



Department of Electrical and Computer Engineering

# ***CG2023: Signal and Systems***

**Course Instructor**

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## **AIMS & OBJECTIVES**

This is a fundamental course in signals and systems, specially developed for computer engineering students. Signals play an important role in carrying information. In particular, the idea of frequency domain analysis of signals and systems are important concepts for all computer engineers. The concepts that will be covered include time and frequency domain representations, Fourier transform, spectrum and bandwidth of a signal, frequency response of systems (Bode diagrams), sampling theorem, aliasing, signal reconstruction, and filtering.

In this course, students will learn things like:

- How to: classify signals based on their properties; apply Fourier techniques to transform signals between their time-domain (waveform) and frequency domain (spectrum) representations; evaluate the energy, power and bandwidth of signals
- How to: apply the concepts of impulse response, frequency response and transfer function to characterize linear time-invariant (LTI) systems; use frequency selective LTI systems (or filters) to shape the spectrum of a signal.
- How to model the sampling process leading to the Nyquist sampling theorem and its application for perfect signal reconstruction.

# LEARNING OUTCOMES

- ❖ Describe a signal in time and frequency domains
- ❖ Compute the Fourier Transforms of simple signals : Spectrum of Periodic and Aperiodic Signals
- ❖ Calculate the bandwidth, power and energy spectra of signals
- ❖ Describe and identify the characteristics of linear time invariant systems
- ❖ Construct the frequency response of systems via Bode plots
- ❖ Explain aliasing and evaluate the impact of the Nyquist sampling theorem

# ASSESSMENT TASKS

**Assignment (5%)**

**Midterm Quiz (20%)**

**Lab (10%)**

**Mini Project (15%)**

**Examination (50%)**

## PRE-REQUISITE

**MA1506: Mathematics II or MA1512 : Differential Equations for Engineering**

## CG2023 TIMETABLE (2021/22-II)

| DAY           |  | TUESDAY       | THURSDAY   | REMARKS                              |
|---------------|--|---------------|--|--------------------------------------|
| TIME          |  | 16:00 – 18:00 | 14:00 – 16:00  |                                      |
| VENUE         |  | zoom          | zoom   |                                      |
| DATES         | Week                                     |               |  |                                      |
|               | 01                                       | 11 Jan 2022   | 13 Jan 2022  |                                      |
|               | 02                                       | 18 Jan 2022   | 20 Jan 2022  |                                      |
|               | 03                                       | 25 Jan 2022   | 27 Jan 2022  |                                      |
|               | 04                                       | 01 Feb 2022   | 03 Feb 2022  |                                      |
|               | 05                                       | 08 Feb 2022   | 10 Feb 2022  |                                      |
|               | 06                                       | 15 Feb 2022   | 17 Feb 2022  |                                      |
|               | RECESS WEEK (19 Feb 2022 – 27 Feb 2022)  |               |  |                                      |
|               | 07                                       | 01 Mar 2022   | 03 Mar 2022  | Midterm : 3 <sup>rd</sup> March 2021 |
|               | 08                                       | 08 Mar 2022   | 10 Mar 2022  |                                      |
|               | 09                                       | 15 Mar 2022   | 17 Mar 2022  |                                      |
|               | 10                                       | 22 Mar 2022   | 24 Mar 2022  |                                      |
|               | 11                                       | 29 Mar 2022   | 31 Mar 2022  |                                      |
|               | 12                                       | 05 Apr 2022   | 07 Apr 2022  |                                      |
|               | 13                                       | 12 Apr 2022   | No classes   |                                      |
|               | READING WEEK (16 Apr 2022 – 22 Apr 2022) |               |  |                                      |
| EXAMINATION → |  |               | Date: 27 April 2022 (Wednesday)<br>Time: 13:00 – 15:00 (120 minutes) |                                      |

