

BL2

$D: \{ \langle \langle 0, 0 \rangle, 1 \rangle, \langle \langle 0, 1 \rangle, 0 \rangle, \langle \langle 1, 0 \rangle, 1 \rangle, \langle \langle 1, 1 \rangle, 1 \rangle \}$

H: Each hypothesis $h \in H$ ($h : X \rightarrow \{0, 1\}$) is represented by a conjunction of constraints on input

- a) $h_0 = \langle \text{null}, \text{null} \rangle$
 $h_1 = \langle 0, 0 \rangle$
 $h_2 = \langle 0, 0 \rangle$
 $h_3 = \langle ?, 0 \rangle$
 $h_4 = \langle ?, ? \rangle$
- b) h_4 is not consistent with D as $\langle 0, 1 \rangle$ satisfies h_4 ($h_4(\langle 0, 1 \rangle) = 1$ but $c(\langle 0, 1 \rangle) = 0$). Hence, $h(x) \neq c(x)$ for $\langle 0, 1 \rangle, 0 \rangle \in D$.
- c) Proposition 2 states that if $c \in H$, then h_n is consistent with D . However, the actual target concept $c \notin H$ since $c(\langle 0, 1 \rangle) = 0$ and $c(x) = 1$ for all other x cannot be represented as a conjunction of constraints on the input attributes. Hence, the implication stated by the proposition is vacuously true and not a contradiction.

BL3

- a) Prove that h is consistent with all positive training examples observed so far, not including d .
 - 1. For all $s \in S$, s is consistent with all training examples observed so far. (def of S)
 - 2. Every positive training instance so far, not including d , satisfies s (by Proposition 1)
 - 3. Since h is a minimal generalization of s , h is more general than s .
 - 4. For all $x \in X$, $s(x) = 1 \rightarrow h(x) = 1$. (def of more general)
 - 5. Every positive training instance observed so far, not including d , satisfies h .
 - 6. Thus, h is consistent with all positive training examples observed thus far, not including d (Proposition 1)
- b) Prove that h is consistent with all negative training examples observed so far.
 - 1. For all $g \in G$, g is consistent with all training examples observed so far. (def of G)
 - 2. Every negative training instance so far does not satisfy g (by Proposition 1)
 - 3. Since some member of G is more general than h , for all $x \in X$, $h(x) = 1 \rightarrow g(x) = 1$. (def of more general)
 - 4. for all $x \in X$, $g(x) = 0 \rightarrow h(x) = 0$. (contrapositive of 3.)
 - 5. Every negative training instance observed so far does not satisfy h .

6. Thus, h is consistent with all negative training examples observed thus far (Prop 1)

TM2.3

X1 = <Sunny, Warm, Normal, Strong, Warm, Same> +ve

X2 = <Sunny, Warm, High, Strong, Warm, Same> +ve

X3 = <Rainy, Cold, High, Strong, Warm, Change> -ve

X4 = <Sunny, Warm, High, Strong, Cool, Change> +ve

S0 = {<null, null, null, null, null, null> V <null, null, null, null, null, null>}

S1 = {<Sunny, Warm, Normal, Strong, Warm, Same> V <null, null, null, null, null, null>}

S2 = {<Sunny, Warm, Normal, Strong, Warm, Same> V <Sunny, Warm, High, Strong, Warm, Same>, <Sunny, Warm, ?, Strong, Warm, Same> V <null, null, null, null, null, null>}

S3 = {<Sunny, Warm, Normal, Strong, Warm, Same> V <Sunny, Warm, High, Strong, Warm, Same>, <Sunny, Warm, ?, Strong, Warm, Same> V <null, null, null, null, null, null>}

S4 = {<Sunny, Warm, ?!, Strong, ?, ?> V <Sunny, Warm, High, Strong, Warm, Same>, <Sunny, Warm, Normal, Strong, Warm, Same> V <Sunny, Warm, High, Strong, ?, ?>, <Sunny, Warm, ?, Strong, Warm, Same> V <Sunny, Warm, High, Strong, Cool, Change>}

G4 = {<Sunny, ?, ?, ?, ?, ?> V <Cloudy, ?, ?, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, Warm, ?, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, Normal, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, Weak, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, ?, Cool, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, ?, Same>, <Cloudy, ?, ?, ?, ?, ?> V <?, Warm, ?, ?, ?, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, Normal, ?, ?, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, Weak, ?, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, ?, Cool, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, ?, Same>, <?, ?, ?, ?, Cool, ?> V <?, ?, ?, ?, Same>}

G3 = {<Sunny, ?, ?, ?, ?, ?> V <Cloudy, ?, ?, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, Warm, ?, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, Normal, ?, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, Weak, ?, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, ?, Cool, ?>, <Sunny, ?, ?, ?, ?, ?> V <?, ?, ?, ?, Same>, <Cloudy, ?, ?, ?, ?, ?> V <?, Warm, ?, ?, ?, ?>, <Cloudy, ?, ?, ?, ?, ?> V <?, ?, ?, ?, Same>, <?, Warm, ?, ?, ?, ?> V <?, ?, Normal, ?, ?, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, Weak, ?, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, ?, Cool, ?>, <?, Warm, ?, ?, ?, ?> V <?, ?, ?, ?, Same>, <?, ?, Normal, ?, ?, ?> V <?, ?, ?, ?, Same>, <?, ?, ?, Weak, ?, ?> V <?, ?, ?, ?, Same>, <?, ?, ?, ?, Cool, ?> V <?, ?, ?, ?, Same>}

G2 = {<?, ?, ?, ?, ?, ?> V <?, ?, ?, ?, ?, ?>}

G1 = {<?, ?, ?, ?, ?, ?> V <?, ?, ?, ?, ?, ?>}

G0 = {<?, ?, ?, ?, ?, ?> V <?, ?, ?, ?, ?, ?>}