

GSMR

Generalised Summary-data-based
Mendelian Randomisation

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Overview

The **gsmr** R-package implements the GSMR (Generalised Summary-data-based Mendelian Randomisation) method to test for putative causal association between a risk factor and a disease using summary-level data

from genome-wide association studies (GWAS) ([Zhu et al. 2018 Nat. Commun.](#)). The R package is developed by [Zhihong Zhu](#), [Zhili Zheng](#), [Futao Zhang](#) and [Jian Yang](#) at Institute for Molecular Bioscience, the University of Queensland. Bug reports or questions: jian.yang@uq.edu.au.

Citation

Zhu, Z. et al. (2018) Causal associations between risk factors and common diseases inferred from GWAS summary data. Nat. Commun. 9, 224 (<https://www.nature.com/articles/s41467-017-02317-2>).

Installation

The **gsmr** requires R ≥ 2.15 , you can install it in R by:

```
# gsmr requires the R-package(s)
install.packages(c('survey'));
# install gsmr
install.packages("http://cnsgenomics.com/software/gsmr/static/gsmr_1.0.6.tar.gz", repos=NULL, type="source")
```

The gsmr source codes are available in [gsmr_1.0.6.tar.gz](#). Sample data is available in [test_data.zip](#).

This online document has been integrated in the gsmr R-package, we can check that by the standard “?function_name” command in R.

Update log

V1.0.6 ([gmr_1.0.6.tar.gz](#) [PDF](#), 13 Dec. 2017): Remove SNPs in high LD and return the filtered SNPs.

V1.0.5 ([gmr_1.0.5.tar.gz](#) [PDF](#), 13 Dec. 2017): Improved the approximation of the sampling covariance matrix.

V1.0.4 ([gsmr_1.0.4.tar.gz](#) [PDF](#), 6 Nov 2017): Add the bi-directional GSMR analysis. The HEIDI-outlier analysis has been integrated in the GSMR analysis by default.

V1.0.3 ([gsmr_1.0.3.tar.gz](#) [PDF](#), 12 Oct 2017): Add more example data.

Removed the initial versions (8 Nov 2016).

Tutorial

The GSMR analysis only requires summary-level data from GWAS. Here is an example, where the risk factor (x) is LDL cholesterol (LDL-c) and the disease (y) is coronary artery disease (CAD). GWAS summary data for both LDL-c and CAD are available in the public domain (Global Lipids Genetics Consortium et al. 2013, Nature Genetics; Nikpay, M. et al. 2015, Nature Genetics).



1. Prepare data for GSMR analysis

1.1 Load the GWAS summary data

```
library("gsmr")
```

```
## Loading required package: metho  
ds
```

```
data("gsmr")  
head(gsmr_data)
```

```
##           SNP a1 a2           freq  
bzx bzx_se bzx_pval bzx_n  
bzy  
## 1 rs10903129  A  G 0.45001947 -  
0.0328 0.0037 3.030e-17 169920.0  
0.008038  
## 2 rs12748152  T  C 0.08087758  
0.0499 0.0066 3.209e-12 172987.5  
0.013671  
## 3 rs11206508  A  G 0.14396988  
0.0434 0.0055 2.256e-14 172239.0  
0.030222
```

```

## 4 rs11206510 C T 0.19128911 -
0.0831 0.0050 2.380e-53 172812.0 -
0.074519
## 5 rs10788994 T C 0.18395430
0.0687 0.0049 8.867e-41 172941.9
0.038267
## 6 rs529787 G C 0.19713099 -
0.0553 0.0052 8.746e-24 161969.0
0.001707
##          bzy_se          bzy_pval    bzy_n
## 1 0.0092442 0.3845651000 184305
## 2 0.0185515 0.4611690000 184305
## 3 0.0141781 0.0330400000 184305
## 4 0.0133438 0.00000000234 184305
## 5 0.0118752 0.0012711000 184305
## 6 0.0135491 0.8997431000 184305

```

```
dim(gsmr_data)
```

```
## [1] 189 12
```

This is the input format for the GSMR

analysis below. In this data set, there are 189 near-independent SNPs associated with LDL-c at a genome-wide significance level (i.e. $p < 5e-8$).

