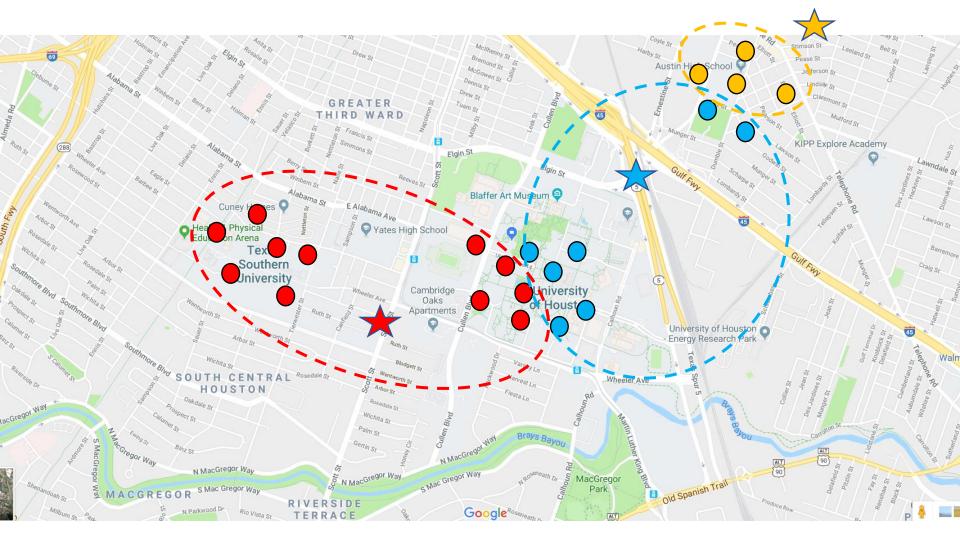
Distribution of customers



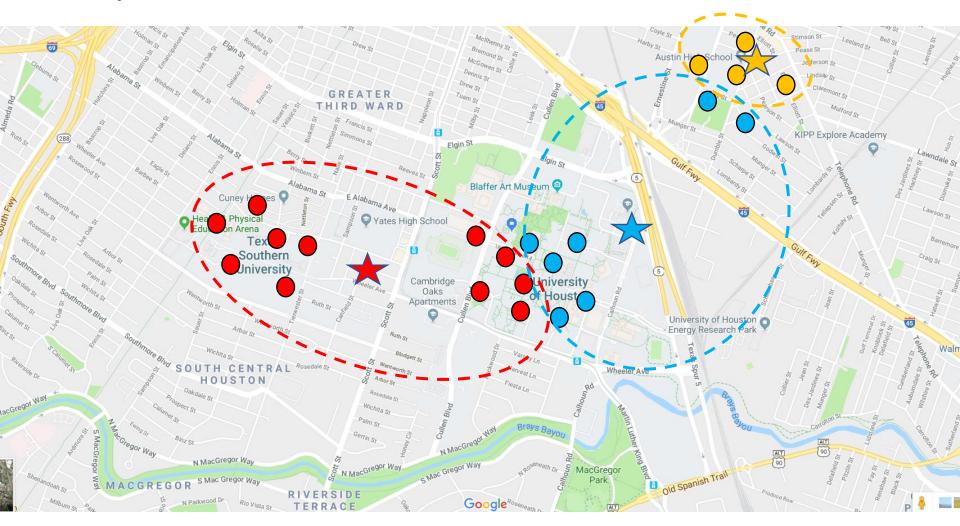
Distribution of customers



