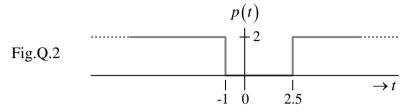
## **CG2023 TUTORIAL 1 (PROBLEMS)**

- Q.1 Let z = x + jy be a complex number where x and y are its real and imaginary parts, respectively. Provide a formula for computing the distinct values of  $z^{1/N}$  where N is a positive integer. Hence, or otherwise, determine  $64^{1/6}$  and  $\left(j81\right)^{1/4}$ .
- Q.2 Consider the signal  $x(t) = 2\sin(\pi t)(p(t)-1)$  where p(t) is shown in Fig.Q.2.

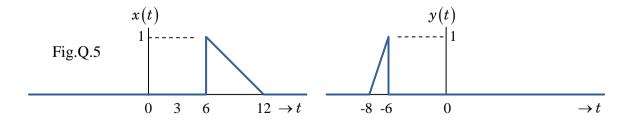


- (a) Express p(t) in terms of the rect( $\bullet$ ) function.
- (b) Sketch and label x(t) and state whether or not x(t) is periodic.
- (c) Find an expression for  $x^2(t)$ . Hence, compute the average power of x(t).
- (d) Based on the results in (b) and (c), How would you classify x(t)?
- Q.3 In digital communications, half-cosine or raised-cosine pulses are sometimes used to pulse shape a binary waveform so as to reduce intersymbol interference. The general expressions for these pulses are

Half-cosine pulse : 
$$x(t) = A\cos(\pi t/T)\operatorname{rect}(t/T)$$
  
Raised-cosine pulse :  $\tilde{x}(t) = 0.5\tilde{A}(1+\cos(2\pi t/\tilde{T}))\operatorname{rect}(t/\tilde{T})$ .

where A,  $\tilde{A}$ , T and  $\tilde{T}$  are positive constants. Sketch and label each pulse. Under what condition(s) will both pulses have the same energy?

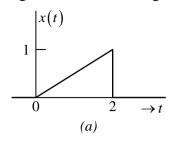
- Q.4 Show that the same pattern of values of the signal  $x(t) = \cos(3.2t) + \sin(1.6t) + \exp(j2.8t)$  is repeated every  $5n\pi$  seconds, where n is any positive integer.
- Q.5 Sketches of two signals, x(t) and y(t), are shown in Fig.Q.5. Express y(t) in terms of x(t).

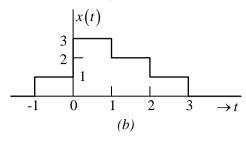


## Supplementary Problems

These problems are for self practice.

Express the signals shown in the figures below in terms of unit step functions. S.1





- Answer: (a)  $x(t) = u(2-t) \cdot \int_{-\infty}^{t} 0.5u(\tau) d\tau$ 
  - (b) x(t) = u(t+1) + 2u(t) u(t-1) u(t-2) u(t-3)
- Evaluate the following integrals:

- (a)  $\int_{-\infty}^{t} \cos(\tau) u(\tau) d\tau$  (b)  $\int_{-\infty}^{t} \cos(\tau) \delta(\tau) d\tau$  (c)  $\int_{-\infty}^{\infty} \cos(t) u(t-1) \delta(t) dt$  (d)  $\int_{0}^{2\pi} t \sin(\frac{t}{2}) \delta(\pi-t) dt$

- Answer: (a)  $\sin(t)u(t)$  (b) u(t)
- - (c) 0
- (d)  $\pi$
- S.3 Any signal x(t) can be expressed as a sum of two component signals, one of which is even and one of which is odd. That is

$$x(t) = x_e(t) + x_o(t)$$

where  $x_e(t) = 0.5[x(t) + x(-t)]$  is the even component and  $x_o(t) = 0.5[x(t) - x(-t)]$  the odd component.

Determine the even and odd components of : (a) x(t) = u(t) (b)  $x(t) = \sin(\omega_c t + \frac{\pi}{4})$ 

Answer: (a) 
$$\begin{cases} x_{e}(t) = \begin{cases} 1; & t = 0 \\ 0.5; & t \neq 0 \end{cases} \\ x_{o}(t) = \begin{cases} 0; & t = 0 \\ 0.5 \operatorname{sgn}(t); & t \neq 0 \end{cases} \end{cases}$$
 (b) 
$$\begin{cases} x_{e}(t) = \frac{1}{\sqrt{2}} \cos(\omega_{c}t) \\ x_{o}(t) = \frac{1}{\sqrt{2}} \sin(\omega_{c}t) \end{cases}$$

(b) 
$$\begin{cases} x_e(t) = \frac{1}{\sqrt{2}}\cos(\omega_c t) \\ x_o(t) = \frac{1}{\sqrt{2}}\sin(\omega_c t) \end{cases}$$

Below is a list of solved problems selected from Chapter 1 of Hwei Hsu (PhD), 'The Schaum's series on Signals & Systems, 2<sup>nd</sup> Edition.

Selected solved-problems: 1.1, 1.9, 1.10, 1.14, 1.16(a)-to-(f), 1.17, 1.18, 1.20(a)-&-(b), 1.21, 1.22, 1.27, 1.30, 1.31

These solved problems should be treated as supplementary module material catered for students who find the need for more examples or practice-problems.