# Effect spatial correlation on audiovisual integration stats analysis

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### Unity judgment

## Fixed effects:

```
# Data cleaning
rm(list = ls())
setwd("/Users/oliviaxujiaming/Desktop/Github/SpatialCorrelation/Experiment_code/stats")
VE_ujdg_data = read_excel('VE_ujdg_trialByTrial_allSubj.xlsx')
VE_ujdg_data["ujdg"] [VE_ujdg_data["ujdg"] == 2] <- 0</pre>
GLMM as ordered factors
GLMM as numeric factors
class(VE_ujdg_data$disc) = "Numeric"
class(VE_ujdg_data$corr) = "Numeric"
GLMMmodel_AV1 <- glmer(ujdg ~ (scale(disc)+scale(disc^2))*</pre>
                         (scale(corr)+scale(corr^2)) + (1|subjID),
                      data = VE_ujdg_data, family='binomial',
                      control = glmerControl(optimizer='bobyqa'))
summary(GLMMmodel_AV1, corr = FALSE)
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
## Family: binomial (logit)
## ujdg ~ (scale(disc) + scale(disc^2)) * (scale(corr) + scale(corr^2)) +
       (1 | subjID)
      Data: VE_ujdg_data
##
## Control: glmerControl(optimizer = "bobyqa")
##
##
        AIC
                       logLik deviance df.resid
    8179.9 8249.3 -4080.0 8159.9
                                           7590
##
##
## Scaled residuals:
               1Q Median
                                ЗQ
       Min
                                       Max
## -3.5781 -0.6362 -0.2637 0.6529 4.1074
##
## Random effects:
## Groups Name
                       Variance Std.Dev.
## subjID (Intercept) 0.4665
                                0.683
## Number of obs: 7600, groups: subjID, 9
```

```
##
                             Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                            -0.116094 0.229324 -0.506 0.61269
## scale(disc)
                           ## scale(disc^2)
                            -1.156832 0.029878 -38.719 < 2e-16 ***
## scale(corr)
                             0.081287 0.027407
                                               2.966 0.00302 **
## scale(corr^2)
                             ## scale(disc):scale(corr)
                           -0.006008 0.028539 -0.211 0.83326
                           -0.008173 0.028520 -0.287
## scale(disc):scale(corr^2)
                                                       0.77445
## scale(disc^2):scale(corr)
                           -0.005856 0.028561 -0.205 0.83754
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Anova(GLMMmodel_AV1)
## Analysis of Deviance Table (Type II Wald chisquare tests)
##
## Response: ujdg
##
                               Chisq Df Pr(>Chisq)
## scale(disc)
                              8.3747 1
                                         0.003805 **
## scale(disc^2)
                          1499.4396 1
                                        < 2.2e-16 ***
## scale(corr)
                              9.0853 1
                                         0.002577 **
## scale(corr^2)
                              0.0988 1
                                         0.753333
                              0.0443 1
## scale(disc):scale(corr)
                                         0.833257
## scale(disc):scale(corr^2)
                              0.0821 1
                                         0.774453
## scale(disc^2):scale(corr)
                             0.0420 1
                                         0.837540
## scale(disc^2):scale(corr^2) 0.0475 1
                                         0.827554
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
confint(GLMMmodel_AV1)
## Computing profile confidence intervals ...
##
                                 2.5 %
                                           97.5 %
## .sig01
                             0.45313681 1.18449763
## (Intercept)
                           -0.61811665 0.38591080
## scale(disc)
                           -0.13835221 -0.02653406
## scale(disc^2)
                           -1.21582413 -1.09869128
## scale(corr)
                           0.02761237 0.13506239
## scale(corr^2)
                          -0.04598339 0.06130821
                           -0.06195925 0.04994376
## scale(disc):scale(corr)
## scale(disc):scale(corr^2) -0.06410021 0.04771717
## scale(disc^2):scale(corr)
                           -0.06182184 0.05016612
## scale(disc^2):scale(corr^2) -0.06220817  0.04962669
Auditory ventriloquism effect
# Data cleaning
audVE_indvd_data <- VE_ujdg_data[, - c(6, 8)]</pre>
audVE_indvd_data <- audVE_indvd_data[complete.cases(audVE_indvd_data), ]</pre>
audVE_indvd_zeroDisc <- audVE_indvd_data[audVE_indvd_data$disc==0, ]</pre>
```

