

MASSEY UNIVERSITY

Geographic Data Visualization

Author
Yang JIANG

Supervisor
Dr Arno LEIST

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in the*

Software Engineering
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Abstract

The Thesis Abstract is written here (and usually kept to just this page). The page is kept centered vertically so can expand into the blank space above the title too.

Keywords: Keywords, for, your, thesis

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1 Introduction

1.1 Background and Overview

1.2 Literature Review

1.2.1 Current Landscape

1.2.2 Respective Limitations

1.3 Aims and Objectives

2 Technology

2.1 Mobile Device

2.1.1 Sensor

2.1.2 Google Cardboard

2.1.3 Android

2.2 OpenGL

OpenGL ES 2.0, 3.0, 3.1, 3.1 ext

2.3 Scene Data

3D scene data format: KML, VRML, COLLADA, glTF

2.3.1 KML

2.3.2 OBJ

2.4 File Server

2.4.1 Golang

2.4.2 Volley

3 Implementation

3.1 Google VR SDK

3.2 Scene

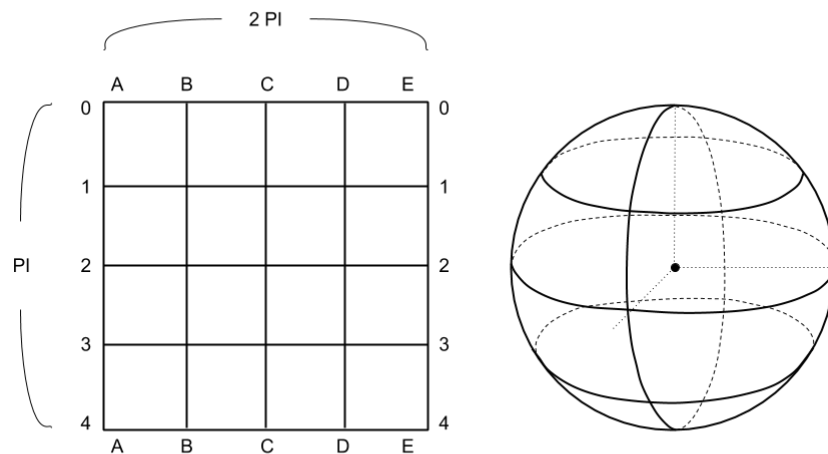
3.2.1 KML

3.2.2 Orcree

3.3 Earth

The Earth is created as a UV Sphere, which somewhat like latitude and longitude lines of the earth, uses rings and segments. Near the poles (both on the Z-axis with the default orientation) the vertical segments converge on the poles. UV spheres are best used in situations where you require a very smooth, symmetrical surface.

FIGURE 3.1: UV sphere mapping



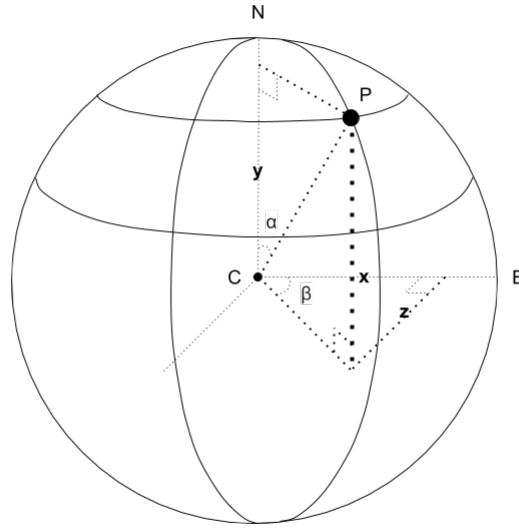
As we can see the mapping from 3.1. Vertex A_0, A_1, A_2, A_3, A_4 and E_0, E_1, E_2, E_3, E_4 are duplicated, and A_0, B_0, C_0, D_0, E_0 converge together as well as A_4, B_4, C_4, D_4, E_4 .

So we can simply define it as a UV sphere has 5 rings and 4 segments. Also be noticed that each ring spans 2π radians, but each segment spans π radians in the sphere mapping.

The total vertex number is:

$$Vertices = Rings \times Segments \quad (3.1)$$

FIGURE 3.2: UV sphere vertex



For each vertex P on sphere from ring r and segment s , we have:

$$\begin{aligned} v &= r \times \frac{1}{rings-1} \\ u &= s \times \frac{1}{segments-1} \\ \angle\alpha &= v \times \pi \\ \angle\beta &= u \times 2\pi \end{aligned}$$

$\therefore P(x, y, z)$

$$\begin{aligned} x &= (\sin(\alpha) \times radius) \times \cos(\beta) \\ y &= \cos(\alpha) \times radius \\ z &= (\sin(\alpha) \times radius) \times \sin(\beta) \end{aligned}$$

& 2D Texture (x, y) mapping for vertex P is:

