

Constraint Reasoning Embedded Structural Prediction



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Example: Vehicle Dispatch Planning

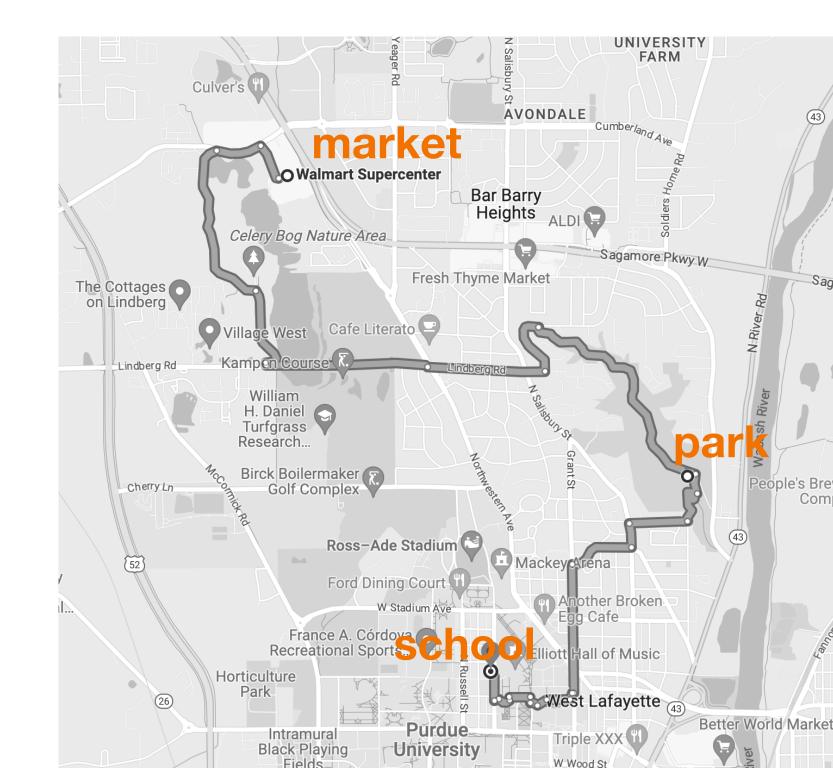
Task: Recommend dispatching routes that

- satisfy daily delivery requests;
- meet drivers' implicit preferences.

Input: a set of locations. {market, park, school}

Output: a visiting order of locations.

market \rightarrow park \rightarrow school.



A pure Learning algorithm

market1 → market2 → market3 × Not a valid route

A pure Reasoning algorithm (like a Traveling Salesman Problem solver)

school → market → park

The driver does not like it.

