

ST2334

R commands to find probabilities and quantiles for some common distributions

Reference: <http://127.0.0.1:31680/library/stats/html/Distributions.html>

This document is for students who want to use R to find probabilities and quantiles

$X \sim \text{Binomial}(n, p)$, where x is the number of successes, n is the number of trials and p is the probability of a success.

To find $\Pr(X \leq x)$, R command: `pbinom(x,n,p,lower=T)`

Example: To find $\Pr(X \leq 5)$ with $n=10$ and $p=0.4$, '`pbinom(5,10,0.4,lower=T)`' gives 0.8337614 .

To find $\Pr(X = x)$, R command: `dbinom(x,n,p)`

Example: To find $\Pr(X = 5)$ with $n=10$ and $p=0.4$, '`dbinom(5,10,0.4)`' gives 0.2006581 .

To find $\Pr(X > x)$, R command: `pbinom(x,n,p,lower=F)`

Example: To find $\Pr(X > 5)$ with $n=10$ and $p=0.4$, '`pbinom(5,10,0.4,lower=F)`' gives 0.1662386 .

To find x such that $\Pr(X \leq x) = a$, R command: `qbinom(a,n,p,lower=T)`, where n is the number of trials and p is the probability of a success.

Example: Find x such that x satisfies $\Pr(X \leq x) \geq 0.05$. '`qbinom(0.05,10,0.4,lower=T)`' gives 2 which means that $\Pr(X \leq 2) \geq 0.05$.

Note: Since Binomial is a discrete distribution, we could not find an x -value such that $\Pr(X \leq x) = 0.05$.

$x=2$ is the smallest value for x such that $\Pr(X \leq 2)$ is at least 5%

That is, $\Pr(X \leq 2) = 0.1672898$ and $\Pr(X \leq 1) = 0.0463574$.

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$X \sim \text{Negative Binomial}(k, p)$, where X is the number of trials, k is the number of successes and p is the probability of a success

To find $\Pr(X \leq x)$, R command: `pnbinom(x-k,k,p,lower=T)`, where $x-k$ and k are the number of failures and the number of successes in x trials respectively.

Example: To find $\Pr(X \leq 6)$ with $k=4$ and $p=0.55$, '`pnbinom(2,4,0.55)`' gives 0.4415177 .

To find $\Pr(X = x)$, R command: `dnbinom(x-k,k,p)`, where $x-k$ = number of failures in x trials.

Example: To find $\Pr(X = 6)$ with $k=4$ and $p=0.55$, '`dnbinom(2,4,0.55)`' gives 0.1853002

To find $\Pr(X > x)$, R commands: `pnbinom(x-k,k,p,lower=F)`, where $x-k$ = number of failures in x trials.

Example: To find $\Pr(X > 6)$ with $k=4$ and $p=0.55$, '`pnbinom(2,4,p,lower=F)`' gives 0.5584823 .

To find x such that $\Pr(X \leq x) = a$, R command: `qnbinom(a,k,p,lower=T)`, where a = probability, k = number of successes, p = probability of a success

Example: To find x such that $\Pr(X \leq x) = 0.25$ with $k=4$ and $p=0.55$,

'`qnbinom(0.25,4,0.55,lower=T)`' gives 1 which means that $\Pr(X \leq 1 + 4) = \Pr(X \leq 5) \geq 0.25$

Note: Since Negative Binomial is a discrete distribution, we could not find an x -value such that $\Pr(X \leq x) = 0.25$.

$x = 5$ is the smallest value for x such that $\Pr(X \leq x)$ is at least 0.25

That is, $\Pr(X \leq 5) = 0.2562175$ and $\Pr(X \leq 4) = 0.09150625$.

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R commands

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$X \sim \text{Poisson}(\lambda)$, where X is the number of successes, λ is the mean, $E(X)$.

To find $\Pr(X \leq x)$, R command: `ppois(x,lambda,lower=T)`, where x = number of successes, λ is the mean and `lower=T` gives the lower tail probability

Example: To find $\Pr(X \leq 6)$ with $\lambda=8$, '`ppois(6,8)`' gives 0.3133743

To find $\Pr(X = x)$, R command: `dpois(x,lambda)`, where x = number of successes and λ is the mean

Example: To find $\Pr(X = 6)$ with $\lambda=8$, '`dpois(6,8)`' gives 0.1221382

To find $\Pr(X > x)$, R commands: `ppois(x,lambda,lower=F)`, where x = number of successes and λ is the mean

Example: To find $\Pr(X > 6)$ with $\lambda=8$, '`ppois(6,8,lower=F)`' gives 0.6866257

To find x such that $\Pr(X \leq x) = a$, R command: `qpois(a,lambda,lower=T)`, where a = probability, x = number of successes, $\lambda = E(X)$

Example: To find x such that $\Pr(X \leq x) = 0.25$ with $\lambda=8$, '`qpois(0.25,8,lower=T)`' gives 6 which means that $\Pr(X \leq 6) \geq 0.25$

Note: Since Poisson is a discrete distribution, we could not find an x -value such that $\Pr(X \leq x) = 0.25$.

