Prep: bring ID, watch, jacket, a pencil, glasses, lots of paper, pen, water and this set of notes **You got this!** 

Scheme			
Arithmetic Operations	(sha (num))	Boolean Operations  (eq? <a> <b>)</b></a>	(amus12 <a> <b> &gt;</b></a>
(+ [num]) scm> (+ 15 6 2)	(abs <num>) scm&gt; (abs -22)</num>	#t if a, b are same num, bool,	(equal? <a> <b>) Checks if a and b are equivalent</b></a>
23	22	symbol, str or object in memory	scm> (equal? '(1 2) '(1
(* [num])	(/ <dvdend> [dvsor])</dvdend>	scm> (eq? '(1 2) '(1 2)) #f	2)) #t
scm> (* 3 2 3) 18	scm> (/ 16 2 2 2 2) 1	scm> (define x '(1 2))	scm> (equal? op '*)
(- <num>)</num>	(expt <base/> <power>)</power>	scm> (eq? x x)	#t
scm> (- 1) -1	scm> (expt 3 2)	#t (not <arg>)</arg>	(= <a> <b>)</b></a>
scm> (- 16 7)	scm> (expt 3 (- 1))	(not vargz)	(< <a> <b>) (&lt;= <a> <b>)</b></a></b></a>
9	0.33333333	scm> (not 0)	scm> (= 2 2)
<pre>(quotient <dvdend> <dvsor>) scm&gt; (quotient 7 3)</dvsor></dvdend></pre>	<pre>(remainder <dvdend> <dvsor>) scm&gt; (remainder 7 3)</dvsor></dvdend></pre>	#f   scm> (not #f)	#t
2	1	#t	
scm> (quotient -4 3)	scm> (remainder -8 3) -2	(even? <num>)</num>	(odd? <num>)</num>
	scm> (remainder -9 3)	scm> (even? 22) #t	scm> (odd? 22) #f
	0		
Type Check		Special Forms	
(null? <arg>)</arg>	(boolean? <arg>)</arg>	<pre>(define <name> <expr>) (define (<name> [param])</name></expr></name></pre>	(if <pred> <conseq> [alt])</conseq></pred>
scm> (null? ())	scm> (boolean? ())	<body>)</body>	(if (null? nums) 0
#t	#f	scm> (define x '(1 2))	(if (null? nums) 0 (length nums))
scm> (null? nil) #t	scm> (boolean? #t) #t	scm> (define op '*)	`
scm> (null? 0)	scm> (boolean? 1)	op	(if (equal? op '*) (list 'mul (cons
#f (list? <arg>)</arg>	<pre>#f (procedure? <args>)</args></pre>	(define (f x) (+ x 1))	'list rest))
scm> (list? ())	scm> (procedure? abs)	(dofine (f m)	(cons op rest)))))
#t	#t	(define (f x) (define (g y) (+ x y))	
List Manipulation		g	
(car <list>)</list>	(cdr <list>)</list>	(or [test])	(and [test])
scm> (define x '(+ 1 2	scm> (cdr x)	#f if no args	#t if no args
3))	(1 2 3)	scm> (or #f #f #f)	scm> (and (> x 10) (< x
scm> (car x) +		#f scm> (or #f 2 3)	20))
(length <args>)</args>	(list <item>)</item>	2	
scm> (= (length '()) 0) #t	scm> (list 1 2 3) (1 2 3)	(cond <clause>)</clause>	(let ([binding]) <body>)</body>
(cons <first> <rest>)</rest></first>	(map <pre>procedure&gt; <list>)</list></pre>	<pre><clause> is of the form   (<test> [expression])</test></clause></pre>	[binding] in the form of ( <name> <expression>)</expression></name>
Equivalent to Pair(first,	<pre><pre><pre><pre><pre>one argument procedure</pre></pre></pre></pre></pre>	(else [expression])	( ,
rest), rest should be a list.	scm> (map (lambda (x) (* x x)) '(1 2 3))	If all clauses are #f, undefined.	(let ((x 1) (y 2))
There is a nil at the end (!)	(1 4 9)	(cond	(+ x y))
scm> (cons 1 2) (1 . 2)	scm> (map abs '(1 -1 3))	((< a b) 1)	(let ((x 5) (y 10))
scm> (cons 1 (cons 2	(1 1 3)	((> a b) 2)	(print x) (print y)
(cons 3 nil)))		(else 3)	(+ x y))
(1 2 3) (append [list])	(reduce <combiner> <lst>)</lst></combiner>	(begin <expression>)</expression>	(lambda ([param]) <body>)</body>
ALL arguments are lists!	<pre><combiner> Two args procedure</combiner></pre>	<pre>(define (sortedpair a b)   (if (&gt; a b)</pre>	(lambda (jz) 7)
Useful for adding to end of lists	Left (combined value) to right	(begin	Immediate calling of lambda
scm> (append '(1 2 3) '(4 5 6))	scm> (reduce (lambda (x y) (+ x y)) '(1 6 5 7))	(print a)	functions
(1 2 3 4 5 6)	19	(cons a (cons b nil))	scm> ((lambda (x y) (+ (*
scm> (append)	scm> (reduce (lambda (x	(begin	x x) (* y y))) 3 4)
() scm> (append '(1 2 3) '(a	y) (+ x y)) '(1)) 1	(print b) (cons b (cons a nil))	25
b c) '(foo bar baz))	scm> (reduce (lambda (x		scm> ((lambda () 4)) 4
(1 2 3 a b c foo bar baz)	y) (+ x y)) '()) Error		
(filter <pred> <lst>)</lst></pred>	(apply <proc> <list>)</list></proc>	(quote <expr>)</expr>	(quasiquote <expr>)</expr>
<pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre>	scm> (apply + '(1 2 3)) 6	equivalent to ' <expr></expr>	scm> (define (make-
scm> (filter (lambda (x) (<= x 5)) '(1 6 5 7))	Ŭ	scm> (quote (1 2 3))	adder n) `(lambda (d)
(1 5)		(1 2 3) scm> (quote (abs 3))	(+ d ,n))) make-adder
<pre>(set-car! <pair> <val>) (set-cdr! <pair> <val>)</val></pair></val></pair></pre>	(eval <expression>)</expression>	(abs 3)	scm> (make-adder 2)
scm> (define x '(1 2))	scm> (eval '(cons 1 (cons	scm> (quote '(abs 3))	(lambda (d) (+ d 2))
х	2 nil)))	(quote (abs 3))	scm> ((eval (make-adder 2)) 3)
scm> (set-car! x 3) scm> x	(1 2)		5
(3 2)	scm> (eval (list	(unquote <expr>)</expr>	mu (dynamic scoping)
scm> (set-cdr! x 3)	'quotient 10 2))	equivalent to , <expr></expr>	Dynamic scoping: parent of the
scm> x (3.3)	5	<pre><see example="" for="" quasiquote=""></see></pre>	frame is the frame in which the procedure is called.
		1 L	p. socaa. o .o oanoa.