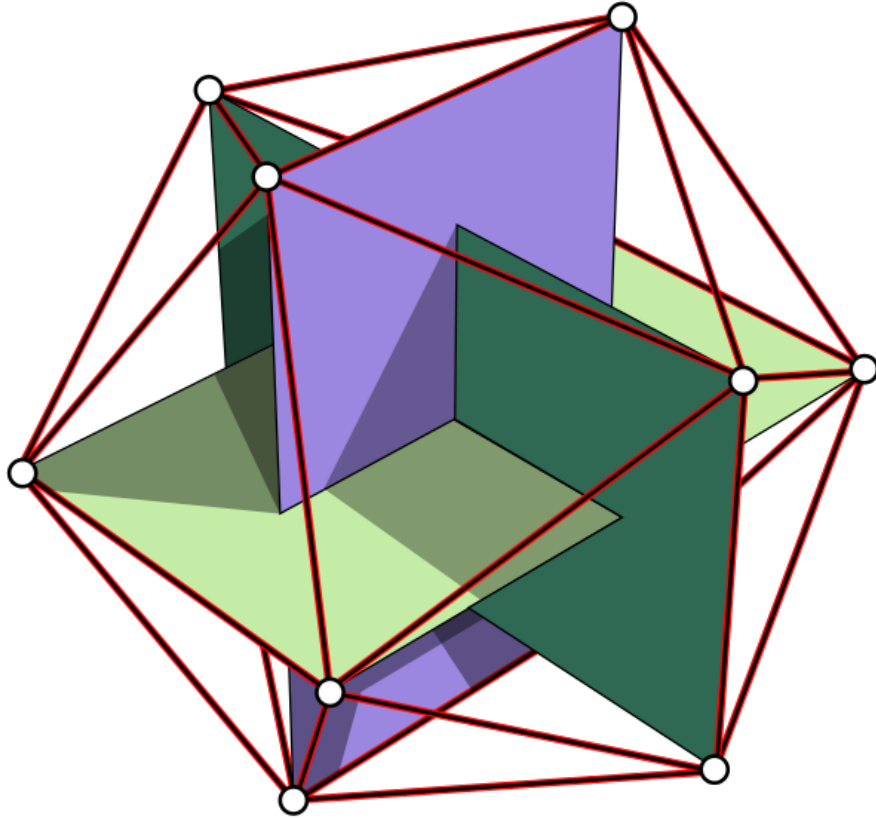
$$\begin{aligned} x &= u \\ y &= v \end{aligned}$$

3.4 Placemaker

3.4.1 Icosphere

Generation of vertices for placemaker is a recursion process of subdividing icosphere. Figure 3.3 shows that the initial vertices of an icosahedron are the corners of three orthogonal rectangles.

FIGURE 3.3: Icosahedron rectangles (Fropuff, 2006)



Rounding icosphere by subdividing a face to an arbitrary level of resolution. One face can be subdivided into four by connecting each edge's midpoint.

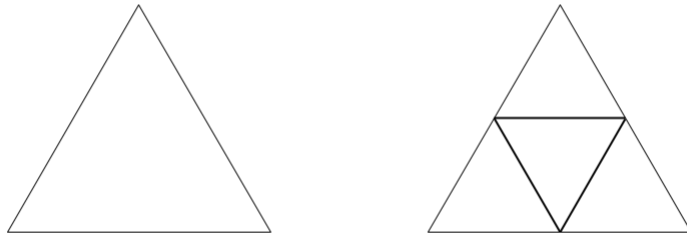


FIGURE 3.4: Icosphere subdivide

Then, push edge's midpoints to surface of the sphere.

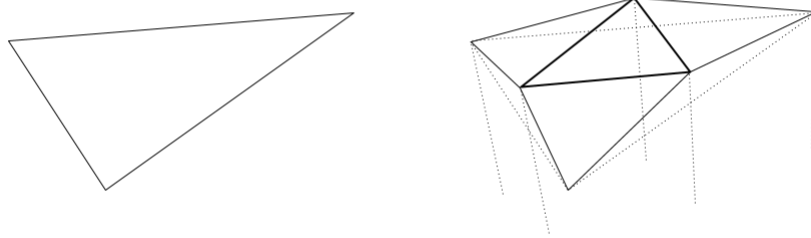


FIGURE 3.5: Icosphere refinement

TABLE 3.1: Rounding Icosphere

Recursion Level	Vertex Count	Face Count	Edge Count
0	12	20	30
1	42	80	120
2	162	320	480
3	642	1280	1920

3.4.2 Geographic Coordinate System

A geographic coordinate system is a coordinate system that enables every location on the Earth to be specified by a set of numbers or letters, or symbols (Wikipedia, 2016c). A common geodetic-mapping coordinates is latitude, longitude and altitude (LLA), which also is the raw location data read from KML.

We introduce ECEF ("earth-centered, earth-fixed") coordinate system for converting LLA coordinates to position coordinates. According to, the z-axis is pointing towards the north but it does not coincide exactly with the instantaneous earth rotational axis. The x-axis intersects the sphere of the earth at 0 latitude and 0 longitude (Wikipedia, 2016b).

