# Do Large Language Models Excel in Complex Logical Reasoning with Formal Language?

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# **Abstract**

Large Language Models (LLMs) have been shown to achieve breakthrough performance on complex logical reasoning tasks. Nevertheless, most existing research focuses on employing formal language to guide LLMs to derive reliable reasoning paths, while systematic evaluations of these capabilities are still limited. In this paper, we aim to conduct a comprehensive evaluation of LLMs across various logical reasoning problems utilizing formal languages. From the perspective of three dimensions, i.e., spectrum of LLMs, taxonomy of tasks, and format of trajectories, our key findings are: 1) Thinking models significantly outperform Instruct models, especially when formal language is employed; 2) All LLMs exhibit limitations in inductive reasoning capability, irrespective of whether they use a formal language; 3) Data with PoT format achieves the best generalization performance across other languages. Additionally, we also curate the formal-relative training data to further enhance the small language models, and the experimental results indicate that a simple rejected fine-tuning method can better enable LLMs to generalize across formal languages and achieve the best overall performance. Our codes and reports are available at https://github.com/wjn1996/ FormalEval.

# 1 Introduction

Logical reasoning, i.e., deductive, inductive, and abductive, is one of the imperative natural language processing (NLP) tasks and plays a significant role in artificial intelligence (AI) to perform human-like decision-making, task-solving, and deep-thinking (Zhang et al., 2021; Yang et al., 2023b; Yu et al., 2024; Xu et al., 2025). Different from conventional natural language understanding and generation, logical reasoning requires the AI systems to explicitly provide meticulous elucidation of thoughts and verifiable derivation chains,

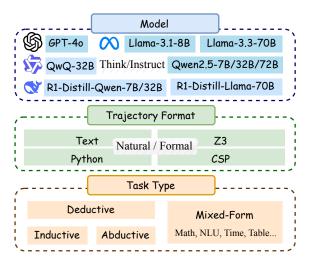


Figure 1: Evaluation framework with three specific dimensions: spectrum of LLMs, taxonomy of logical reasoning tasks, and format of trajectories.

which is crucial and challenging (Cummins et al., 1991). Early works have developed multiple formal languages with symbol solvers to make the reasoning steps computable and structured (RANISE, 2003; Bulatov et al., 2005; Bjørner et al., 2015).

Recently, the emergence of reasoning capabilities in large language models (LLMs) has incentivized significant progress in complex reasoning tasks, such as mathematics, commonsense, and symbol (Achiam et al., 2023; Bi et al., 2024). Current studies <sup>1</sup> have found that LLMs can achieve remarkable performance with the aid of formal language and symbol solvers, especially when integrating well-designed task-specific instructs (Lyu et al., 2023; Pan et al., 2023), chain-of-thought (CoT) reasoning patterns (Wei et al., 2022; Ye et al., 2023), and valuable solvers' feedback (He-Yueya et al., 2023; Gao et al., 2023; Wang et al., 2024). Such approaches aim to formalize the given logical problem and constantly adjust the results lean on

<sup>&</sup>lt;sup>1</sup>Due to the space limitations, the detailed description about related works are moved in Appendix A.

the solver's feedback. Despite substantial efforts exhibiting exceptional performance, there are still relatively limited systematic and comprehensive evaluations. Thus, a natural question remains open: whether the LLM really excels in complex logical reasoning problems with formal language?

To bridge the gap, this paper endeavors to perform a comprehensive evaluation of LLMs utilizing various formal languages to tackle diverse logical reasoning problems. At first, we develop the evaluation architecture to clearly express the entire assessment view (As illustrated in Section 2), with the framework shown in Figure 1. Specifically, we divide the entire assessment into three distinct dimensions, including the spectrum of LLMs, the taxonomy of logical reasoning tasks, and the format of trajectories. For the family of LLMs, we further consider different reasoning patterns which has been injected into the model training, such as short thinking (e.g., GPT-40 (Achiam et al., 2023), Qwen1.5/2/2.5 (Bai et al., 2023), LLaMA3/3.1/3.3 (Grattafiori et al., 2024)) and long thinking (e.g., DeepSeek-R1-Dsitill-Qwen (Guo et al., 2025)). For the logical reasoning, we adhere to the classic definitions (Flach and Kakas, 2000), categorizing tasks into deductive, inductive, and abductive reasoning. Additionally, we account for tasks that may integrate multiple reasoning types by introducing a new category referred to as mixedform reasoning. Regarding the format of trajectories, we consider three main formal languages ("Python", "Z3", "CSP") with a default natural language format as "Text".

Secondly, we perform a thorough evaluation across these three dimensions (as detailed in Section 3). Many contemporary benchmarks purely emphasize informal text patterns and lack comprehensive integration of different formal languages and logical reasoning tasks (Lei et al., 2024; Xu et al., 2025; Xia et al., 2025). For instance, it is widely recognized that Python is superior to plain text when addressing mathematical problems (Friedman, 2023; Gao et al., 2023), but it remains unclear whether Python is equally effective in resolving BBH (Suzgun et al., 2022) and bbeh (Kazemi et al., 2025) problems. To fill this blank, this part aims to investigate whether current LLMs can solve a variety of logical reasoning tasks utilizing different formal languages. From this study, we derive several intriguing observations: 1) Thinking models significantly outperform Instruct models, especially when formal language is employed; 2) All LLMs exhibit limitations in inductive reasoning capability, irrespective of whether they use a formal language; 3) LLMs typically produce inferior performance on difficult tasks. These findings prompt a new inquiry *Do large models possess generalization capabilities when employing formal languages?* 

Thirdly, we further investigate the generalization across different reasoning tasks and formal languages (As illustrated in Section 4). To reach this goal, we collect a few training data from the training set of current evaluation tasks, which is classified into three types: deductive, inductive, and abductive. For each task type, we also provide different trajectories according to the usages of (in)formal languages. To make a fair comparison, we only use data from a single language type for SFT training, and the training data has the same scale size. From the experiments, we observe that the LLM can obtain significant in-domain performance on multiple logical reasoning tasks. In addition, we also discovered an elusive phenomenon that CSP is hard to generalize to other formal and informal languages, but it is easy to generalize from other languages to CSP. Therefore, we speculate that the poor performance of LLM on some formal languages can be blamed on the lack of pertinent knowledge and potential for stimulated reasoning.

Lastly, based on the previous exploration, we aim to amplify the capabilities of weaker models in using formal languages to solve reasoning problems. Concretely, we propose a simple but effective rejected fine-tuning (RFT) approach to curate different formal-relative training data. After the enrichment, the overall accuracy of using informal and formal languages for complex logical tasks can be improved by more than 10%.

In summary, the main contributions are as follows:

- In light of the insufficient evaluations of existing works, we aim to collect 66 tasks with multiple widely used formal languages, and provide a comprehensive evaluation for current LLMs across three dimensions, including the spectrum of LLMs, the taxonomy of tasks, and the format of trajectories.
- Considering that different formal languages have different expressions for reasoning, we explore the generalization across various formal languages.

• To further enhance the capability of LLMs in utilizing formal languages to solve complex logic reasoning, we introduce a simple but effective rejected fine-tuning method with curated formal-relative data. The experimental results indicate the effectiveness of considering the generalization of formal language across various logical tasks.

# 2 Preliminary

As illustrated in Figure 1, our evaluation framework is structured along three dimensions: Model, Trajectory Format, and Task Type. In this section, we introduce the two key points of complex reasoning task categorization (Section 2.1) and trajectory format design (Section 2.2).

# 2.1 Taxonomy of Complex Logical Reasoning

Inspired by Xu et al. (2025), we present a unified taxonomy that categorizes a wide range of complex reasoning tasks into four major types: Deductive, Inductive, Abductive, and Mixed-Form. To elaborate, the categorization is based on the nature of reasoning required in human-like thinking in the real world: 1) **Deductive reasoning** is the forward reasoning process with rules that starts from the given premises to the conclusion (Goel, 2007; Johnson-Laird, 1999). Formally, we can denote the process as  $premise \xrightarrow{\text{rule}} conclusion$ . 2) **Inductive** reasoning is the process that infers specific rules based on multiple premises and conclusions. It can be represented as (premise, conclusion) $\rightarrow$ rule. 3) Abductive reasoning is the backward process of deductive which aims to obtain the premise based on conclusion, and the process can be viewed as conclusion premise. 4) Mix-Form Reasoning involves at least two of the above three types of reasoning. In real-life scenarios, most complex problems involve mixed reasoning, including but not limited to temporal-spatial reasoning, NLU, knowledge reasoning, and mathematical reasoning.

In pursuit of specific benchmarks based on these categories, we meticulously collect **66** subsets of data, and the detailed information can be found in Table 2. The details of the specific datasets are shown in Appendix B.

# 2.2 Trajectory Format

As shown in Figure 1, we categorize trajectory formats into two main types: **informal language** (natural language) and **formal language**. Informal

language can be expressed as free-form text, while formal languages include programming languages (e.g., Python) and logic-based languages (e.g., Z3 and CSP). They can be modeled as:

$$\mathcal{LLM}(Q) = \langle s_1, s_2, \dots, s_n \rangle \xrightarrow{\text{Exec}} A$$

where Q is the input question, and  $\mathcal{LLM}(Q)$  represents the trajectory generated by LLM. Each step  $s_i \in \mathcal{L}_{\text{LLM}}$  corresponds to a structured unit (e.g., code or logic expression), and the trajectory is executed by an external engine to produce the final answer A.

For **PoT**, we use Python 3.12 and its standard library as the execution environment. Each step  $s_i \in \mathcal{LLM}_{PoT}$  is a valid Python statement. For **Z3**, we adopt the Z3 theorem prover as the executor and Z3 trajectories are composed of declarative symbolic steps  $s_i \in \mathcal{LLM}_{Z3}$ . For **CSP**, we use the python-constraint library as the trajectory executor. Each CSP trajectory  $s_i \in \mathcal{LLM}_{CSP}$  consists of variable declarations, domain assignments, and constraint definitions.

In addition, we chose Z3 over Prover9 because Z3 not only supports first-order logic (Prover9-FOL) but also natively supports rich theories such as integers and arrays. More detailed description can be found in section C.

# 3 PART I: Evaluation across LLMs, Tasks, Trajectories

In PART I, we present a comprehensive evaluation across three dimensions: **Models**, **Trajectory Formats**, and **Reasoning Task Types**. Specifically, we evaluate both *Instruct* and *Thinking* models, ranging from 7B to 72B (see Figure 1). For reasoning tasks, we follow the taxonomy introduced in Section 2.1. For trajectory formats, we evaluate three formal languages and natural language, as detailed in Section 2.2. All evaluations are conducted in a zero-shot setting. For formal languages (PoT, Z3, CSP), we apply a three-step self-refinement process during code execution. Detailed evaluation settings are provided in Appendix D.1.

# 3.1 Model Performance for Reasoning Tasks and Trajectory Formats

As shown in Figure 2, the radar chart (Overall+Fine-grained) illustrates the model's performance under different task types and trajectory formats. The complete results can be found in Appendix E.

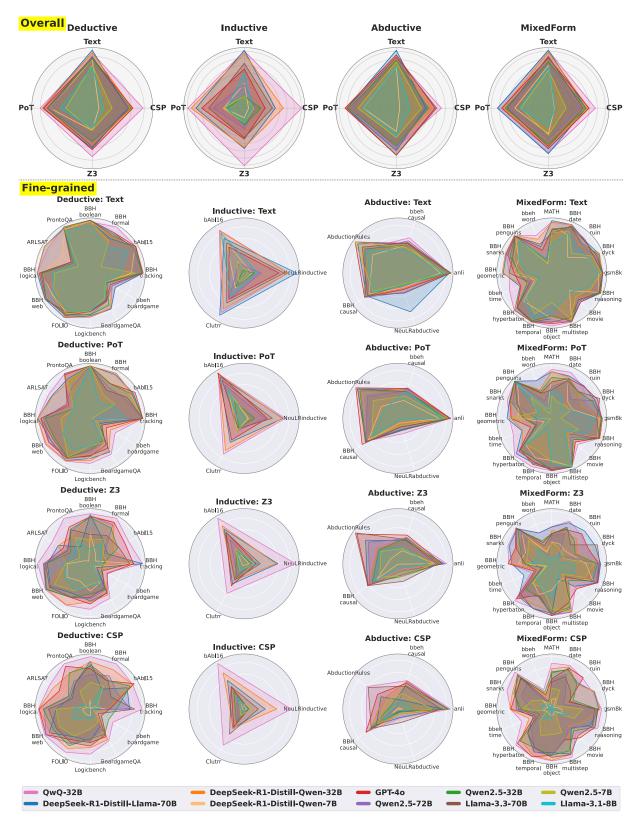


Figure 2: Radar plots illustrating the performance (%) of multiple LLMs across different reasoning task types (Deductive, Inductive, Abductive, Mixed Form) and trajectory formats (Text, PoT, Z3, CSP). Overall (top  $1 \times 4$ ) shows aggregated performance by reasoning type and format. Fine-grained (below  $4 \times 4$ ) present fine-grained results on individual tasks

Thinking model outperforms Instruct model From the overall part, we can observe that series of Thinking models (e.g., QwQ-32B, etc.) outperform the Instruct series in most tasks, especially in the Inductive and Mixed-Form tasks. The disparities between them reflect that the Thinking mode can better elicit the LLM to provide reliable trajectories for formal reasoning. Previous evaluations (Xu et al., 2025) have demonstrated a similar finding that Instruct models have achieved unsatisfactory results in inductive reasoning, but they do not provide the suggestion that the Thinking model can perform well.

