# Part 2: Functional Dependencies, Decompositions, Normal Forms

```
1)
a) BH \rightarrow AD
            BH+ = ABCDEFGH //does not violate; BH superkey
    D \rightarrow BH
            D+ = ABCDEFGH
                                  //does not violate; D superkey
    BCE \rightarrow F
                                  //violates
            BCE+ = BCEF
    F \rightarrow C
           F+=CF
                                  //violates
    A \rightarrow GEF
           A + = ACEGF
                                  //violates
    Answer: BCE \rightarrow F, F \rightarrow C, A \rightarrow GEF violates BCNF
b) BCNF Decomposition
    BH + = ABCDEFGH
                                                                 (does not violate)
    D+ = ABCDEFGH
                                                                 (does not violate)
                                                                 (violates)
    A + = ACEFG
    Decomposition:
    R1 = ACEFG
    R2 = ABDH
            Project FDs onto R1(ACEFG)
            R_1(ACEFG):
                   A+ = ACEFG -- A \rightarrow GEF, F \rightarrow C; A superkey, does not violate
                   C + = C --nothing
                   E + = E --nothing
                   F+=CF--F\rightarrow C violates, abort
                   Decomposition
                   R3 = FC
                   R4 = AEFG
                           Project FDs onto R3(FC)
                           F+=FC - F \rightarrow C; F superkey, does not violate
                           C + = C --nothing
                           FC + = FC --nothing
                           R3 satisfies BCNF
```

## **Project FDs onto R4(AEFG)**

A+ = AGEF,  $A \rightarrow GEF$ ; A superkey, does not violate

E+ = E --nothing

F+ = FC -- nothing

G+=G --nothing

dont need to check supersets of A (weaker)

EF+ = EFC --nothing

FG+ = CFG --nothing

EG+ = EG --nothing

## **R4** satisfies BCNF

## Return to R2. Project FDs onto R2(ABDH)

### R<sub>2</sub>(ABDH)

A+ = AGEFC -- nothing

B+ = B --nothing

 $D+ = ABDH - D \rightarrow BH$ ,  $BH \rightarrow AD$ ; D superkey, does not violate

H+=H-- nothing

AB+ = ABCEFG -- nothing

dont need to check supersets of D (weaker)

AH+ = AGEFCH -- nothing

BH+ = BHAD, D  $\rightarrow$  BH, BH  $\rightarrow$  AD; BH superkey doesn't violate

## R2 satisfies BCNF

#### Answer:

BCNF Decomposition Result:

R<sub>2</sub>(A,B,D,H), R<sub>3</sub>(C,F), R<sub>4</sub>(A,E,F,G)

#### 2)

a) Answer:

D+ = ABCDEFG; D is a key for R and no superset of D can be a key.

The rest of the FDs except for  $EF \rightarrow B$  contain D so I don't need to consider those. And EF is not a key since EF+=EFB.

#### b) S1

$1 \text{ DBE} \to F$	DBE+=ABCDEFG, discard
$2 \text{ DBE} \rightarrow C$	DBE+=ABCDEFG, discard
$3 \text{ CD} \rightarrow \text{A}$	CD+=CDFABGE, discard
$4 \text{ CD} \rightarrow \text{F}$	CD+=ABCDEFG, discard
$5 D \rightarrow A$	no other way to get A, keep
$6 D \rightarrow B$	no other way to get B, keep
$7 D \rightarrow G$	no other way to get G, keep
$8 \text{ BADE} \rightarrow C$	no other way to get C, keep
$9 \text{ ABD} \rightarrow \text{E}$	no other way to get E, keep

$10 D \rightarrow F$	no other way to get F, keep
11 EF $\rightarrow$ B	no other way to get B, keep
S2	
$5 D \rightarrow A$	no other way to get A, keep
$6 D \rightarrow B$	no other way to get B, keep
$7 D \rightarrow G$	no other way to get G, keep
$8  \text{BADE} \rightarrow \text{C}$	can be simplified to $D \rightarrow C$
$9 \frac{AB}{D} \rightarrow E$	can be simplified to $D \rightarrow E$
10 D $\rightarrow$ F	no other way to get F, keep
11 EF $\rightarrow$ B	no other way to get B, keep

#### Answer:

The minimal basis for S is:

 $D \rightarrow A$ 

 $D \rightarrow C$ 

 $D \rightarrow E$ 

 $D \rightarrow F$ 

 $D \rightarrow G$ 

 $EF \rightarrow B$ 

c) Merge the right hand sides.

$$D \rightarrow ACEFG$$
$$EF \rightarrow B$$

The set of relations that would result would have these attributes:

 $R_1(A,C,D,E,F,G)$   $R_2(B,E,F)$ 

None of the attributes completely overlap. So we can't eliminate any relations. D is a key for R so there is no need to add another relation that includes a key.

So the final set of relations is:  $R_1(A,C,D,E,F,G)$ ,  $R_2(B,E,F)$ 

d) Because we formed each relation from an FD, the LHS of those FDs are indeed superkeys for their relations. However there may be other FDs that violate BCNF and therefore allow redundancy. Find out by projecting FDs onto each relation.

 $EF \rightarrow B$  projects onto R2. EF+=EFB (does not violate), E+=E (does not violate), B+=B (does not violate), BE+=BE (does not violate), BF+=BF (does not violate).

 $D \rightarrow ACEFG$  projects onto R1. D+ = ABCDEFG (does not violate) but the subset EF+ = EFB which is not a superkey so it violates BCNF.

So yes, this schema allows redundancy.