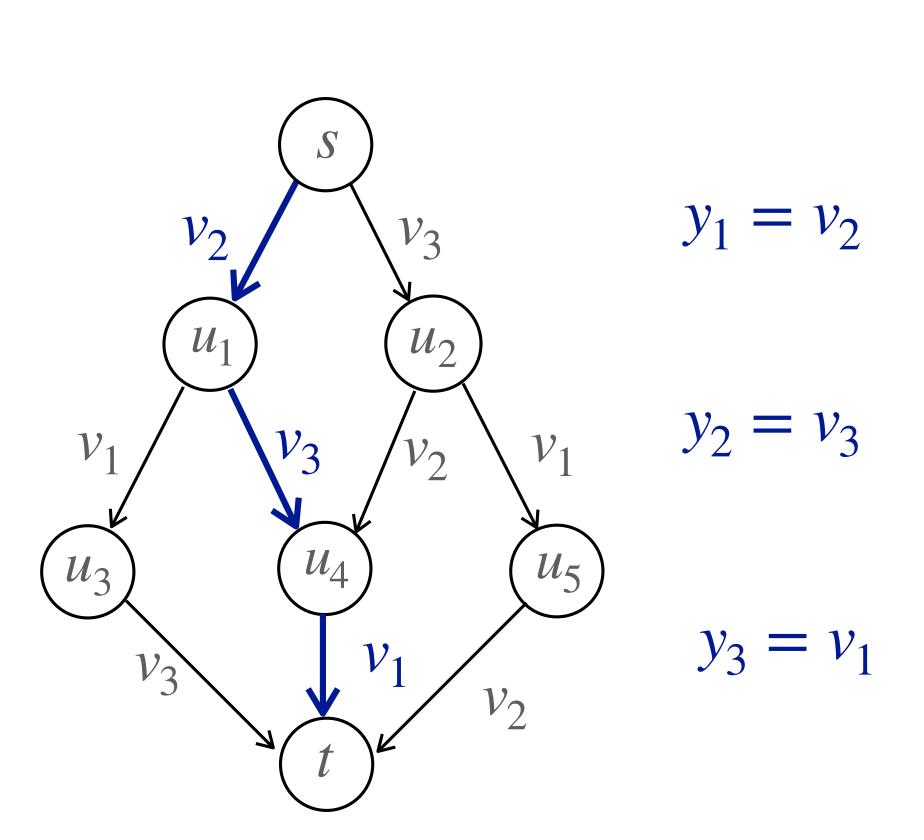
Background: Decision Diagram

A constraint reasoning tool that represents the set of solutions to combinatorial optimization problems as a space-compact directed acyclic graph.

3 variables $\{y_1, y_2, y_3\}$, which can take assignments $y_i \in \{v_1, v_2, v_3\}$.

Two constraints C:

- First location should not be v_1 .
- Three variables have different assignments.

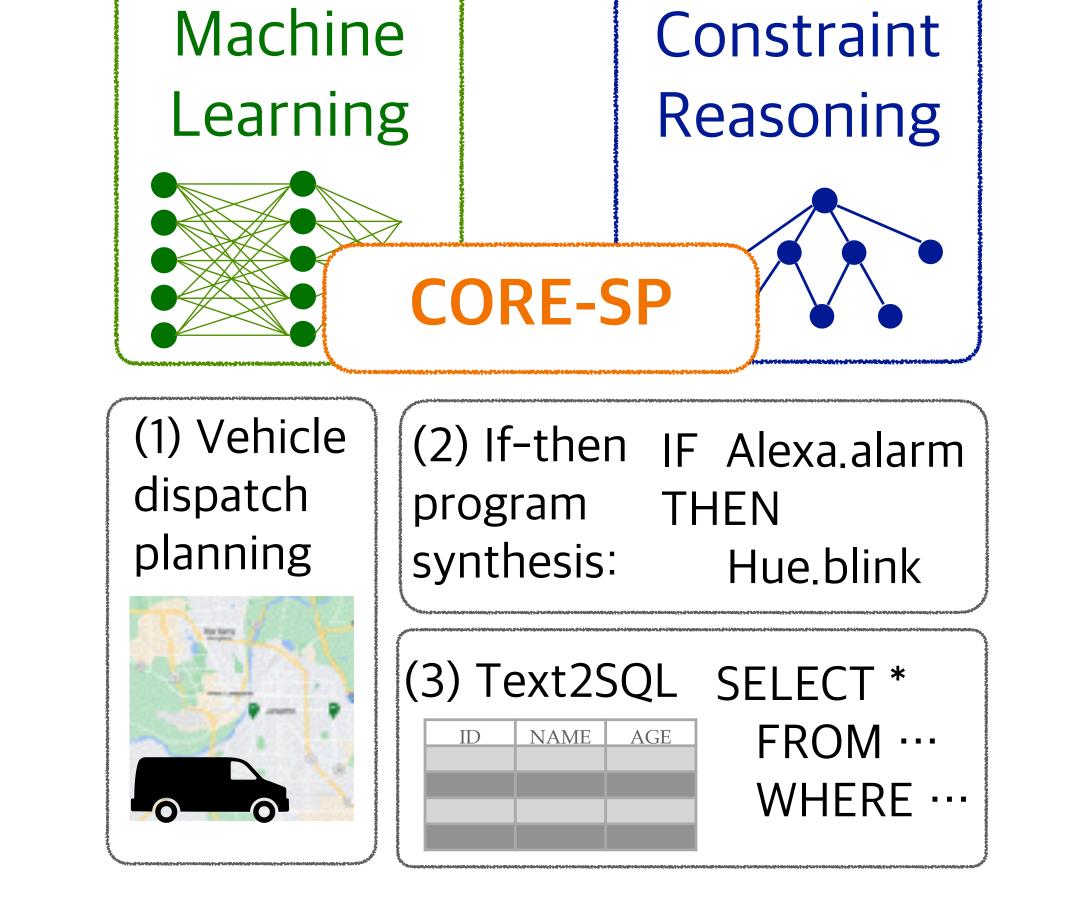


Every $s \rightarrow t$ path in the graph corresponds to a valid variables' assignment with these constraints.