True

# Scheme (continued)

# List equivalence

(1 2 3)	(list 1 2 3)	(quote (1 2 3))
(cons 1 (co	ns 2 (cons 3 nil)	))

### Reversing a list

```
(define (reverse lst curlst)
  (if (null? lst)
      curlst
      (reverse (cdr lst) (cons (car lst) curlst)))
(define (deep-reverse lst)
      (cond ((list? lst) (reverse (map deep-reverse lst)
nil)) (else lst))
```

#### Tricks

Symbols	Dot '.'
scm> ((lambda (x) `(,x 2)) 4) (4 2)	equivalent to cons
scm> ((lambda (x) `(x 2)) 4) (x 2)	scm> '(1 . (2)) (1 2) scm> '(1 . (2 3)) (1 2 3)

## Backus-Naur Form (BNF)

## Can parse more things.

```
rstring: "r\"" regex* "\""
?regex: character | word | group | pipe
class | range | plus_quant | star_quant
num quant
character: LETTER | NUMBER
word: WORD
group: "(" regex ")"
class: "[" (character*range*)* "]"
plus quant: (group | character | class) "+"
star_quant: (group | character | class) "*"
num_quant: (group | character | class) "{"
interval "}"
?interval: (NUMBER+ ",") | ("," NUMBER+) |
("NUMBER+ "," NUMBER+)
%import /\s+/
%import common.LETTER
%import common.NUMBER
%import common.WORD
```

#### Calculator

```
def calc eval(exp):
 if isinstance(exp, (int, float)):
   return exp
 elif isinstance(exp, Pair):
   arguments = exp.rest.map(calc eval)
   return calc apply(exp.first, arguments)
 else: raise TypeError
def calc_apply(operator, args):
 if operator == '+':
   return reduce(add, args, 0)
 elif operator == '-':
    # logic
 elif operator == '*':
   # logic
 elif operator == '/':
   # logic
 else: raise TypeError
```

```
Regex (import re)
```

• re.match(<pattern>, <str>)
Anchored at the start. Searches from the start of
<str>>, returns True if matches any prefix.
>>> x = re.match("jz", "jz)
<re.Match object; span=(0, 2), match='jz'>
>>> bool(x)

re.search(<pattern>, <str>)
 Not anchored. Searches and matches any part of <str>