# TABLE OF CONTENTS

| TOPICS   | Page |
|--|------|
| <b>1. Signals and Classification of Signals</b>                            | 1-1  |
| 1.1 Signals  | 1-1  |
| 1.1.1 Classification of Signals  | 1-2  |
| 1.2 Basic Signals  | 1-14 |
| 1.3 Time-Scaling, -Reversal and -Shifting of Signals                       | 1-19 |
| <i>End of Chapter</i>  | 1-21 |
| <b>2. Discrete-Frequency Spectrum (Fourier Series)</b>                     | 2-1  |
| 2.1 What is a Spectrum in the Context of Signals?                          | 2-1  |
| 2.2 Spectrum of a Sinusoid   | 2-2  |
| 2.2.1 Complex Exponentials and Phasors (The concept of negative frequency) | 2-6  |
| 2.3 Fourier Series   | 2-7  |
| 2.3.1 Complex Exponential Fourier Series                                   | 2-7  |
| 2.3.2 Trigonometric Fourier Series   | 2-9  |
| <i>End of Chapter</i>  | 2-14 |
| <b>3. Continuous-Frequency Spectrum (Fourier Transform)</b>                | 3-1  |
| 3.1 Fourier Transform  | 3-1  |
| 3.2 Properties of Fourier Transform  | 3-8  |
| 3.3 Spectral Properties of a REAL Signal                                   | 3-19 |
| 3.4 The Dirac- $\delta$ and Spectrum of Periodic Signals                   | 3-23 |
| 3.4.1 The Continuous-time Unit Impulse (Dirac- $\delta$ function)          | 3-23 |

| TOPICS  | Page |
|---|------|
| 3.4.2 Spectrum of Periodic Signals                                  | 3-26 |
| <i>End of Chapter</i>   | 3-31 |
| <b>4. ESD, PSD and Bandwidth</b>                                    | 4-1  |
| 4.1 Energy Spectral Density (ESD) - - - a.k.a. Energy Spectrum      | 4-1  |
| 4.2 Power Spectral Density (PSD) - - - a.k.a. Power Spectrum        | 4-4  |
| 4.2.1 PSD of Periodic Signals                                       | 4-7  |
| 4.3 Bandwidth   | 4-10 |
| 4.3.1 Bandlimited Signals   | 4-10 |
| 4.3.2 Signals with Unrestricted Band                                | 4-13 |
| <i>End of Chapter</i>   | 4-17 |
| <b>5. Systems and Classification of Systems</b>                     | 5-1  |
| 5.1 Systems   | 5-1  |
| 5.1.1 Classification of Systems                                     | 5-2  |
| 5.2 Remarks   | 5-7  |
| <i>End of Chapter</i>   | 5-7  |
| <b>6. Linear Time-Invariant Systems</b>                             | 6-1  |
| 6.1 Impulse Response  | 6-2  |
| 6.2 Frequency Response  | 6-5  |
| 6.2.1 Notation for Expressing Fourier Transform in $\omega$ -domain | 6-7  |
| 6.3 Bode Diagram  | 6-10 |
| 6.3.1 Transfer Function   | 6-11 |
| 6.3.2 Construction of Straight-line Bode Plots                      | 6-14 |

| TOPICS   | Page |
|--|------|
| 6.3.3 Resonance in Second Order Systems                      | 6-29 |
| 6.3.4 Asymptotic Behavior of Bode Straight-line Plots        | 6-32 |
| <i>End of Chapter</i>  | 6-34 |
| <b>7. Sampling Theorem</b>                                   | 7-1  |
| 7.1 Idealized Filters  | 7-2  |
| 7.2 Continuous-time Sampling and Reconstruction of Signals   | 7-4  |
| 7.3 Sampling Band-limited Bandpass Signal below Nyquist Rate | 7-10 |
| <i>End of Chapter</i>  | 7-13 |



# REFERENCES

1. Hwei Hsu, Schaum's Outline of Signals and Systems, McGraw Hill.
2. Erhan Kudeki and David C. Munson, Jr, Analog Signals and Systems, Pearson Prentice Hall.

# PRE-REQUISITE KNOWLEDGE

## ❖ Calculus

## ❖ Complex number arithmetic and Complex functions

- Cartesian form ( $z = \text{Re}[z] + j \text{Im}[z]$ )
- Polar form ( $z = |z| \exp(j\angle z)$ )
- Relationship between Polar and Cartesian form  $\left[ \exp(j\theta) = \cos(\theta) + j \sin(\theta) \right]$   
*..... Euler's Formula .....*

## ❖ Sinusoids: $A \sin(\omega t + \phi)$ , $A \cos(\omega t + \phi)$ and $A \exp[j(\omega t + \phi)]$

- Converting between cyclic frequency and angular frequency
- Converting between period and frequency