

4. a)

x_1	x_2	x_3	$x_1 \vee x_2$	$x_1 \Rightarrow x_3$	$\neg x_2$	KB	α
T	T	T	T	T	F	F	T
T	T	F	T	F	F	F	T
T	F	T	T	T	T	T	T
T	F	F	T	F	T	F	F
F	T	T	T	T	F	F	T
F	T	F	T	T	F	F	T
F	F	T	F	T	T	F	T
F	F	F	F	T	T	F	F

$$KB = (x_1 \vee x_2) \wedge (x_1 \Rightarrow x_3) \wedge \neg x_2$$

$$\alpha = x_3 \vee x_2$$

$$M(KB) \subseteq M(\alpha) \Rightarrow KB \models \alpha$$

when KB is T, α is T

b)

x_1	x_2	x_3	$x_1 \vee x_3$	$x_1 \Rightarrow \neg x_2$	KB	α
T	T	T	T	F	F	F
T	T	F	T	F	F	F
T	F	T	T	T	T	T
T	F	F	T	T	T	T
F	T	T	T	T	T	F
F	T	F	F	T	F	F
F	F	T	T	T	T	T
F	F	F	F	T	F	T

$$KB = (x_1 \vee x_3) \wedge (x_1 \Rightarrow \neg x_2)$$

$$\alpha = \neg x_2$$

$$M(KB) \not\subseteq M(\alpha) \Rightarrow KB \not\models \alpha$$

when $x_1 = F, x_2 = T, x_3 = T$, KB is T but $\alpha = F$