- SNP: the genetic instrument
- a1: effect allele
- a2: the other allele
- freq: frequency of a1
- bzx: the effect size of a1 on risk factor
- bzx_se: standard error of bzx
- bzx_pval: p value for bzx
- bzx_n: per-SNP sample size of GWAS for the risk factor
- bzy: the effect size of a1 on disease
- bzy_se: standard error of bzy
- bzy_pval: p value for bzy
- bzy_n: per-SNP sample size of GWAS for the disease

1.2 Estimate the LD correlation matrix

```
# Save the genetic variants and effect alleles in a text file using R
write.table(gsmr_data[,c(1,2)], "gsmr_example_snps.allele", col.names=F, row.names=F, quote=F)
# Extract the genotype data from a PLINK file using GCTA
gcta64 --bfile gsmr_example --extract gsmr_example_snps.allele --update-ref-allele gsmr_example_snps.allele --recode --out gsmr_example
```

Note: the two steps above guarantee that the LD correlations are calculated based on the effect alleles for the SNP effects.

```
# Estimate LD correlation matrix using R
snp_coeff_id = scan("gsmr_example.xmat.gz", what="", nlines=1)
snp_coeff = read.table("gsmr_example.xmat.gz", header=F, skip=2)
```

```
# Take the same SNPs with same order
snp_id = Reduce(intersect, list(gsmr_data$SNP, snp_coeff_id))
gsmr_data = gsmr_data[match(snp_id, gsmr_data$SNP),]
snp_order = match(snp_id, snp_coeff_id)
snp_coeff_id = snp_coeff_id[snp_order]
snp_coeff = snp_coeff[, snp_order]

# Calculate LD correlation matrix
ldrho = cor(snp_coeff)

# Check the size of the correlation matrix and double-check if the order of the SNPs in the LD correlation matrix is consistent with that in the GWAS summary data
colnames(ldrho) = rownames(ldrho) = snp_coeff_id
```

```
dim(ldrho)
```

```
## [1] 189 189
```

```
# Show the first 5 rows and columns of the matrix  
ldrho[1:5,1:5]
```

```
##                rs10903129      rs12
748152      rs11206508      rs11206510
## rs10903129      1.0000000000 -0.0045
378845      0.008066621 -0.01372112
## rs12748152 -0.004537884      1.0000
000000 -0.006687181      0.00445927
## rs11206508      0.008066621 -0.0066
871806      1.0000000000 -0.21125757
## rs11206510 -0.013721120      0.0044
592696 -0.211257567      1.000000000
## rs10788994 -0.023444710      0.0003
629201      0.051259343 -0.18427062
##                rs10788994
## rs10903129 -0.0234447102
## rs12748152      0.0003629201
## rs11206508      0.0512593434
## rs11206510 -0.1842706205
## rs10788994      1.0000000000
```

Note: all the analyses implemented in this R-package only require the summary data (e.g. “gsmr_data”) and the LD correlation matrix (e.g. “ldrho”)

listed above.

2. Standardization

This is an optional process. If the risk factor was not standardised in GWAS, the effect sizes can be scaled using the method below. Note that this process requires allele frequencies, z-statistics and sample size. After the scaling, b_{zx} is interpreted as the per-allele effect of a SNP on the exposure in standard deviation units.

```

snpfreq = gsmr_data$freq
# minor allele frequencies of SNPs
bzx = gsmr_data$bzx      # effects
of instruments on risk factor
bzx_se = gsmr_data$bzx_se      #
standard errors of bzx
bzx_n = gsmr_data$bzx_n      #
sample size for GWAS of the risk f
actor
std_zx = std_effect(snpfreq, bzx,
bzx_se, bzx_n)      # perform standa
rdize
gsmr_data$std_bzx = std_zx$b      #
standardized bzx
gsmr_data$std_bzx_se = std_zx$se
# standardized bzx_se
head(gsmr_data)

```

```

##           SNP a1 a2           freq
bzx bzx_se  bzx_pval    bzx_n
bzy
## 1 rs10903129  A  G 0.45001947 -
0.0328 0.0037 3.030e-17 169920.0
0.008038