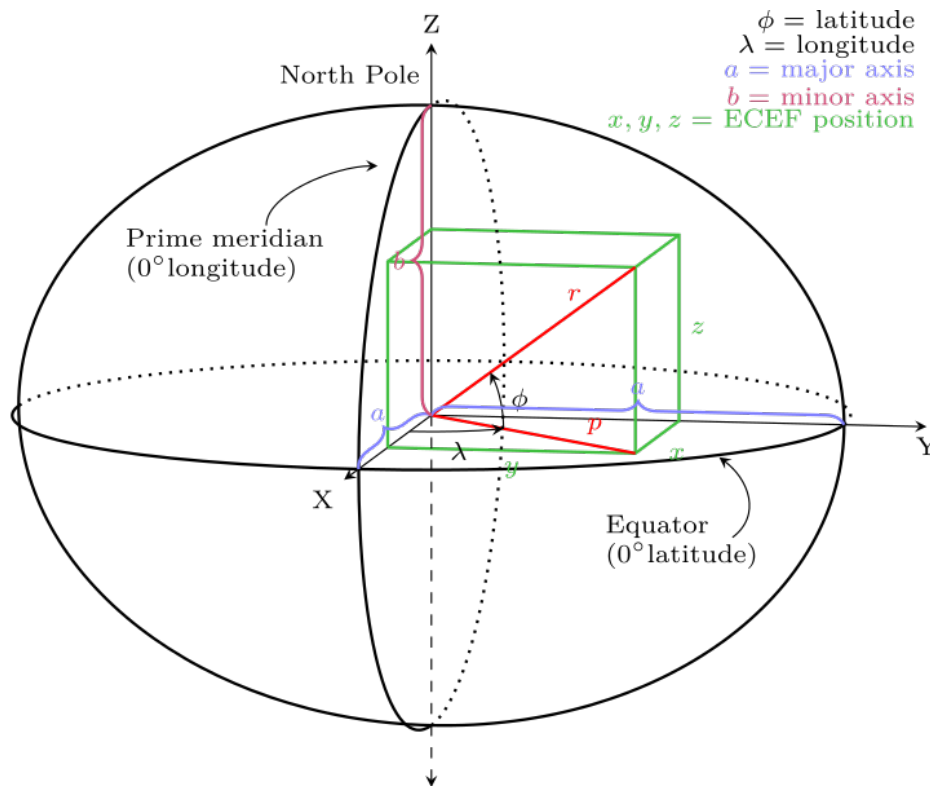


FIGURE 3.6: earth-centered, earth-fixed (Wikipedia, 2016b)

The ECEF coordinates are expressed in a reference system that is related to mapping representations. Because the earth has a complex shape, a simple, yet accurate, method to approximate the earth's shape is required. The use of a reference ellipsoid allows for the conversion between ECEF and LLA (blox, 1999).

A reference ellipsoid can be described by a series of parameters that define its shape and which include a semi-major axis (a), a semi-minor axis (b), its first eccentricity (e_1) and its second eccentricity (e_2) as shown in Table 3.2.

TABLE 3.2: WGS 84 parameters

Parameter	Notation	Value
Reciprocal of flattening	$1/f$	298.257 223 563
Semi-major axis	a	6 378 137 m
Semi-minor axis	b	$a (1 - f)$
First eccentricity squared	e_1^2	$1 - b^2/a^2 = 2 f - f^2$
Second eccentricity squared	e_2^2	$a^2/b^2 - 1 = f (2 - f)/(1 - f)^2$

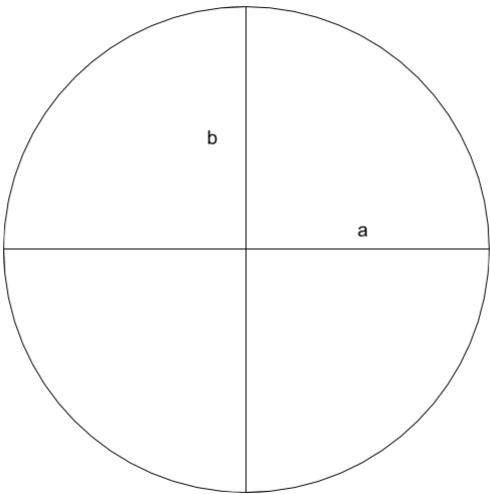


FIGURE 3.7: Ellipsoid Parameters

The conversion from LLA to ECEF is shown below.

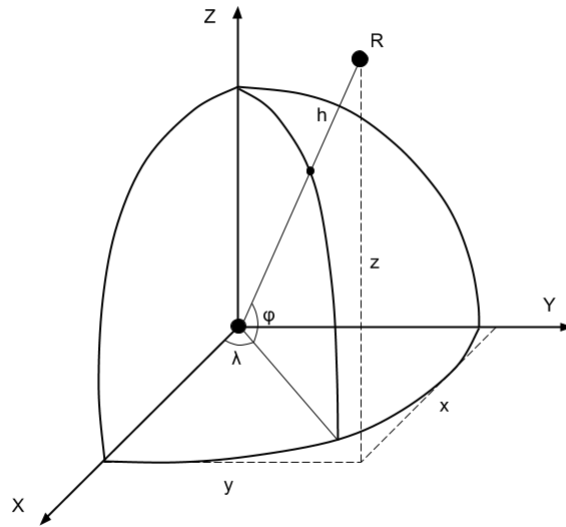


FIGURE 3.8: LLA to ECEF

$$\begin{aligned}
 x &= (N + h) \cos(\varphi) \cos(\lambda) \\
 y &= (N + h) \cos(\varphi) \sin(\lambda) \\
 z &= \left(\frac{b^2}{a^2} N + h\right) \sin(\varphi)
 \end{aligned}$$

Where

φ = latitude

λ = longitude

h = height above ellipsoid (meters)

N = Radius of Curvature (meters), defined as:

$$= \frac{a}{\sqrt{1 - e^2 \sin^2(\varphi)}}$$

At last, for this project usage, where high accuracy is not required, a equals to b . And also the ECEF coordinate system is y-east, z-north (up), and x points to 0 latitude and 0 longitude, but for project specific, we still need to convert ECEF to x-east, y-north (up), and x points to 0 latitude and 180 longitude.