#### LMM as ordered factors

## ---

```
audVE_indvd_data$disc<-factor(audVE_indvd_data$disc, ordered=TRUE)</pre>
audVE_indvd_data$corr<-factor(audVE_indvd_data$corr, ordered=TRUE)</pre>
audVE_indvd_data$subjID<-factor(audVE_indvd_data$subjID, ordered=TRUE)
lmer_resultsAV <-lmer(audVE~ disc * corr + (1|subjID),</pre>
                        data=audVE_indvd_data)
summary(lmer_resultsAV)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: audVE ~ disc * corr + (1 | subjID)
##
      Data: audVE_indvd_data
##
## REML criterion at convergence: 25188.3
##
## Scaled residuals:
##
       Min
                1Q Median
                                 3Q
                                         Max
## -6.3921 -0.6331 0.0080 0.6266
##
## Random effects:
  Groups
##
             Name
                          Variance Std.Dev.
  subjID
                         2.393
                                   1.547
             (Intercept)
## Residual
                          44.270
                                   6.654
## Number of obs: 3800, groups:
                                  subjID, 9
##
## Fixed effects:
##
                    Estimate Std. Error
                                                 df t value Pr(>|t|)
                                                     -0.597
## (Intercept)
                    -0.31460
                                0.52693
                                            8.02318
                                                               0.5669
## disc.L
                    13.33967
                                0.24107 3767.38077
                                                     55.336
                                                               <2e-16 ***
## disc.Q
                                0.24155 3767.30665
                                                     -0.435
                    -0.10511
                                                               0.6635
## disc.C
                                0.24204 3767.22526 -10.553
                    -2.55420
                                                               <2e-16 ***
## disc<sup>4</sup>
                    0.38945
                                0.24254 3767.16141
                                                      1.606
                                                               0.1084
                    0.23543
                                0.24293 3767.11537
                                                      0.969
## corr.L
                                                               0.3325
                                0.24195 3767.87840
## corr.Q
                    0.11454
                                                      0.473
                                                               0.6360
## corr.C
                    0.10923
                                0.24224 3767.24978
                                                      0.451
                                                               0.6521
## corr<sup>4</sup>
                                0.24036 3767.62994
                                                      1.481
                    0.35599
                                                               0.1387
## disc.L:corr.L
                   -0.05681
                                0.54390 3767.32941
                                                     -0.104
                                                               0.9168
## disc.Q:corr.L
                    0.30910
                                0.54259 3767.32525
                                                      0.570
                                                               0.5689
## disc.C:corr.L
                   -0.46382
                                0.54486 3767.29199
                                                     -0.851
                                                               0.3947
## disc^4:corr.L
                    0.75543
                                0.54210 3767.28755
                                                      1.394
                                                               0.1635
## disc.L:corr.Q
                   -1.18209
                                0.53945 3767.53565
                                                     -2.191
                                                               0.0285 *
## disc.Q:corr.Q
                    0.64375
                                0.54088 3767.90397
                                                      1.190
                                                               0.2340
## disc.C:corr.Q
                    0.62087
                                0.54044 3767.32782
                                                      1.149
                                                               0.2507
## disc^4:corr.Q
                    0.17852
                                0.54196 3767.29457
                                                      0.329
                                                               0.7419
## disc.L:corr.C
                    -0.59116
                                0.53961 3767.29814
                                                     -1.096
                                                               0.2734
## disc.Q:corr.C
                    -0.72612
                                0.54047 3767.57534
                                                     -1.344
                                                               0.1792
## disc.C:corr.C
                    0.69576
                                0.54374 3767.37508
                                                      1.280
                                                               0.2008
## disc^4:corr.C
                    0.41813
                                0.54332 3767.39946
                                                      0.770
                                                               0.4416
## disc.L:corr^4
                    0.67610
                                0.53304 3767.41526
                                                      1.268
                                                               0.2047
## disc.Q:corr^4
                    0.81444
                                0.53726 3767.33194
                                                      1.516
                                                               0.1296
## disc.C:corr^4
                   -0.37519
                                0.53624 3767.48018
                                                     -0.700
                                                               0.4842
## disc^4:corr^4
                   -0.03207
                                0.54263 3767.46389
                                                     -0.059
                                                               0.9529
```

```
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation matrix not shown by default, as p = 25 > 12.
## Use print(x, correlation=TRUE) or
       vcov(x)
                     if you need it
Anova(lmer resultsAV)
## Analysis of Deviance Table (Type II Wald chisquare tests)
##
## Response: audVE
                 Chisq Df Pr(>Chisq)
##
## disc
            3185.0489 4
                             <2e-16 ***
                             0.4457
## corr
               3.7169 4
## disc:corr
              20.1817 16
                             0.2121
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
confint(lmer_resultsAV)
## Computing profile confidence intervals ...
##
                      2.5 %
                                97.5 %
## .sig01
                 0.94541985 2.5496983
## .sigma
                 6.48593597
                             6.7846080
## (Intercept)
                -1.40220588 0.7721681
## disc.L
                12.86837395 13.8105787
## disc.Q
                -0.57717171 0.3669136
## disc.C
                -3.02701145 -2.0810145
## disc^4
                -0.08450103 0.8634596
## corr.L
                -0.23947376 0.7100258
## corr.Q
                -0.35869920 0.5869609
## corr.C
                -0.36423961 0.5825414
## corr^4
                -0.11393764 0.8255246
## disc.L:corr.L -1.11965902 1.0061721
## disc.Q:corr.L -0.75078112 1.3699175
## disc.C:corr.L -1.52854749 0.6010323
## disc^4:corr.L -0.30367778 1.8151299
## disc.L:corr.Q -2.23611078 -0.1276840
## disc.Q:corr.Q -0.41391431 1.7001060
## disc.C:corr.Q -0.43591287
                             1.6764218
## disc^4:corr.Q -0.88025807
                             1.2380078
## disc.L:corr.C -1.64620341 0.4628718
## disc.Q:corr.C -1.78208329 0.3303286
## disc.C:corr.C -0.36659095 1.7586010
## disc^4:corr.C -0.64346706 1.4800955
## disc.L:corr<sup>4</sup> -0.36646783 1.7169553
```