```

```

## 2 rs12748152 T C 0.08087758
0.0499 0.0066 3.209e-12 172987.5
0.013671
## 3 rs11206508 A G 0.14396988
0.0434 0.0055 2.256e-14 172239.0
0.030222
## 4 rs11206510 C T 0.19128911 -
0.0831 0.0050 2.380e-53 172812.0 -
0.074519
## 5 rs10788994 T C 0.18395430
0.0687 0.0049 8.867e-41 172941.9
0.038267
## 6 rs529787 G C 0.19713099 -
0.0553 0.0052 8.746e-24 161969.0
0.001707
## bzy_se bzy_pval bzy_n
std_bzx std_bzx_se
## 1 0.0092442 0.3845651000 184305
-0.03055942 0.003447252
## 2 0.0185515 0.4611690000 184305
0.04713698 0.006234550
## 3 0.0141781 0.0330400000 184305
0.03829018 0.004852442
## 4 0.0133438 0.0000000234 184305
-0.07181919 0.004321251
## 5 0.0118752 0.0012711000 184305

```



```
## 5 0.0118752 0.0012711000 184305  
0.06149455 0.004386074  
## 6 0.0135491 0.8997431000 184305  
-0.04695042 0.004414868
```

3. GSMR analysis

This is the main analysis of this R-package. It uses SNPs associated with the risk factor (e.g. at $p < 5e-8$) as the instruments to test for putative causal effect of the risk factor on the disease. The analysis involves a step that uses the [HEIDI-outlier](#) approach to remove SNPs that have effects on both the risk factor and the disease because of pleiotropy.

```
bzx = gsmr_data$std_bzx      # SNP e  
ffects on risk factor  
bzx_se = gsmr_data$std_bzx_se  #  
standard errors of bxz
```

standard errors of bzx

```
bzx_pval = gsmr_data$bzx_pval #
```

p-values for bzx

```
bzy = gsmr_data$bzy # SNP effects on disease
```

```
bzy_se = gsmr_data$bzy_se # standard errors of bzy
```

```
bzy_pval = gsmr_data$bzy_pval # p-values for bzy
```

```
n_ref = 7703 # Sample size of the reference sample
```

```
gwas_thresh = 5e-8 # GWAS threshold to select SNPs as the instruments for the GSMR analysis
```

```
heidi_outlier_thresh = 0.01 # HEIDI-outlier threshold
```

```
nsnps_thresh = 10 # the minimum number of instruments required for the GSMR analysis
```

```
heidi_outlier_flag = T # flag for HEIDI-outlier analysis
```

```
ld_r2_thresh = 0.1 # LD r2 threshold to remove SNPs in high LD
```

```
ld_fdr_thresh = 0.05 # FDR threshold to remove the chance correlations between SNP instruments
```

```
gsmr_results = gsmr(bzx, bzx_se, bzx_pval, bzy, bzy_se, ldrho, snp_coeff_id, n_ref, heidi_outlier_flag, gwas_thresh, heidi_outlier_threshold, nsnp_thresh, ld_r2_thresh, ld_fdr_thresh) # GSMR analysis
cat("Effect of exposure on outcome : ",gsmr_results$bxy)
```

```
## Effect of exposure on outcome: 0.4082179
```

```
cat("Standard error of bxy: ",gsmr_results$bxy_se)
```

```
## Standard error of bxy: 0.02294163
```

```
cat("P-value of bxy: ", gsmr_results$bxy_pval)
```

```
## P-value of bxy: 7.898847e-71
```

```
cat("Used index to GMR analysis:  
", gsmr_results$used_index[1:5], "  
...")
```

```
## Used index to GMR analysis: 1  
2 3 5 6 ...
```

```
cat("Number of SNPs with missing v  
alue: ", length(gsmr_results$na_sn  
ps))
```

```
## Number of SNPs with missing val  
ue: 0
```

```
cat("Number of non-significant SNPs: ", length(gsmr_results$weak_snps))
```

```
## Number of non-significant SNPs: 38
```

```
cat("Number of SNPs in LD: ", length(gsmr_results$linkage_snps))
```

```
## Number of SNPs in LD: 2
```

```
cat("Number of pleiotropic SNPs: ", length(gsmr_results$pleio_snps))
```

```
## Number of pleiotropic SNPs: 12
```

4. HEIDI-outlier analysis

The estimate of causal effect of risk factor on disease can be biased by pleiotropy ([Zhu et al. 2017 bioRxiv](#)).

