

## Questions to be discussed: 1, 2, 3, 4

1. Consider the following relation instance  $r$  of the relational schema  $R(A, B, C, D)$ .

| R |   |   |   |
|---|---|---|---|
| A | B | C | D |
| 8 | 6 | 1 | 7 |
| 0 | 4 | 1 | 9 |
| 8 | 6 | 1 | 7 |
| 8 | 5 | 2 | 7 |

List all the functional dependencies of the form  $\alpha \rightarrow \beta$  where  $\alpha \subseteq R^1$  and  $\beta \in R$  that *definitely* do not hold on  $R$ . In fact, this can be symbolised as  $\alpha \nrightarrow \beta$ .

2. Consider the relational schema  $R$  and let  $a, b, c, d \subseteq R$ . Use only Armstrong's axioms to prove the soundness of the following two inference rules:

(a) *Pseudo Transitivity*: If  $a \rightarrow b$  and  $bc \rightarrow d$ , then  $ac \rightarrow d$ .

(b) *Composition Rule*: If  $a \rightarrow b$  and  $c \rightarrow d$ , then  $ac \rightarrow bd$ .

You can try writing the proofs move systematically at <https://www.comp.nus.edu.sg/~adi-yoga/CS2102/FD/>.

3. Consider  $R(A, B, C, D, E, G)^2$  with set of functional dependencies  $F = \{ABC \rightarrow E, BD \rightarrow A, CG \rightarrow B\}$ .

(a) Use Armstrong's axioms to show that  $F$  implies  $CDG \rightarrow E$ .

(b) Compute  $\{CDG\}^+$ .

(c) Find all the keys of  $R$ .

You can try writing the proofs move systematically at <https://www.comp.nus.edu.sg/~adi-yoga/CS2102/FD/>.

4. Consider  $R(A, B, C, D, E)$  with set of functional dependencies  $F = \{AB \rightarrow CDE, AC \rightarrow BDE, B \rightarrow C, C \rightarrow B, C \rightarrow D, B \rightarrow E\}$ .

Find all the keys of  $R$ .

<sup>1</sup>Basically,  $\alpha$  is a *set of attributes* and  $\beta$  is a *single attribute*.

<sup>2</sup>Why  $G$  and not  $F$ ? We reserve  $F$  for the set of functional dependencies.