# missing data

## Contents

Examine Missing Data		1
Solutions		4
Delete	 	٤
Encode Missing Data	 	6
Impute	 	8
mice	 	8
caret	 	10

Missing data are quite common in real datasets. This may be driven by a number of reasons including, data was not available, was not gathered, or coded incorrectly.

A number of predictive models require complete data. And, even among the predictive models that can function with less than complete data, missing data can only exist in predictors not the response variable. Before we proceed to find a solution to missing data let us examine the reasons for it. The reasons may be broadly categorized as 1. Random: The cause of missing data may be completely random. Survey respondents may neglect to answer certain questions by chance. Person coding data may commit a data entry error. 2. Data deficiency: This may be a missing component of a predictor. Consider a survey containing the alternatives male and female for a question on gender. Those not conforming to a particular gender may not respond.

3. Specific Causes: There are situations where missing data can be clearly attributed to a cause. Survey respondents may refuse to respond to questions on politically sensitive issues such as abortion and right to bear arms. In clinical studies where patients are measured periodically over time, a patient may drop off due to an adverse side effect.

# Examine Missing Data

The pattern of missing data is likely to shed light on the reasons behind it. For small and medium datasets, it is possible to visualize missing data in a chart such as a heatmap. When the dataset has a large number of variables or observations, the data must be suitably condensed before visualizing.

To illustrate, let us create some missing data in the mtcars dataset

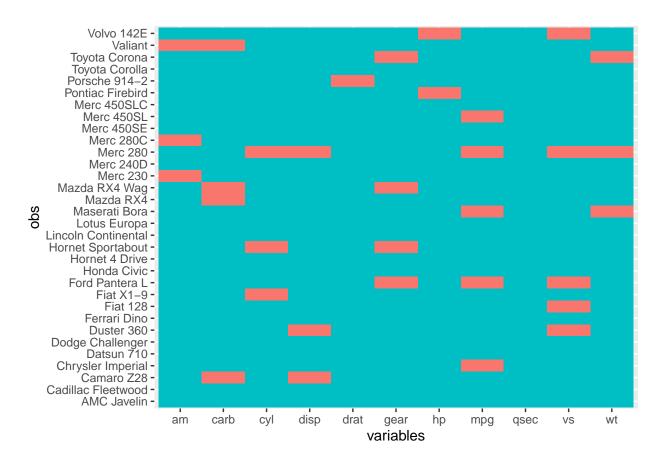
```
mtcars_missing = mtcars
for(i in 1:35){
  set.seed(i)
  x = sample(1:nrow(mtcars), 1)
  y = sample(1:ncol(mtcars), 1)
  mtcars_missing[x, y] = NA
mtcars_missing
                        mpg cyl disp hp drat
                                                       qsec vs am gear carb
                                                   wt
## Mazda RX4
                       21.0
                              6 160.0 110 3.90 2.620 16.46
                                                                          ΝA
                              6 160.0 110 3.90 2.875 17.02
## Mazda RX4 Wag
                       21.0
                                                                         NA
                                                                    NΑ
## Datsun 710
                       22.8
                              4 108.0 93 3.85 2.320 18.61
```

```
## Hornet 4 Drive
                       21.4
                               6 258.0 110 3.08 3.215 19.44
                       18.7
                             NA 360.0 175 3.15 3.440 17.02
                                                                     NA
                                                                           2
## Hornet Sportabout
                                                              0
                                                                 0
## Valiant
                       18.1
                               6 225.0 105 2.76 3.460 20.22
                                                                      3
                                                                          NA
                                                                           4
## Duster 360
                       14.3
                                    NA 245 3.21 3.570 15.84 NA
                                                                      3
## Merc 240D
                       24.4
                               4 146.7
                                        62 3.69 3.190 20.00
                                                                           2
## Merc 230
                       22.8
                               4 140.8 95 3.92 3.150 22.90
                                                                      4
                                                                           2
                                                              1 NA
## Merc 280
                         NA NA
                                    NA 123 3.92
                                                   NA 18.30 NA
## Merc 280C
                       17.8
                               6 167.6 123 3.92 3.440 18.90
                                                              1 NA
                                                                      4
                                                                           4
## Merc 450SE
                       16.4
                               8 275.8 180 3.07 4.070 17.40
                                                                      3
                                                                           3
                                                                      3
## Merc 450SL
                         NA
                               8 275.8 180 3.07 3.730 17.60
                                                                           3
## Merc 450SLC
                       15.2
                               8 275.8 180 3.07 3.780 18.00
                                                                      3
                                                                           3
                                                                      3
## Cadillac Fleetwood 10.4
                               8 472.0 205 2.93 5.250 17.98
                                                                           4
                                                                      3
## Lincoln Continental 10.4
                               8 460.0 215 3.00 5.424 17.82
                                                                 0
                                                                           4
                               8 440.0 230 3.23 5.345 17.42
                                                                      3
## Chrysler Imperial
                         NA
## Fiat 128
                       32.4
                               4 78.7
                                        66 4.08 2.200 19.47 NA
                                                                      4
                                                                 1
                                                                           1
## Honda Civic
                       30.4
                               4
                                 75.7
                                        52 4.93 1.615 18.52
                                                              1
                                                                      4
                                                                           2
                       33.9
                               4 71.1 65 4.22 1.835 19.90
                                                                      4
## Toyota Corolla
                                                              1
                                                                 1
                                                                           1
## Toyota Corona
                       21.5
                               4 120.1 97 3.70
                                                   NA 20.01
                                                                     NA
                                                                           1
                               8 318.0 150 2.76 3.520 16.87
## Dodge Challenger
                                                                           2
                       15.5
                                                                 0
                                                                           2
## AMC Javelin
                       15.2
                              8 304.0 150 3.15 3.435 17.30
                                                                      3
## Camaro Z28
                       13.3
                               8
                                    NA 245 3.73 3.840 15.41
                                                              Ω
                                                                 Λ
                                                                      3
                                                                          NA
## Pontiac Firebird
                       19.2
                               8 400.0
                                       NA 3.08 3.845 17.05
                                                                           2
## Fiat X1-9
                       27.3 NA 79.0
                                       66 4.08 1.935 18.90
                                                                      4
                                                                           1
                                                              1
                                                                 1
## Porsche 914-2
                       26.0
                               4 120.3
                                             NA 2.140 16.70
                                                                      5
                                                                           2
                                       91
                                                                      5
                                                                           2
## Lotus Europa
                       30.4
                               4 95.1 113 3.77 1.513 16.90
                                                              1
                                                                 1
## Ford Pantera L
                         NA
                               8 351.0 264 4.22 3.170 14.50 NA
                                                                     NA
                                                                           4
## Ferrari Dino
                       19.7
                               6 145.0 175 3.62 2.770 15.50
                                                                      5
                                                                           6
                               8 301.0 335 3.54
                                                                      5
                                                                           8
## Maserati Bora
                         NA
                                                   NA 14.60
                                                              0
                               4 121.0 NA 4.11 2.780 18.60 NA 1
                                                                           2
## Volvo 142E
                       21.4
```