This is an analysis to detect and eliminate from the analysis instruments that show significant pleiotropic effects on both risk factor and disease. The HEIDI-outlier analysis requires `bzx` (effect of genetic instrument on risk factor), `bzx_se` (standard error of `bzx`), `bzx_pval` (p-value of `bzx`), `bzy` (effect of genetic instrument on disease), `bzy_se` (standard error of `bzy`) and `ldrho` (LD matrix of instruments). Note that LD matrix can be estimated from a reference sample with individual-level

genotype data.

The HEIDI-outlier analysis has been integrated in the GSMR analysis above (with the `heidi_outlier_flag` and `heidi_outlier_thresh` flags). It can also be performed separately following the example below.

```
heidi_results = heidi_outlier(bzx,
                              bzx_se, bzx_pval, bzy, bzy_se, ldr,
                              ho, snp_coeff_id, n_ref, gwas_thresh,
                              heidi_outlier_thresh, nsnp_thresh,
                              ld_r2_thresh, ld_fdr_thresh)
# perform HEIDI-outlier analysis
cat("Number of SNPs in LD: ", length(gsmr_results$linkage_snps))
```

```
## Number of SNPs in LD: 2
```

```
cat("Number of pleiotropic SNPs: "  
    , length(heidi_results$pleio_snps)  
    )
```

```
## Number of pleiotropic SNPs: 12
```

```
filtered_index = heidi_results$remain_index  
filtered_gsmr_data = gsmr_data[filtered_index,] # select data passed  
HEIDI-outlier filtering  
filtered_snp_id = snp_coeff_id[filtered_index] # select SNPs that  
passed HEIDI-outlier filtering  
dim(filtered_gsmr_data)
```

```
## [1] 137 14
```



```
# number of SNPs in the gsmr_data  
with bzx_pval < 5e-8  
dim(gsmr_data[gsmr_data$bzx_pval <  
5e-8, ])
```

```
## [1] 151 14
```

In the example above, 14 SNPs are filtered out by HEIDI-outlier.

5. Bi-directional GSMR analysis

The script below runs bi-directional GSMR analyses, i.e. a forward-GSMR analysis as described above and a reverse-GSMR analysis that uses SNPs associated with the disease (e.g. at $p < 5e-8$) as the instruments to

test for putative causal effect of the disease on the risk factor.

```
gsmr_results = bi_gsmr(bzx, bzx_se  
, bzx_pval, bzy, bzy_se, bzy_pval,  
ldrho, snp_coeff_id, n_ref, heidi_  
outlier_flag, gwas_thresh, heidi_  
outlier_thresh, nsnp_thresh, ld_r2_  
_thresh, ld_fdr_thresh)      # GSMR  
analysis  
cat("Effect of risk factor on dise  
ase: ",gsmr_results$forward_bxy)
```

```
## Effect of risk factor on diseas  
e:  0.4082179
```

```
cat("Standard error of bxy from th  
e forward-GSMR analysis: ",gsmr_re  
sults$forward_bxy_se)
```

```
## Standard error of bxy from the  
forward-GSMR analysis: 0.02294163
```

```
cat("P-value of bxy from the forward-GSMR analysis: ", gsmr_results$forward_bxy_pval)
```

```
## P-value of bxy from the forward-GSMR analysis: 7.898847e-71
```

```
cat("Effect of disease on risk factor: ", gsmr_results$reverse_bxy)
```

```
## Effect of disease on risk factor: -0.02376614
```

```
cat("Standard error of bxy from the reverse-GSMR analysis: ", gsmr_results$reverse_bxy_se)
```

```
## Standard error of bxy from the reverse-GSMR analysis: 0.00958462
```

```
cat("P-value of bxy from the reverse-GSMR analysis: ", gsmr_results$reverse_bxy_pval)
```

```
## P-value of bxy from the reverse-GSMR analysis: 0.01315254
```

6. Visualization

```
effect_col = colors()[75]  
vals = c(bzx[filtered_index]-bzx_se[filtered_index], bzx[filtered_index]+bzx_se[filtered_index])
```