# • re.findall(<pattern>, <str>) Returns list of all matches

```
txt = "The rain in Spain"
x = re.findall("ai", txt) # ['ai', 'ai']
y = re.findall("in$", txt) # ['in']
m = re.findall("(jz).*(app)", "jz app")
# [('jz', 'app')]
```

re.fullmatch(<pattern>, <str>)
 Anchored at start and end. Must remember to bool()

```
>>> bool(re.fullmatch(r'\s', '\n'))
True
>>> bool(re.fullmatch(r'[^A-Za-z]', 'b'))
False
>>> bool(re.fullmatch(r'hi|hello', 'hello'))
True
```

Regex	Explanation
[abc]	'a' or 'b' or 'c'
[a-z]	any char between 'a' and 'z' (incl)
[^A-Z]	any char not between 'A' and 'Z'
	(incl), applies to the whole []
\w	equiv to [A-Za-z0-9_]
\d	equiv to [0-9]
\s	<pre>any whitespace char, including ' ', '\t', '\n', '\r'</pre>
Combinat	tions
AB	Concatenation (A followed by B)
AB	Or (Either pattern A or pattern B)
()	Capturing group
(?:)	Non capturing group
Anchors	
\$	Start of line character
^	End of line character
\b	Word boundary (zero-length)
	- Before first char if it is \w
	- After last char if it is \w
	- Between two char, one \w, one \w
Special C	characters (12 of them)
'\', '{	', '[', '(', ')', '+', '*', '?', '\$', ', '
	rs (apply to previous)
?	0 or 1
*	0 or more
+	1 or more

#### Examples

r'-?\d+'	Matches any number (negative too)	)
r'.*'	Matches any string	

{1,3} Range from 1 to 3 inclusive

## SQL General Structure

Gener	ai Siruc	luie					
SELECT	г	FROM		WHERE	]	GROUP	BY
	HAVING		ORDER	ВҮ	[.	ASC DE	SC]

# Order of Operations:

- 1. WHERE to filter
- 2. GROUP by
- 3. HAVING to filter the groups
- ARITHMETIC OPERATIONS IN SELECT like MAX(), COUNT(\*) and ORDER BY

#### Arithmetic Functions (in SELECT)

Function	Description / Use case
ROUND(col)	ROUND(release_year/10.0)
AVG(col)	Average value of numeric column
SUM(col)	Total sum of numeric column
MAX(col)	Maximum entry of numeric column
MIN(col)	Minimum entry of numeric column
COUNT(*)	Number of rows in table; preserves
	duplicate row; include rows with null.
COUNT(col)	Number of non-null entries in col
COUNT	Number of distinct entries in col
(DISTINCT col)	

Creating Table Examples

```
CREATE TABLE table1 AS

SELECT col1, col2 FROM table WHERE

col1="jz" AND col2="jj";

CREATE TABLE table2 AS

SELECT col1 FROM table GROUP BY smallest

HAVING COUNT(smallest)=1 ORDER BY smallest

CREATE TABLE table3 AS

SELECT a.col1 FROM table1 AS a, table2 AS

b WHERE a.col2=7 AND b.'7'='True';

CREATE TABLE table4 AS

SELECT ROUND(AVG(ABS(a.number -
b.number))) FROM students AS a;

CREATE TABLE table5 AS

SELECT name FROM dino WHERE name <> "t-
rex" GROUP BY weight/legs HAVING COUNT(*)>1
```

#### Common Phrases

COMMINGITY MICHIGAN
<pre>HAVING SUM(weight/legs) &gt; 0;</pre>
SELECT MAX(legs) - MIN(legs) AS diff FROM
animals GROUP BY weight ORDER BY diff DESC
LIMIT 1;
SELECT "Thank you, "   name FROM players
WHERE SUBSTR(name, 5) = "Chase";
SELECT team, SUM(points) FROM scoring,
players
WHERE player=name GROUP BY team;
Cal 24
Stanford 20
SELECT DISTINCT col1, col2 FROM table;
Returns pairwise distinct col1, col2 entries.

