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## Problem 1

Explore order:

1 4 2 3 10 6 8 7 5 9

Value (pre, post):

vertex 1 :(1,20)

vertex 2 :(3,18)

vertex 3 :(4,17)

vertex 4 :(2,19)

vertex 5 :(9,12)

vertex 6 :(6,15)

vertex 7 :(8,13)

vertex 8 :(7,14)

vertex 9 :(10,11)

vertex 10 :(5,16)

edge classification:

tree :

[(1, 4), (2, 3), (3, 10), (4, 2), (5, 9), (6, 8), (7, 5), (8, 7), (10, 6)]

forward:

[(1, 5), (1, 6), (2, 7), (2, 9), (4, 6), (6, 9), (8, 9), (10, 8)]

back :

[(2, 4), (3, 2), (4, 1), (5, 1), (5, 7), (6, 1), (6, 4), (6, 10), (7, 2), (7, 8), (8, 6), (8, 10),  
(9, 2), (9, 5), (9, 6), (9, 8), (10, 3)]

cross

[]

## Step by Step and Call Depth

now exploring 1

depth 1

visited[1] sets True

pre[1] sets 1

clock increase from 1 to 2

**now exploring 4**

depth 2

visited[4] sets True

pre[4] sets 2

clock increase from 2 to 3

4 is already explored

**now exploring 2**

depth 3

visited[2] sets True

pre[2] sets 3

clock increase from 3 to 4

**now exploring 3**

depth 4

visited[3] sets True

pre[3] sets 4

clock increase from 4 to 5

3 is already explored

**now exploring 10**

depth 5

visited[10] sets True

pre[10] sets 5

clock increase from 5 to 6

10 is already explored

**now exploring 6**

depth 6

visited[6] sets True

pre[6] sets 6

clock increase from 6 to 7

6 is already explored

6 is already explored

**now exploring 8**

depth 7

visited[8] sets True  
pre[8] sets 7  
clock increase from 7 to 8  
8 is already explored  
**now exploring 7**  
depth 8  
visited[7] sets True  
pre[7] sets 8  
clock increase from 8 to 9  
7 is already explored  
**now exploring 5**  
depth 9  
visited[5] sets True  
pre[5] sets 9  
clock increase from 9 to 10  
5 is already explored  
5 is already explored  
**now exploring 9**  
depth 10  
visited[9] sets True  
pre[9] sets 10  
clock increase from 10 to 11  
9 is already explored  
9 is already explored  
9 is already explored  
9 is already explored  
post[9] sets 11  
clock increase from 11 to 12  
post[5] sets 12  
clock increase from 12 to 13  
7 is already explored  
post[7] sets 13  
clock increase from 13 to 14

8 is already explored  
8 is already explored  
post[8] sets 14  
clock increase from 14 to 15  
6 is already explored  
6 is already explored  
post[6] sets 15  
clock increase from 15 to 16  
10 is already explored  
post[10] sets 16  
clock increase from 16 to 17  
post[3] sets 17  
clock increase from 17 to 18  
2 is already explored  
2 is already explored  
2 is already explored  
post[2] sets 18  
clock increase from 18 to 19  
4 is already explored  
post[4] sets 19  
clock increase from 19 to 20  
1 is already explored  
1 is already explored  
post[1] sets 20

## Problem 2

Explore order:

1 3 4 10 8 2 5 6 7 9

Topologically sort:

9 7 6 5 2 1 10 8 3 4 (the reverse sort of post number)

Value (pre, post):

vertex 1 :(1,10)

vertex 2 :(11,12)

vertex 3 :(2,5)

vertex 4 :(3,4)

vertex 5 :(13,14)

vertex 6 :(15,16)

vertex 7 :(17,18)

vertex 8 :(7,8)

vertex 9 :(19,20)

vertex 10 :(6,9)

edge classification:

tree :

[(1, 3), (1, 10), (3, 4), (10, 8)]

forward:

[(1,4)]

back:

[]

cross:

[(2, 8), (5, 2), (5, 10), (6, 10), (7, 3), (7, 4), (7, 10), (8, 3), (9, 2), (9, 3), (9, 4), (9, 5),  
(9, 8), (10, 3), (10, 4)]

Determine it is acyclic:

According to text book, there are no back edges in this graph, so it is acyclic.

### **Step by Step and Call Depth**

#### **now exploring 1**

depth 1

visited[1] sets True

pre[1] sets 1

clock increase from 1 to 2

#### **now exploring 3**

depth 2

visited[3] sets True

pre[3] sets 2

clock increase from 2 to 3

**now exploring 4**

depth 3

visited[4] sets True

pre[4] sets 3

clock increase from 3 to 4

post[4] sets 4

clock increase from 4 to 5

post[3] sets 5

clock increase from 5 to 6

1 is already explored

**now exploring 10**

depth 2

visited[10] sets True

pre[10] sets 6

clock increase from 6 to 7

10 is already explored

10 is already explored

**now exploring 8**

depth 3

visited[8] sets True

pre[8] sets 7

clock increase from 7 to 8

8 is already explored

post[8] sets 8

clock increase from 8 to 9

post[10] sets 9

clock increase from 9 to 10

post[1] sets 10

clock increase from 10 to 11

**now exploring 2**

depth 1

visited[2] sets True  
pre[2] sets 11  
clock increase from 11 to 12  
2 is already explored  
post[2] sets 12  
clock increase from 12 to 13  
**now exploring 5**  
depth 1  
visited[5] sets True  
pre[5] sets 13  
clock increase from 13 to 14  
5 is already explored  
5 is already explored  
post[5] sets 14  
clock increase from 14 to 15  
**now exploring 6**  
depth 1  
visited[6] sets True  
pre[6] sets 15  
clock increase from 15 to 16  
6 is already explored  
post[6] sets 16  
clock increase from 16 to 17  
**now exploring 7**  
depth 1  
visited[7] sets True  
pre[7] sets 17  
clock increase from 17 to 18  
7 is already explored  
7 is already explored  
7 is already explored  
post[7] sets 18  
clock increase from 18 to 19

**now exploring 9**

depth 1

visited[9] sets True

pre[9] sets 19

clock increase from 19 to 20

9 is already explored

9 is already explored

9 is already explored

9 is already explored

9 is already explored

post[9] sets 20