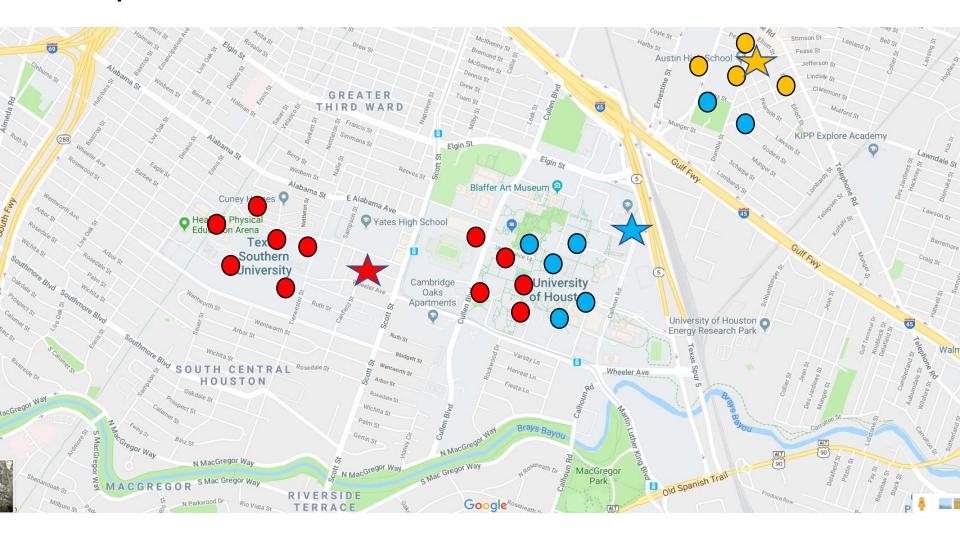
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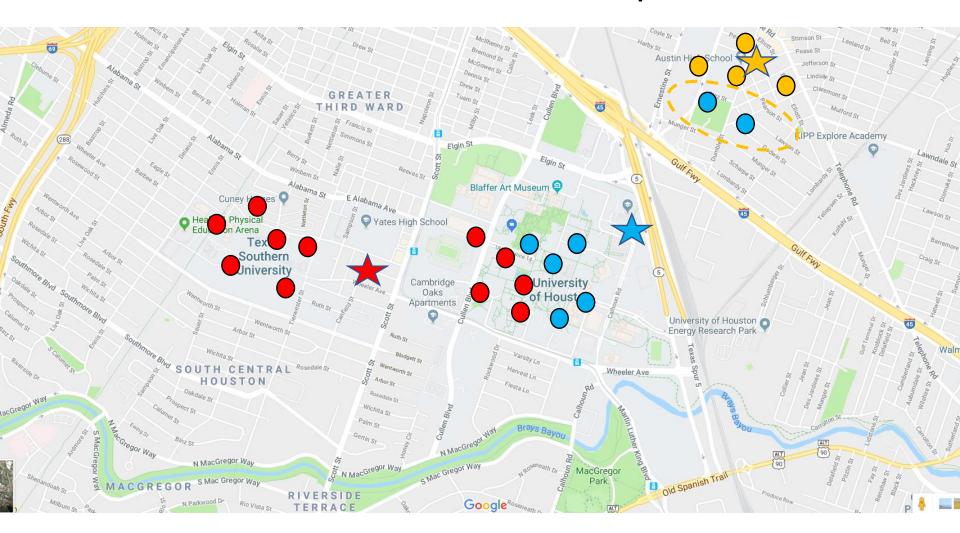