# Trampolining

```
def trampoline(f, *args):
    v = f(*args)
    while callable(v):
        v = v()
    return v

def f_thunked(n, k):
    if n == 0:
        return k
    else:
        return lambda: f_thunked(n - 1, k * n)
```

## Exception

## Try-except blocks

try:	try:
# logic	quot = 10/0
except <exp> as e: # logic</exp>	<pre>except ZeroDivisionError as e:    print('Error, type(e))</pre>
	quot = 0

Example: except StopIteration:

#### Assert

assert <expr>, <string>

raises exception of the type AssertionError

#### Raise

raise <expr> # e.g. raise TypeError('bad arg')

# Tail Recursion

- Last body sub-expression in a lambda expression
- Sub-expressions 2 and 3 in a tail context if expression
- All non-predicate subexpression in a tail context cond
- The last subexpression in a tail context and, or, begin or let

Bottom line: last evaluated function of the function is either terminal or the function itself.

#### **Final Checks**

#### **Scheme**

- Check all operators (- x 1) instead of (x-1) and (< 1 2) instead of (1 < 2)</li>
- cons always 2 arguments (even nil)
- Cannot have a list of integers that are not in quotes (Error: int is not callable)
- Check each variable: list or procedure?

#### **BNF**

Empty terminals not allowed – leave blank

#### Regex

- Remember anchors (\b, \$, ^)
- Did you escape special characters?
- Use non-capturing groups for safety

## **SQL**

- Remember the ';'
- Eliminate double counting (a.id < b.id;)</li>
- Use single quotes
- Check: referenced correct table and cols.

#### General

For high-value problems, check and recheck the answers - can't afford loss of points

# **WWPD**

>>> "hi"	>>> repr([1, 2, 3])
'hi'	'[1, 2, 3]'
>>> 'hi'	>>> x = {}
'hi'	>>> x["jz"] = "rn"
>>> 1 == True	>>> repr(x)
True	"{'jz':'rn'}"
>>> 0 == False	
True	
<pre>&gt;&gt;&gt; repr("jianzhi")</pre>	>>> repr(2)
"'jianzhi'"	121
>>> str("jianzhi")	>>> repr(None)
ʻjianzhi'	'None'
>>> "jianzhi"	>>> str(None)
'jianzhi'	'None'

## Tree, Link

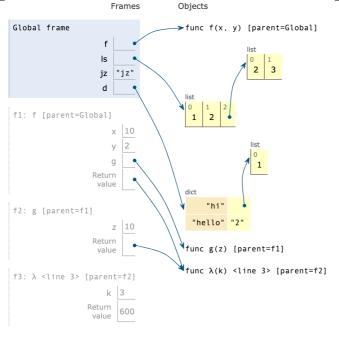
#### Link

* <b>L</b> IIIIX	
Class Var	Constructor
Link.empty	1 = Link(1, Link(2))
Instance Var	Methods
l.first	
1.rest # must be	
Link instance	

## Tree

Class Var	Constructor
None	t = Tree(label,
	branches=[])
	t = Tree(2)
Instance Var	Methods
t.label	t.is_leaf() # FUNCTION
t.branches	_

# **Environmental Diagram (Example)**



## **Data Structures**

# 1. <u>List</u>

Method	Remarks
ls.append(x)	Returns None
<pre>ls.insert(1,     "a")</pre>	Returns None
ls.pop()	Returns <element></element>
ls.pop(1)	Returns <element></element>
ls.reverse()	Returns None
ls.remove(x)	Returns None
ls.extend([1])	Returns None
ls.copy()	Returns new list
ls.index(x)	Returns index of x
ls.count(x)	Returns number of x
ls[:]	Returns new list

# <u>List Comprehensions</u>

[x for x in range(1, 12) if 12 % x == 0]
[x if 12 % x == 0 else 1 for x in range(1, n)]

# **Shallow Copy**

list(ls)	[ls[0], ls[1],	, ls[n]]
ls + []	ls[:]	ls.copy()

## 2. String

" ".join( <iterable>)</iterable>
" ".join(["b", "luv", "z"]) # delimiter
s.split("e") # split by delimiter into list
s.split() # default " "

# 3. <u>Dictionary</u>

Method	Return
d.get("x", 0)	d[x] if "x" in d else 0
d.pop("key")	d["key"] else KeyError
list(d.keys())	list of keys
list(d.items())	list of (key, item)
<pre>dd = d.copy()</pre>	returns a shallow copy dd == d # True dd is d # False
d.clear()	clears the dictionary
<pre>d.popitem()</pre>	returns the item last
	inserted and removes it
d.setdefault("x",	returns d["x"] if x in d,
v)	else return d["x"] = v

### Iteration

<pre>for i in d.keys():     print(i)</pre>	<pre>for k, v in d.items():     print(k, v)</pre>
iter(prices.keys())	<pre>iter(prices.items())</pre>

# **Dictionary Comprehensions**

 $x = \{i : s[i] \text{ for } i \text{ in range}(len(s)) \text{ if } s[i] \\ != w\}$ 