When the dataset has a reasonable number of observations and variables, a simple method to visualize missing information is a heatmap. With library(ggplot2), geom\_tile can be used to generate a simple heatmap.

We first classify all observations based on whether they are missing (0) or not (1)

```
mtcars_missing_bi = mtcars_missing
mtcars_missing_bi[!is.na(mtcars_missing)] = 1
mtcars_missing_bi[is.na(mtcars_missing)] = 0
library(tidyr); library(dplyr); library(ggplot2)
mtcars_missing_bi %>%
    as_tibble()%>%
    mutate(obs = rownames(mtcars_missing_bi))%>%
    select(obs, everything())%>%
    pivot_longer(cols = 2:12, names_to = 'variables', values_to = 'values' )%>%
    ggplot(aes(variables, obs, fill= factor(values))) +
    geom_tile()+
    guides(fill=F)
```



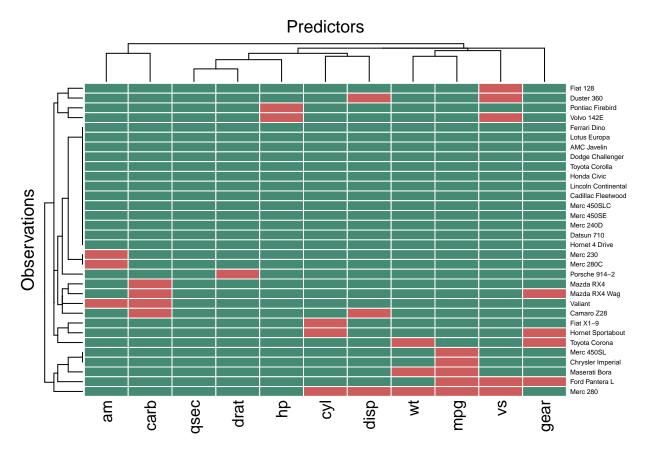
Identifying patterns in a moderate sized heatmap can be challenging. To aid interpretation, library(ComplexHeatMap) groups variables and observations and represents the groups using a dendrogram. The author has a nice book on the bells and whistles of ComplexHeatMap.