## disc.Q:corr^4 -0.23540168 1.8644682 ## disc.C:corr^4 -1.42297223 0.6729164 ## disc^4:corr^4 -1.09194762 1.0289344

#### LMM as numeric factors

```
class(audVE indvd data$disc) = "Numeric"
class(audVE_indvd_data$corr) = "Numeric"
class(audVE_indvd_data$subjID) = "Numeric"
lmer resultsAV1 <- lmer(audVE ~ (scale(disc)+scale(disc^2))*</pre>
                          (scale(corr)+scale(corr^2)) +
                          (1|subjID), data = audVE_indvd_data)
summary(lmer_resultsAV1,corr = FALSE)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula:
## audVE ~ (scale(disc) + scale(disc^2)) * (scale(corr) + scale(corr^2)) +
##
       (1 | subjID)
##
      Data: audVE_indvd_data
##
## REML criterion at convergence: 25319.3
##
## Scaled residuals:
              1Q Median
##
      Min
                                3Q
                                       Max
## -6.3299 -0.6544 0.0017 0.6529 7.9022
## Random effects:
## Groups
                         Variance Std.Dev.
            Name
             (Intercept) 2.338
                                  1.529
## subjID
                         45.602
## Residual
                                  6.753
## Number of obs: 3800, groups:
                                 subjID, 9
## Fixed effects:
                                                             df t value Pr(>|t|)
                                 Estimate Std. Error
## (Intercept)
                                             0.52141
                                                        8.02489 -0.345
                                                                           0.739
                                 -0.18000
## scale(disc)
                                  6.32196
                                             0.56913 3783.30894 11.108
                                                                          <2e-16
## scale(disc^2)
                                 -0.34582
                                             0.56915 3783.32888
                                                                -0.608
                                                                           0.543
## scale(corr)
                                 -0.07232
                                             0.56282 3783.84469
                                                                -0.128
                                                                           0.898
## scale(corr^2)
                                  0.17682
                                             0.56286 3783.89686
                                                                 0.314
                                                                           0.753
                                                                 1.462
## scale(disc):scale(corr)
                                             2.92476 3783.93389
                                  4.27654
                                                                           0.144
## scale(disc):scale(corr^2)
                                 -4.68354 2.93008 3783.85241 -1.598
                                                                           0.110
## scale(disc^2):scale(corr)
                                                                           0.278
                                 -3.17183
                                             2.92398 3784.02292 -1.085
## scale(disc^2):scale(corr^2)
                                  3.56190
                                             2.92545 3783.92969
                                                                 1.218
                                                                           0.223
##
## (Intercept)
## scale(disc)
                               ***
## scale(disc^2)
## scale(corr)
## scale(corr^2)
## scale(disc):scale(corr)
## scale(disc):scale(corr^2)
## scale(disc^2):scale(corr)
## scale(disc^2):scale(corr^2)
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