**Text outperforms formal languages, except for QwQ-32B** Most models outperform formal languages in the Text trajectory format. In the Finegrained section, as the trajectory format shifts from Text to CSP, the radar map coverage area gradually decreases, especially in the bbeh series of subtasks. However, QwQ-32B is the only model that stays ahead in all tasks and trajectories, maintaining a high level of performance in all formal languages.

Formal language performance drops significantly on difficult tasks Models can achieve comparable or even better performance than Text with formal languages in simple tasks (e.g., Z3, CSP in Deducitve-BBH\_web), but the performance of formal languages drops off substantially in complex tasks(e.g., Deductive-bbeh\_boardgameQA). This phenomenon again suggests that current large models are better at using non-formal languages when expressing complex logic. Possible reasons include: 1) the model training process is dominated by natural language, with a scarcity of formal language samples; and 2) the model lacks augmentation for difficult and complex problems. The performance of text formatting is average, while formal language significantly decreases. It is worth noting that GPT-4o's performance in this area is relatively stable, possibly due to its optimization in data.

Small models perform poorly on formal language Both *Instruct* and *Thinking* small models have acceptable overall performance under Text, but when dealing with formal languages, the performance drops rapidly. Taking R1-Distill-Qwen-7B as an example, its performance under the CSP trajectory is even significantly lower than similar *Instruct* models, indicating that the Thinking mechanism is difficult to effectively support formal lan-

guage reasoning at low parameter scales. In addition, in high complexity tasks such as *bbeh-time*, *bbeh-shuffle*, etc., the small model is almost completely ineffective in structured trajectories such as Z3 and CSP, and it is difficult to complete the basic logical steps, which shows its serious lack of ability to deal with formal reasoning problems.

Overall, all models except QwQ-32B show a continuous performance degradation in the trajectory format change from Text to formal language (PoT, Z3, CSP). This phenomenon suggests that the current mainstream LLMs are more adept at handling natural language tasks, while they are still deficient in formal language reasoning.

# 3.2 Different Reasoning Tasks Prefer Different Trajectory Format

In this section, we use the GPT-40 result as an anchor point to conduct a detailed analysis of how different tasks exhibit varying preferences for trajectory formats. As shown in Figure 3, GPT-40 exhibits diverse preferences across trajectory formats. Below, we summarize the main observations.

Text performs better in language comprehension and open-ended tasks First, in tasks such as BBH\_snarks, bbeh\_linguini, bbeh\_nycc, Text is closer to the nature of the task in humor comprehension, linguistic style recognition, and fuzzy semantic parsing, and is superior to formal language. Secondly, in induction and abduction tasks such as AbductionRules, NeuLRabductive, NeuLRinductive, and Clutrr, where reasoning relies on linguistic expressions, the Text format is more advantageous. In addition, LogicQA, although categorized as a logic task, is more akin to a general knowledge quiz. It originates from the Chinese Civil Service Exam, where textual ability plays a dominant role in performance. (Cases in Figure 6)

Well-structured tasks prefer PoT PoT format is particularly effective in tasks with strong structural characteristics, such as numerical computation and symbolic reasoning tasks like BBH\_dyck\_languages and BBH\_word\_sorting. In these settings, PoT enables efficient computation and facilitates the handling of rules involving nesting and ordering. Additionally, in tasks that involve temporal sequences, object tracking, and spatial reasoning, such as bAbI16, bbeh\_shuffled\_objects, and bbeh\_spatial\_reasoning, PoT demonstrates strong performance by leveraging programmatic

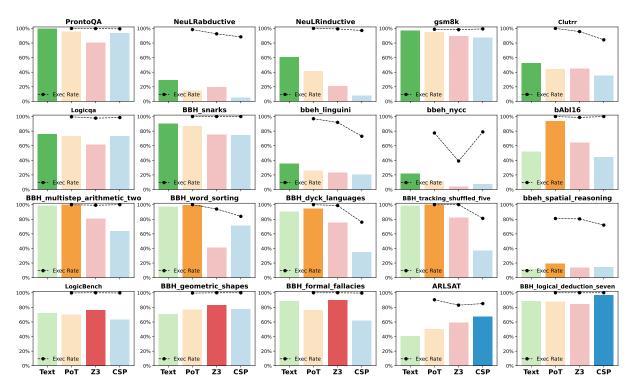


Figure 3: Preferred reasoning task performance across different trajectory formats (Text, PoT, Z3, CSP) in GPT-40 results. Each subplot shows task accuracy under different formats, with execution rate (Exec Rate) plotted as a black line. The highlighted bars represent the most preferred trajectory format for each task.

trajectories to clearly express intermediate states and transformation processes. (Case in Figure 7)

Z3 handles formal and FOL reasoning well.
Z3 format shows a good adaptation to formal

Z3 format shows a good adaptation to formal logic tasks, especially in tasks with strict logical rules: LogicBench, BBH\_formal\_fallacies, BBH\_logical\_deduction. This type of task is essentially convertible to first-order logical expressions, so using an SMT solver (e.g., Z3) as the trajectory language is more suitable. In addition, BBH\_geometric\_shapes involves spatial reasoning, where the boolean logical expressiveness of Z3 is more advantageous. (Case in Figure 9)

# CSP shows advantages in complex constraints

CSP format shows advantages in some structured logic tasks, such as *BBH\_logical\_deduction*, a result consistent with the findings of Logic-LM (Pan et al., 2023). More interestingly, in *ARLSAT*, a task derived from the Law School Admission Test, CSP also achieves the optimal result, which contrasts with the previous (Pan et al., 2023) literature's conclusion that Z3 is better suited for this task. This difference may stem from the characteristics of the tasks themselves; in ARLSAT, the stems of the questions typically contain constraints, which are more consistent in form with the way CSPs are

expressed. (Case in Figure 9)

Beyond the four dimensions mentioned above, we can observe that execution success rate (Exec Rate) is also a key factor underlying the differences among various forms of language. Moreover, gsm8k achieves its best performance under the Text format, which is inconsistent with findings from previous studies (e.g., Ye et al. (2023); He-Yueya et al. (2023)). This discrepancy may be attributed to two factors: 1) Prior work often involves task-specific optimization for mathematical reasoning; 2) Current large language models are trained on substantial amounts of mathematical natural language reasoning data, which enhances their generalization ability in Text formats.

Overall, task trajectory alignment plays a critical role. Different tasks exhibit preferences for specific trajectory formats—some tasks are inherently better suited to certain formal representations, and using inappropriate formats may even hinder model performance. Therefore, when constructing multi-trajectory training or evaluation frameworks, it is important to carefully consider the alignment among task structure, target language, and model capabilities.

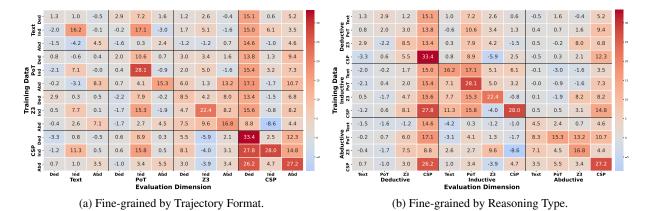


Figure 4: Generalization performance across **fine-grained** (task type  $\times$  format) configurations. Each cell shows the performance gain ( $\Delta$ ) from training on the row configuration and evaluating on the column configuration

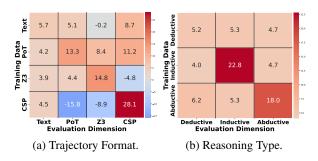


Figure 5: Generalization performance across reasoning types and trajectory formats (**coarse-grained** analysis). Each cell reports the performance gain ( $\Delta$ ) when training on the row group and evaluating on the column group.

# 4 PART II: Generalization Analysis across Reasoning Tasks and Trajectory Formats

# 4.1 Setup and Visualization Overview

We collected the training split of the evaluation dataset, categorized into three reasoning types: Deductive, Inductive, and Abductive (excluding Mixed-Form due to variable control challenges). Each training instance is represented in four trajectory formats: Text, PoT, Z3, and CSP. Details are provided in Section 5.1.

Based on the above data, we conduct two sets of analytical experiments: coarse-grained and fine-grained. 1): **Coarse-grained** experiments, as shown in Figure 5, involve training on 7 groups of data (3 reasoning types + 4 trajectory formats), each mixed with general-domain data, and evaluating on the same 3 reasoning types and 4 formats. 2): **Fine-grained** experiments, as shown in Figure 4, involve training on 12 groups of data (3 reasoning types × 4 trajectory formats), each mixed

with general-domain data, and evaluating across all 12 combinations of reasoning types and formats. Each heatmap cell shows the performance gain  $(\Delta)$  when training on the configuration in the row and evaluating on the configuration in the column. The performance gain reflects the improvement introduced by our constructed data when mixed with the general-domain data (Trained on Qwen-2.5-7B).

# 4.2 Coarse-Grained Generalization Analysis

Significant in-domain improvement The strongest performance gains are observed along the diagonal, indicating that the model benefits most when the training and evaluation data come from the same group. Notably, the improvements for CSP (Train) → CSP (Eval) and Inductive (Train) → Inductive (Eval) reach 28.1 and 22.8, respectively. Combined with observations from Part-I, this can be partially attributed to the relatively low baseline performance of the Qwen2.5-7B model on the CSP and Inductive dimensions, meaning that even a small amount of in-domain data leads to significant improvement.

# PoT transfers well, while CSP transfers poorly Outside the diagonal, in figure 5a, PoT migrates well in Text, Z3, and CSP. This might be related to the fact that there is a lot of code data in the pre-training data. CSP, on the other hand, has an effect only on Text and CSP, with significant negative effects on PoT (-15.8) and Z3 (-8.9). This suggests that there may be structural differences among formal languages.

Reasoning types: all exhibit positive transfer The overall transfer effect is relatively balanced between the different reasoning types (Fig.5b). The relatively small improvement on Deductive itself

	Text	Text PoT			<b>Z</b> 3	(	CSP	Avg		
Model	Acc	Acc	Exec Rate	Acc	Exec Rate	Acc	Exec Rate	Acc	Exec Rate	
GPT-40	66.7	64.0	91.5	54.5	87.4	53.0	83.98	59.0	87.6	
Qwen2.5-7B-Instruct	52.3	37.0	<u>78.6</u>	33.0	70.0	<u>25.0</u>	52.1	37.0	<u>66.9</u>	
Qwen2.5-72B-Instruct	63.4	54.0	85.1	42.5	79.6	43.0	75.2	51.0	80.0	
Qwen2.5-7B-Baseline Qwen2.5-7B-Base w.Formal	49.7 52.7 <sup>+3.0</sup>	40.0 44.0 <sup>+4.0</sup>	75.4 83.5 <sup>+8.1</sup>	27.1 34.8 <sup>+7.7</sup>	68.2 76.5 <sup>+8.3</sup>	20.0 37.0 <sup>+17.0</sup>	52.2 68.1 <sup>+15.9</sup>	34.0 42.0 <sup>+8.0</sup>	65.3 76.0 <sup>+10.7</sup>	

Table 1: Performance of LLM on different trajectory formats before and after formal data enhancement. Accuracy (Acc) and execution rate (Exec Rate) are reported for text, PoT, Z3, and CSP formats. **Qwen2.5-7B-Baseline** denotes the baseline model trained with general data only; **Qwen2.5-7B-Base w.Formal** denotes the augmented model trained with a mixture of formal language data. Improvements after augmentation are shown in green.

may be related to the higher base level of the model on Deductive.

# 4.3 Fine-Grained Generalization Analysis

**Deductive-CSP is most easily generalized** In Figure 4, all entries in the Deductive-CSP column show improvements. The inclusion of any data contributes positively to its performance. This is mainly because CSP has a relatively low baseline, and the Deductive category contains some relatively simple tasks (*BBH\_logical\_deduction\_three* from 40 % to 92%). As a result, adding similar data leads to performance gains.

