

ST2334

Python code to find probabilities and quantiles for some common distributions

Reference: <https://docs.scipy.org/doc/scipy/reference/stats.html>

This document is for students who want to use Python to find probabilities and quantiles.

import the following library

from scipy import stats

$X \sim B(10, 0.4)$, where X = number of successes, with number of trials = 10 and prob of a success = 0.4

To find $\Pr(X \leq 5)$, 'stats.binom.cdf(5,10,0.4)' gives 0.833761

To find $\Pr(X = 5)$, 'stats.binom.pmf(5,10,0.4)' gives 0.200658

To find $\Pr(X > 5)$, '1-stats.binom.cdf(5,10,0.4)' gives 0.166239

To find x such that $\Pr(X \leq x) \geq 0.05$, 'stats.binom.ppf(0.05,10,0.4)' gives 2

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$X \sim NB(4, 0.55)$, where X = number of trials, with number of successes = 4 and prob of a success = 0.55

To find $\Pr(X \leq 6)$, 'stats.nbinom.cdf(2,4,0.55)' gives 0.441518 , where 2 = number of failures

To find $\Pr(X = 6)$, 'stats.nbinom.pmf(2,4,0.55)' gives 0.1853

To find $\Pr(X > 6)$, '1-stats.nbinom.cdf(2,4,0.55)' gives 0.558482

To find x such that $\Pr(X \leq x) \geq 0.25$, 'stats.binom.ppf(0.25,4,0.55)' gives 1 which is the number of failures. Hence, $x = 5$

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$X \sim P(8)$, where $E(X) = \lambda = 8$

To find $\Pr(X \leq 6)$, 'stats.poisson.cdf(6,8)' gives 0.313374

To find $\Pr(X = 6)$, 'stats.poisson.pmf(6,8)' gives 0.122138

To find $\Pr(X > 6)$, '1-stats.poisson.cdf(6,8)' gives 0.686626

To find x such that $\Pr(X \leq x) \geq 0.25$, 'stats.poisson.ppf(0.25,8)' gives 6

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$X \sim \text{Exp}(1/5)$, where $E(X) = 5$

To find $\Pr(X \leq 8)$, 'stats.expon.cdf(8,0.5)' gives 0.798103 with the second argument being the lower limit of the x range and 3rd argument = $E(X)$

To find pdf $f(8)$, 'stats.expon.pdf(8,0.5)' gives 0.0403793

To find $\Pr(X > 8)$, '1-stats.expon.cdf(8,0.5)' gives 0.201897

To find x such that $\Pr(X \leq x) = 0.05$, 'stats.expon.ppf(0.05,0.5)' gives 0.256466

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Python code

$X \sim N(50, 10^2)$, where $\mu=E(X)=50$ and $\sigma^2=V(X)=10^2$

To find $\Pr(X \leq 45)$, 'stats.norm.cdf(45,50,10)' gives 0.308538

To find pdf $f(45)$, 'stats.norm.pdf(45,50,10)' gives 0.0352065

To find $\Pr(X > 45)$, '1-stats.norm.cdf(45,50,10)' gives 0.691462

To find x such that $\Pr(X \leq x) = 0.05$, 'stats.norm.ppf(0.05,50,10)' gives 33.5515

To find z such that $\Pr(Z \geq z) = 0.05$ with $Z \sim N(0,1)$, 'stats.norm.ppf(0.95,0,1)' gives 1.64485

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$X \sim t(10)$, where degrees of freedom = 10

To find $\Pr(X \leq 1.5)$, 'stats.t.cdf(1.5,10)' gives 0.917746

To find pdf $f(1.5)$, 'stats.t.pdf(1.5,10)' gives 0.127445

To find $\Pr(X > 1.5)$, '1-stats.t.cdf(1.5,10)' gives 0.0822537

To find x such that $\Pr(X \leq x) = 0.05$, 'stats.t.ppf(0.05,10)' gives -1.81246

To find x such that $\Pr(X \geq x) = 0.05$, 'stats.t.ppf(0.95,10)' gives 1.81246

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$X \sim \text{Chisq}(10)$, where degrees of freedom = 10

To find $\Pr(X \leq 12)$, 'stats.chi2.cdf(12,10)' gives 0.714943

To find pdf $f(12)$, 'stats.chi2.pdf(12,10)' gives 0.0669263

To find $\Pr(X > 12)$, '1-stats.chi2.cdf(12,10)' gives 0.285057

To find x such that $\Pr(X \leq x) = 0.05$, 'stats.chi2.ppf(0.05,10)' gives 3.9403

To find x such that $\Pr(X \geq x) = 0.05$, 'stats.chi2.ppf(0.95,10)' gives 18.307

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$X \sim F(12,10)$, where degrees of freedom are 12 and 10

To find $\Pr(X \leq 3)$, 'stats.f.cdf(3,12,10)' gives 0.954299

To find pdf $f(3)$, 'stats.f.pdf(3,12,10)' gives 0.046852

To find $\Pr(X > 3)$, '1-stats.f.cdf(3,12,10)' gives 0.0457007

To find x such that $\Pr(X \leq x) = 0.05$, 'stats.f.ppf(0.05,12,10)' gives 0.363189

To find x such that $\Pr(X \geq x) = 0.05$, 'stats.f.ppf(0.95,10)' gives 2.91298