Method: An Integrated System (Learning + Reasoning)

Given:

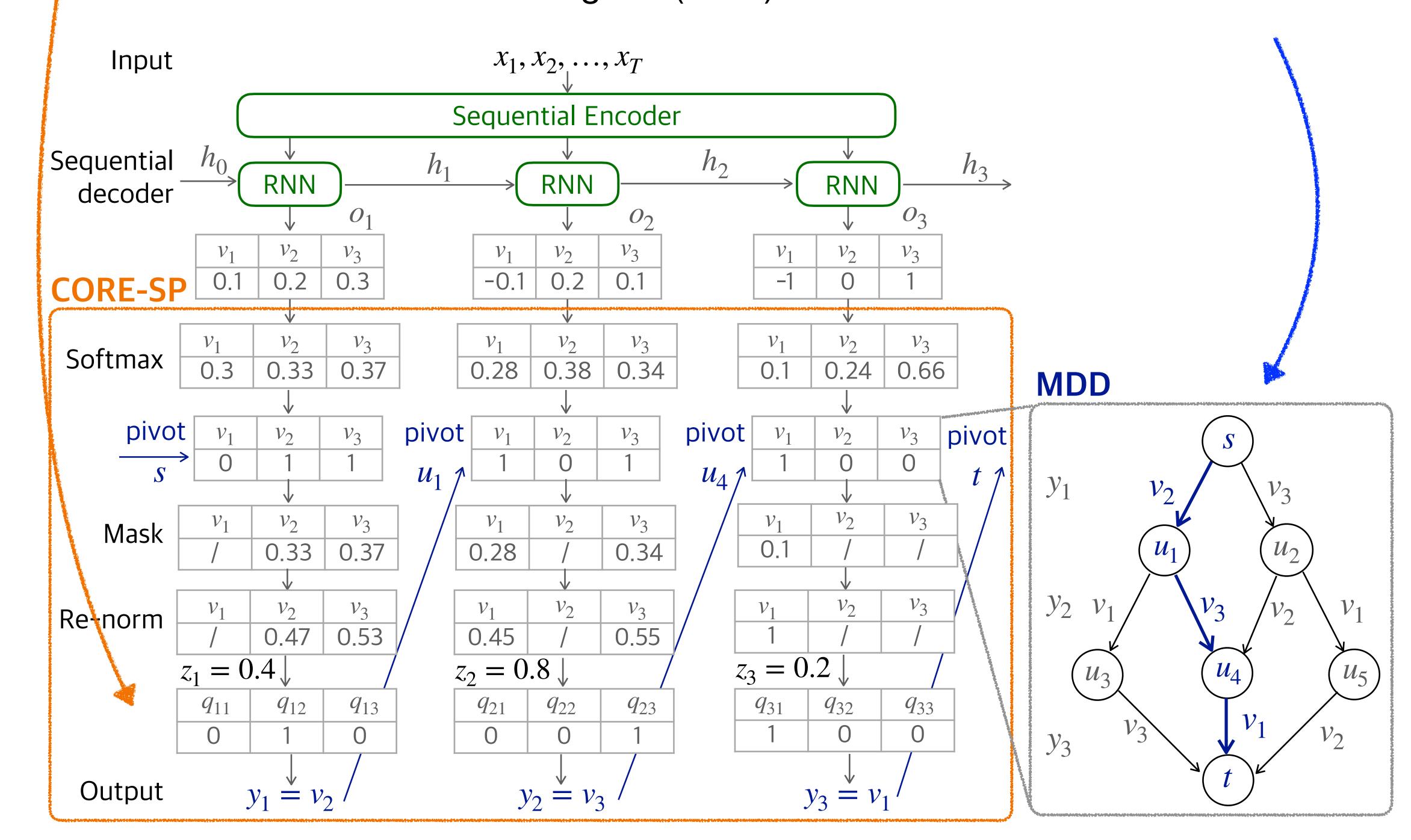
- Training data $\{(x_1, y_1), ..., (x_n, y_n)\};$
- Structured-output space $Y = \{0,1\}^m$;
- Constraints C for the output space Y.