CSP and Z3 transfer well across reasoning types In Figure 4a, all entries (Ded/Ind/Abd) within the CSP and Z3 blocks show positive gains, indicating that regardless of reasoning type, CSP and Z3 formats can be effectively transferred.

Abductive transfers well across trajectory formats In Figure 4b, all entries (Text/PoT/CSP/Z3) within the Abductive block show improvements, suggesting that regardless of trajectory format, Abductive reasoning can be effectively transferred and improved.

# 5 PART III: Enhancing LLMs with Formal Data

# 5.1 Formal Data Construction via RFT

To enhance model capability in formal languages, we collect the portions of current evaluation datasets that overlap with training data as part of our training set. All dataset details are provided in Table 2. Similarly, the training data is categorized into three types: Deductive, Inductive, and Abductive, and four trajectory formats: Text, PoT, Z3, and CSP.

First, we extract up to 3,000 samples from all training data. Then, GPT-40 was chosen as the

output for teacher model construction. In order to obtain high quality response data, we used **Rejection sampling Fine-Tuning (RFT)**. We used GPT-40 to sample the questions several times and then filtered out those samples whose code was executable and whose final answers are verified to be correct. The statistics of the filtered data are shown in Table 3. The number in parentheses after each model name indicates the amount of added data.

# 5.2 Main Result

As shown in Table 1, the enhanced model improves accuracy by 3.0% on Text, 7.7% on Z3 (with an 8.3% gain in execution rate), and 17.0% on CSP (from 20.0% to 37.0%, with a 15.9% increase in execution rate). Overall, average accuracy rises from 34.0% to 42.0%, and execution rate from 65.3% to 76.0%.

Beyond outperforming the baseline, our formal-data-enhanced model also surpasses the open-source model Qwen2.5-7B-Instruct across all formats. Qwen2.5-7B-Base w.Formal has a smaller parameter size than Qwen2.5-72B, but the performance gap is narrowed by formal data fine-tuning. This suggests that formal data augmentation can effectively improve the competitiveness of small models in formal reasoning tasks.

### 6 Conclusion

In this paper, we provide a comprehensive evaluation of LLMs utilizing various formal languages to solve different categories of logical reasoning tasks. We first develop a systematic evaluation architecture and decompose it into three dimensions. Then, we perform a thorough evaluation across these three dimensions to show whether the current LLMs can excel in formal language utilization. Furthermore, we explore the generalization across multiple formal languages and provide a simple but

effective method on the capability enhancement for small language models.

For future directions, on the one hand, we should strive to enhance the model's reasoning capabilities in a balanced manner across different trajectory formats and task types, especially for Instruct models. At the same time, it may be valuable to construct formal language reasoning datasets in a "thinking" style. On the other hand, we can leverage the task-specific preferences for trajectory formats to further expand the capability boundaries of the model. One approach is to incorporate reasoning results from different trajectory formats as individual voters in a majority voting scheme. Another approach is to introduce multiple symbolic solvers for different reasoning trajectories during the thinking stage of the think model.

# Limitations

This work provides a step toward evaluating and enhancing LLMs through formal reasoning formats, but several limitations remain. First, the landscape of LLMs is evolving rapidly. Our experiments focus on a limited set of models available at the time, and newer models may change performance trends. Second, while we include various reasoning types and benchmark datasets, the overall dataset coverage is limited. Our formal data augmentation is applied to a subset of tasks and may not generalize to other domains. Third, we focus on three formal formats, "PoT, Z3, and CSP," due to their executability and popularity. However, this excludes other symbolic systems such as Lean, Prolog, Coq, or SMT-LIB, which future work could explore. Finally, our formal data construction is based on the Instruct model (GPT-40). With the rise of stronger Thinking models, generating think-style formal data may become more feasible and diverse in the future.

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# A Related Work

# A.1 Symbolic Solver Enhances LLM Reasoning

The integration of symbolic solvers with large language models (LLMs) has emerged as a promising approach to enhance logical reasoning. Early efforts focused on translating natural language to firstorder logic (FOL), exemplified by the creation of the MALLS dataset and the LogicLLaMA model, which demonstrated improved NL-to-FOL translation (Yang et al., 2023a). The Logic-LM framework further explored this direction by employing different formal languages and solvers tailored to specific reasoning tasks, such as FOL with Prover9, CSP solvers for constraint satisfaction, and Z3 for SMT problems (Pan et al., 2023). SATLM introduced declarative prompting to generate task specifications in logical formulas for SAT solvers (Ye et al., 2023), while LINC utilized LLMs for semantic parsing into FOL, offloading inference to theorem provers (Olausson et al., 2023). Subsequent research investigated strategies for improving NL-to-FOL translation through data generation and fine-tuning (Xiong et al., 2024), multi-step refinement of symbolic formulations (Wang et al., 2024), and the impact of pre-training data, including programming languages, on logical inference (Uchiyama et al., 2023). Frameworks like VERUS-LM aimed for versatility by supporting various reasoning tasks with a clear separation of knowledge and queries (Callewaert et al., 2025).

# A.2 Complex Logical Reasoning Tasks

Evaluating the logical reasoning capabilities of LLMs necessitates challenging and diverse datasets that probe various aspects of inference. FOLIO, annotated with first-order logic, focuses on complex logical reasoning in natural language (Han et al., 2024). ProntoQA utilizes logic programming and emphasizes chain-of-thought reasoning (Saparov and He, 2023), while LogicBench covers propositional, first-order, and non-monotonic logic with a focus on single inference rules (Parmar et al., 2023). BOARDGAMEQA assesses reasoning with contradictory information and preferences (Kazemi et al., 2023), and AR-LSAT tests analytical reasoning skills using logic constraints (Zhong et al., 2022). The BIG-Bench Hard (BBH) benchmark includes a wide array of challenging tasks like Boolean Expressions (Suzgun et al., 2022), formal fallacies (Suzgun et al., 2022), logical deduction (Suzgun et al., 2022), shuffled objects (Suzgun et al., 2022), and web of lies (Suzgun et al., 2022). Other datasets like bAbI (Weston et al., 2015), CLUTRR (Sinha et al., 2019),  $\alpha$ -NLI (Zhao et al., 2021), AbductiveRules (Bhagavatula et al., 2020), LogiQA (Liu et al., 2020), and gsm8k (Cobbe et al., 2021) target specific reasoning types such as deductive, inductive, abductive, temporal, spatial, and mathematical reasoning. The variety in these datasets and their annotations highlights the multifaceted nature of complex reasoning and the ongoing efforts to evaluate and enhance LLMs in this domain.

# **B** Details of Datasets

Table 2 provides a comprehensive overview of all datasets used in our study. Each dataset is annotated with its reasoning type (Deductive, Inductive, Abductive, or Mixed-Form), along with the number of evaluation and training examples. We also include the original source for each dataset.

The classification follows our taxonomy introduced in Section 2.1. In particular:

- Deductive datasets include tasks that require formal logical reasoning based on explicit rules or premises.
- **Inductive** datasets focus on pattern discovery and generalization from limited examples.
- **Abductive** datasets involve generating plausible explanations under uncertainty.
- **Mixed-Form** includes tasks with hybrid or ambiguous reasoning types, further grouped into subcategories such as Temporal, NLU, Symbolic, Spatial, Knowledge, and Math.

Some datasets (e.g., BBH and bbeh) are split into finer task categories, each treated independently during evaluation. For large-scale datasets like GSM8K and MATH, we use a subset of examples (denoted by \*) to maintain balance across task types.

This dataset collection forms the foundation for our evaluation across models, trajectory formats, and reasoning types.

# C Detail of Trajectory Format

We extend the unified trajectory formulation to three specific formal languages: Python (PoT), Z3, and CSP. Each trajectory consists of a sequence of symbolic steps, which are executed by an external engine to compute the final answer.

We denote the model-generated trajectory as:

$$\mathcal{LLM}(Q) = \langle s_1, s_2, \dots, s_n \rangle \xrightarrow{\text{Exec}} A$$
 (1)

Where Q is the input query, each  $s_i$  is a step in a domain-specific language, and A is the final answer produced by executing the trajectory.

# Python (PoT) Trajectory

In the Python format, each step  $s_i$  is a syntactically valid Python statement. The trajectory consists of variable assignments, arithmetic operations, control logic, and ends with a print(A) statement.

The Python trajectory is formalized as:

$$\mathcal{LLM}_{\text{Python}}(Q) = \tag{2}$$

$$\langle \mathsf{stmt}_1, \mathsf{stmt}_2, \dots, \mathsf{stmt}_n,$$
 (3)

$$\operatorname{print}(A)\rangle \xrightarrow{\operatorname{Python 3.12}} A$$
 (4)

This trajectory is interpreted and executed sequentially using a Python 3.12 interpreter.

# **Z3** Trajectory

Inspired by Logic-LM (Pan et al., 2023), for Z3, the reasoning trajectory is constructed using the Z3 theorem prover. A typical trajectory includes symbolic variable declarations such as x = Int('x'), followed by logical assertions like s.add(x > 1, x < 5), and ends with solver calls s.check() and s.model() to extract a result.

We represent the Z3 trajectory as:

$$\mathcal{LLM}_{Z3}(Q) = \tag{5}$$

$$\langle Declare, Assert_1, \dots, Assert_k,$$
 (6)

CheckSat,print(A)
$$\rangle$$
  $\xrightarrow{Z3 \text{ Solver}}$   $A$  (7)

Z3 supports a wide range of built-in logical theories, such as integer arithmetic, arrays, and bitvectors.

# **CSP Trajectory**

Constraint Satisfaction Problems (CSPs) are defined by a triple (X, D, C), where  $X = \{x_1, \ldots, x_n\}$  denotes variables,  $D = \{D_1, \ldots, D_n\}$  their domains, and  $C = \{C_1, \ldots, C_m\}$  the set of constraints. Each constraint  $C_j = \langle t_j, R_j \rangle$  is defined over a subset of variables and a relation on their domains.

