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Bit Operator

Leading zeros ∅ (i.e., to the left) are meaningless

~ NOT

- Invert a bit
- Examples:

```
0 \sim 0 = 1

0 \sim 1 = 0

0 \sim 0111 = 1000

0 \sim 100 = 011
```

• In Java, ~ inverts an int and not single bits, so:

& AND

- Results in 1 in each position if the corresponding first bit and second bit are 1, otherwise 0.
- Enables to find if a certain bit in a number contains 1 or ∅. Can be considered like multiplying all bits.
- Examples:

```
10 & 11 = 100011 & 0010 = 0010
```

OR

- Results in 1 in each position if the corresponding first bit *or* second bit are 1, otherwise 0.
- Enables to set a specific bit to 1.
- Examples:

```
10 | 11 = 110011 | 0010 = 0011
```

^ XOR

- Exclusive OR results in 1 in each position if the corresponding first bit or second bit are 1, but not both, otherwise 0.
- Enables to compare two bits − 1 means they are different, 0 means they are the same.
- Can be used to invert selected bits in a register. Any bit can be toggled by XOR-ing it with 1.
- XOR-ing a value against itself yields zero.
- Examples:

```
0101 ^ 0011 = 01100010 ^ 1010 = 1000
```

- XOR can be used for "backup":
 - Calculate a and b's XOR: x = a^b

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```
If needed, recover a: a = b^x
If needed, recover b: b = a^x
```

<< Shift Left

- Add n 0 bits to the right.
- A left arithmetic shift by ${\color{red} n}$ is equivalent to multiplying the number by ${\color{red} 2^n}$.
- For example: 10111 << 1 = 101110

>> Shift Right

- Remove n bits from the right (0 or 1).
- A right arithmetic shift by n is equivalent to dividing by 2^n.
- For example: 10010111 >> 1 = 1001011

Binary Numbers

```
0 = 0
1 = 1
10 = 2
11 = 3
100 = 4
101 = 5
110 = 6
111 = 7
1000 = 8
1001 = 9
1010 = 10
1011 = 11
1100 = 12
1101 = 13
1110 = 14
1111 = 15
10000 = 16
```

Having a 1 in the k-th bit, means that the decimal number is comprised of 2^k. For example, for the above number:

```
2^7 + 2^4 + 2^2 + 2^1 = 150
```

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