Learn: a constrained probability distribution: for $y \in Y$,

$$P_{\theta}(y \mid x; C) \begin{cases} > 0 & \text{if } y \text{ satisfies } C \\ = 0 & \text{if } y \text{ violates } C \end{cases}$$

A valid output from the sequence-to-sequence model corresponds to a path in the multi-valued decision diagram (MDD).

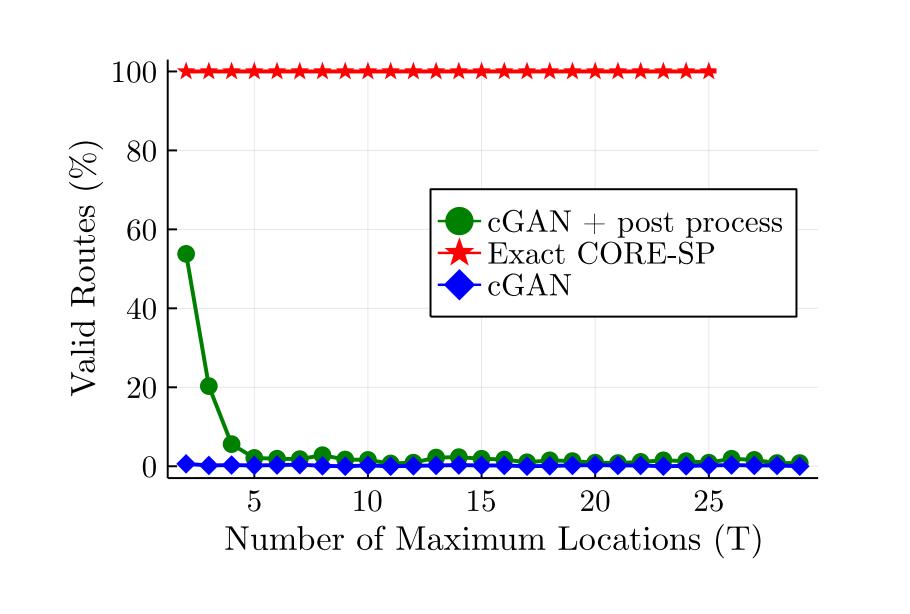


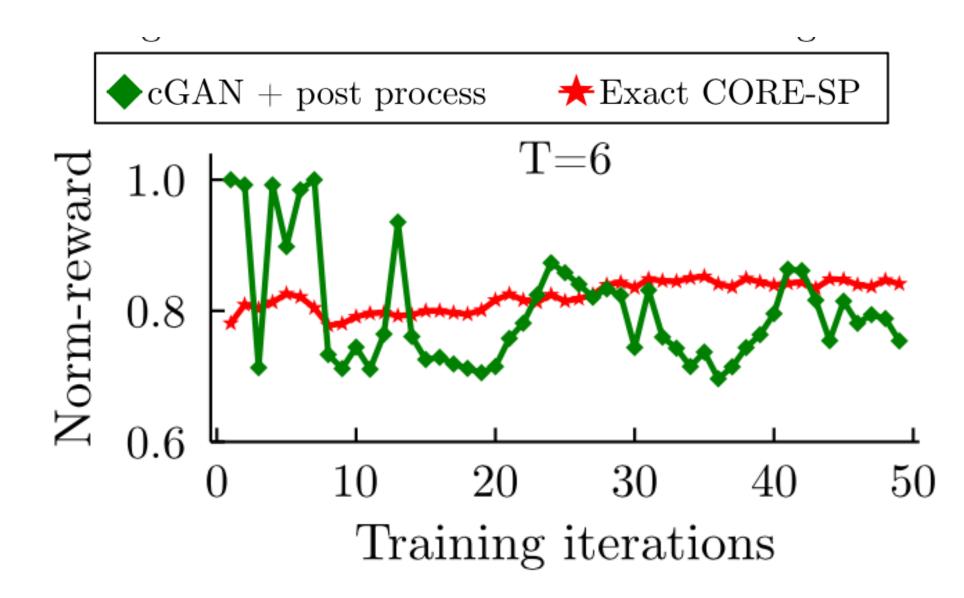
Experiments

1) The structures generated with exact decision diagram satisfy 100% of the constraints.

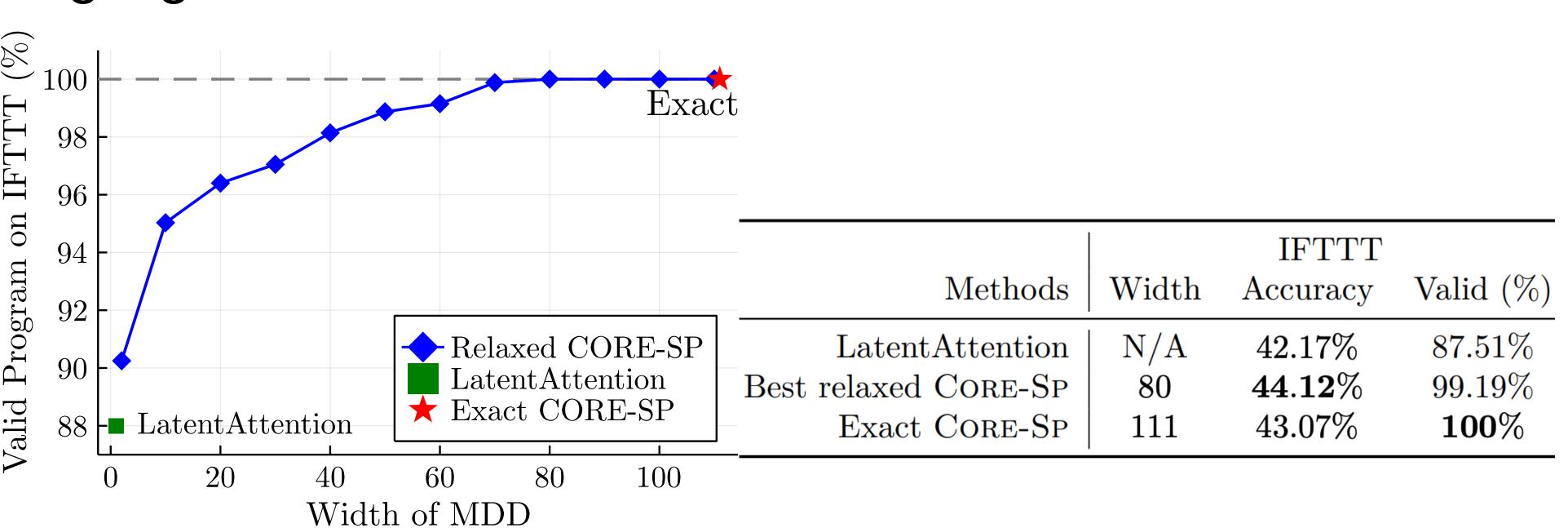
2) boosts learning performance (higher reward, accuracy on testing set) by reducing the modeling space via constraint satisfaction.

(1) Vehicle dispatch planning: Recommend dispatching routes.





(2) If-then Program synthesis: Learn a program from natural language.



(3) Text2SQL generation. Learn a SQL program from natural language.

	Moderate test set		
	SQLNova	Core-Sp	
Valid SQL	94.3%	100%	
	Hard test set SQLNova Core-Sp		
	SQLNova	Core-Sp	
Valid SQL	83.7%	100 %	

Overall Accuracy	SQLNova	Core-Sp
Logical Accuracy Execution Accuracy	79.3% 85.5%	79.9% 86.1%
Valid SQL	99.3%	100.0%