$x = 6$ is the smallest value for x such that $\Pr(X \leq x)$ is at least 0.25 .

That is, $\Pr(X \leq 6) = 0.3133743$ and $\Pr(X \leq 5) = 0.1912361$.

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$X \sim \text{Exponential}(\alpha)$, where X is the time to occur, $\alpha = 1/\text{mean} = 1/E(X)$.

To find $\Pr(X \leq x)$, R command: `pexp(x,alpha,lower=T)`, where X is the time to occur, $\alpha = 1/\text{mean}$ and `lower=T` gives the lower tail probability

Example: To find $\Pr(X \leq 8)$ with $\alpha = 1/5$ or $\text{mean} = 5$, '`pexp(8,1/5)`' gives 0.7981035

To find the pdf $f_X(x)$, R command: `dexp(x,alpha)`, where X is the time to occur and $\alpha = 1/\text{mean}$.

Example: To find the pdf $f_X(8)$ with $\alpha = 1/5$ or $\text{mean} = 5$, '`dexp(8,1/5)`' gives 0.0403793

To find $\Pr(X > x)$, R commands: `1-pexp(x,alpha,lower=F)`, where x = the time to occur and $\alpha = 1/\text{mean}$

Example: To find $\Pr(X > 8)$ with $\alpha = 1/5$ or $\text{mean} = 5$, '`pexp(8,1/5,lower=F)`' gives 0.2018965

To find x such that $\Pr(X \leq x) = a$, R command: `qexp(a,alpha,lower=T)`, where a = probability, x = the time to occur and $\alpha = 1/\text{mean}$

Example: To find x such that $\Pr(X \leq x) = 0.05$ with $\alpha = 1/5$ or $\text{mean} = 5$, '`qexp(0.05,1/5,lower=T)`' gives 0.2564665 which means that $\Pr(X \leq 0.2564665) = 0.05$

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$X \sim \text{Normal}(\mu, \sigma^2)$, where $\mu = E(X)$, $\sigma^2 = \text{Var}(X)$.

To find $\Pr(X \leq x)$, R command: `pnorm(x, mu, sigma, lower=T)`, where $E(X) = \mu$, $\text{Var}(X) = \sigma^2$.

Example: To find $\Pr(X \leq 45)$ with $\mu = 50$ and $\sigma = 10$, '`pnorm(45,50,10,lower=T)`' gives 0.3085375

To find the pdf $f_X(x)$, R command: `dnorm(x, mu, sigma)`, where $X \sim N(\mu, \sigma^2)$.

Example: To find the pdf $f_X(45)$ with $\mu = 50$ and $\sigma = 10$, '`dnorm(45,50,10)`' gives 0.03520653

To find $\Pr(X > x)$, R command: `pnorm(x, mu, sigma, lower=F)`, where $X \sim N(\mu, \sigma^2)$.

Example: To find $\Pr(X > 45)$ with $\mu = 50$ and $\sigma = 10$, '`pnorm(45,50,10,lower=F)`' gives 0.6914625

To find x such that $\Pr(X \leq x) = a$, R command: `qnorm(a, mu, sigma, lower=T)`, where $a =$ probability, $X \sim N(\mu, \sigma^2)$.

Example: To find x such that $\Pr(X \leq x) = 0.05$ with $X \sim N(50, 10^2)$.

'`qnorm(0.05,50,10,lower=T)`' gives 33.55146 which means that $\Pr(X \leq 33.55146) = 0.05$

Example: To find $z_{(0.05)}$ such that $\Pr(Z \geq z_{(0.05)}) = 0.05$ with $Z \sim N(0, 1)$,

'`qnorm(0.05,0,1,lower=F)`' gives 1.644854 .

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$X \sim t(v)$, where v is the degrees of freedom.

To find $\Pr(X \leq x)$, R command: `pt(x, v, lower=T)`, where v is the degrees of freedom.