3.4.3 Extra Model

A simple and common OBJ format model can be loaded as an extra model for the placemaker.

3.5 Textfield

A textfield is a a rectangle vertices based renderable component to display text on a flat plane. Since it is a GL scene, the actual text will be drawn as a texture. By a constant width and native `android.text.StaticLayout` support, the height of the texture can be calculated.

A menu contains multi-textfield can be seen as an empty textfield based which texture is fill full a pure background color, and several textfields are laid out on the top of it with a certain vertical dimension.

A head rotation matrix (quaternion matrix (Verth, 2013)) is required for locating object in front of camera (mathworks, 2016) .

3.6 Camera Movement

In general, there are two sensors can be useful to manager camera movement: ACCELEROMETER (API level 3), LINEAR_ACCELERATION (API level 9) and STEP_DETECTOR (API level 19).

LINEAR_ACCELERATION is same as ACCELERATION which measures the acceleration force in meter per second repeatedly, except linear acceleration sensor is a synthetic sensor with gravity filtered out.

$$\begin{aligned} \text{LinearAcceleration} &= \text{AccelerometerData} - \text{Gravity} \\ v &= \int a \, dt \\ x &= \int v \, dt \end{aligned}$$

First of all, we take the acclerometer data and remove gravity that is called gravity compensation, whatever is left is linear movement. Then we have to integrate it one to get velocity, integrated again to get position, which is called double integral. Now if the first integral creates drift, double integrals are really nasty that they create horrible drift. Because of these noise, using acceleration data it isn't so accurate, it is really hard to do any kind of linear movement (GoogleTechTalks, 2010).

On the other hand, use step counter from STEP_DETECTOR, and pedometer algorithm for pedestrian navigation, that in fact works very well for this project.

$$\begin{aligned} p_1 &= p_0 + v_0 \times dt \\ v_1 &= v_0 + a \times dt \end{aligned}$$

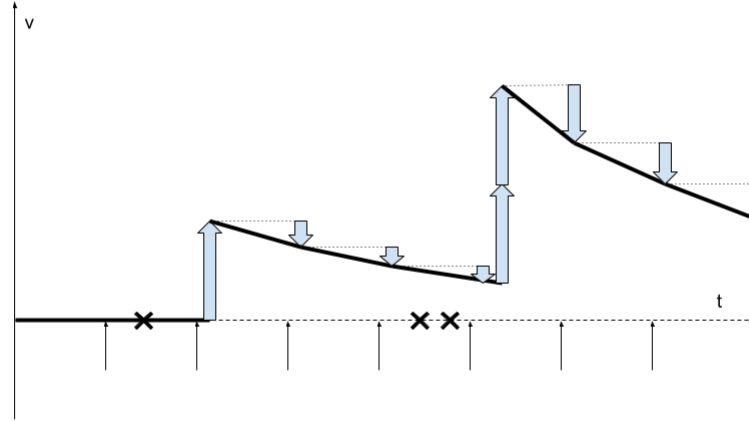
The accuracy of this depends on how precision we can get for changing velocity. Considering that velocity is made of 3-axis directions, the current heading direction is required for a correct velocity calculation. Since the frame life cycle is implemented based on (Google, 2016), which provide the heading direction in each frame callback. So I collect everything I need from the last frame to new frame, and update both velocity and position for each new frame.

For updating process, first of all,

First of all, damping is required. I reduce velocity by a percentage. It is simply for avoiding that camear taking too long to stop. Damping by percentage can stable and stop the camera in a certain of time that won't be affected by the current camera speed.

Secondly, a constant value in head forwarding direction is been used as a pulse for each step. Because a step is happening instantaneously which implies $a \, dt$ made by each step is actually can be replace by a constant value.

FIGURE 3.9: Camera movement



For each new frame:

$$\begin{aligned}
 \vec{V}_0 &= \vec{V}_0 \cdot Damping \\
 \vec{P}_1 &= \vec{P}_0 + \vec{V}_0 \cdot dt \\
 \vec{V}_1 &= \vec{V}_0 + \overrightarrow{Forwarding} \cdot Pulse \cdot Steps \\
 Damping &\in [0, 1] \\
 Pulse &\in [0, \infty)
 \end{aligned}$$