Туре	Dataset	Eval	Train	Original Source
	FOLIO	134	674	Han et al. (2024)
	ProntoQA	500	50818	Han et al. (2024)
	LogicBench	500	12908	Parmar et al. (2023)
	BOARDGAMEQA	14K	750K	Kazemi et al. (2023)
	AR-LSAT	230	1629	Zhong et al. (2021)
	BBH (Boolean Expression)	250	-	Suzgun et al. (2022)
	bbeh (Boolean Expressions)	200	-	Kazemi et al. (2025)
	BBH (formal_fallacies)	250	-	Suzgun et al. (2022)
	bbeh (Zebra Puzzles)	200	-	Kazemi et al. (2025)
	BBH (logical_deductive_five_objects)	250	-	Suzgun et al. (2022)
Deductive	BBH (logical_deductive_seven_objects)	250	-	Suzgun et al. (2022)
Deddelive	BBH (logical_deductive_three_objects)	250	-	Suzgun et al. (2022)
	bbeh (Boardgame QA)	200	-	Kazemi et al. (2025)
	BBH (tracking_shuffled_objects_five_objects)	250	-	Suzgun et al. (2022)
	BBH (tracking_shuffled_objects_seven_objects)	250	-	Suzgun et al. (2022)
	BBH (tracking_shuffled_objects_three_objects)	250	-	Suzgun et al. (2022)
	bbeh (Shuffled Objects)	200	_	Kazemi et al. (2025)
	BBH (web_of_lies)	250	_	Suzgun et al. (2022)
	bbeh (Web of Lies)	200	_	Kazemi et al. (2025)
	bAbI-15	1000	900	Weston et al. (2016)
	NeuLR-deductive	7001	-	Xu et al. (2025)
	CLUTRR	1042	2452	Sinha et al. (2019)
Inductive	bAbI-16	1000	900	Weston et al. (2016)
	NeuLR-inductive	7001	-	Xu et al. (2025)
	$\alpha$ -NLI	3059	169k	Valentino et al. (2022
	AbductiveRules	2536	8848	Young et al. (2022)
Abductive	BBH (causal_judgement)	250	-	Suzgun et al. (2022)
Abductive	bbeh (Causal Understanding)	200	_	Kazemi et al. (2025)
	NeuLR-abductive	6001	_	Xu et al. (2025)
	Treatiff acquerite	0001		114 01 411 (2020)
Mixed-Form				
Logical	LogiQA	1572		Liu et al. (2021)
Temporal	BBH (date_understanding)	250	-	Suzgun et al. (2022)
	bbeh (Time Arithmetic)	200	-	Kazemi et al. (2025)
	BBH (temporal_sequences)	250	-	Suzgun et al. (2022)
	bbeh (Temporal Sequences)	_ 200_		Kazemi et al. (2025)
NLU	BBH (disambiguation_qa)	250	-	Suzgun et al. (2022)
	bbeh (Disambiguation QA)	200	-	Kazemi et al. (2025)
	BBH (hyperbaton)	250	-	Suzgun et al. (2022)
	bbeh (Hyperbaton)	200	-	Kazemi et al. (2025)
	BBH (ruin_names)	250	-	Suzgun et al. (2022)
	bbeh (New Yorker Cartoon Caption)	200	-	Kazemi et al. (2025)
	BBH (salient_translation_error_detection)	250	-	Suzgun et al. (2022)
	bbeh (Linguini)	200	-	Kazemi et al. (2025)
	BBH (snarks)	250	-	Suzgun et al. (2022)
	bbeh (SARC Triples)	200	-	Kazemi et al. (2025)
Symbolic	BBH (dyck_languages)	250		Suzgun et al. (2022)
	bbeh (Dyck Language)	200	-	Kazemi et al. (2025)
	BBH (word_sorting)	250	-	Suzgun et al. (2022)
	bbeh (Word Sorting)	200	-	Kazemi et al. (2025)
Space	BBH (geometric_shapes)	250		Suzgun et al. (2022)
•	bbeh (Geometric Shapes)	200	-	Kazemi et al. (2025)
	BBH (navigate)	250	-	Suzgun et al. (2022)
	bbeh (Spatial Reasoning)	200	_	Kazemi et al. (2025)
T.1.1.	BBH (penguins_in_a_table)	$-\frac{250}{250}$		Suzgun et al. (2022)
Tapie	bbeh (Buggy Tables)	200	_	Kazemi et al. (2025)
Table				Suzgun et al. (2022)
		250	_	
Knowledge	BBH (moive_recommendation)	250 200	-	
	BBH (moive_recommendation) bbeh (Movie Recommendation)	200	-	Kazemi et al. (2025)
	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding)	200 250	- - -	Kazemi et al. (2025) Suzgun et al. (2022)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA)	200 250 200	- - - - 	Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025)
	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K	$200 \\ 250 \\ -200 \\ -\overline{1319}$	- - - - *8790 *7500	Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH	200 250 200 -1319 5000	- - - - *8790 *7500	Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (202
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH BBH (multistep_arithmetaic_two)	200 250 200 1319 5000 250		Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (202 Suzgun et al. (2022)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH BBH (multistep_arithmetaic_two) bbeh (Multi-step Arithmetic)	200 250 200 1319 5000 250 200		Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (202 Suzgun et al. (2022) Kazemi et al. (2025)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH BBH (multistep_arithmetaic_two) bbeh (Multi-step Arithmetic) BBH (object_counting)	200 250 200 1319 5000 250 200 250		Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (202 Suzgun et al. (2022) Kazemi et al. (2025) Suzgun et al. (2022)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH BBH (multistep_arithmetaic_two) bbeh (Multi-step Arithmetic) BBH (object_counting) bbeh (Object Counting)	200 250 200 1319 5000 250 200 250 200		Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (202 Suzgun et al. (2022) Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2022) Kazemi et al. (2025)
Knowledge	BBH (moive_recommendation) bbeh (Movie Recommendation) BBH (sports_understanding) bbeh (SportQA) GSM8K MATH BBH (multistep_arithmetaic_two) bbeh (Multi-step Arithmetic) BBH (object_counting)	200 250 200 1319 5000 250 200 250		Kazemi et al. (2025) Suzgun et al. (2025) Kazemi et al. (2025) Cobbe et al. (2021) Hendrycks et al. (2022) Kazemi et al. (2022) Kazemi et al. (2025) Suzgun et al. (2022) Kazemi et al. (2025) Suzgun et al. (2025) Suzgun et al. (2025) Suzgun et al. (2022) Suzgun et al. (2022)

Table 2: Complex Logical Reasoning data categorization, data statistics, and sources.

The CSP trajectory is modeled as:

$$\mathcal{LLM}_{\mathrm{CSP}}(Q) = \tag{8}$$

$$\langle \operatorname{AddVar}_1, \dots, \operatorname{AddVar}_n, \operatorname{AddConst}_1, \dots,$$

$$\operatorname{AddConst}_m, \operatorname{GetSolution},$$

$$\operatorname{print}(A) \rangle \xrightarrow{\operatorname{python-constraint}} A \tag{9}$$

The execution uses the python-constraint solver. Variables are added through addVariable(), constraints through addConstraint(), and solutions are obtained via getSolution() or getSolutions(). The solver applies standard algorithms such as backtracking and constraint propagation.

While Prover9-FOL supports classical first-order logic, we choose Z3 for its broader practical applicability. Z3 not only supports FOL reasoning but also natively handles richer theories such as integers, arrays, and linear arithmetic. This allows it to express a wider range of constraints found in real-world reasoning tasks.

# **D** Implementation Setups

# **D.1** Evaluations Details

In the inference phase, we use the vLLM (Kwon et al., 2023) framework for deployment. The inference configuration adopts greedy decoding strategy and sets the maximum generation length to 16K tokens. For the evaluation of model output, we adopt Qwen-2.5-72B-Instruct as the model evaluator to score.

# **D.2** Training Details

In terms of training implementation, we use Megatron-LM as the training framework with the following configurations: a cosine learning rate schedule is adopted with an initial learning rate of 1e-5, a warmup ratio of 0.03, and the learning rate decays to 0; the maximum sequence length is set to 8192, with a global batch size of 128, and the number of training epochs is set to 3. All experiments are completed with Supervised Fine-tuning (SFT) on a computing cluster consisting of 32 NVIDIA A100 GPUs.

# **E** Complete results for different models

As shown in Table 3, we evaluated a total of 31 models across the three parts of this paper. Due to space constraints, we present the results of several representative models here: QwQ-32B (Table 4), GPT-40 (Table 5), Qwen2.5-7B (Table 6),

and Qwen2.5-7B-Base w. Formal (Table 7). The complete results are provided in the supplementary files in Excel format.

# F Case Study

# F.1 Case for PART I

We give cases where Text (Fig 6), PoT(Fig 7), Z3(Fig 8) and CSP(Fig 9) specialize in each case to show their strengths.

# F.2 From Logic-LM Few-Shot Eval to Zero-Shot

Logic-LM uses few-shots setting and rule extraction to build "task-specific executable code" for "a particular formal language" and "a particular task". We use zero-shot directly for evaluation. As shown in the case study in Figure 10, both approaches behave similarly and can evaluate the model's formal language reasoning ability. Meanwhile, the zero-shot setting has better generalization, and this paper considers a subset of 66 datasets based on it.

# G Prompts

For text, we use questions directly as input to the rubric. For formal languages, we use zero-shot reviews. Prompts are as follows: PoT in Figure 11; Z3 in Figure 12; CSP in Figure 13. The Prompt for evaluating models is in Figure 14.

Section	Number	Model
PART-I	4 Thinking-Model  + 6 Instruct-Model =10	QwQ-32B DeepSeek-R1-Distill-Llama-70B DeepSeek-R1-Distill-Qwen-32B DeepSeek-R1-Distill-Qwen-7B GPT-40 Qwen2.5-72B Qwen2.5-32B Llama-3.3-70B Qwen2.5-7B Llama-3.1-8B
	3 (Deductive, Inductive, Abductive) + 4 (Text, PoT, Z3, CSP) =7	Qwen2.5-7B-Base.w. Deductive (+5653) Qwen2.5-7B-Base.w. Inductive (+4947) Qwen2.5-7B-Base.w. Abductive (+6557) Qwen2.5-7B-Base.w. Text (+7384) Qwen2.5-7B-Base.w. PoT (+7448) Qwen2.5-7B-Base.w. Z3 (+6882) Qwen2.5-7B-Base.w. CSP (+6346)
PART-II	3 (Deductive, Inductive, Abductive)  × 4 (Text, PoT, Z3, CSP)  =12	Qwen2.5-7B-Base.w. Deductive_Text (1376) Qwen2.5-7B-Base.w. Deductive_PoT (+1393) Qwen2.5-7B-Base.w. Deductive_Z3 (+1374) Qwen2.5-7B-Base.w. Deductive_CSP (+1510) Qwen2.5-7B-Base.w. Inductive_Text (+1263) Qwen2.5-7B-Base.w. Inductive_PoT (+1476) Qwen2.5-7B-Base.w. Inductive_Z3 (+1166) Qwen2.5-7B-Base.w. Inductive_CSP (+1042) Qwen2.5-7B-Base.w. Abductive_Text (+1820) Qwen2.5-7B-Base.w. Abductive_PoT (+1775) Qwen2.5-7B-Base.w. Abductive_Z3 (+1667) Qwen2.5-7B-Base.w. Abductive_CSP (+1295)
PART-III	1 Baseline-Model+ 1 Formal Data Enhanced Model =2	Qwen2.5-7B-Baseline* (15k) <b>Qwen2.5-7B-Base.w. Formal (+28060)</b>
ALL	31	-

Table 3: Comprehensive Overview of Model Evaluation Experiments in the Entire Paper (Models in Bold Are Presented with Full Results Later). Parentheses after the model in PART-II indicate the corresponding amount of data. All data are based on the 15k generic data of Qwen2.5-7B-Baseline\*, plus (+) the corresponding amount of our synthetic data.

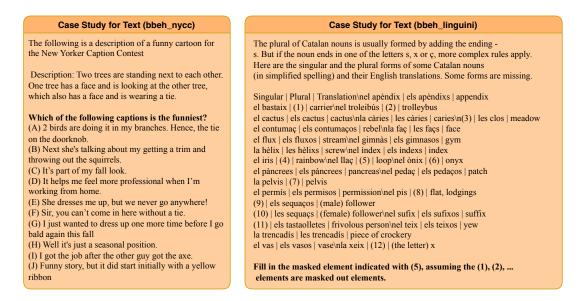


Figure 6: Case for Text. 3.2. These issues are closely related to semantic understanding. They are better suited for textual representation and are difficult to address using formalized languages. Return to section 3.2.

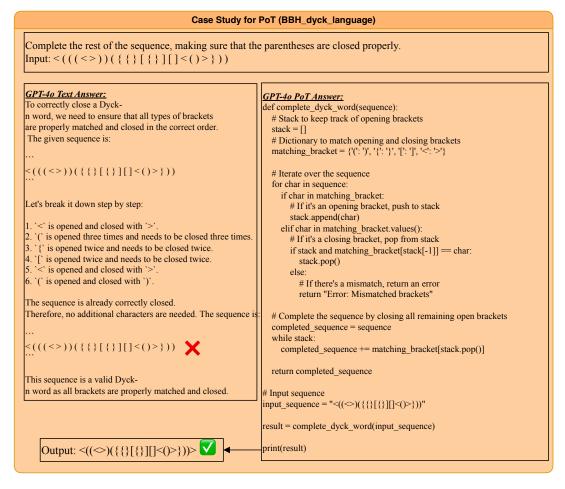


Figure 7: Case for PoT. Symbolic reasoning tasks are inherently well-suited to programming languages, and such problems may in fact originate from coding algorithm questions. Return to section 3.2

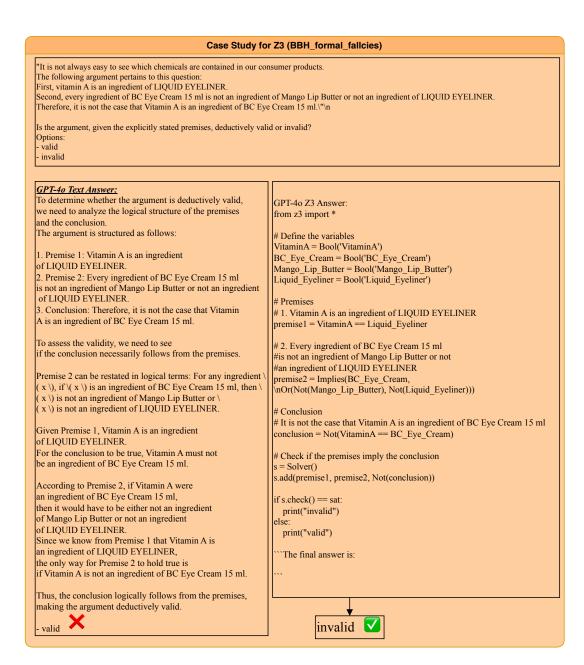


Figure 8: Case for Z3. Z3 (which, in this context, incorporates the first-order logic reasoning capabilities of Prover9) excels at solving formal first-order logic problems. Return to section 3.2

