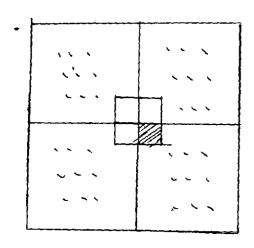
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1. ① if n=1, the board is 2x2.

It is sure that 3-gnomon can cover the board no matter which square deleted.

Dassume 27.2° can be covered as required. Let's Prove 2<sup>n+1</sup>, 2<sup>n+1</sup> can also be covered.



2<sup>n+1</sup>·2<sup>n+1</sup> board is the combination of 4 2<sup>n</sup>·2<sup>n</sup> boards. Put a 3 exgnomon in the center of 2<sup>n+1</sup>·2<sup>n+1</sup> as above. The square to the deleted is the one in shadow.

By doing this, each of the 4 2?2" boards deleted one square. Thus each of them can be covered as required according to assumption. So 2nd 2nd can be covered is proved.

2. In other files outlached.

3. a. 
$$f(n) = n^2 + f(\lceil \frac{3}{7}n \rceil)$$
.  
 $a=1$ ,  $b=\frac{7}{3}$ ,  $c=2$   
 $P = \frac{\log 1}{\log \frac{7}{3}} = 0$ .  
So  $P < C$ ,  $T(n) = (H)(n^2)$ 

b. 
$$g(n) = \lceil \sqrt{n} \rceil + 5g(L_{1}^{4}n_{1}) + pg(L_{5}^{1}n_{1})$$
  
solve  $5(\frac{4}{7})^{p} + 10 \times (\frac{1}{5})^{p} = 1$   
using Motlab  $p = 3.02 > \frac{1}{2}$   
so  $T(n) = \Theta(n^{3.02})$ .

$$\Theta 5n^{-5}+4n^{-4} \sim \Theta(n^{-4})$$

(3) 50 + 
$$\frac{\log n^2}{n}$$
 ~ (1) ( $n^{-1} \log n$ )

$$\bigoplus n \sqrt{n}$$
 $\sim \bigoplus (n^{\frac{3}{2}})$ 

$$(0.2)^{\circ}$$
  $\sim$   $(0.2)^{\circ}$ 

$$\sqrt{n!} = \sqrt{n^n e^{-n} (2\pi n)^{\frac{1}{2}}} = (n^n e^{-n} (2\pi n)^{\frac{1}{2}})^{\frac{1}{2}}$$

$$= n^{\frac{n}{2}} e^{-\frac{n}{2}} (2\pi n)^{\frac{1}{4}}$$

the decreasing order of growth is:

$$\sqrt{n!} > 10n^{6} + 5^{n} > 1.2^{n} > n^{2} \log n^{2} + n \log n$$

$$> n \sqrt{n} > (094^{n} > n^{0.2})$$

$$> \log(n + \log n) > 50 + \frac{\log n^{2}}{n}$$

$$> 5n^{-5} + 4n^{-4} > 0.2^{n}$$

$$5.1 c=3 p=8 c=\frac{5}{7}$$

$$P = log_8^3$$
  $Q = log_8^2 \sqrt{2}$  so  $P > C$ .  
 $T(N) = \Theta(n^{log_8^3})$ .

2. 
$$Q=6$$
  $b=4$   $C=1.3$ .  
 $P=109_{4}b \approx 1.292 < C$ 

$$T(n) = (H)(n^{1.3})$$

3. 
$$\frac{A=5}{5}$$
  $\frac{b=2}{5}$  formula:  $5(\frac{1}{3})^{p}+2(\frac{1}{4})^{p}=1$ .  $C=3$ 

(3) 
$$\int \Pi! \qquad ( \Pi ) \begin{pmatrix} \frac{2n+1}{4}e^{-\frac{\Lambda}{2}} \end{pmatrix} \sim ( \Pi ) \begin{pmatrix} \frac{n}{2} \end{pmatrix} \qquad ( \Pi ) \begin{pmatrix} \frac{n}{2} \end{pmatrix}$$

4. formula: 
$$2(\frac{1}{5})^{p} + 4(\frac{1}{3})^{p} = 1$$
,  $C = \frac{3}{2}$ .  
if  $p = \frac{3}{2}$ ,  $2 \times (\frac{1}{5})^{\frac{3}{6}} + 4 \times (\frac{1}{3})^{\frac{1}{6}} \approx 0.94 < 1$ .

$$T(n) = H(n^{\frac{3}{2}}).$$

formula: 
$$3(\frac{1}{5})^p + 2x(\frac{1}{4})^p + (\frac{1}{3})^p = 1$$
using mathab:  $p = 1.256$ 
According to Akara - Bazzi,  $T(n) \in (H)(n^{125})$ 