3.7 Ray Intersection

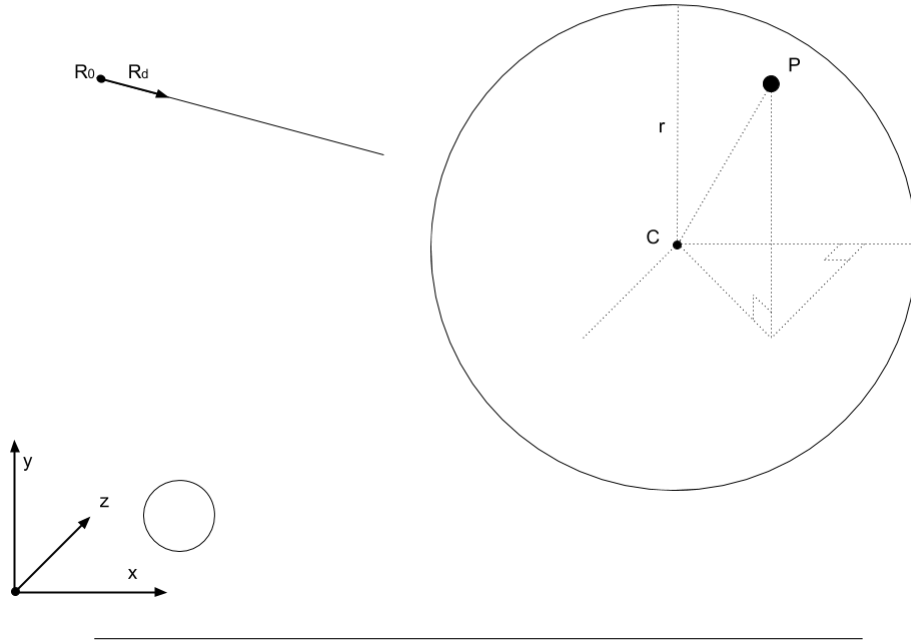
Detect collisions between ray and models is the key to allow user selecting objects in the VR world, which is one of the important experience for user interaction.

A ray can be describe in a equation with known ray start position \vec{R}_0 and ray direction \vec{R}_d .

$$\vec{R}(t) = \vec{R}_0 + \vec{R}_d \cdot t \quad (3.2)$$

3.7.1 Ray-Sphere

FIGURE 3.10: Ray-Sphere intersection



A point P on the surface of sphere should match the equation:

$$(x_p - x_c)^2 + (y_p - y_c)^2 + (z_p - z_c)^2 = r^2 \quad (3.3)$$

If the ray intersects with the sphere at any position P must match the equation 3.2 and 3.3. Therefore the solution of t in the cointegrate equation implies whether or not the ray will intersect with the sphere:

$$\begin{aligned} (x_{R_0} + x_{R_d} \cdot t - x_c)^2 + (y_{R_0} + y_{R_d} \cdot t - y_c)^2 + (z_{R_0} + z_{R_d} \cdot t - z_c)^2 &= r^2 \\ \vdots \\ x_{R_d}^2 t^2 + (2 x_{R_d} (x_{R_0} - x_c)) t + (x_{R_0}^2 - 2 x_{R_0} x_c + x_c^2) \\ + y_{R_d}^2 t^2 + (2 y_{R_d} (y_{R_0} - y_c)) t + (y_{R_0}^2 - 2 y_{R_0} y_c + y_c^2) \\ + z_{R_d}^2 t^2 + (2 z_{R_d} (z_{R_0} - z_c)) t + (z_{R_0}^2 - 2 z_{R_0} z_c + z_c^2) &= r^2 \end{aligned}$$

It can be seen as a quadratic formula:

$$a t^2 + b t + c = 0 \quad (3.4)$$

At this point, we are able to solve the t :

$$t = \begin{cases} \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} & \text{if } b^2 - 4ac > 0 \\ \frac{-b}{2a} & \text{if } b^2 - 4ac = 0 \\ \emptyset & \text{if } b^2 - 4ac < 0 \end{cases}$$

Then, I take a further step to get rid of formula complexity.

\therefore Equation 3.3, 3.4

$$\begin{cases} a = x_{R_d}^2 + y_{R_d}^2 + z_{R_d}^2 \\ b = 2(x_{R_d}(x_{R_0} - x_c) + y_{R_d}(y_{R_0} - y_c) + z_{R_d}(z_{R_0} - z_c)) \\ c = (x_{R_0} - x_c)^2 + (y_{R_0} - y_c)^2 + (z_{R_0} - z_c)^2 - r^2 \end{cases}$$

&

$$\begin{aligned} |\vec{R_d}| &= \sqrt{x_{R_d}^2 + y_{R_d}^2 + z_{R_d}^2} = 1 \\ \vec{V_{c_R_0}} &= \vec{R_0} - \vec{C} = (x_{R_0} - x_c, y_{R_0} - y_c, z_{R_0} - z_c) \end{aligned}$$

\therefore

$$\begin{cases} a = 1 \\ b = 2 \cdot \vec{R_d} \cdot \vec{V_{c_R_0}} \\ c = \vec{V_{c_R_0}} \cdot \vec{V_{c_R_0}} \cdot r^2 \end{cases}$$

\therefore The formula for t can also be optimized

$$\begin{cases} \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = -\alpha \pm \sqrt{\beta} \\ \alpha = \frac{1}{2}b \\ \beta = \alpha^2 - c \end{cases}$$

\therefore The final solution for t

$$t = \begin{cases} -\alpha \pm \sqrt{\beta} & \text{if } \beta > 0 \\ -\alpha & \text{if } \beta = 0 \\ \emptyset & \text{if } \beta < 0 \end{cases}$$