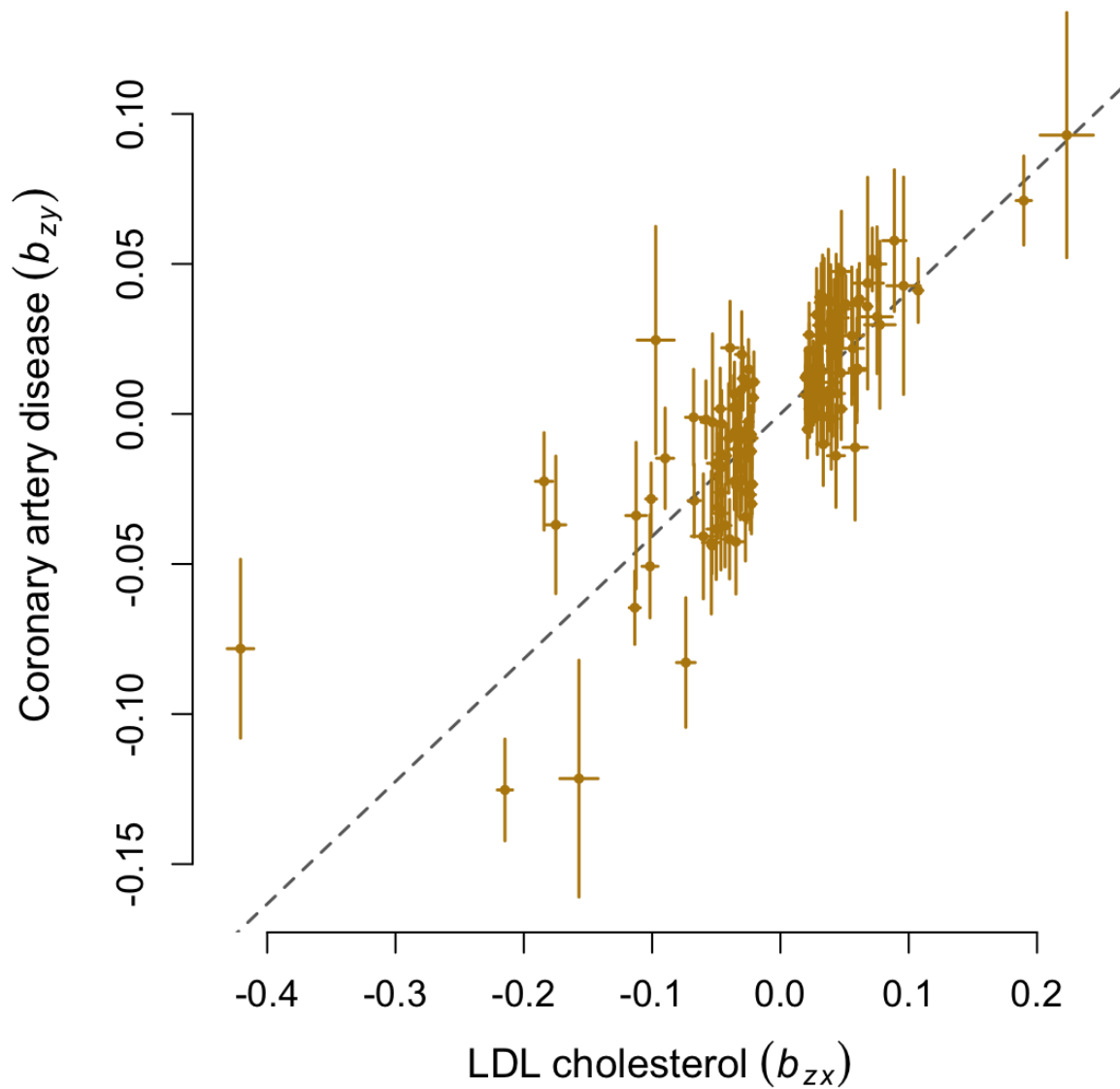
```

dex]+bzx_se[filtered_index])
xmin = min(vals); xmax = max(vals)
vals = c(bzy[filtered_index]-bzy_se[filtered_index], bzy[filtered_index]+bzy_se[filtered_index])
ymin = min(vals); ymax = max(vals)
par(mar=c(5,5,4,2))
plot(bzx[filtered_index], bzy[filtered_index], pch=20, cex=0.8, bty="n",
      cex.axis=1.1, cex.lab=1.2,
      col=effect_col, xlim=c(xmin, xmax), ylim=c(ymin, ymax),
      xlab=expression(LDL~cholesterol~(italic(b[zx]))),
      ylab=expression(Coronary~artery~disease~(italic(b[zy]))))
abline(0, gsmr_results$forward_bxy, lwd=1.5, lty=2, col="dim grey")

nsnps = length(bzx[filtered_index])
for( i in 1:nsnps ) {
  # x axis
  xstart = bzx[filtered_index[i]] - bzx_se[filtered_index[i]]; xend = bzx[filtered_index[i]] + bzx_se[filtered_index[i]]
  # y axis
  ystart = bzy[filtered_index[i]] - bzy_se[filtered_index[i]]; yend = bzy[filtered_index[i]] + bzy_se[filtered_index[i]]
  # plot
  plot(xstart, ystart, xend, yend, pch=20, cex=0.8, bty="n",
        col=effect_col, xlim=c(xmin, xmax), ylim=c(ymin, ymax),
        xlab=expression(LDL~cholesterol~(italic(b[zx]))),
        ylab=expression(Coronary~artery~disease~(italic(b[zy]))))
  abline(0, gsmr_results$forward_bxy, lwd=1.5, lty=2, col="dim grey")
}