```
Anova(lmer_resultsAV1)
## Analysis of Deviance Table (Type II Wald chisquare tests)
## Response: audVE
##
                                 Chisq Df Pr(>Chisq)
## scale(disc)
                              123.4204 1
                                              <2e-16 ***
## scale(disc^2)
                                0.3681 1
                                              0.5440
## scale(corr)
                                0.0175 1
                                              0.8947
## scale(corr^2)
                                0.0998 1
                                              0.7521
## scale(disc):scale(corr)
                                2.1380 1
                                              0.1437
## scale(disc):scale(corr^2)
                                             0.1099
                                2.5550 1
## scale(disc^2):scale(corr)
                                1.1767 1
                                             0.2780
## scale(disc^2):scale(corr^2)
                                1.4824 1
                                            0.2234
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
confint(lmer_resultsAV1)
## Computing profile confidence intervals ...
                                    2.5 %
                                              97.5 %
## .sig01
                                0.9327331 2.5220283
## .sigma
                                6.5967902 6.9005667
## (Intercept)
                               -1.2563179 0.8954508
## scale(disc)
                               5.2073561 7.4365166
## scale(disc^2)
                               -1.4605075 0.7687202
## scale(corr)
                             -1.1736742 1.0308140
## scale(corr^2)
                              -0.9264875 1.2781754
## scale(disc):scale(corr)
                             -1.4557661 10.0000288
## scale(disc):scale(corr^2) -10.4178715 1.0587371
## scale(disc^2):scale(corr)
                               -8.8939025 2.5588196
## scale(disc^2):scale(corr^2) -2.1711528 9.2872968
At 0 discrepancy
lmer_resultsAV2 <- lmer(audVE ~ (scale(corr)+scale(corr^2)) +</pre>
                         (1|subjID), data = audVE_indvd_zeroDisc)
summary(lmer_resultsAV2,corr = FALSE)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: audVE ~ (scale(corr) + scale(corr^2)) + (1 | subjID)
##
     Data: audVE_indvd_zeroDisc
##
## REML criterion at convergence: 4534.2
##
## Scaled residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -8.8893 -0.5792 0.0586 0.6184 2.6581
```

##

```
## Random effects:
## Groups Name Variance Std.Dev.
## subjID (Intercept) 2.843 1.686
                        23.658 4.864
## Residual
## Number of obs: 752, groups: subjID, 9
##
## Fixed effects:
##
                  Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept)
                 -0.001669 0.589599 8.041281 -0.003
                                                           0.998
## scale(corr)
                 1.599
                                                           0.110
## scale(corr^2) -0.066416 0.178582 742.714606 -0.372
                                                           0.710
Anova(lmer_resultsAV2)
## Analysis of Deviance Table (Type II Wald chisquare tests)
## Response: audVE
##
                 Chisq Df Pr(>Chisq)
                2.5573 1
                              0.1098
## scale(corr)
## scale(corr^2) 0.1383 1
                              0.7100
confint(lmer_resultsAV2)
## Computing profile confidence intervals ...
                      2.5 %
                               97.5 %
##
               0.98403863 2.8252646
## .sig01
## .sigma
                4.62048270 5.1151796
## (Intercept)
                -1.21956485 1.2133558
## scale(corr) -0.06437676 0.6319706
## scale(corr^2) -0.41594485 0.2840326
Visual ventriloquism effect
# Data cleaning
visVE_indvd_data <- VE_ujdg_data[, - c(6, 7)]</pre>
visVE_indvd_data <- visVE_indvd_data[complete.cases(visVE_indvd_data), ]</pre>
LMM as ordered factors
LMM as numeric factors
class(visVE_indvd_data$disc) = "Numeric"
class(visVE_indvd_data$corr) = "Numeric"
class(visVE_indvd_data$subjID) = "Numeric"
lmer_resultsAV4 <- lmer(visVE ~ (scale(disc)+scale(disc^2))*</pre>
                         (scale(corr)+scale(corr^2)) +
                         (1|subjID), data = visVE_indvd_data)
summary(lmer_resultsAV4,corr = FALSE)
```

## Linear mixed model fit by REML. t-tests use Satterthwaite's method [