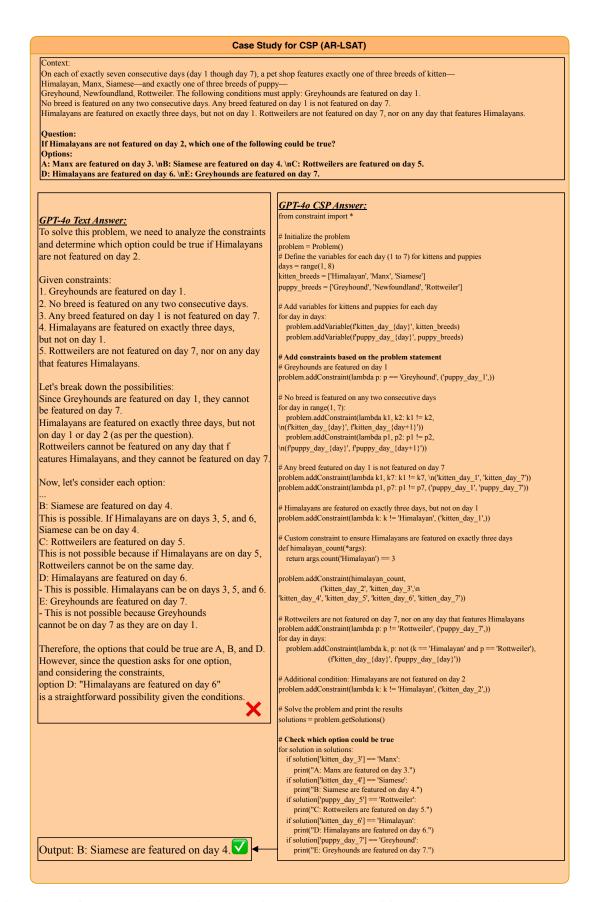


Figure 9: Case for CSP. The problems in ARLSAT involve numerous conditional constraints, which closely resemble the modeling approach used in Constraint Satisfaction Problems (CSPs). Return to section 3.2

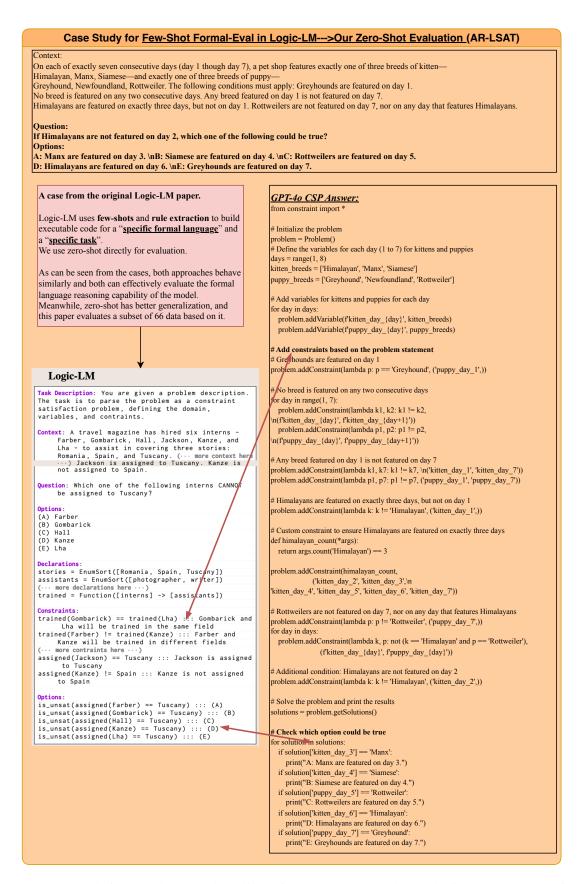


Figure 10: Case Study for Few-Shot Formal-Eval in Logic-LM—>Our Zero-Shot Evaluation (AR-LSAT). Logic-LM uses few-shots and rule extraction to build executable code for a "specific formal language" and a "specific task". We use zero-shot directly for evaluation. As can be seen from the cases, both approaches behave similarly and both can effectively evaluate the formal language reasoning capability of the model. Meanwhile, zero-shot has better generalization, and this paper evaluates a subset of 66 data based on it.

<b>~</b>	Text		PoT		<b>Z</b> 3		CSP		AVG
Dataset	ACC	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate
Average	75.0	68.6	85.1	61.9	79.4	65.1	82.2	67.6	82.2
FOLIO	94.0	94.0	100.0	91.0	99.3	94.0	100.0	93.3	99.8
ProntoQA	99.6	97.8	100.0	99.4	100.0	98.8	100.0	98.9	100.0
logicbenchBQA	82.9	85.6	100.0	86.4	100.0	85.3	100.0	85.1	100.0
BoardgameQA ARLSAT	78.5 92.2	79.3 91.3	99.9 100.0	75.1 83.0	100.0 97.0	69.6 89.1	100.0 100.0	75.6 88.9	100.0 99.0
BBH boolean expressions	96.4	98.8	100.0	94.8	100.0	99.2	100.0	97.3	100.0
bbeh_boolean_expressions	57.0	41.5	53.5	30.0	36.0	42.5	58.5	42.8	49.3
BBH_formal_fallacies	100.0	99.2	100.0	99.6	99.6	98.8	100.0	99.4	99.9
bbeh_zebra_puzzles	44.5	15.5	35.5	2.5	5.5	8.9	11.4	17.9	17.:
BBH_logical_deduction_five_objects	100.0	100.0	100.0	99.6	100.0	98.0	100.0	99.4	100.
BBH_logical_deduction_seven_objects	99.2	99.6	100.0	100.0	100.0	100.0	100.0	99.7	100.
BBH_logical_deduction_three_objects	100.0	100.0	100.0	99.2	99.6	99.2	100.0	99.6	99.
bbeh_boardgame_qa BBH_tracking_shuffled_objects_five_objects	54.5 100.0	55.0 100.0	99.0 100.0	35.0 98.8	73.0 99.6	49.5 98.0	87.5 100.0	48.5 99.2	86. 99.
BBH_tracking_shuffled_objects_seven_objects	100.0	100.0	100.0	96.8	100.0	99.2	100.0	99.2	100.
BBH_tracking_shuffled_objects_three_objects	100.0	100.0	100.0	100.0	100.0	99.2	100.0	99.8	100.
bbeh_shuffled_objects	41.5	0.5	2.0	3.5	10.0	3.0	9.5	12.1	7.
BBH_web_of_lies	92.8	98.8	100.0	98.0	99.6	99.2	100.0	97.2	99.
bbeh_web_of_lies	58.0	37.5	43.5	12.0	17.0	21.5	24.5	32.3	28.
bAbI15	99.3	92.8	100.0	84.1	98.1	92.6	99.9	92.2	99.
NeuLRdeductive	99.9	97.3	100.0	80.9	98.2	95.8	100.0	93.5	99.
clutrr	78.8	73.3	100.0	60.1	94.2	71.0	98.7	70.8 89.8	97.
bAbI16 NeuLRinductive	85.5 76.3	91.8 73.3	100.0 99.9	92.1 90.1	100.0 99.6	89.7 80.7	100.0 99.8	80.1	100. 99.
anli	86.8	86.9	100.0	81.3	99.9	85.9	99.9	85.2	99.
AbductionRules	68.8	71.5	100.0	45.5	98.8	62.8	94.0	62.2	97.
BBH_causal_judgement	64.2	64.7	100.0	59.4	100.0	64.2	100.0	63.1	100.
bbeh_causal_understanding	62.0	53.5	99.5	46.5	90.5	49.0	94.5	52.8	94.
NeuLRabductive	26.0	26.9	99.9	9.9	95.7	15.1	94.1	19.5	96.
logicqa	86.5	82.9	100.0	77.9	99.6	80.5	99.9	82.0	99.
BBH_date_understanding	96.8	94.8	100.0	88.0	98.8	89.6	100.0	92.3	99.
bbeh_time_arithmetic BBH_temporal_sequences	86.5 100.0	79.5 99.6	87.5 100.0	42.5 91.6	50.5 99.2	61.5 97.2	72.5 99.2	67.5 97.1	70. 99.
bbeh_temporal_sequence	52.5	0.0	0.5	0.0	0.0	1.0	1.5	13.4	0.
BBH_disambiguation_qa	48.0	54.0	100.0	38.8	100.0	46.4	100.0	46.8	100.0
bbeh_disambiguation_qa	58.3	50.8	97.5	40.8	82.5	51.7	86.7	50.4	88.
BBH_hyperbaton	100.0	100.0	100.0	99.6	100.0	96.4	100.0	99.0	100.
bbeh_hyperbaton	38.0	26.5	56.5	19.0	35.0	18.0	52.0	25.4	47.
BBH_ruin_names	80.0	84.4	100.0	78.4	96.4	82.8	100.0	81.4	98.
bbeh_nycc	15.0	8.5	72.0	11.5	82.5	10.5	75.0	11.4	76.
BBH_salient_translation_error_detection bbeh_linguini	76.8 46.0	74.8 22.0	100.0 79.5	76.0 24.5	99.6 65.5	75.6 17.5	99.6 51.0	75.8 27.5	99. 65.
BBH_snarks	93.8	91.6	98.9	90.5	100.0	92.1	100.0	92.0	99.
bbeh_sarc_triples	32.0	39.0	100.0	25.5	71.5	19.0	83.0	28.9	84.
BBH_dyck_languages	91.6	73.6	83.2	72.4	92.0	84.0	98.8	80.4	91.
bbeh_dyck_languages	49.0	30.0	79.5	22.0	69.0	28.0	67.5	32.3	72.
BBH_word_sorting	98.8	100.0	100.0	20.4	21.2	79.2	88.0	74.6	69.
bbeh_word_sorting	77.0	77.5	92.5	63.5	76.0	40.0	62.0	64.5	76.
BBH_geometric_shapes	80.0 40.5	80.8 9.0	100.0 19.5	82.0 12.5	99.2 25.5	78.4 14.5	100.0 32.0	80.3 19.1	99.′ 25.′
bbeh_geometric_shapes BBH_navigate	97.6	98.4	100.0	93.6	99.6	95.2	99.6	96.2	23. 99.
bbeh_spatial_reasoning	43.0	40.5	53.0	32.5	48.0	30.5	47.5	36.6	49.:
BBH_penguins_in_a_table	99.3	99.3	100.0	95.2	95.2	99.3	100.0	98.3	98.
bbeh_buggy_tables	25.0	16.5	28.5	8.0	16.0	3.5	15.0	13.3	19.
BBH_movie_recommendation	70.0	70.0	100.0	63.6	97.6	65.2	100.0	67.2	99.
bbeh_movie_recommendation	59.5	40.0	79.0	28.5	56.5	22.5	47.5	37.6	61.
BBH_sports_understanding	81.6	80.4	100.0	77.2	99.6	80.0	100.0	79.8	99.
bbeh_sportqa	53.0	15.0	23.0	17.0	34.0	17.5	34.5	25.6	30.
gsm8k MATH	96.4	96.7	99.9 99.4	93.2	98.8	94.5	99.5 99.0	95.2 86.9	99. 95.
MATH BBH_multistep_arithmetic_two	96.5 100.0	93.1 100.0	100.0	70.7 100.0	88.3 100.0	87.1 99.6	99.0 99.6	86.9 99.9	95 99
bbeh_multistep_arithmetic	53.0	38.0	40.5	20.5	29.5	22.7	32.8	33.6	34.
BBH_object_counting	100.0	100.0	100.0	98.8	99.6	98.4	99.6	99.3	99.
bbeh_object_counting	58.0	31.0	85.5	40.5	71.0	22.5	61.0	38.0	72.
BBH_reasoning_about_colored_objects	100.0	98.8	100.0	95.6	99.2	94.4	99.2	97.2	99.:
bbeh_object_properties	31.5	5.5	7.0	17.5	29.5	39.0	51.5	23.4	29.1

Table 4: QwQ-32B Full Result.