Example: To find $\Pr(X \leq 1.5)$ with $v = 10$, '`pt(1.5,10,lower=T)`' gives 0.9177463 .

To find the pdf $f_X(x)$, R command: `dt(x, v)`, where $X \sim t(10)$.

Example: To find the pdf $f_X(1.5)$ with $v = 10$, '`dt(1.5,10)`' gives 0.1274448 .

To find $\Pr(X > x)$, R commands: `1-pt(x, v, lower=T)`, where $X \sim t(v)$.

Example: To find $\Pr(X > 1.5)$ with $v = 10$, '`pt(1.5,10,lower=F)`' gives 0.08225366 .

To find x such that $\Pr(X \leq x) = a$, R command: `qt(a, v, lower=T)`, where $a =$ probability, $X \sim t(v)$.

Example: To find x such that $\Pr(X \leq x) = 0.05$ with $X \sim t(10)$. '`qt(0.05,10,lower=T)`' gives -1.812461 which means that $\Pr(X \leq -1.812461) = 0.05$.

Example: To find $t_{(0.05,10)}$ such that $\Pr(T \geq t_{(0.05,10)}) = 0.05$ with $T \sim t(10)$,

'`qt(0.05,10,lower=F)`' gives 1.812461 .

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$X \sim \text{chisq}(v)$, where v is the degrees of freedom.

To find $\Pr(X \leq x)$, R command: `pchisq(x, v, lower=T)`, where v is the degrees of freedom.

Example: To find $\Pr(X \leq 12)$ with $v = 10$, '`pchisq(12,10,lower=T)`' gives 0.7149435

To find the pdf $f_X(x)$, R command: `dchisq(x, v)`, where $X \sim \text{chisq}(v)$.

Example: To find the pdf $f_X(12)$ with $v=10$, '`dchisq(12,10)`' gives 0.06692631

To find $\Pr(X > x)$, R commands: `pchisq(x,v,lower=F)`, where $X \sim \text{chisq}(v)$.

Example: To find $\Pr(X > 12)$ with $v=10$, '`pchisq(12,10,lower=F)`' gives 0.2850565

To find x such that $\Pr(X \leq x) = a$, R command: `qchisq(a,v,lower=T)`, where a = probability, $X \sim \text{chisq}(v)$.

Example: To find x such that $\Pr(X \leq x) = 0.05$ with $X \sim \text{chisq}(10)$. '`qchisq(0.05,10,lower=T)`' gives 3.940299 which means that $\Pr(X \leq 3.940299) = 0.05$

Example: To find $\text{chisq}_\alpha(0.05,10)$ such that $\Pr(W \geq \text{chisq}_\alpha(0.05,10)) = 0.05$ with $W \sim \text{chisq}(10)$, '`qchisq(0.05,10,lower=F)`' gives 18.30704 .

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$X \sim F(v_1, v_2)$, where v_1 and v_2 are the degrees of freedom.

To find $\Pr(X \leq x)$, R command: `pf(x,v1,v2,lower=T)`, where v_1 and v_2 are the degrees of freedom.

Example: To find $\Pr(X \leq 3)$ with $v_1=12$, $v_2=10$, '`pf(3,12,10,lower=T)`' gives 0.9542993

To find the pdf $f_X(x)$, R command: `df(x,v1,v2)`, where $X \sim F(12,10)$.

Example: To find the pdf $f_X(3)$ with $v_1=12$, $v_2=10$, '`df(3,12,10)`' gives 0.046852

To find $\Pr(X > x)$, R commands: `pf(x,v1,v2,lower=F)`, where $X \sim F(v_1, v_2)$.

Example: To find $\Pr(X > 3)$ with $v_1=12$, $v_2=10$, '`pf(3,12,10,lower=F)`' gives 0.04570066

To find x such that $\Pr(X \leq x) = a$, R command: `qf(a,v1,v2,lower=T)`, where a = probability, $X \sim F(v_1, v_2)$.

Example: To find x such that $\Pr(X \leq x) = 0.05$ with $X \sim F(12,10)$. '`qf(0.05,12,10,lower=T)`' gives 0.3631891 which means that $\Pr(X \leq 0.3631891) = 0.05$

Example: To find $f_\alpha(0.05,12,10)$ such that $\Pr(F \geq f_\alpha(0.05,12,10)) = 0.05$ with $F \sim F(12,10)$, '`qf(0.05,12,10,lower=F)`' gives 2.912977 .