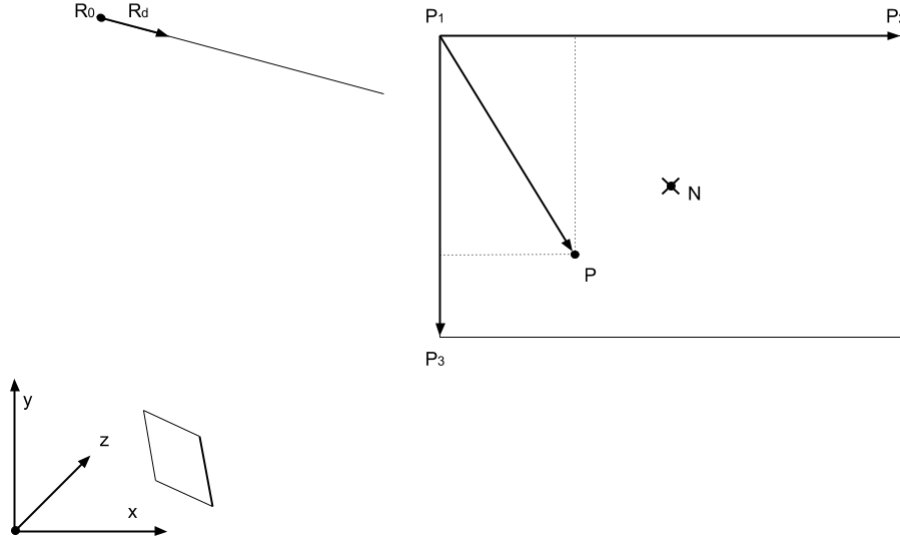
And the collision position for each t is:

$$\vec{P} = \vec{R_0} + \vec{R_d} \cdot t$$

3.7.2 Ray-Plane

(user3146587, 2014)

FIGURE 3.11: Ray-Plane intersection



If a point P on the plane and also belongs to the ray, we have quadric equation:

$$\begin{cases} (\vec{P} - \vec{P}_1) \cdot \vec{N} = 0 \\ \vec{P} = \vec{R}_0 + \vec{R}_d \cdot t \end{cases} \quad (3.5)$$

Solution for the t is:

$$t = \begin{cases} \frac{-\vec{N} \cdot (\vec{R}_0 - \vec{P}_1)}{\vec{N} \cdot \vec{R}_d} & \text{if } \vec{N} \cdot \vec{R}_d \neq 0 \\ \emptyset & \text{if } \vec{N} \cdot \vec{R}_d \sim 0 \end{cases}$$

At last, we have to verify if the collision is inside of the quadrangle by putting t back to 3.5, and the t is valid only if:

$$\begin{aligned} \mu &= \sqrt{(\vec{P} - \vec{P}_1) \cdot (\vec{P}_2 - \vec{P}_1)} \in [0, |\vec{P}_2 - \vec{P}_1|] \\ \nu &= \sqrt{(\vec{P} - \vec{P}_1) \cdot (\vec{P}_3 - \vec{P}_1)} \in [0, |\vec{P}_3 - \vec{P}_1|] \end{aligned}$$

3.7.3 Ray-Box

(Williams et al., 2005)

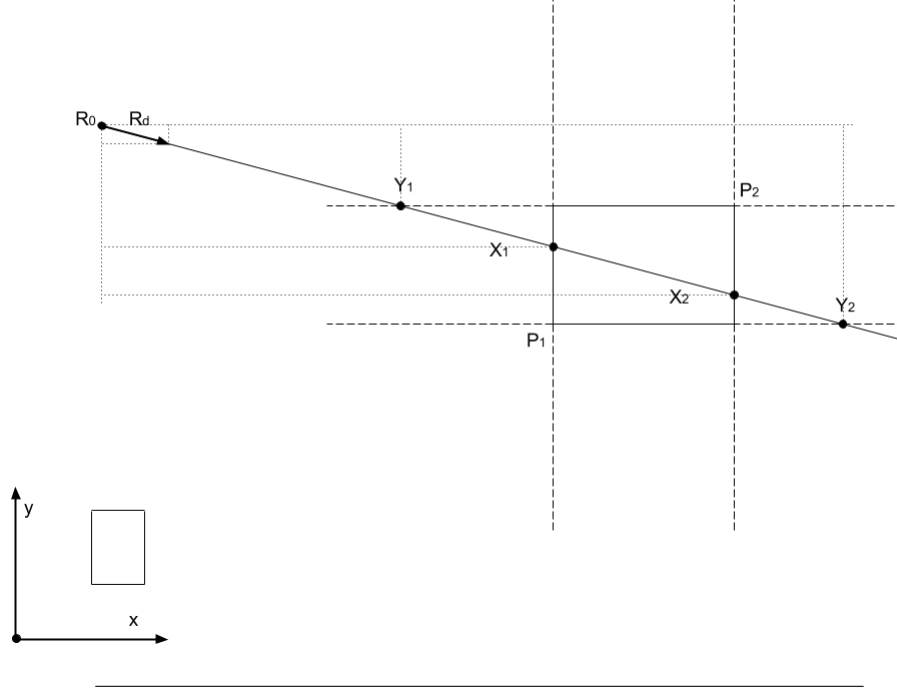
(Barnes, 2011)

(Scratchapixel, 2014)

There is a octree implementation in the VR 3D world that separate the 3D world to invisible 3D boxes that each box contains a certain number of other models. It is to avoid unnecessary ray-object collision detection. In this section, I am going to first explain Ray-Box-2D collision detection, then derive out Ray-Box-3D intersection.