```

```
se[filtered_index[i]]
    ystart = bzy[filtered_index[i]]
]; yend = bzy[filtered_index[i]]
    segments(xstart, ystart, xend,
yend, lwd=1.5, col=effect_col)
    # y axis
    xstart = bzx[filtered_index[i]]
]; xend = bzx[filtered_index[i]]
    ystart = bzy[filtered_index[i]]
] - bzy_se[filtered_index[i]]; yend = bzy[filtered_index[i]] + bzy_se[filtered_index[i]]
    segments(xstart, ystart, xend,
yend, lwd=1.5, col=effect_col)
}
```



Package Document

bi_gsmr

Bi-directional GSMR analysis is

composed of a forward-GSMR analysis and a reverse-GSMR analysis that uses SNPs associated with the disease (e.g. at $< 5e-8$) as the instruments to test for putative causal effect of the disease on the risk factor.

Usage

```
bi_gsmr(bzx, bzx_se, bzx_pval, bzy,  
bzy_se, bzy_pval, ldrho, snpid, hei  
di_outlier_flag=T, gwas_thresh=5e-8  
, heidi_outlier_thresh=0.01, nsnps_  
thresh=10)
```

Arguments

bzx

vector, SNP
effects on risk
factor

bzx_se

vector, standard
errors of bzx

bzx_pval

vector, p values
for bzx

bzy

vector, SNP
effects on
disease

bzy_se

vector, standard
errors of bzy

bzy_pval

vector, p values
for bzy

ldrho

LD correlation
matrix of the
SNPs

snpid

genetic

instruments

`n_ref`

sample size of
the reference
sample

`heidi_outlier_flag`

flag for HEIDI-
outlier analysis

`gwas_thresh`

threshold p-
value to select
instruments
from GWAS for
risk factor

`heidi_outlier_thresh`

HEIDI-outlier
threshold

`nsnps_thresh`

the minimum
number of
instruments

required for the
GSMR analysis
(we do not
recommend
users to set this
number smaller
than 10)

ld_r2_thresh

LD r2 threshold
to remove
correlated SNPs

ld_fdr_thresh

FDR threshold
to remove the
chance
correlations
between SNP
instruments

Value

Estimate of causative effect of risk factor on disease (forward_bxy), the corresponding standard error (forward_bxy_se), p-value (forward_bxy_pval) and SNP index (forward_index), and estimate of causative effect of disease on risk factor (reverse_bxy), the corresponding standard error (reverse_bxy_se), p-value (reverse_bxy_pval), SNP index (reverse_index), SNPs with missing values, with non-significant p-values and those in LD.

Examples

```
data("gsmr")
gsmr_result = bi_gsmr(gsmr_data$bzx, gsmr_data$bzx_se, gsmr_data$bzx_pval, gsmr_data$bzy, gsmr_data$bzy_se, gsmr_data$bzy_pval, ldrho, gsmr_data$SNP, n_ref, T, 5e-8, 0.01, 10, 0.1, 0.05)
```

gsmr

GSMR (Generalised Summary-data-based Mendelian Randomisation) is a flexible and powerful approach that utilises multiple genetic instruments to test for causal association between a risk factor and disease using summary-level data from independent genome-wide association studies.