ComplexHeatMap can be installed from Bioconductor

```
# install.packages('BiocManager')
# BiocManager::install('ComplexHeatmap')
Alternatively, the most recent version can be obtained from github
#library(devtools)
#install_github("jokergoo/ComplexHeatmap")
```

The following heatmap groups the tiles to make it easier to spot patterns in missing data.

```
library(ComplexHeatmap)
library(circlize)
Heatmap(mtcars_missing_bi,
    rect_gp = gpar(col = "white", lwd = 1),
    name = 'Seeing What is Missing',
    column_title = 'Predictors',
    row_title = 'Observations',
    col = circlize::colorRamp2(c(0,1),c('indianred','aquamarine4')),
    show_heatmap_legend = F,
    row_names_gp = gpar(fontsize = 5))
```



For larger datasets, the data needs to be reduced (using a technique such as principal components analysis) before constructing a heatmap. Another valuable tool for examining the nature and degree of missing data are numerical summaries. For the mtcars\_missing, for each variable, here are the (a) number of missing values

```
apply(mtcars_missing,
      MARGIN = 2,
      FUN = function(x) sum(is.na(x)))
         cyl disp
##
                     hp drat
    mpg
                                wt qsec
                                           ٧s
                                                am gear
                                                         carb
##
           3
                                 3
                                            5
                                                 3
                                                       4
 (b) percent of missing values
apply(mtcars_missing,
      MARGIN = 2,
      FUN = \frac{function(x)}{100*sum(is.na(x))/(sum(is.na(x)) + sum(!is.na(x)))}
##
                              hp
                                   drat
                                                                         gear
                                                                                carb
      mpg
              cyl
                    disp
                                             wt
                                                  qsec
                                                                   am
           9.375
                   9.375
                          6.250 3.125 9.375 0.000 15.625 9.375 12.500 12.500
```

## **Solutions**

Before we examine solutions, it is worth noting that while many popular predictive models such as linear regression, penalized regression models, support vector machines and neural networks cannot tolerate any amount of missing values, there are a few predictive models such as classification and regression trees and other tree-based models that can handle incomplete data.

For the vast majority of predictive models and also a number unsupervised learning methods, missing values need to be addressed. There are three broad categories of solutions, (a) delete (or ignore) missing values, (b) encode missing data, (c) impute.

#### **Delete**

By far, the simplest solution to missing data is remove them either by deleting or ignoring. The most common approach is to conduct listwise deletion wherein the entire row is deleted if even a single element is missing. In mtcars\_missing, the following rows are missing at least one value.

apply(mtcars\_missing, MARGIN = 1, function(x) any(is.na(x)))

##	Mazda RX4	Mazda RX4 Wag	Datsun 710	Hornet 4 Drive
##	TRUE	TRUE	FALSE	FALSE
##	Hornet Sportabout	Valiant	Duster 360	Merc 240D
##	TRUE	TRUE	TRUE	FALSE
##	Merc 230	Merc 280	Merc 280C	Merc 450SE
##	TRUE	TRUE	TRUE	FALSE
##	Merc 450SL	Merc 450SLC	Cadillac Fleetwood	Lincoln Continental
##	TRUE	FALSE	FALSE	FALSE
##	Chrysler Imperial	Fiat 128	Honda Civic	Toyota Corolla
##	TRUE	TRUE	FALSE	FALSE
##	Toyota Corona	Dodge Challenger	AMC Javelin	Camaro Z28
##	TRUE	FALSE	FALSE	TRUE
##	Pontiac Firebird	Fiat X1-9	Porsche 914-2	Lotus Europa
##	TRUE	TRUE	TRUE	FALSE
##	Ford Pantera L	Ferrari Dino	Maserati Bora	Volvo 142E
##	TRUE	FALSE	TRUE	TRUE

Removing them leaves only 13 of the 32 rows in mtcars\_missing!

```
mtcars_missing[!apply(mtcars_missing, MARGIN = 1, function(x) any(is.na(x))),]
```

```
##
                        mpg cyl disp hp drat
                                                   wt
                                                      qsec vs am gear carb
## Datsun 710
                       22.8
                              4 108.0
                                        93 3.85 2.320 18.61
                                                             1
                                                                1
                                                                           1
## Hornet 4 Drive
                       21.4
                              6 258.0 110 3.08 3.215 19.44
                                                             1
                                                                0
                                                                      3
                                                                           1
## Merc 240D
                       24.4
                              4 146.7 62 3.69 3.190 20.00
                                                                      4
                                                                           2
## Merc 450SE
                       16.4
                              8 275.8 180 3.07 4.070 17.40
                                                                      3
                                                                           3
                                                                Ω
## Merc 450SLC
                       15.2
                              8 275.8 180 3.07 3.780 18.00
                                                                           3
## Cadillac Fleetwood 10.4
                              8 472.0 205 2.93 5.250 17.98
                                                                      3
                                                                           4
                              8 460.0 215 3.00 5.424 17.82
## Lincoln Continental 10.4
                                                                           4
## Honda Civic
                       30.4
                              4 75.7
                                       52 4.93 1.615 18.52
                                                                      4
                                                                           2
                                                             1
                                                                1
## Toyota Corolla
                       33.9
                              4 71.1 65 4.22 1.835 19.90
                                                             1
                                                                      4
                                                                           1
                                                                      3
                                                                           2
## Dodge Challenger
                       15.5
                              8 318.0 150 2.76 3.520 16.87
                                                                0
## AMC Javelin
                       15.2
                              8 304.0 150 3.15 3.435 17.30
                                                             0
                                                                      3
                                                                           2
                              4 95.1 113 3.77 1.513 16.90
                                                                           2
## Lotus Europa
                       30.4
                                                                      5
                              6 145.0 175 3.62 2.770 15.50
## Ferrari Dino
                       19.7
                                                                      5
                                                                           6
```