<b>D</b> ( )	Text		PoT		<b>Z</b> 3		CSP		AVG
Dataset	ACC	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rat
Average	66.7	63.5	91.5	54.5	87.4	52.8	84.0	59.4	87.
FOLIO	92.5	88.1	100.0	73.9	88.8	67.2	98.5	80.4	95.
ProntoQA	100.0	95.8	100.0	80.2	99.8	93.2	99.4	92.3	99.
logicbenchBQA	72.3	70.5	99.8	76.3	100.0	63.3	99.8	70.6	99.
BoardgameQA	59.7	66.0	100.0	63.5	97.9	60.2	98.1	62.4	98.
ARLSAT BBH_boolean_expressions	40.9 99.6	50.4 100.0	90.4 100.0	59.1 89.2	83.0 100.0	67.8 76.4	85.2 96.4	54.6 91.3	86.1 98.1
bbeh_boolean_expressions	59.5	51.5	55.0	1.5	2.0	56.5	60.0	42.3	39.
BBH formal fallacies	88.4	76.4	100.0	90.4	100.0	62.0	99.6	79.3	99.
bbeh_zebra_puzzles	38.0	6.5	19.0	8.5	49.0	3.0	4.0	14.0	24.
BBH_logical_deduction_five_objects	93.2	94.0	99.6	87.6	99.6	96.4	100.0	92.8	99.
BBH_logical_deduction_seven_objects	88.8	88.0	100.0	84.8	100.0	96.8	100.0	89.6	100
BBH_logical_deduction_three_objects	99.2	95.2	100.0	92.8	99.2	99.6	100.0	96.7	99.
bbeh_boardgame_qa	37.0	35.5	90.5	37.5	90.0	24.5	65.0	33.6	81.
BBH_tracking_shuffled_objects_five_objects	98.4	100.0	100.0	82.0	100.0	36.8	81.2	79.3	93.
BBH_tracking_shuffled_objects_seven_objects	100.0	99.6	100.0	82.4	100.0	41.6	75.2	80.9	91.
BBH_tracking_shuffled_objects_three_objects	100.0	100.0	100.0	55.6	100.0	53.6	74.4	77.3	91.
bbeh_shuffled_objects	29.5 96.4	59.0 91.2	83.5	36.0	77.5 100.0	23.5 96.4	49.0	37.0 95.1	70. 100.
BBH_web_of_lies bbeh_web_of_lies	33.5	91.2 11.0	100.0 51.5	96.4 11.0	20.5	96.4	100.0 14.5	95.1 16.8	100 28
bAbI15	99.6	98.7	100.0	76.2	20.3 97.9	95.9	99.8	92.6	28 99
NeuLRdeductive	99.8	97.0	100.0	55.2	93.9	87.2	97.8	84.8	97
clutrr	52.7	44.2	100.0	44.6	95.7	35.6	84.4	44.3	93
bAbI16	51.8	93.4	100.0	64.4	98.8	44.1	100.0	63.4	99
NeuLRinductive	60.3	41.2	100.0	21.1	99.3	7.9	97.2	32.6	98
anli	88.8	87.6	100.0	73.4	99.9	81.6	100.0	82.9	100
AbductionRules	88.5	86.6	100.0	84.3	100.0	41.2	63.8	75.2	87
BBH_causal_judgement	69.0	73.8	100.0	61.0	100.0	64.7	100.0	67.1	100
bbeh_causal_understanding	52.0	52.5	100.0	50.0	99.0	44.5	96.5	49.8	98
NeuLRabductive	29.0	15.0	98.4	19.8	92.6	5.2	88.4	17.3	93
logicqa	76.0	73.2 82.0	99.6	61.7	97.8	72.7 84.4	98.6	70.9 82.7	98
BBH_date_understanding bbeh_time_arithmetic	94.0 63.5	43.5	100.0 74.0	70.4 36.0	98.8 66.0	35.0	100.0 73.5	82.7 44.5	99 71
BBH_temporal_sequences	99.6	89.2	99.6	64.4	98.0	98.0	99.6	87.8	99
bbeh_temporal_sequence	5.5	2.0	87.5	1.0	52.0	2.5	81.5	2.8	73
BBH_disambiguation_qa	53.6	50.0	100.0	38.0	100.0	36.8	100.0	44.6	100
bbeh_disambiguation_qa	63.3	54.2	98.3	44.2	96.7	70.8	93.3	58.1	96
BBH_hyperbaton	92.8	88.4	100.0	94.8	99.6	92.0	99.2	92.0	99
bbeh_hyperbaton	30.5	13.0	87.0	28.0	90.0	17.0	42.5	22.1	73
BBH_ruin_names	86.4	86.0	100.0	80.8	98.4	84.4	99.2	84.4	99
bbeh_nycc	21.5	11.5	77.5	3.5	39.0	7.0	79.0	10.9	65
BBH_salient_translation_error_detection	73.2	80.0	100.0	84.4	100.0	76.8	100.0	78.6	100
bbeh_linguini	35.0 89.9	25.5	97.0	23.0	92.0	20.0	73.0	25.9	87 100
BBH_snarks bbeh_sarc_triples	30.0	86.5 37.5	100.0 97.5	75.3 17.5	100.0 45.5	74.7 35.5	100.0 85.0	81.6 30.1	76
BBH_dyck_languages	90.4	94.4	100.0	75.2	98.8	35.2	76.0	73.8	91
bbeh_dyck_languages	17.5	6.5	86.5	7.5	96.0	10.0	88.0	10.4	90
BBH_word_sorting	97.6	99.2	100.0	41.2	94.0	71.6	84.0	77.4	92
bbeh_word_sorting	46.5	53.0	89.5	43.5	83.5	30.0	61.5	43.3	78
BBH_geometric_shapes	71.2	77.2	99.6	83.2	100.0	77.6	100.0	77.3	99
bbeh_geometric_shapes	38.5	16.0	65.0	35.0	80.5	33.5	69.5	30.8	71
BBH_navigate	99.2	98.0	100.0	78.4	100.0	74.4	98.0	87.5	99
bbeh_spatial_reasoning	11.5	19.0	81.0	13.5	80.5	14.5	72.0	14.6	77
BBH_penguins_in_a_table	98.6	100.0	100.0	96.6	99.3	82.2	97.3	94.4	98
bbeh_buggy_tables	21.0	19.0	49.5	16.5	54.0	19.5	40.0	19.0	47
BBH_movie_recommendation bbeh_movie_recommendation	77.2 60.5	63.6 26.0	100.0 99.5	67.2 34.0	99.2 85.0	76.8 27.5	99.6 85.0	71.2 37.0	99 89
BBH_sports_understanding	86.8	26.0 87.6	100.0	54.4	100.0	60.8	100.0	72.4	100
bbeh_sportqa	29.5	58.5	100.0	23.5	89.5	26.0	85.5	34.4	91
gsm8k	96.7	94.6	98.8	89.3	98.3	87.6	99.3	92.1	98
MATH	81.3	69.3	88.7	57.9	91.2	57.7	83.5	66.6	87
BBH_multistep_arithmetic_two	98.8	100.0	100.0	81.2	99.2	63.6	100.0	85.9	99
bbeh_multistep_arithmetic	27.0	1.5	23.0	1.0	13.5	1.0	16.0	7.6	17
BBH_object_counting	95.6	99.6	100.0	98.8	100.0	88.0	100.0	95.5	100
bbeh_object_counting	16.0	14.0	98.5	11.0	97.5	13.0	97.0	13.5	97
$BBH\_reasoning\_about\_colored\_objects$	97.6	97.6	100.0	94.4	98.8	89.2	99.6	94.7	99
bbeh_object_properties	10.5	5.5	50.5	9.5	52.5	1.0	38.5	6.6	47

Table 5: GPT-40 Full Result.