Ray-Box-2D

FIGURE 3.12: Ray-Box-2D intersection



\therefore Known R_0, R_d, P_1, P_2

$$X_1 = \begin{cases} x_{P_1} - x_{R_0} & \text{if } x_{R_d} > 0 \\ x_{P_2} - x_{R_0} & \text{if } x_{R_d} < 0 \end{cases} \quad Y_1 = \begin{cases} y_{P_1} - y_{R_0} & \text{if } y_{R_d} > 0 \\ y_{P_2} - y_{R_0} & \text{if } y_{R_d} < 0 \end{cases}$$

$$X_2 = \begin{cases} x_{P_2} - x_{R_0} & \text{if } x_{R_d} > 0 \\ x_{P_1} - x_{R_0} & \text{if } x_{R_d} < 0 \end{cases} \quad Y_2 = \begin{cases} y_{P_2} - y_{R_0} & \text{if } y_{R_d} > 0 \\ y_{P_1} - y_{R_0} & \text{if } y_{R_d} < 0 \end{cases}$$

$$t_{X_1} = \frac{X_1}{x_{R_d}} \quad t_{Y_1} = \frac{Y_1}{y_{R_d}}$$

$$t_{X_2} = \frac{X_2}{x_{R_d}} \quad t_{Y_2} = \frac{Y_2}{y_{R_d}}$$

& When collision happens, we have formula

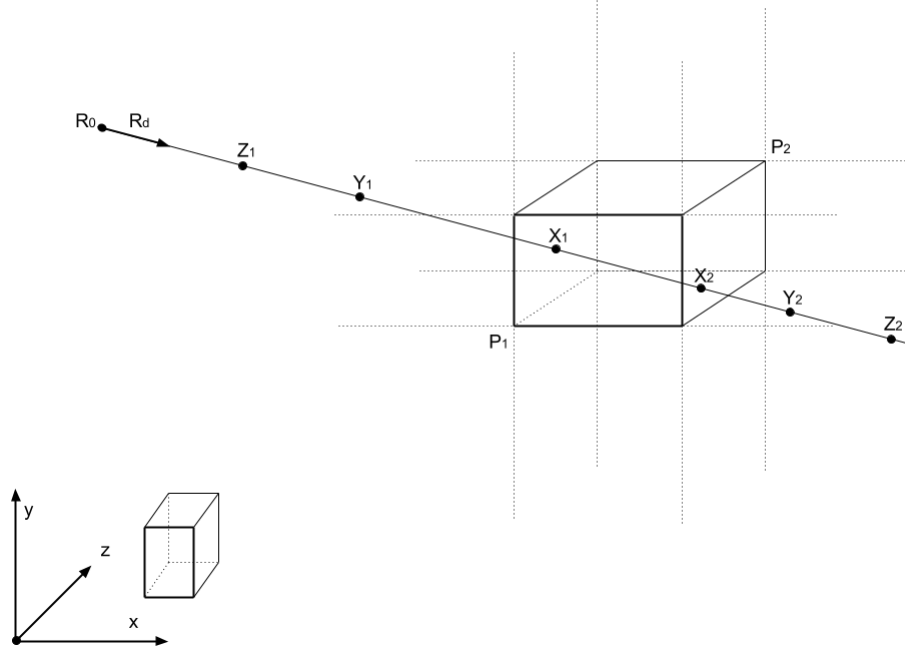
$$\begin{cases} t_{X_1} < t_{X_2} \\ t_{Y_1} < t_{Y_2} \end{cases}$$

\therefore Which is

$$\max(t_{X_1}, t_{Y_1}) < \min(t_{X_2}, t_{Y_2}) \quad (3.6)$$

Ray-Box-3D

FIGURE 3.13: Ray-Box-3D intersection



\therefore Known R_0, R_d, P_1, P_2

$$X_1 = \begin{cases} x_{P_1} - x_{R_0} & \text{if } x_{R_d} > 0 \\ x_{P_2} - x_{R_0} & \text{if } x_{R_d} < 0 \end{cases} \quad Y_1 = \begin{cases} y_{P_1} - y_{R_0} & \text{if } y_{R_d} > 0 \\ y_{P_2} - y_{R_0} & \text{if } y_{R_d} < 0 \end{cases}$$

$$X_2 = \begin{cases} x_{P_2} - x_{R_0} & \text{if } x_{R_d} > 0 \\ x_{P_1} - x_{R_0} & \text{if } x_{R_d} < 0 \end{cases} \quad Y_2 = \begin{cases} y_{P_2} - y_{R_0} & \text{if } y_{R_d} > 0 \\ y_{P_1} - y_{R_0} & \text{if } y_{R_d} < 0 \end{cases}$$