Many predictive modeling functions (e.g., 1m) will automatically conduct listwise deletion. Note in the following output, "19 observations deleted due to missingness"

```
summary(lm(mpg~.,mtcars_missing))
##
## Call:
## lm(formula = mpg ~ ., data = mtcars_missing)
##
## Residuals:
```

```
##
            Datsun 710
                             Hornet 4 Drive
                                                       Merc 240D
                                                                            Merc 450SE
            -1.108e+00
                                 -7.352e-01
##
                                                      -6.661e-16
                                                                             9.495e-01
##
           Merc 450SLC
                         Cadillac Fleetwood Lincoln Continental
                                                                           Honda Civic
##
                                  2.706e-01
                                                        2.980e-02
                                                                             4.134e-01
             2.421e-01
##
        Toyota Corolla
                           Dodge Challenger
                                                     AMC Javelin
                                                                         Lotus Europa
##
             6.943e-01
                                  1.810e+00
                                                      -2.566e+00
                                                                             7.352e-01
##
          Ferrari Dino
##
            -7.352e-01
##
##
  Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                            166.37953
                                       -1.689
## (Intercept) -280.98109
                                                  0.233
                  19.61883
                             13.19206
                                         1.487
                                                  0.275
## cyl
## disp
                  -0.04405
                              0.04758
                                        -0.926
                                                  0.452
                                        -1.055
                                                  0.402
## hp
                  -0.17579
                              0.16670
                  7.01319
                              5.20404
                                         1.348
                                                  0.310
## drat
## wt
                  8.77079
                             11.02143
                                                  0.510
                                         0.796
                  3.41823
                              2.04149
                                                  0.236
## qsec
                                         1.674
## vs
                  26.01966
                             19.08962
                                         1.363
                                                  0.306
## am
                  10.87792
                             10.71197
                                         1.015
                                                  0.417
## gear
                  25.82345
                             15.41268
                                         1.675
                                                  0.236
                  -3.63447
## carb
                              3.04106
                                       -1.195
                                                  0.355
##
## Residual standard error: 2.683 on 2 degrees of freedom
##
     (19 observations deleted due to missingness)
## Multiple R-squared: 0.9794, Adjusted R-squared: 0.8765
## F-statistic: 9.518 on 10 and 2 DF, p-value: 0.09876
```

An important consideration in using deletion is loss of sample. With listwise deletion, even a small number of missing elements can result in a large number of rows getting deleted. Consider the above example where the original data was missing only 11.34375% values but listwise deletion eliminated 59.375% of the rows

```
sum(is.na(mtcars_missing))/nrow(mtcars)*ncol(mtcars) # Percent missing values
## [1] 11.34375
100* nrow(mtcars_missing[apply(mtcars_missing, MARGIN = 1, function(x) any(is.na(x))),])/nrow(mtcars_missing)
## [1] 59.375
```

A second consideration is the cost of acquiring more observations.

A third and perhaps most important consideration is the likelihood of introducing bias into the model. Consider a clinical study where half the respondents receive the current standard care of treatment while the other half receive the new treatment. The new treatment may induce adverse effects causing patients to drop out of the study. Such missing data is clearly not random and deleting them is bound to bias results.

### **Encode Missing Data**

Missing data may represent information. In a survey that only contains two alternatives for gender, those not conforming to either gender may skip the question. In this case, non-response may contain information valuable gender orientation. As another example, survey respondents may refuse to respond to questions on politically sensitive issues such as abortion and right to bear arms. Here again, non-response may contain useful information.

