Consistency result

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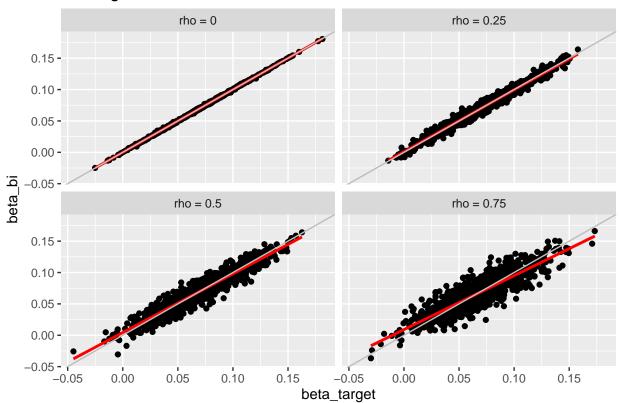
Simulation Set-up

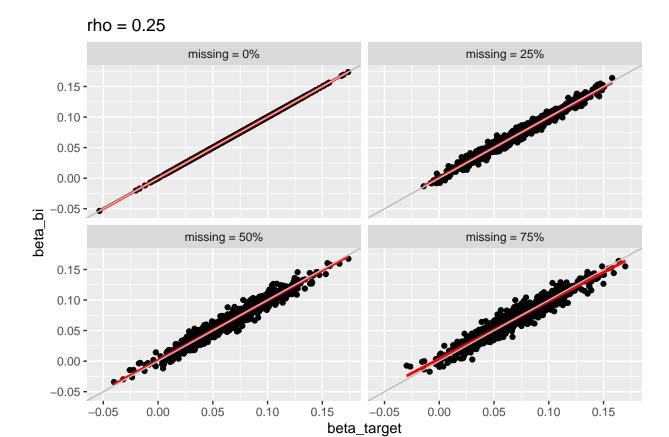
$$\begin{bmatrix} Y_i \\ \hat{Y}_i \end{bmatrix} \mid Z_{ik} \sim N\left(\begin{bmatrix} \beta_G G + \beta X_i \\ \alpha X_i \end{bmatrix}, \begin{bmatrix} 1 & \rho \\ \rho & 1 \end{bmatrix} \right)$$

- $G \sim Bin(2, maf)$
- $maf = 0.25, X_i \sim N(0, 1)$
- $\alpha = \beta = 0.11, \, \beta_g = 0.11575982$
- missing rate $\in \{0, 0.25, 0.5, 0.75\}$
- $\rho \in \{0, 0.25, 0.5, 0.75\}$
- Number of complete cases = 10^3 .

Main Figures

Missing Rate = 25%





${\bf Supplementary\ Figs/Tables}$

Table 1: Bivariate Estimation

| | missing | rho | beta_g | point est | se | emperical se |
|----------|----------------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|
| 65 | 0.00 | 0.00 | 0.1157598 | 0.0697191 | 0.0397092 | 0.0309110 |
| 66 | 0.25 | 0.00 | 0.1157598 | 0.0694879 | 0.0397151 | 0.0307663 |
| 67 | 0.50 | 0.00 | 0.1157598 | 0.0695181 | 0.0397127 | 0.0297711 |
| 68 | 0.75 | 0.00 | 0.1157598 | 0.0696430 | 0.0397014 | 0.0309347 |
| 69 | 0.00 | 0.25 | 0.1157598 | 0.0686581 | 0.0397103 | 0.0318338 |
| 70 | 0.25 | 0.25 | 0.1157598 | 0.0691605 | 0.0393008 | 0.0312436 |
| 71 | 0.50 | 0.25 | 0.1157598 | 0.0694455 | 0.0390990 | 0.0315717 |
| 72 | 0.75 | 0.25 | 0.1157598 | 0.0684193 | 0.0388008 | 0.0303511 |
| 73 | 0.00 | 0.50 | 0.1157598 | 0.0681583 | 0.0396936 | 0.0314101 |
| 74 | 0.25 | 0.50 | 0.1157598 | 0.0686685 | 0.0383947 | 0.0313101 |
| 75 76 | 0.50 | 0.50 | 0.1157598 | 0.0683728 | 0.0371665 | 0.0312167 |
| 76 | 0.75 | 0.50 | 0.1157598 | 0.0693495 | 0.0358030 | 0.0291662 |
| 77 70 | 0.00 | $0.75 \\ 0.75$ | 0.1157598 0.1157598 | 0.0685038 0.0676915 | 0.0397165 | 0.0302826 |
| 78 79 | $0.25 \\ 0.50$ | $0.75 \\ 0.75$ | 0.1157598 0.1157598 | 0.0676915 0.0685051 | 0.0368032 0.0336568 | 0.0296063 0.0279384 |
| 80 | 0.30 | 0.75 | 0.1157598 0.1157598 | 0.0693219 | 0.0302865 | 0.0279384 0.0294390 |

