## One hole: d9 sector

Each symbol denotes a block of states; U denotes int matrix

	$d_{\uparrow}^{9}$	$d_{\uparrow\downarrow}^8 s_{\uparrow}$	$d_{\uparrow\uparrow}^8 s_{\downarrow}$	$d_{\downarrow}^{9}$	$d_{\downarrow\downarrow}^8 s_{\uparrow}$	$d_{\downarrow\uparrow}^8 s_{\downarrow}$
$d_{\uparrow}^{9}$	$\epsilon_d$	$t_{ds}$	$t_{ds}$	0	0	0
$d_{\uparrow\downarrow}^8 s_{\uparrow}$		$2\epsilon_d$ +U	U?	0	0?	0?
$d_{\uparrow\uparrow}^8 s_{\downarrow}$			$2\epsilon_d$ +U	0	0?	0?
$\frac{d_{\downarrow}^{9}}{d_{\downarrow\downarrow}^{8}s_{\uparrow}}$ $d_{\downarrow\uparrow}^{8}s_{\downarrow}$	Above red U matrix is only finite between two triplet d8 states: S=Sz=1? All 1A, 1B, 1E symmetry channels are zero?			$\epsilon_d$	$t_{ds}$ $2\epsilon_d$ +U $2\epsilon_d$	$t_{ds}$ $U$ ? $2\epsilon_d$ +U

## One hole

The complete VS consists of  $d_{\uparrow}^9$ ,  $d_{\downarrow}^9$ ,  $L_{\uparrow}$ ,  $L_{\downarrow}$  sectors

To reduce VS, can consider only  $d_{\uparrow}^9$  sector and skip  $d_{\downarrow}^9$  (previous slide);

Similarly, only need keep  $L_{\uparrow}$  sector because  $L_{\downarrow}$  does not connect with neither  $L_{\uparrow}$  nor  $d_{\uparrow}^9$  sectors So only 6 states below:

$$d_{\uparrow}^{9}$$
  $d_{\uparrow\downarrow}^{8}s_{\uparrow}$   $d_{\uparrow\uparrow}^{8}s_{\downarrow}$   $L_{\uparrow}$   $d_{\downarrow}^{9}L_{\uparrow}s_{\uparrow}$   $d_{\uparrow}^{9}L_{\uparrow}s_{\downarrow}$ 

## Two hole (only d9L sector leading to d8)

	$d_{\uparrow}^{9}L_{\sigma} d_{\uparrow\downarrow}^{8}L_{\sigma}s_{\uparrow}$	$d_{\uparrow\uparrow}^{8}L_{\sigma}s_{\downarrow}$	$d_{\downarrow}^{9}L_{\sigma}$	$d_{\downarrow\downarrow}^{8}L_{\sigma}s_{\uparrow}$	$d_{\downarrow\uparrow}^{8}L_{\sigma}s_{\downarrow}$
$d_{\uparrow}^{9}L_{\sigma}$	$\epsilon_{d,p}$ $t_{ds}$	$t_{ds}$	0	0	0
$d_{\uparrow\downarrow}^8 L_{\sigma} s_{\uparrow}$	$2\epsilon_d$ +U	U?	0	0?	0?
$d_{\uparrow\uparrow}^{8}L_{\sigma}s_{\downarrow}$		$2\epsilon_d$ +U	0	0?	0?
$d_{\downarrow}^{9}L_{\sigma}$	So above red U only finite bet	$\epsilon_{d,p}$	$t_{ds}$	$t_{ds}$	
$d_{\downarrow\downarrow}^8 L_\sigma s_\uparrow$	triplet states: All 1A, 1B, 1E		$2\epsilon_d$ +U	U?	
$d_{\downarrow\uparrow}^8 L_{\sigma} s_{\downarrow}$	channels ar	$2\epsilon_d$ +U			

## Two hole

The complete VS consists of  $d_{\sigma\sigma'}^8$   $d_{\sigma}^9 L_{\sigma'}$   $d^{10} L_{\sigma\sigma'}$  sectors

To reduce VS, can consider only  $d_{\uparrow}^9 L_{\sigma}$  sector and skip  $d_{\downarrow}^9 L_{\sigma}$ ; Hence, only need to keep  $d_{\uparrow\sigma}^8$  and  $d^{10} L_{\uparrow\sigma}$  sectors connecting with  $d_{\uparrow}^9 L_{\sigma}$ ;

So reduced VS has only states below:

$$\begin{array}{ccc} d_{\uparrow}^9L_{\sigma} & d_{\uparrow\downarrow}^8L_{\sigma}s_{\uparrow} & d_{\uparrow\uparrow}^8L_{\sigma}s_{\downarrow} \\ d_{\uparrow\sigma}^8 & & & \\ d^{10}L_{\uparrow\sigma} & d_{\downarrow}^9L_{\uparrow\sigma}s_{\uparrow} & d_{\uparrow}^9L_{\uparrow\sigma}s_{\downarrow} \end{array}$$
 Only need to consider  $\sigma=\uparrow$ ?