In a categorical variable, missing data may be encoded as another level. Consider the following example.

```
set.seed(61710)
gender = sample(c('Male', 'Female', NA), 10, T)
```

```
gender
                                                                 "Female" "Male"
## [1] NA
                  "Female" "Male"
                                    NΑ
                                              "Male"
                                                       "Male"
   [9] "Female" "Female"
gender_encoded = gender
gender_encoded[is.na(gender)] = 'Did Not Respond'
gender encoded
    [1] "Did Not Respond" "Female"
                                              "Male"
                                                                 "Did Not Respond"
##
    [5] "Male"
                           "Male"
                                              "Female"
                                                                 "Male"
##
    [9] "Female"
                           "Female"
Missing data in a continuous variable may be represented using a dummy variable.
mtcars_missing_encoded = mtcars_missing
mtcars_missing_encoded %>%
  mutate(cyl_missing = ifelse(is.na(mtcars_missing_encoded$cyl),0,1))%>%
  select(mpg, cyl, cyl_missing, everything())
##
                         mpg cyl cyl_missing disp hp drat
                                                                 wt gsec vs am gear
                                            1 160.0 110 3.90 2.620 16.46
## Mazda RX4
                        21.0
                                                                           0
                               6
## Mazda RX4 Wag
                        21.0
                               6
                                            1 160.0 110 3.90 2.875 17.02
                                                                                   NA
## Datsun 710
                        22.8
                               4
                                            1 108.0 93 3.85 2.320 18.61
                                                                           1
                                                                                    4
## Hornet 4 Drive
                                            1 258.0 110 3.08 3.215 19.44
                                                                                    3
                        21.4
                               6
                                            0 360.0 175 3.15 3.440 17.02
## Hornet Sportabout
                        18.7
                                                                              0
                              NA
                                                                                   NA
## Valiant
                                            1 225.0 105 2.76 3.460 20.22
                        18.1
                               6
                                                                           1 NA
                                                                                    3
## Duster 360
                        14.3
                               8
                                            1
                                                 NA 245 3.21 3.570 15.84 NA
                                                                                    3
## Merc 240D
                        24.4
                                            1 146.7
                                                     62 3.69 3.190 20.00
                                                                                    4
## Merc 230
                        22.8
                                            1 140.8 95 3.92 3.150 22.90 1 NA
                               4
                                                                                    4
## Merc 280
                          NA
                              NA
                                                 NA 123 3.92
                                                                 NA 18.30 NA
                                                                                    4
                                            1 167.6 123 3.92 3.440 18.90
## Merc 280C
                        17.8
                               6
                                                                           1 NA
                                                                                    4
## Merc 450SE
                        16.4
                                            1 275.8 180 3.07 4.070 17.40
                                                                                    3
                               8
## Merc 450SL
                          NA
                               8
                                            1 275.8 180 3.07 3.730 17.60
                                                                              0
                                                                                    3
## Merc 450SLC
                        15.2
                               8
                                            1 275.8 180 3.07 3.780 18.00
                                                                           0
                                                                                    3
## Cadillac Fleetwood
                                            1 472.0 205 2.93 5.250 17.98
                                                                                    3
## Lincoln Continental 10.4
                                            1 460.0 215 3.00 5.424 17.82
                                                                                    3
                               8
## Chrysler Imperial
                               8
                                            1 440.0 230 3.23 5.345 17.42
                                                                           0
                                                                                    3
                          NA
## Fiat 128
                                                     66 4.08 2.200 19.47 NA
                                                                                    4
                        32.4
                               4
                                              78.7
## Honda Civic
                        30.4
                                              75.7 52 4.93 1.615 18.52
## Toyota Corolla
                        33.9
                                            1 71.1
                                                     65 4.22 1.835 19.90
                               4
                                                                           1
                                                                                    4
## Toyota Corona
                        21.5
                                            1 120.1
                                                     97 3.70
                                                                 NA 20.01
                               4
                                                                           1
                                                                                   NA
                                            1 318.0 150 2.76 3.520 16.87
                                                                                    3
## Dodge Challenger
                        15.5
                               8
## AMC Javelin
                        15.2
                               8
                                            1 304.0 150 3.15 3.435 17.30
                                                                                    3
## Camaro Z28
                        13.3
                                                 NA 245 3.73 3.840 15.41
                                                                                    3
                               8
## Pontiac Firebird
                        19.2
                               8
                                            1 400.0
                                                     NA 3.08 3.845 17.05
                                                                                    3
## Fiat X1-9
                        27.3
                                            0 79.0
                                                     66 4.08 1.935 18.90
                                                                                    4
                              NA
                                                                           1
## Porsche 914-2
                        26.0
                               4
                                            1 120.3 91
                                                          NA 2.140 16.70
                                                                                    5
                                            1 95.1 113 3.77 1.513 16.90
## Lotus Europa
                        30.4
                               4
                                                                           1
                                                                              1
                                                                                    5
## Ford Pantera L
                          NA
                               8
                                            1 351.0 264 4.22 3.170 14.50 NA
                                                                                   NΑ
## Ferrari Dino
                        19.7
                               6
                                            1 145.0 175 3.62 2.770 15.50
                                                                                    5
## Maserati Bora
                          NA
                               8
                                            1 301.0 335 3.54
                                                                 NA 14.60
                                                                           Ω
                                                                              1
                                                                                    5
## Volvo 142E
                        21.4
                               4
                                            1 121.0 NA 4.11 2.780 18.60 NA
                                                                                    4
##
                        carb
## Mazda RX4
                          NA
## Mazda RX4 Wag
                          NΑ
## Datsun 710
                           1
```

##	Hornet 4 Drive	1
##	Hornet Sportabout	2
##	Valiant	NA
##	Duster 360	4
##	Merc 240D	2
##	Merc 230	2
##	Merc 280	4
##	Merc 280C	4
##	Merc 450SE	3
##	Merc 450SL	3
##	Merc 450SLC	3
##	Cadillac Fleetwood	4
##	Lincoln Continental	4
##	Chrysler Imperial	4
##	Fiat 128	1
##	Honda Civic	2
##	Toyota Corolla	1
##	Toyota Corona	1
##	Dodge Challenger	2
##	AMC Javelin	2
	Camaro Z28	NA
##	Pontiac Firebird	2
	Fiat X1-9	1
##	Porsche 914-2	2
##	Lotus Europa	2
##	Ford Pantera L	4
##	Ferrari Dino	6
##	Maserati Bora	8
##	Volvo 142E	2

## Impute

In imputation, information and relationships among non-missing predictors is used to estimate missing values. Approaches to imputation differ based on whether they are designed for inferences or prediction. Our focus is going to be on the latter, so the quality of an imputation procedure will be judged by its ability to accurately predict missing values.