Poliset   ACC   ACC   Exer. Bate   ACC   Exer. Ba		Text		PoT		Z3		CSP		AVG
Protection   Pro	Dataset	ACC	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate
ProntoOA   94	Average	52.3	36.9	78.6	33.0	70.0	24.8	52.1	36.7	66.9
DegicementBOA   71.6   52.1   10.0   30.4   98.5   37.8   79.8   50.2	FOLIO	88.8	85.1	100.0	59.7	87.3	59.0	84.3	73.1	90.5
BBH   Decian expressions   97.6   99.6   100.0   45.2   11.3   8.7   22.6   22.2   BBH   Decian expressions   97.6   99.6   100.0   45.2   11.6   50.8   95.2   73.3   10.0   1	ProntoQA	99.4		98.6		87.6	38.4	54.8		80.3
ARI SAT*         25.2         36.5         93.0         22.2         13.1         8.7         22.6         23.2           BBH Donolean expressions         70.5         1.5         1.5         0.5         0.5         10.0         10.5         20.6         88.8         59.8         69.2         44.8         69.2         64.8         92.2         74.2         67.6         70.8         94.8         59.8         58.8         58.8         59.8         74.4         10.0         48.8         73.2         70.2         70.5         5.0         10.8         89.8         59.8         40.0         40.0         43.2         80.1         60.0         60.0         40.0         43.2         80.1         60.0         60.0         40.0         43.2         80.1         60.0         60.0         40.0         40.0         40.0         40.0 </td <td>9</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>92.8</td>	9									92.8
BBH, boolean expressions both-hobolean expressions both-hobolean expressions both-hobolean expressions both-polean expressions BBH logical deduction, five, objects BBH logical deduction, five, objects BBH logical deduction, three-objects BBH logical deduction, three-objects both-hoboardgame.qa 33.0 18.5 46.5 7.0 20.5 0.5 5.0 14.8 BBH tracking, shuffled objects, seven objects BBH tracking, shuffled objects, seven objects BBH tracking, shuffled objects, seven objects BBH tracking, shuffled objects, three objects BBH tracking, shuffled objects, three objects BBH, tracking, shuffled objects, three objects BBH, who of lies	3 2									87.5
bheh.   bookean expressions   70.5   1.5   1.5   0.5   0.5   10.0   10.5   20.6     BBH.   formal, fallacies   69.6   50.8   30.5   3.5   5.0   20.5   0.0   0.0   10.0     BBH.   beh. zebra, puzzles   34.5   0.5   3.5   5.0   20.5   0.0   0.0   10.0     BBH.   logical deduction, five, objects   68   56.0   10.0   47.2   67.6   70.8   94.8   59.8     BBH.   logical deduction, seven objects   50.0   57.2   100.0   47.2   67.6   70.8   94.8   59.8     BBH.   tracking, shuffled, objects, five, objects   84.8   36.8   100.0   47.2   67.6   70.8   20.5   10.5   10.8     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   43.2   82.0   15.6   68.4   37.3     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   35.6   76.4   22.0   56.4   37.3     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   35.6   76.4   22.0   56.4   36.8     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   35.6   76.4   22.0   56.4   36.8     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   76.4   94.4   66.8   76.3   36.8     BBH.   tracking, shuffled, objects, five, objects   85.2   5.2   100.0   76.4   94.4   66.8   76.3   36.8     BBH.   tracking, shuffled, objects, five, objects   85.2   95.2   100.0   76.4   94.4   66.8   76.3   36.8     BBH.   tracking, shuffled, objects, five, objects   85.2   95.2   100.0   76.4   94.4   66.8   76.8   76.8     BBH.   tracking, shuffled, objects, five, objects   85.2   95.2   100.0   76.4   94.4   66.8   76.8   76.8     BBH.   tracking, shuffled, objects, five, objects   85.2   85.2   10.0   85.5   85.8     BBH.   tracking, shuffled, objects, five, objects   85.2   95.2   10.0   95.5   10.5   40.0   16.8     BBH.   tracking, shuffled, objects, five, objects   85.2   95.2   10.0   95.5   10.5   40.0   16.8     BBH.   tracking, shuffled, objects, five, objects, shuffled, objects, five, objects, shuffled, objects, five, objects, shuffled, objects, five, objects, shuffled, objects, five, objects										55.9
BBH   formal fallacies										88.9 4.2
BBH   logical deduction five objects   66.0   55.2   100.0   47.2   67.6   70.8   94.8   95.2   86.8										93.3
BBH   logical   deduction free, objects   66.8   55.0   100.0   46.8   69.2   64.8   95.2   85.8   BBH   logical   deduction   three   objects   80.6   74.4   100.0   48.8   70.2   72.4   72.4   72.6   70.8   94.8   59.8   BBH   logical   deduction   three   objects   80.6   74.4   100.0   48.8   70.2   72.4										8.0
BBH Logical deduction seven objects         60.0         55.2         100.0         47.2         67.6         70.8         94.8         79.8           BBB Logical deduction three objects         89.6         74.4         100.0         48.8         73.2         72.4         92.4         71.3           BBH Lracking shuffled objects five objects         88.2         3.0         100.0         34.8         82.0         15.6         68.4         37.3           BBH Lracking shuffled objects, seven objects         89.2         0.4         100.0         35.6         76.4         22.0         58.4         36.8           BBH Lracking shuffled objects, seven objects         89.2         0.4         100.0         35.6         60.4         37.3           BBH Lyeb, objects, seven objects         89.2         0.4         100.0         35.6         60.4         10.1         60.0         66.8         47.8         11.0         66.0         74.0         16.0         68.4         37.3         68.0         61.1         90.0         40.0         10.0         60.0         60.5         35.3         6         60.0         74.0         88.1         96.5         20.4         77.0         77.7         48.8         96.5         10.1         14.4<	= -*									88.
BBH_tracking_shuffled_objects_five_objects   84.8   36.0   10.00   34.8   82.0   16.8   63.6   55.0   18.8	_ 2	66.0	55.2		47.2	67.6	70.8	94.8		87.:
BBHL tracking_shuffled_objects_seven_objects   84.8   3.6   100.0   34.8   82.0   16.8   63.6   35.5   BBHL tracking_shuffled_objects_seven_objects   82.2   5.2   100.0   35.6   76.4   22.0   58.4   36.8   BBHL tracking_shuffled_objects   89.5   4.0   100.0   35.6   76.4   22.0   58.4   36.8   BBHL tracking_shuffled_objects   89.5   4.0   100.0   35.6   76.4   22.0   58.4   36.8   BBHL web_of_lies   89.5   4.0   100.0   78.4   94.4   66.8   77.8   71.4   10.4   10.5   10.5   10.5   3.5   3.6   10.4   10.5   10.5   10.5   3.5   3.6   10.4   10.5   10.5   10.5   3.5   3.6   10.4   10.5   10.5   10.5   10.5   10.5   3.5   3.6   10.4   10.4   10.5	BBH_logical_deduction_three_objects	89.6	74.4	100.0	48.8	73.2	72.4	92.4	71.3	88
BBH tracking shuffled objects even objects   S2   52   100   43.2   82.0   15.6   68.4   37.3   BBH tracking shuffled objects   S9.2   0.4   100.0   35.6   76.4   22.0   58.4   36.8   BBH tracking shuffled objects   S9.2   0.4   100.0   78.4   94.4   66.8   74.8   71.4   16.8   BBH_web_of_lies   S1.2   59.2   100.0   78.4   94.4   66.8   74.8   71.4   16.8   16.	bbeh_boardgame_qa	33.0	18.5	46.5		20.5	0.5	5.0		24.0
BBH tracking shuffled objects three objects   892   0.4   100.0   35.6   76.4   22.0   58.4   36.8   10.6   10.5	_									81.9
bibeh_shuffled_objects										83.:
BBH_web_of_lies										78
bbeh_web_of_lies   9.0										14.
NeulRedeductive										89.' 7.:
NeuLRedeuctive clutrr         91,9 bol.4 bol.16 clutrr         96,5 bol.2 bol.4 bol.16 clutrr         77,0 bol.4 bol.16 clutrr         17,7 bol.4 bol.16 clutrr         23,7 bol.8 bol.16 clutrr         23,7 bol.8 bol.16 clutrr         28,8 bol.5 bol.6 clutre bol.1 bol.1 bol.1 lot.4 lot.										7 84.
Celutr										71.
NeuLRinductive										80.9
anli         77,7         78.8         99.8         59.8         95.1         55.6         83.7         68.0           AbductionRules         88.3         50.6         81.4         34.8         41.8         23.9         70.0         49.4           BBH_causal_judgement         51.9         54.0         100.0         37.4         92.5         40.6         85.6         46.0           bbeh_causal_understanding         48.0         39.0         98.0         26.5         82.0         26.5         69.0         34.3           NeuLRabductive         20.8         12.9         83.5         22.0         52.5         82.2         21.6         16.0           logicqa         68.2         64.8         98.2         54.9         95.9         40.8         82.5         57.2           BBH_date_understanding         48.8         32.0         100.0         33.6         73.6         38.4         48.8         47.2           bbeh_time arithmetic         30.5         30.3         32.0         90.0         52.5         10.5         46.0         13.3           BBH_time permatecquence         83.6         67.2         100.0         34.5         0.0         15.5         12.0										85.0
AbductionRules         88.3         50.6         81.4         34.8         41.8         23.9         37.0         49.4           BBH_causal_judgement         51.9         54.0         100.0         37.4         92.5         40.6         85.6         46.0           bbeh_causal_undgerstanding         45.0         39.0         98.0         26.5         82.0         26.5         69.0         34.3           Neul.Rabductive         20.8         12.9         83.5         22.0         52.5         8.2         21.6         16.0           BBH_disal         20.0         100.0         33.6         73.6         38.4         84.8         47.2           bbeh_time arithmetic         30.5         3.0         32.0         9.0         52.5         10.5         40.0         13.3           BBH_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         5.0         1.3           bbeh_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_disambiguation_qa         45.8         29.2         90.0         35.8         81.7         15.8         44.2         31.5 </td <td>NeuLRinductive</td> <td>7.4</td> <td>8.8</td> <td>96.5</td> <td>16.1</td> <td>91.1</td> <td>14.4</td> <td>53.3</td> <td>11.7</td> <td>80.</td>	NeuLRinductive	7.4	8.8	96.5	16.1	91.1	14.4	53.3	11.7	80.
BBH_causal_judgement         51.9         54.0         100.0         37.4         92.5         40.6         85.6         46.0           bbeh_causal_understanding         45.0         39.0         98.0         26.5         82.0         21.6         60.0         34.3           Neul_Rabductive         20.8         12.9         83.5         22.0         52.5         8.2         21.6         16.0           BBH_date_understanding         84.8         32.0         100.0         33.6         73.6         38.4         84.8         87.2           bbeh_time_arithmetic         30.5         30.0         32.0         90.0         52.5         10.5         46.0         13.3           BBH_temporal_sequences         83.6         67.2         100.0         48.4         85.6         54.0         72.8         63.3           bbeh_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         50.1         13.3           BBH_disambiguation_qa         44.8         29.2         90.0         35.8         81.7         15.8         44.2         31.7           BBH_b_thyperbaton         68.0         70.0         100.0         35.6         94.0         70.0 <td>anli</td> <td>77.7</td> <td>78.8</td> <td>99.8</td> <td>59.8</td> <td>95.1</td> <td>55.6</td> <td>83.7</td> <td>68.0</td> <td>92.</td>	anli	77.7	78.8	99.8	59.8	95.1	55.6	83.7	68.0	92.
bbeh_causal_understanding         45.0         39.0         98.0         26.5         82.0         26.5         69.0         34.3           NeuLRabductive         20.8         12.9         83.5         22.0         52.5         8.2         21.6         16.0           logicqa         68.2         64.8         98.2         54.9         95.9         40.8         82.5         57.2           BBH_del understanding         84.8         32.0         100.0         33.6         73.6         38.4         84.8         47.2           bbeh_time_arithmetic         30.5         30.0         32.0         90.0         52.5         10.5         46.0         13.3           BBH_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         50.1         1.3           BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           BBH_hyperbaton         0.5         1.5         29.0         35.8         81.7         15.8         44.2         31.7           BBH_phyperbaton         0.5         1.5         94.0         7.0         0.0         0.5         0.8	AbductionRules	88.3		81.4		41.8	23.9	37.0	49.4	53.
NeuLRabductive logicqa (object)         68.2 (64.8)         83.5 (54.9)         52.5 (8.2)         8.2 (16.8)         16.0 (object)           BBH date_understanding         84.8 (32.0)         100.00 (33.6)         73.6 (38.4)         84.8 (47.2)         74.2 (46.0)         13.3 (38.4)         84.8 (47.2)         84.8 (32.0)         100.00 (33.6)         73.6 (38.4)         84.8 (47.2)         83.6 (72.2)         100.0 (33.6)         73.6 (38.4)         84.8 (47.2)         84.8 (47.2)         84.8 (32.0)         100.0 (33.6)         73.6 (38.4)         84.8 (47.2)         84.8 (37.2)         90.0 (37.2)         52.5 (10.5)         46.0 (13.3)         13.3 (38.4)         84.8 (47.2)         84.8 (47.2)         84.1 (38.4)         85.6 (54.0)         72.8 (63.3)         84.1 (38.4)         85.6 (54.0)         72.8 (63.3)         84.1 (38.4)         84.8 (33.3)         84.2 (30.4)         84.1 (38.4)         84.8 (33.3)         84.2 (30.4)         85.0 (33.3)         84.2 (30.4)         83.2 (30.4)         83.6 (37.2)         88.0 (37.2)         88.0 (37.2)         88.0 (37.2)         89.0 (37.2)         93.6 (37.2)         88.0 (37.2)         88.0 (37.2)         88.0 (37.2)         88.0 (37.2)         88.0 (37.2)         88.0 (37.2)         89.0 (37.2)         89.0 (37.2)         89.0 (37.2)         89.0 (37.2)         89.0 (37.2)         89.0 (37.2)         89.0 (37.2)										92.
BBH_date_understanding										83.
BBH_date_understanding         84.8         32.0         100.0         33.6         73.6         38.4         84.8         47.2           bbeh_time_arithmetic         30.5         3.0         32.0         9.0         52.5         10.5         46.0         13.3           BBH_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         5.0         1.3           BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_disambiguation_qa         45.8         29.2         90.0         35.8         81.7         15.8         44.2         31.7           BBH_hyperbaton         68.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_hyperbaton         0.5         1.5         22.0         1.0         27.0         0.0         0.5         6.0           BBH_ruin_ames         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_lycc         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6										52
bbeh_time_arithmetic         30.5         3.0         32.0         9.0         52.5         10.5         46.0         13.3           BBH_temporal_sequences         83.6         67.2         100.0         48.4         85.6         54.0         72.8         63.3           bbeh_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         55.6         54.0         75.0         13.3           BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_lisperbaton         68.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_nyerbaton         0.5         1.5         22.0         1.0         27.0         0.0         0.5         0.8           BBH_ruin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_nycc         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.	© <b>1</b>									92 86.
BBH_temporal_sequence         83.6         67.2         100.0         48.4         85.6         54.0         72.8         63.3           bbeh_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         5.0         1.3           BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_lyperbaton         68.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_nyce         10.5         15.5         22.0         1.0         29.7         0.0         0.5         0.8           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         600.2         27.3           bbeh_inycini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_salient_translation_error_detection         47.2         10.0         80.0         30.4         58.0         21.6         600.2         27.3           bbeh_singuini         18.0         16.0         21.5         100.0         49.2         49.2<	_									43.
bbeh_temporal_sequence         5.0         0.0         34.5         0.0         41.5         0.0         5.0         1.3           BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_disambiguation_qa         45.8         29.2         90.0         35.8         81.7         15.8         44.2         31.7           BBH_prepriation         66.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_hyperbation         0.5         1.5         22.0         1.0         27.0         0.0         0.5         0.8           BBH_ruin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_sizer_triples         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           BBH_salient_translation_error_detection         47.2         10.0         40.0         74.5         5.5         <										86.
BBH_disambiguation_qa         41.2         59.2         100.0         37.2         93.6         37.2         88.0         43.7           bbeh_disambiguation_qa         45.8         29.2         90.0         35.8         81.7         15.8         44.2         31.7           BBH_hyperbaton         68.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_hyperbaton         0.5         1.5         22.0         1.0         27.0         0.0         0.5         0.8           BBH_ruin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_nyce         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_salient_translation_         77.5         31.5         110.0         49.4         97.2         41.0         84.8<										27.0
BBH_hyperbaton         68.0         70.0         100.0         53.6         94.4         32.4         57.6         56.0           bbeh_byperbaton         0.5         1.5         22.0         1.0         27.0         0.0         0.5         0.8           BBH_ruin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_bh_nycc         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salien_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           BBH_salien_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_dinguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_salien_trinslation_error_detection         47.2         10.0         49.4         97.2         41.0         84.8         49.9           bbeh_gate_dyk_languages         45.5         15.2         20.0         49.4         97.2         41.0	- · - ·	41.2	59.2	100.0	37.2	93.6	37.2	88.0	43.7	93.9
bbeh_hyperbaton         0.5         1.5         22.0         1.0         27.0         0.0         0.5         0.8           BBH_urin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_sarc_triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         22.5         11.5           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4	bbeh_disambiguation_qa	45.8		90.0	35.8	81.7	15.8	44.2	31.7	71.9
BBH_ruin_names         53.2         36.0         100.0         28.4         82.8         10.4         39.2         32.0           bbeh_nyce         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salien_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         22.5         11.5           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         <										84.
bbeh_nyce         10.5         8.5         94.0         7.0         59.0         4.5         41.5         7.6           BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_sarc_triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         22.0         11.5           BBH_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2										16.
BBH_salient_translation_error_detection         47.2         10.0         100.0         30.4         58.0         21.6         60.0         27.3           bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_sarc_triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         29.6         50.8										74.
bbeh_linguini         18.0         16.0         81.5         6.0         73.5         4.5         52.0         11.1           BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_sarc triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_spontial_reasoning         6.0         1.5         22.5         40         49.6         50.8         51.9      <	= 2									64. 72.
BBH_snarks         77.5         31.5         100.0         49.4         97.2         41.0         84.8         49.9           bbeh_sarc_triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbel_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8 <th< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></th<>										
bbeh_sare_triples         16.0         12.5         91.5         12.0         74.5         5.5         22.5         11.5           BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0										69. 94.
BBH_dyck_languages         83.2         39.2         100.0         24.8         76.8         14.8         40.0         40.5           bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6 <td><del>-</del></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>62.</td>	<del>-</del>									62.
bbeh_dyck_languages         4.5         1.5         26.0         8.0         57.5         0.5         26.0         3.6           BBH_word_sorting         32.4         97.2         100.0         61.2         86.0         6.0         32.4         49.2           bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0										72.
bbeh_word_sorting         21.0         10.0         58.5         23.0         76.0         10.5         27.5         16.1           BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         <	- • - 0 0									36.
BBH_geometric_shapes         62.0         80.4         100.0         48.4         86.0         55.2         89.2         61.5           bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4		32.4	97.2	100.0	61.2	86.0	6.0	32.4	49.2	72.
bbeh_geometric_shapes         28.5         19.5         53.5         30.0         98.5         30.0         65.0         27.0           BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0 <th< td=""><td></td><td></td><td></td><td></td><td></td><td>76.0</td><td></td><td></td><td></td><td>54.</td></th<>						76.0				54.
BBH_navigate         84.0         50.4         100.0         43.6         86.0         29.6         50.8         51.9           bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3										91.
bbeh_spatial_reasoning         6.0         1.5         22.0         4.0         27.5         4.0         19.0         3.9           BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         4	-									72.
BBH_penguins_in_a_table         91.1         56.2         100.0         63.0         78.8         24.7         48.6         58.7           bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0	_ 0									78.
bbeh_buggy_tables         32.5         0.0         6.0         0.5         5.5         0.0         2.0         8.3           BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0	-									22.
BBH_movie_recommendation         63.2         42.0         100.0         28.8         72.4         10.0         42.0         36.0           bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>75.</td>										75.
bbeh_movie_recommendation         33.0         23.5         83.5         26.5         84.0         3.5         16.0         21.6           BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0	_ 66.									4. 71.
BBH_sports_understanding         74.0         58.0         100.0         55.6         99.2         48.4         95.6         59.0           bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6										61.
bbeh_sportqa         17.0         35.0         82.0         19.5         59.5         4.0         17.5         18.9           gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6										98.
gsm8k         93.0         17.1         21.3         81.1         96.5         58.9         81.3         62.5           MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6										53
MATH         76.7         42.3         100.0         40.7         74.7         39.9         71.1         49.9           BBH_multistep_arithmetic_two         94.0         98.8         100.0         98.4         99.6         48.4         82.0         84.9           bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6										66.
bbeh_multistep_arithmetic         6.5         0.0         0.0         0.5         7.0         0.0         3.0         1.8           BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6										81.
BBH_object_counting         56.0         82.8         100.0         86.4         95.6         48.8         71.2         68.5           bbeh_object_counting         18.0         0.0         25.5         0.0         63.0         0.5         31.0         4.6		94.0	98.8	100.0	98.4	99.6	48.4	82.0	84.9	93.
<b>bbeh_object_counting</b> 18.0 0.0 25.5 0.0 63.0 0.5 31.0 4.6	_ •									3.
										88.
<b>BBH_reasoning_about_colored_objects</b> 79.6 54.8 100.0 68.4 84.4 46.0 71.6 62.2	_ U _ U									39.
bbeh object properties 21.0 0.5 25.0 2.0 37.0 0.0 22.5 5.9	_									85.i 28.i