$$t_{X_1} = \frac{X_1}{x_{R_d}} \quad t_{Y_1} = \frac{Y_1}{y_{R_d}}$$

$$t_{X_2} = \frac{X_2}{x_{R_d}} \quad t_{Y_2} = \frac{Y_2}{y_{R_d}}$$

$$Z_1 = \begin{cases} z_{P_1} - z_{R_0} & \text{if } z_{R_d} > 0 \\ z_{P_2} - z_{R_0} & \text{if } z_{R_d} < 0 \end{cases}$$

$$Z_2 = \begin{cases} z_{P_2} - z_{R_0} & \text{if } z_{R_d} > 0 \\ z_{P_1} - z_{R_0} & \text{if } z_{R_d} < 0 \end{cases}$$

$$t_{Z_1} = \frac{Z_1}{z_{R_d}} \quad t_{Z_2} = \frac{Z_2}{z_{R_d}}$$

& When collision happens, we have formula

$$\begin{cases} t_{X_1} < t_{X_2} \\ t_{Y_1} < t_{Y_2} \\ t_{Z_1} < t_{Z_2} \end{cases}$$

∴ Which is

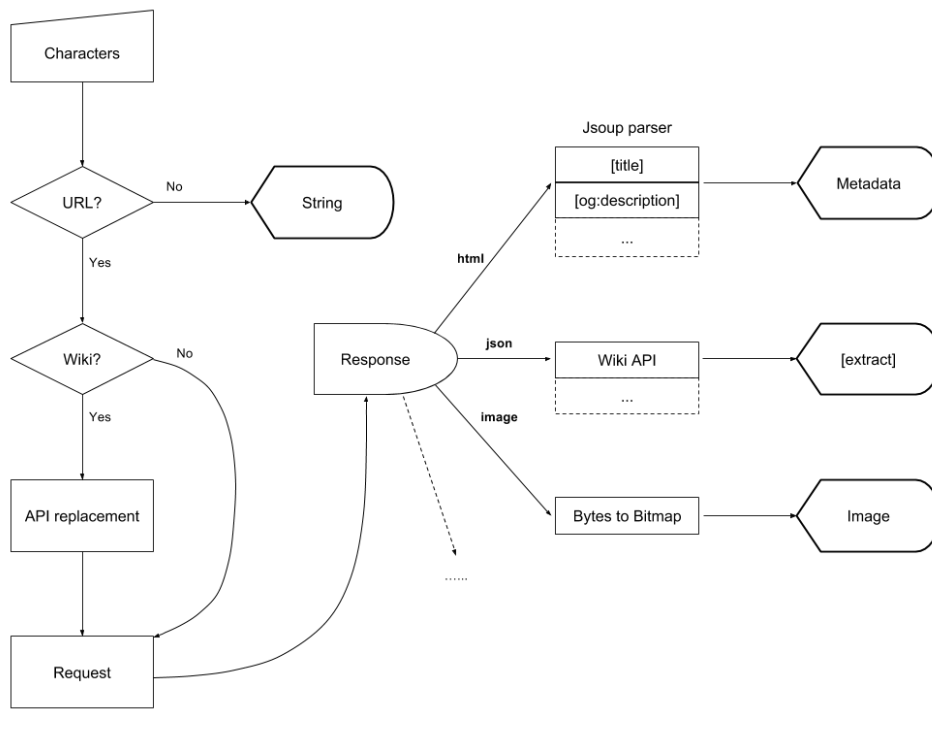
$$\max(t_{X_1}, t_{Y_1}, t_{Z_1}) < \min(t_{X_2}, t_{Y_2}, t_{Z_2}) \quad (3.7)$$

3.8 Description Analysis

Description of placemaker requires an appropriate analysis for display. The raw data of description is a set of characters that could be a normal text, an image URL, an URL returns different type of content, or maybe just some meaningless characters.

Although the implementation of analysis in this project did not cover every situation, but it is flexible and extendable for more functionality.

FIGURE 3.14: Description Analysis



In order to get an extracted content from a wikipedia page, we can transform the URL to a Wiki-API based open-search url (Wikipedia, 2016a), which will returns a json format raw data that we can easily get what we need from different json tags.

Replace `.wikipedia.org/wiki/`
To `.wikipedia.org/w/api.php?APIs`

Where *APIs* is:

```
format=json
&action=query
&redirects=1
&prop=extracts
&exintro=
&explaintext=
&indexpageids=
&titles=
```

For *html* parser, we introduced jsoup (it is a Java library for working with real-world HTML (jsoup, 2016)), to get the basic information we need, such as *title*, and some other metadata. In this project, I am also use *og : description* (one of the open graph meta tags (ogp, 2014)) from the html source if it exist.

3.9 File Server

3.9.1 Golang

3.9.2 Patch

3.9.3 Port Forwarding

3.10 OpenGL ES

Pass Perspective matrix, View matrix, and Model matrix to shader to avoid calculate MV or MVP in cpu

Perspective: eye.getPerspective(float zNear, float zFar)

View: eye.getEyeView() * camera.matrix

camera.matrix: build by position, lookAt, up

Model: translation * scale * rotation * mat(1)

4 Discussion

4.1 Evaluation

4.2 Perspective

5 Conclusion

A Appendix A

Write your Appendix content here.

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