It is important to remember that imputed values are merely estimates of the true value for missing data. Thus, one must limit how much missing data is imputed. While there isn't a universal rule on how much data can be imputed, no more than 20% for a variable may be a good thumb rule to use.

Imputation must occur prior to other steps in data preparation.

There are a number of methods available for imputing missing data (e.g., predictive mean matching, knearest neighbors, trees and tree-based methods) and a number of R package that implement these (e.g., mice, caret)

#### mice

mice() implements a number of imputation methods. This illustration uses the default, which for numeric data is predictive mean matching. For more information, see author's website. In version 3.12.0, mice library implemented a new matchindex C function that makes predictive mean matching 50 to 600 times faster, however this affects reproducibility of the algorithm. Read more about the update (here)[https://cran.r-project.org/web/packages/mice/news/news.html]. (If you wish to reproduce the behavior of the previous version of mice, include use.matcher=T in the mice function). Finally, tidyr has an identically named complete function. To prevent conflicts, it is best to include the package reference, mice::complete(...)

```
library(mice)
mtcars_mice = mice::complete(mice(mtcars_missing,seed = 617))
##
##
    iter imp variable
##
     1
         1 mpg cyl disp
                              hp
                                  drat
                                                             carb
                                         wt
                                             VS
                                                  am
                                                      gear
                                         wt
##
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                             VS
                                                  am
                                                      gear
##
                  cyl
                       disp
                                  {\tt drat}
     1
            mpg
                              hp
                                         wt
                                             VS
                                                  am
                                                      gear
                                                             carb
##
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             vs
                                                  am
                                                      gear
                                                             carb
##
     1
         5
                                  drat
                  cyl
                       disp
                              hp
                                         wt
                                                      gear
                                                             carb
            mpg
                                             ٧s
                                                  am
##
                       disp
                              hp
                                  drat
            mpg
                  cyl
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     2
                  cyl
         2
                       disp
            mpg
                              hp
                                  drat
                                         wt
                                             ٧S
                                                  am
                                                      gear
                                                             carb
##
     2
         3
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧S
                                                  am
                                                      gear
                                                             carb
##
     2
         4
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     2
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                      gear
                                             VS
                                                  am
                                                             carb
##
     3
         1
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
     3
                                         wt
##
         2
                  cyl
                       disp
                              hp
                                  drat
            mpg
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     3
         3
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                      gear
                                             ٧S
##
     3
         4
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                      gear
                                             VS
                                                  am
                                                             carb
##
     3
         5
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     4
         1
                  cyl disp
                              hp
                                  drat
                                         wt
                                                             carb
            mpg
                                             VS
                                                  am
                                                      gear
##
     4
         2
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             vs
                                                      gear
##
     4
         3
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     4
         4
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                      gear
            mpg
                                             ٧s
                                                  am
##
     4
                                  {\tt drat}
                                                      gear
         5
                  cyl
                       disp
                              hp
            mpg
                                         wt
                                             VS
                                                  am
                                                             carb
##
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             vs
                                                  am
                                                      gear
##
     5
         2
                  cyl
            mpg
                       disp
                              hp
                                  drat
                                                      gear
                                                             carb
                                         wt
                                             ٧s
                                                  am
##
     5
         3
                  cyl disp
                                  drat
            mpg
                              hp
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     5
                  cyl disp
                              hp
                                  drat
                                         wt
                                                             carb
            mpg
                                             ٧S
                                                  am
                                                      gear
                 cyl disp hp
            mpg
                                  drat
                                         wt
                                             ٧S
                                                  am
                                                      gear
                                                             carb
head(mtcars_mice)
##
                       mpg cyl disp hp drat
                                                   wt
                                                      qsec vs am gear carb
## Mazda RX4
                                 160 110 3.90 2.620 16.46
                       21.0
                                                                            3
## Mazda RX4 Wag
                       21.0
                              6
                                 160 110 3.90 2.875 17.02
                                                              0
                                                                       4
                                                                            4
                                                                 1
## Datsun 710
                       22.8
                              4
                                 108 93 3.85 2.320 18.61
                                                              1
                                                                       4
                              6
                                 258 110 3.08 3.215 19.44
                                                                       3
                                                                            1
## Hornet 4 Drive
                       21.4
                                                              1
                                                                            2
## Hornet Sportabout 18.7
                              8
                                 360 175 3.15 3.440 17.02
                                 225 105 2.76 3.460 20.22
## Valiant
                       18.1
                              6
                                                              1
                                                                            1
library(mice)
mtcars_mice_rf = mice::complete(mice(mtcars_missing,method = 'rf',seed = 617))
##
##
    iter imp variable
##
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
         2
     1
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                      gear
                                                             carb
                                             ٧s
                                                  \mathtt{am}
##
         3
     1
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
         4
     1
                  cyl
                       disp
                              hp
                                  drat
            mpg
                                         wt
                                             ٧S