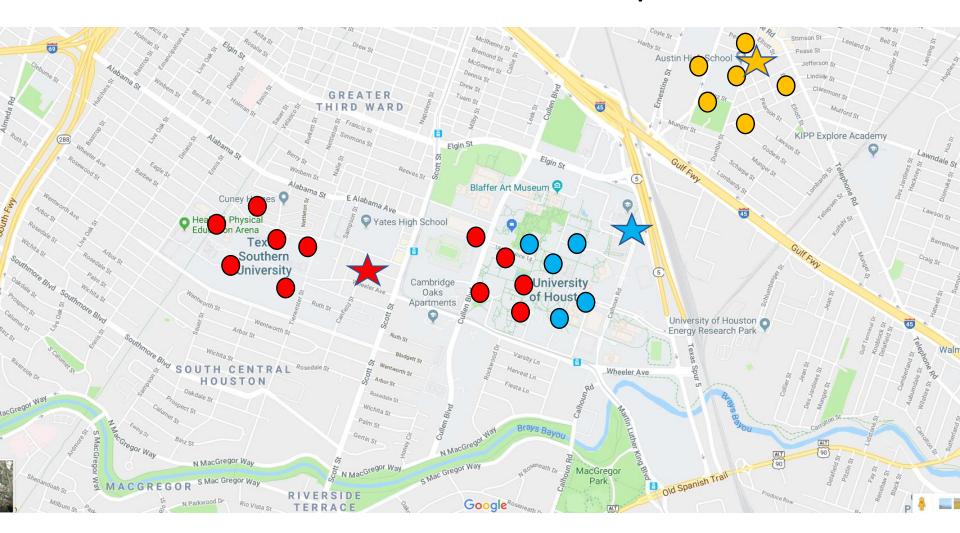
Update store locations

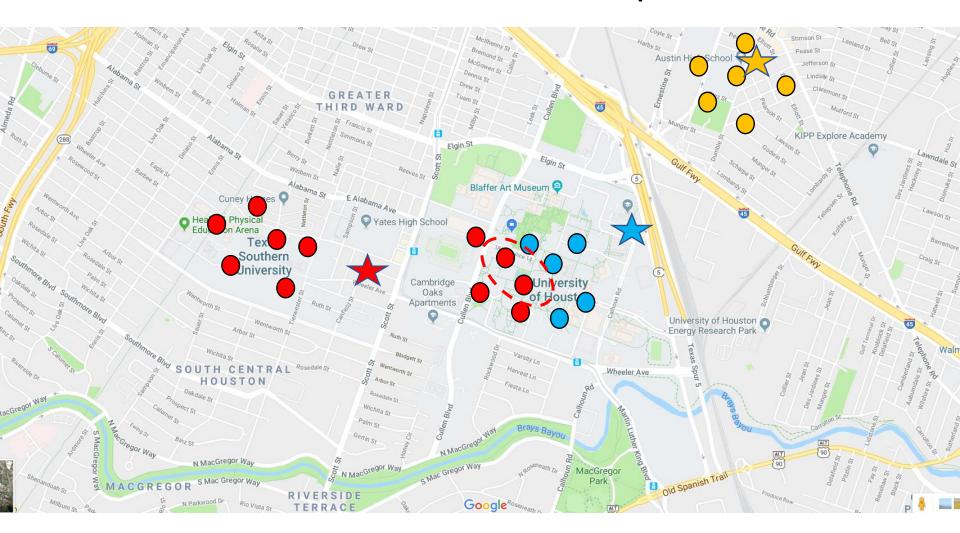


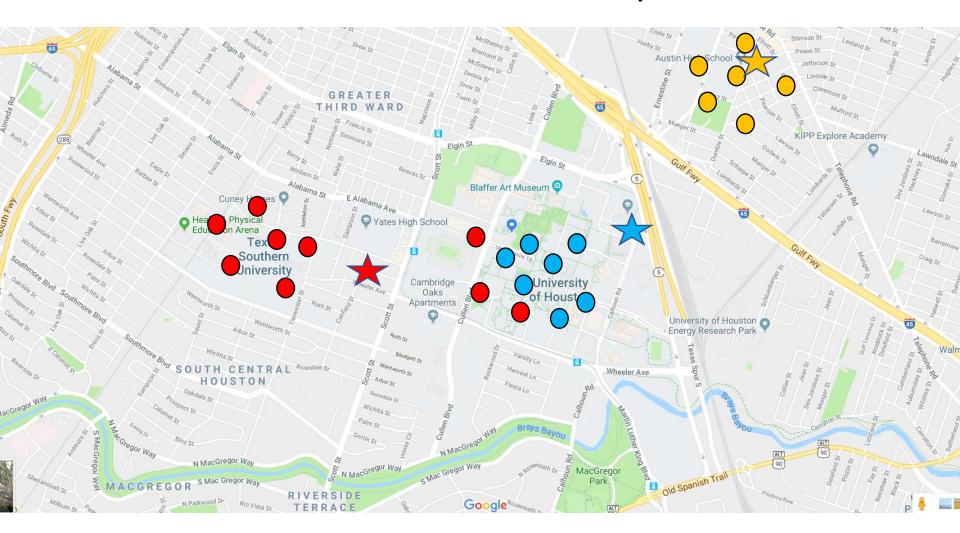
Update store locations



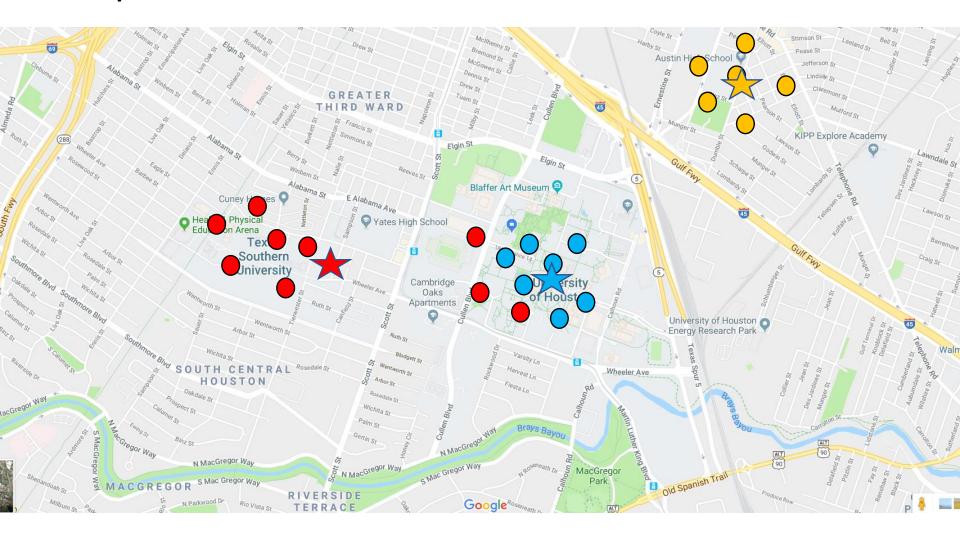




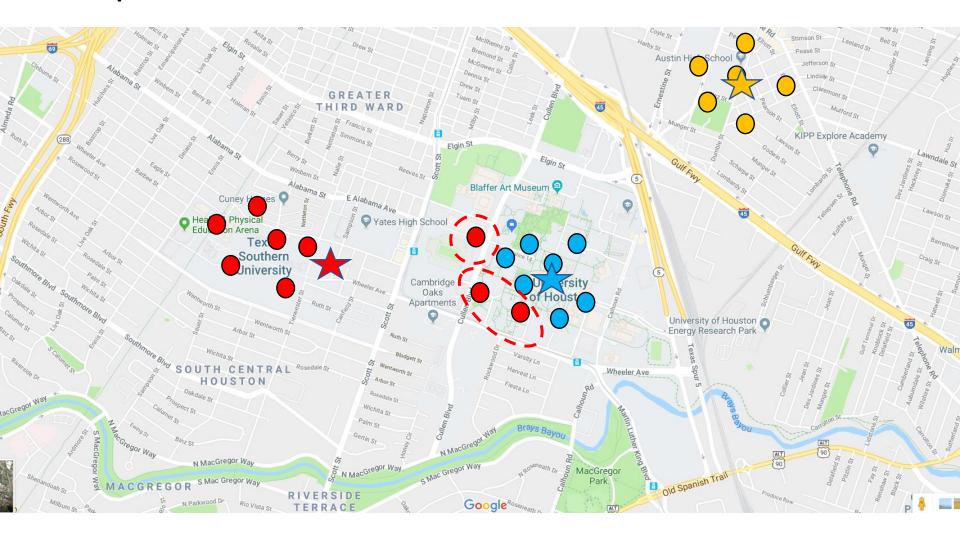




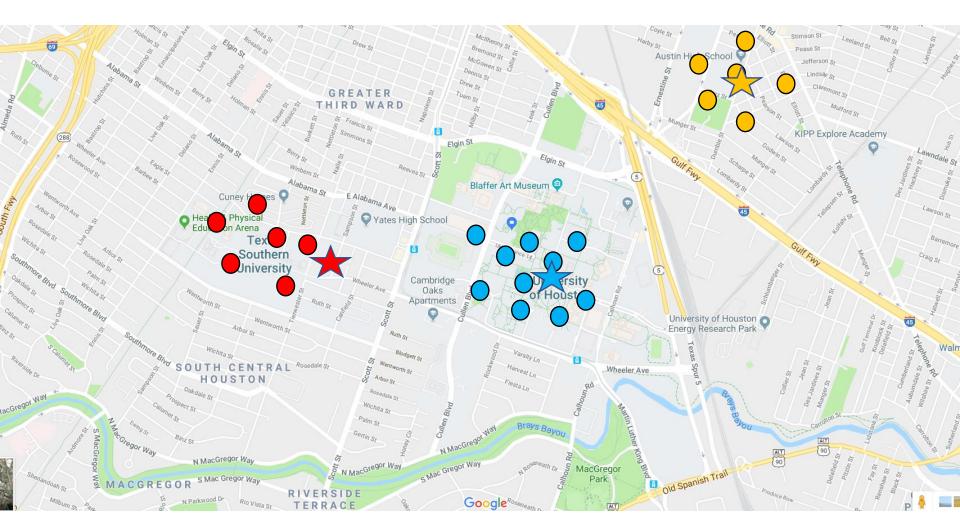
Update store locations



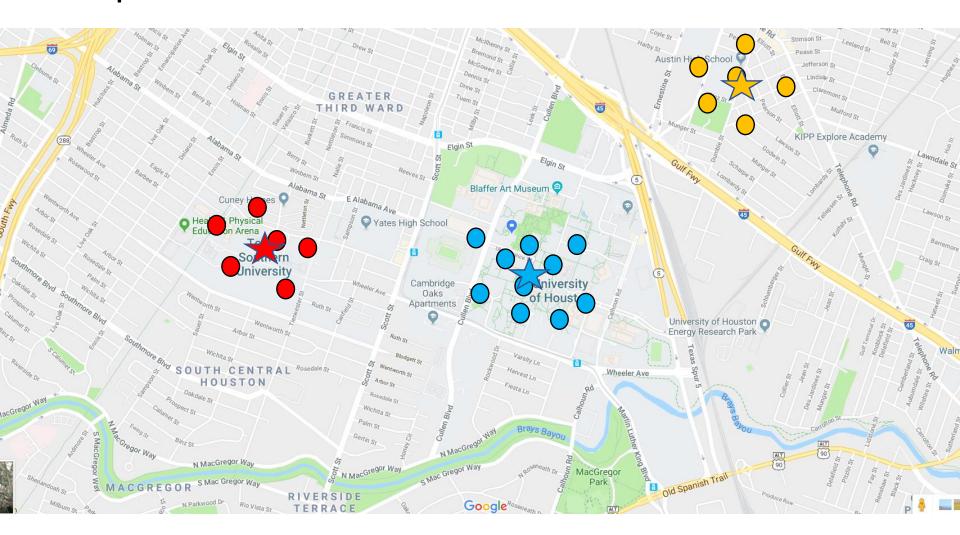
Update customer distributions



K-means clustering



Update store locations



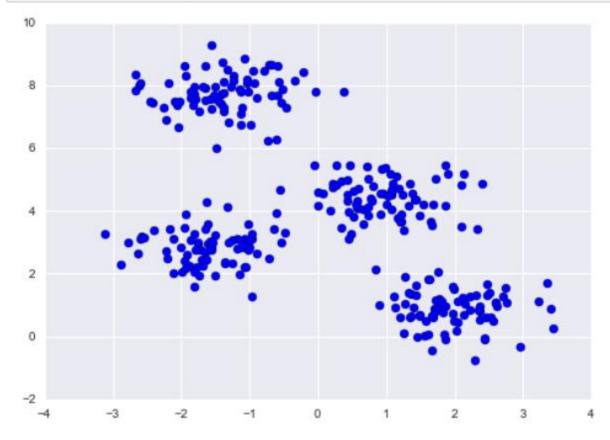
K-means clustering: terminology

- The pizza store locations are called cluster centers or centroids.
- Each group of customers is called a cluster
- Each location or building is called an observation (or an object/instance).

K-means clustering: how it works

- Start with random initial cluster centers
- While (not converge)
 - Calculate distance between each cluster center and each instance.
 - Assign each instance to the nearest cluster center
 - Update cluster centers by calculating the mean of all the instances assigned to the same cluster
- end

Implementation in Scikit-learn



Implementation in Scikit-learn

```
from sklearn.cluster import KMeans
kmeans = KMeans(n_clusters=4)
kmeans.fit(X)
y_kmeans = kmeans.predict(X)
```

Implementation in Scikit-learn

```
plt.scatter(X[:, 0], X[:, 1], c=y_kmeans, s=50, cmap='viridis')
centers = kmeans.cluster_centers_
plt.scatter(centers[:, 0], centers[:, 1], c='black', s=200, alpha=0.5);
```

