```
var, x, y, z
 context,\ G
                                  ::=
                                         nil
                                         G, x
 type, t, A, B
                                        int
                                        forall x.t
                                                                       \mathsf{bind}\ x\ \mathsf{in}\ t
                                        t_1 - > t_2
                                                                       S
                                         (t)
                                        [t_1/x]t_2
                                                                       Μ
formula
                                        judgement
                                         x \# G
                                                                       Μ
 Monotype
                                         \mathbf{mono}\,A
 In Context
                                         x in G
 Declarative Subtyping
                                      |-G|
                                        G|-t
G|-t_1 <: t_2
judgement
                                         Monotype
                                         In Context
                                         Declarative Subtyping \\
 user\_syntax
                                  ::=
                                         var
                                         context
                                         type
                                         formula
\mathbf{mono}\,A
                                                              {\rm MONO\_INT}
                                               \mathbf{mono}\,\mathbf{int}
                                                             MONO\_VAR
                                               \mathbf{mono}\,x
                                             \mathbf{mono}\ t_1
                                             \mathbf{mono}\;t_2
                                                               MONO_ARROW
                                        \overline{\text{mono } t_1 - > t_2}
  \overline{x} in G
```

 $\overline{x \text{ in } G, x}$ 

IN\_HERE

$$\frac{x \text{ in } G}{x \text{ in } G, y}$$
 IN\_THERE

| | - G |

G|-t

$$\frac{|-G|}{G|-\text{int}} \quad \text{WF\_TYP\_INT}$$

$$|-G|$$

$$\frac{x \text{ in } G}{G|-x} \quad \text{WF\_TYP\_VAR}$$

$$|-G|$$

$$G|-t_1$$

$$G|-t_2$$

$$G|-t_1->t_2$$

$$WF\_TYP\_ARROW$$

 $|G|-t_1 <: t_2$ 

$$\frac{x \text{ in } G}{G|-x<:x} \quad \text{S_VAR}$$

$$\overline{G|-\text{int}<:\text{int}} \quad \text{S_INT}$$

$$G|-B_1<:A_1$$

$$G|-A_2<:A_2$$

$$\overline{G|-A_1->A_2<:B_1->B_2} \quad \text{S_ARROW}$$

$$G|-t$$

$$\begin{array}{c} G|-t\\ \text{mono } t\\ \hline G|-\text{forall } x.A<:B \\ \hline G|-\text{forall } x.A<:B \\ \hline G|-A<:\text{forall } x.B \\ \end{array}$$

$$\text{S_FORALLL}$$

Definition rules: 15 good 0 bad Definition rule clauses: 33 good 0 bad