                                                  am
                                                      gear
                                                             carb
##
                                                      gear
     1
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             VS
                                                  am
                                                             carb
     2
##
         1
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     2
         2
                  cyl
                       disp
                              hp
                                  drat
                                         wt
            mpg
                                             ٧s
                                                  am
                                                      gear
                                                             carb
##
     2
         3
            mpg
                  cyl
                       disp
                              hp
                                  drat
                                         wt
                                                             carb
                                             ٧S
                                                  am
                                                      gear
##
                              hp
                       disp
                                  drat
            mpg
                  cyl
                                         wt
                                                  am
                                                      gear
                                                             carb
                                             VS
##
            mpg
                  cyl
                       disp hp
                                  drat
                                         wt
                                             ٧s
                                                  am
                                                      gear
                                                             carb
```

```
##
     3
          1
             mpg
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                                carb
                                                VS
                                                     am
                                                         gear
     3
##
          2
                         disp
             mpg
                   cyl
                                hp
                                     drat
                                           wt.
                                                VS
                                                     am
                                                         gear
                                                                carb
##
     3
          3
             mpg
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                vs
                                                     am
                                                                carb
                                                         gear
     3
##
          4
             mpg
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                ٧s
                                                     am
                                                         gear
                                                                carb
##
     3
          5
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                         gear
             mpg
                                                VS
                                                     am
                                                                carb
                                hp
     4
          1
##
             mpg
                   cyl
                         disp
                                     drat
                                           wt
                                                ٧s
                                                     am
                                                         gear
                                                                 carb
##
     4
          2
                   cyl
                         disp
                                hp
                                     drat
             mpg
                                           wt
                                                         gear
                                                VS
                                                     am
                                                                carb
##
     4
          3
             mpg
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                VS
                                                     am
                                                          gear
                                                                 carb
##
     4
          4
             mpg
                   cyl
                         disp
                                hp
                                     drat
                                           wt.
                                                VS
                                                     am
                                                         gear
                                                                carb
##
     4
          5
                   cyl
                         disp
                                hp
                                     drat
                                           wt
                                                ٧s
                                                     am
                                                                 carb
             mpg
                                                         gear
##
     5
                         disp
          1
                   cyl
                                hp
                                     drat
                                           wt
                                                         gear
             mpg
                                                     am
                                                                carb
                                                VS
     5
          2
                                     drat
##
                   cyl
                         disp
                                hp
                                           wt
             mpg
                                                ٧S
                                                     am
                                                         gear
                                                                carb
##
     5
          3
                   cyl
                                hp
             mpg
                                     drat
                         disp
                                           wt
                                                ٧S
                                                     am
                                                         gear
                                                                carb
                                hp
                                                         gear
##
             mpg
                   cyl
                         disp
                                     drat
                                            wt
                                                ٧s
                                                     am
                                                                carb
     5
##
          5
                   cyl
                         disp
                                hp
                                     drat
                                           wt
             mpg
                                                ٧S
                                                     am
                                                         gear
                                                                carb
head(mtcars_mice_rf)
##
                         mpg cyl disp
                                        hp drat
                                                      wt
                                                          gsec
                                                                vs am
                                                                       gear
## Mazda RX4
                        21.0
                                6
                                   160 110 3.90 2.620 16.46
                                                                  0
                                                                           4
                                                                                 2
                                                                     1
## Mazda RX4 Wag
                        21.0
                                6
                                   160 110 3.90 2.875 17.02
                                                                 0
                                                                           5
                                                                                 1
## Datsun 710
                        22.8
                                4
                                   108
                                         93 3.85 2.320 18.61
                                                                  1
                                                                           4
                                                                                 1
## Hornet 4 Drive
                                                                           3
                        21.4
                                   258 110 3.08 3.215 19.44
                                                                                 1
                                                                           3
                                                                                2
## Hornet Sportabout 18.7
                                8
                                   360 175 3.15 3.440 17.02
                                                                 0
                                                                     0
                                   225 105 2.76 3.460 20.22
## Valiant
                        18.1
                                                                                 1
```