Table 6: Qwen2.5-7B Full Result.

<b>-</b> .	Text		PoT		<b>Z</b> 3		CSP	AVG	
Dataset	ACC	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate	ACC	Exec_Rate
Average	52.7	43.9	83.5	34.8	76.5	37.0	68.1	42.1	76.0
FOLIO	83.6	78.4	99.3	71.6	100.0	61.2	97.8	73.7	99.0
ProntoQA	99.0	84.8	99.4	54.6	90.2	81.2	93.8	79.9	94.5
logicbenchBQA	80.1 68.8	70.4 50.0	100.0	72.3 50.9	99.1 97.8	64.2 46.5	99.6 92.3	71.8 54.1	99.0
BoardgameQA ARLSAT	23.9	31.7	94.9 85.7	30.9	97.8 68.7	30.0	61.3	29.1	95.0 71.9
BBH boolean expressions	96.8	98.8	100.0	42.0	74.8	64.4	99.2	75.5	91.
bbeh_boolean_expressions	70.0	0.0	53.0	3.0	4.0	22.5	33.0	23.9	30.
BBH_formal_fallacies	68.0	58.4	100.0	61.2	100.0	54.8	98.0	60.6	99.
bbeh_zebra_puzzles	39.0	12.5	46.5	13.5	39.5	8.0	22.0	18.3	36.
BBH_logical_deduction_five_objects	61.6 50.4	57.6 44.0	100.0 100.0	62.8 57.2	94.0 99.6	77.6 70.0	96.8 83.6	64.9 55.4	96. 94.
BBH_logical_deduction_seven_objects BBH_logical_deduction_three_objects	84.8	75.6	100.0	74.8	99.6	92.0	94.8	81.8	94. 95.
bbeh_boardgame_qa	31.5	0.0	84.5	12.5	37.0	18.0	46.0	15.5	55.
BBH_tracking_shuffled_objects_five_objects	78.8	100.0	100.0	2.4	99.2	4.4	28.0	46.4	75.
BBH_tracking_shuffled_objects_seven_objects	71.2	100.0	100.0	2.4	100.0	2.4	22.8	44.0	74.
BBH_tracking_shuffled_objects_three_objects	80.8	99.6	100.0	8.0	100.0	5.2	16.8	48.4	72.
bbeh_shuffled_objects	42.0	6.0	19.5	9.5	23.0	10.5	23.0	17.0	21.
BBH_web_of_lies	85.6 12.5	63.2 13.0	100.0 51.5	77.2 1.0	100.0 9.5	58.0 2.5	64.0 7.0	71.0 7.3	88 22
bbeh_web_of_lies bAbI15	99.1	96.1	97.3	89.6	9.5 99.1	2.5 89.2	7.0 98.5	93.5	98
NeuLRdeductive	92.1	85.7	99.0	37.1	84.9	49.8	86.7	66.2	90
clutrr	46.8	30.3	99.9	34.4	99.5	46.0	99.8	39.4	99
bAbI16	93.0	96.7	100.0	78.4	99.6	83.9	100.0	88.0	99
NeuLRinductive	8.2	8.6	100.0	18.0	98.6	14.1	93.8	12.2	97
anli	84.1	76.7	100.0	69.7	100.0	80.3	99.9	77.7	100
AbductionRules BBH_causal_judgement	91.0 55.1	85.7 61.5	99.8 100.0	47.7 55.6	95.0 100.0	48.3 49.7	81.1 100.0	68.2 55.5	92 100
bbeh_causal_understanding	42.5	0.0	87.0	43.0	96.5	40.0	95.5	31.4	93
NeuLRabductive	12.0	15.4	93.8	17.3	84.3	1.0	27.4	11.4	68
logicqa	63.8	53.8	99.5	42.4	98.9	45.1	97.1	51.3	98
BBH_date_understanding	74.0	54.4	100.0	40.4	97.2	55.6	96.8	56.1	98
bbeh_time_arithmetic	32.0	10.5	59.5	7.5	43.5	10.5	45.5	15.1	49
BBH_temporal_sequences	30.0	42.8	98.8	33.6	98.4	36.0	76.0	35.6	91
bbeh_temporal_sequence BBH_disambiguation_qa	9.0 35.6	0.0 46.0	42.5 100.0	0.0 41.2	20.0 99.2	0.0 64.0	30.5 99.2	2.3 46.7	31 99
bbeh disambiguation qa	42.5	0.0	43.3	34.2	90.0	61.7	100.0	34.6	77
BBH_hyperbaton	72.0	66.8	91.2	66.4	100.0	82.0	96.8	71.8	96
bbeh_hyperbaton	1.0	0.0	64.0	3.0	33.5	2.0	18.0	1.5	38
BBH_ruin_names	37.2	32.4	100.0	28.0	98.8	39.6	94.4	34.3	97
bbeh_nycc	8.0	0.0	62.5	1.5	95.5	5.0	72.5	3.6	76
BBH_salient_translation_error_detection	44.4	27.6	100.0	38.4	99.6	26.8	100.0	34.3	99
bbeh_linguini BBH_snarks	18.0 73.6	0.0 50.6	53.5 100.0	2.5 51.1	79.0 98.9	10.5 41.6	63.0 100.0	7.8 54.2	65 99
bbeh_sarc_triples	16.5	12.0	96.5	16.5	43.0	34.0	100.0	19.8	79
BBH_dyck_languages	64.4	38.8	97.6	14.4	96.8	3.2	31.2	30.2	75
bbeh_dyck_languages	2.5	0.0	24.5	4.5	47.0	0.5	18.0	1.9	29
BBH_word_sorting	20.8	96.4	100.0	25.2	86.8	4.4	31.6	36.7	72
bbeh_word_sorting	20.5	12.5	73.5	6.5	84.5	1.5	15.0 99.2	10.3 39.3	57 99
BBH_geometric_shapes bbeh_geometric_shapes	53.6 20.0	13.6 1.5	100.0 68.5	29.2 17.0	99.2 58.5	60.8 42.5	73.0	20.3	66
BBH_navigate	88.8	75.2	96.0	65.2	94.0	55.2	97.2	71.1	95
bbeh_spatial_reasoning	7.5	9.5	41.5	7.5	32.0	3.5	21.5	7.0	31
BBH_penguins_in_a_table	84.3	98.0	100.0	82.2	98.6	50.7	85.6	78.8	94
bbeh_buggy_tables	86.5	0.0	28.0	1.0	13.5	0.0	7.0	21.9	16
BBH_movie_recommendation	75.2	47.2	99.2	21.2	90.0	70.8	100.0	53.6	96
bbeh_movie_recommendation BBH_sports_understanding	49.0 73.6	0.0 56.0	52.5 99.2	11.0 62.8	71.0 100.0	9.0 53.6	74.5 99.2	17.3 61.5	66 99
bbeh_sportqa	73.6 11.5	42.5	99.2 87.5	4.0	100.0	3.0	11.5	15.3	37
gsm8k	90.6	89.2	100.0	74.8	99.0	60.0	95.4	78.6	98
MATH	71.6	60.8	92.3	33.1	68.5	36.4	85.6	50.5	82
BBH_multistep_arithmetic_two	96.4	98.0	100.0	95.2	100.0	85.2	100.0	93.7	100
bbeh_multistep_arithmetic	10.5	0.0	60.5	0.0	2.0	0.0	7.0	2.6	23
BBH_object_counting	41.2	72.8	100.0	76.0	91.2	53.6	88.8	60.9	93
bbeh_object_counting	16.5 71.6	0.0 87.2	41.5 100.0	0.0 60.4	19.5 96.0	0.0 59.2	5.5 90.8	4.1 69.6	22 95
BBH_reasoning_about_colored_objects									

Table 7: Qwen2.5-7B-Base.w.Formal Full result.

# **Prompt for PoT**

{question}

Let's write a **Python** program to solve the problem. Please give the python code in the following format:

```python

and print the final result.

Figure 11: Prompt for PoT

# **Prompt for Z3**

{question}

Let's write code in Python that utilizes **z3-solver** to solve the problem.

Requires code to start with:

"from z3 import \*".

Please give the python code in the following format:

```python

and print the final result.",

Figure 12: Prompt for Z3

# **Prompt for CSP**

{question}

Let's write code in Python that utilizes **python-constraint** to solve the question. The task is to parse the problem as a constraint satisfaction problem, defining the domain, variables, and contraints. Requires code to start with: 'from constraint import \* problem = Problem()'.

Please give the python code in the following format:

"python\n" and print the final result.

Figure 13: Prompt for CSP

# **Prompt for Model Evaluation**

[Instruction]

Please act as an impartial judge and evaluate the quality of the response provided by an Al assistant to the user question displayed below. Your evaluation should consider the correctness. You will be given a reference answer and the assistant's answer. Begin your evaluation by comparing the assistant's answer with the reference answer, you must identify whether the response is correct or wrong by strictly following this format: "<correct or wrong>", for example: "<correct>" or "<wrong>".

[Question] {question}

{completion}

[The Start of Reference Answer] {answer}
[The End of Reference Answer]

[The Start of Assistant's Answer]

[The End of Assistant's Answer]

Figure 14: Prompt for Model Eval