Usage

```
gsmr(bzx, bzx_se, bzx_pval, bzy, bzy_se, ldrho, snpid, heidi_outlier_flag=T, gwas_thresh=5e-8, heidi_outlier_thresh=0.01, nsnp_thresh=10)
```

Arguments

bzx

vector, SNP effects on risk factor

bzx_se

vector, standard errors of bzx

bzx_pval

vector, p values for bzx

bzy

vector, SNP effects on disease

bzy_se

vector, standard
errors of bzy

ldrho

LD correlation
matrix of the
SNPs

snpid

genetic
instruments

n_ref

sample size of
the reference
sample

heidi_outlier_flag

flag for HEIDI-
outlier analysis

gwas_thresh

threshold p-
value to select
instruments

from GWAS for
risk factor

`heidi_outlier_thresh`

HEIDI-outlier
threshold

`nsnps_thresh`

the minimum
number of
instruments
required for the
GSMR analysis
(we do not
recommend
users to set this
number smaller
than 10)

`ld_r2_thresh`

LD r^2 threshold
to remove
correlated SNPs

`ld_fdr_thresh`

FDR threshold
to remove the
chance
correlations
between SNP
instruments

Value

Estimate of causative effect of risk factor on disease (bxy), the corresponding standard error (bxy_se), p-value (bxy_pval), SNP index (used_index), SNPs with missing values, with non-significant p-values and those in LD.

Examples

```
data("gsmr")
gsmr_result = gsmr(gsmr_data$bzx,
gsmr_data$bzx_se, gsmr_data$bzx_pval, gsmr_data$bzy, gsmr_data$bzy_se, ldrho, gsmr_data$SNP, n_ref, T, 5e-8, 0.01, 10, 0.1, 0.05)
```

heidi_outlier

An analysis to detect and eliminate from the analysis instruments that show significant pleiotropic effects on both risk factor and disease

Usage

```
heidi_outlier(bzx, bzx_se, bzx_pval, bzy, bzy_se, ldrho, snpid, n_ref, gwas_thresh=5e-8, heidi_outlier_thresh=0.01, nsnp_thresh=10, ld_fdr_thresh=0.05)
```

Arguments

`bzx`

vector, SNP
effects on risk
factor

`bzx_se`

vector, standard
errors of bzx

`bzx_pval`

vector, p values
for bzx

`bzy`

vector, SNP
effects on
disease

`bzy_se`

vector, standard
errors of bzy

`ldrho`

LD correlation

matrix of the
SNPs

`snpid`

genetic
instruments

`n_ref`

sample size of
the reference
sample

`gwas_thresh`

threshold p-
value to select
instruments
from GWAS for
risk factor

`heidi_outlier_thresh`

threshold p-
value to remove
pleiotropic
outliers (the
default value is

0.01)

`nsnps_thresh`

the minimum number of instruments required for the GSMR analysis (we do not recommend users to set this number smaller than 10)

`ld_r2_thresh`

LD r^2 threshold to remove correlated SNPs

`ld_fdr_thresh`

FDR threshold to remove the chance

correlations
between SNP
instruments

Value

Retained index of genetic instruments, SNPs with missing values, with non-significant p-values and those in LD.

Examples

```
data("gsmr")  
filtered_index = heidi_outlier(gsm  
r_data$bzx, gsmr_data$bzx_se, gsmr  
_data$bzx_pval, gsmr_data$bzy, gsm  
r_data$bzy_se, ldrho, gsmr_data$SN  
P, n_ref, 5e-8, 0.01, 10, 0.1, 0.0  
5)
```

Standardization of SNP effect and its standard error using z-statistic, allele frequency and sample size

Usage

```
std_effect(snp_freq, b, se, n)
```

Arguments

snp_freq vector, allele frequencies

b vector, SNP effects on risk factor

se vector, standard errors of b

n vector, per-SNP sample sizes for GWAS of the risk factor

Value

Standardised effect (b) and standard error (se)

Examples

```
data("gsmr")  
std_effects = std_effect(gsmr_data  
$freq, gsmr_data$bzx, gsmr_data$bz  
x_se, gsmr_data$bzx_n)
```