#### caret

caret is a full blown machine learning framework that contains a number of handy functions. preprocess() can be used for imputing, among other things. Here, we are using a bagImpute, which works by fitting a bagged tree model for each predictor (as a function of all the others). This method is quite accurate, but has much higher computational cost than say medianImpute.

```
library(caret)
set.seed(617)
mtcars_caret = predict(preProcess(mtcars_missing,
                                   method = 'bagImpute'),
                       newdata = mtcars_missing)
head(mtcars_caret)
##
                                cyl disp hp drat
                                                      wt
                                                         qsec vs
                      mpg
                                                                                gear
## Mazda RX4
                     21.0 6.000000
                                     160 110 3.90 2.620 16.46
                                                                0 1.0000000 4.000000
## Mazda RX4 Wag
                     21.0 6.000000
                                     160 110 3.90 2.875 17.02
                                                                0 1.0000000 3.615385
## Datsun 710
                     22.8 4.000000
                                     108
                                         93 3.85 2.320 18.61
                                                                1 1.0000000 4.000000
## Hornet 4 Drive
                     21.4 6.000000
                                     258 110 3.08 3.215 19.44
                                                                1 0.0000000 3.000000
## Hornet Sportabout 18.7 6.246154
                                     360 175 3.15 3.440 17.02
                                                                0 0.0000000 3.615385
## Valiant
                     18.1 6.000000
                                     225 105 2.76 3.460 20.22
                                                               1 0.3538462 3.000000
##
                         carb
## Mazda RX4
                     2.438462
## Mazda RX4 Wag
                     2.438462
## Datsun 710
                     1.000000
## Hornet 4 Drive
                     1.000000
## Hornet Sportabout 2.000000
## Valiant
                     2.438462
```

There are a number of imputation methods available but no single method is the best in every situation. Here is a comparison of the different imputation methods on the missing data.

```
df = data.frame(true_values = mtcars[is.na(mtcars_missing)],
           mice_pmm = mtcars_mice[is.na(mtcars_missing)],
           mice_rf = mtcars_mice_rf[is.na(mtcars_missing)],
           caret_bagImpute = mtcars_caret[is.na(mtcars_missing)])
df
##
      true values mice pmm mice rf caret bagImpute
## 1
           19.200
                      18.70 18.700
                                         20.9530769
## 2
           17.300
                      15.20 19.200
                                         20.9530769
## 3
           14.700
                     10.40 19.200
                                         20.9530769
## 4
           15.800
                     19.70 13.300
                                         20.9530769
                     15.20
                            13.300
## 5
           15.000
                                         20.9530769
## 6
            8.000
                      8.00
                              8.000
                                          6.2461538
## 7
            6.000
                      6.00
                              6.000
                                          6.2461538
## 8
            4.000
                      4.00
                              4.000
                                          6.2461538
                    351.00 275.800
## 9
          360.000
                                        244.3669231
                    304.00 160.000
## 10
          167.600
                                        244.3669231
## 11
          350.000
                    472.00 275.800
                                        244.3669231
## 12
          175.000
                    175.00 180.000
                                        135.1461538
          109.000
## 13
                     95.00 110.000
                                        135.1461538
## 14
            4.430
                      4.08
                              4.220
                                          3.4791538
## 15
                      3.73
                              1.513
            3.440
                                          3.3680077
## 16
            2.465
                      2.14
                              2.320
                                          3.3680077
## 17
            3.570
                      3.73
                              3.845
                                          3.3680077
## 18
            0.000
                      0.00
                              0.000
                                          0.4307692
## 19
            1.000
                      0.00
                              1.000
                                          0.4307692
## 20
            1.000
                      1.00
                              1.000
                                          0.4307692
## 21
            0.000
                      0.00
                              0.000
                                          0.4307692
## 22
            1.000
                      1.00
                                          0.4307692
                              0.000
## 23
            0.000
                      0.00
                              0.000
                                          0.3538462
## 24
            0.000
                      0.00
                              1.000
                                          0.3538462
## 25
            0.000
                      1.00
                              0.000
                                          0.3538462
            4.000
                      4.00
                                          3.6153846
## 26
                              5.000
## 27
            3.000
                      3.00
                              3.000
                                          3.6153846
## 28
            3.000
                      4.00
                              5.000
                                          3.6153846
## 29
            5.000
                      4.00
                              4.000
                                          3.6153846
## 30
            4.000
                      3.00
                              2.000
                                          2.4384615
## 31
            4.000
                      4.00
                              1.000
                                          2.4384615
            1.000
                       1.00
                              1.000
## 32
                                          2.4384615
## 33
            4.000
                      4.00
                              4.000
                                          2.4384615
library(ggplot2); library(tidyr)
rownames(df)
    [1] "1" "2"
                  "3"
                        "4" "5" "6" "7" "8" "9" "10" "11" "12" "13" "14" "15"
   [16] "16" "17" "18" "19" "20" "21" "22" "23" "24" "25" "26" "27" "28" "29" "30"
## [31] "31" "32" "33"
df %>%
  mutate(id = as.integer(rownames(df)))%>%
  select(id, everything())%>%
  pivot_longer(2:5,names_to = 'method',values_to ='values')%>%
  mutate(true_value = factor(ifelse(method == 'true_values',1,0),labels = c('True Value','Imputed Value
  ggplot(aes(x = id, y=values, color=true_value, shape = method))+
  geom_point()+theme_bw()
```