```
## lmerModLmerTest]
## Formula:
## visVE ~ (scale(disc) + scale(disc^2)) * (scale(corr) + scale(corr^2)) +
##
       (1 | subjID)
##
      Data: visVE_indvd_data
##
## REML criterion at convergence: 18142.3
##
## Scaled residuals:
      Min
##
               1Q Median
                                3Q
                                       Max
## -9.8496 -0.4775 0.0112 0.4930 8.8777
##
## Random effects:
            Name
## Groups
                         Variance Std.Dev.
             (Intercept) 0.1336
                                 0.3655
## subjID
## Residual
                         6.8807
                                  2.6231
## Number of obs: 3800, groups: subjID, 9
## Fixed effects:
##
                                Estimate Std. Error
                                                             df t value Pr(>|t|)
## (Intercept)
                                -0.01269
                                            0.12910
                                                       8.06840 -0.098
                                                                           0.924
## scale(disc)
                                -0.96662
                                             0.21899 3783.76915 -4.414 1.04e-05
                                            0.21900 3783.82383
## scale(disc^2)
                                 0.15652
                                                                0.715
                                                                           0.475
## scale(corr)
                                 0.24502
                                            0.22185 3785.03793
                                                                 1.104
                                                                           0.269
## scale(corr^2)
                                            0.22186 3785.14282 -0.942
                                -0.20895
                                                                           0.346
## scale(disc):scale(corr)
                                -0.53738
                                            1.14090 3785.21285 -0.471
                                                                           0.638
## scale(disc):scale(corr^2)
                                 0.57531
                                            1.13888 3785.02159
                                                                 0.505
                                                                           0.613
## scale(disc^2):scale(corr)
                                          1.14140 3785.41437
                                                                 0.206
                                 0.23557
                                                                           0.837
## scale(disc^2):scale(corr^2)
                                 -0.21807 1.14082 3785.20479 -0.191
                                                                           0.848
##
## (Intercept)
## scale(disc)
                               ***
## scale(disc^2)
## scale(corr)
## scale(corr^2)
## scale(disc):scale(corr)
## scale(disc):scale(corr^2)
## scale(disc^2):scale(corr)
## scale(disc^2):scale(corr^2)
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Anova(lmer_resultsAV4)
## Analysis of Deviance Table (Type II Wald chisquare tests)
## Response: visVE
##
                                Chisq Df Pr(>Chisq)
## scale(disc)
                               19.4860
                                          1.013e-05 ***
                                       1
## scale(disc^2)
                               0.5113 1
                                              0.4746
## scale(corr)
                               1.2081
                                       1
                                              0.2717
## scale(corr^2)
                               0.8796 1
                                              0.3483
## scale(disc):scale(corr)
                               0.2219 1
                                              0.6376
## scale(disc):scale(corr^2)
                               0.2552 1
                                              0.6134
```

```
## scale(disc^2):scale(corr) 0.0426 1 0.8365
## scale(disc^2):scale(corr^2) 0.0365 1 0.8484
## ---
## Signif. codes: 0 '*** 0.001 '** 0.05 '.' 0.1 ' ' 1
confint(lmer_resultsAV4)
```

## ## Computing profile confidence intervals ...

```
##
                                  2.5 %
                                        97.5 %
## .sig01
                              0.2094673 0.6161298
## .sigma
                             2.5624357 2.6804327
## (Intercept)
                             -0.2790727 0.2535620
## scale(disc)
                             -1.3948944 -0.5370943
## scale(disc^2)
                            -0.2730218 0.5848106
## scale(corr)
                            -0.1901067 0.6788780
                             -0.6428281 0.2262155
## scale(corr^2)
## scale(disc):scale(corr)
                            -2.7710707 1.6974998
## scale(disc):scale(corr^2) -1.6554325 2.8052404
## scale(disc^2):scale(corr) -2.0004260 2.4701132
## scale(disc^2):scale(corr^2) -2.4515482 2.0167118
```