## **Iterators and Generators**

lterables: [], (), "string", range(1, 21),
{"dict": 1}

# Functions on Iterable

list(<iterable>)
list(<iterator>)
tuple(<iterable>)
tuple(<iterator>)

### **Iterable Functions:**

- list(<iterable>)
- type(<iterable>) # == tuple, list, dict,
  str
- sorted(<iterable>)

```
if (type([1, 2, 3]) == list):
    # logic
```

#### **Iterator Functions:**

- iter(<iterable>)
- iter(<iterator>) returns itself
- next(<iterator>)
- list(<iterator>) # exhausts the iterator

```
for i in <iterator>: # python calls next()
    # logic
```

# If called on an iterator, will exhaust it. StopIteration exception

#### Generator:

- Key words: yield, yield from
- Usually comes with while loop
- If you do a yield from, remember to return

# **Generator Functions:**

- yield from <iterable>
- yield from <generator>
- list(<generator\_with\_args>)

```
for i in <generator_function>:
    # logic
```

## reversed(<iterable>)

```
<reversed object at 0x7fe37836dc70>
# same as reversed iterator
it = reversed(["jz", "doing", "cs61a"])
next(it) # 'cs61a'
```

#### all(<iterable>)

```
all(<iterable>) # returns a boolean
all([]) == True
```

## any(<iterable>)

```
any(<iterable>) # returns a boolean
any([]) == False
```

# max(<iterable>) / min(<iterable>)

```
max(["jz", "hi", "wang"]) = "wang" #
lexigraphic
max([]) # ValueError
max(["jianzhi", "hi", "wang"], key = lambda x:
len(x)) # "jianzhi"
```

## • sum(<iterable>, <initial value>)

```
sum([]) == 0
sum([1, 2, 3]) == 6
>>> sum([[x] for x in [1, 2, 3]], [])
[1, 2, 3]
>>> sum([[[x]] for x in [1, 2, 3]], [])
[[1], [2], [3]]
sum([[t.label + x for x in f(y)] for y in
z], []) # double list summation
```

#### string

- text.lower()
- text.upper()
- text.split()

# OOP and Inheritance

#### Method Resolution Order (MRO)

```
class A(B, C):
    # logic
    # searches A then B then C
```

# Calling super's methods:

```
super().__init__(title, author)
super().__str__()
# calls the str (self) in super class
class Car:
   wheels = 4
    def __init__(self, name):
        self.name = name
        self.fuel = 0
   def add_fuel(self, x):
       self.fuel += x
x = Car("Tesla")
x.add_fuel(10) # equiv to Car.add_fuel(x, 10)
class FastCar(Car):
   def __init__(self, name, brand):
        super().__init__(name)
        self.brand = brand
    def add fuel(self, x):
        super().add_fuel(2*x)
```

# \_Dunder\_\_\_()

str() and repr()

def \_\_str\_\_(self):

return f'hi'

```
>>> repr(x)
'<probably with quotes>'
repr() Calls __repr__(), returns a string
```

```
>>> print(obj)
<str(obj) - probably no quotes>
print(obj) implicitly calls str() on it, and
then removes one layer of quotes
```

```
>>> obj
<repr(obj) - probably no quotes>

Python calls repr() method on it, obtain res, calls print on res, which removes quotes.
```

```
>>> str("a")
    'a'

Just strings

# called during print(), which removes quotes
# called during str()
# if not defined, defaults to __repr__
```

```
CS61A
                                                Finals Sheet
                                                                                                 Wang Jianzhi
          # equiv to Car.add fuel(self, 2*x)
                                                        # called during >>> obj
                                                        def __repr__(self):
 Car.wheel #4
                                                            return f"PaperReam('{self.x}')"
 x.wheel #4
                                                        def __iter__(self):
 CANNOT to modify class var through instance
                                                            return iter(self.leds)
                                                        def __iter__(self):
    for led in self.leds:
 >>> getattr(obj, "name") # returns value or
 AttributeError
                                                                yield led
 >>> hasattr(obj, "name") # returns boolean
 Misc
                                                        Last Resorts
 Range (exclusive)
                                                            1. Python ternary:
                                                        return x if <condition> else y
        range(start=0, stop, step=1)
        range(start, stop)
                                                            2. Tuple assignment:
        range(stop)
                                                        x, y = y, x + y
 zip(*iterables)
 >>> zip([1, 2, 3], [7, 8, 9]) # iterator
                                                            3. Chaining assignment (just use tuple)
 <zip object at 0x7f810aa4f440>
                                                        L = L.rest = L.rest.rest
 for i, j in x: # next(x) returns tuple
     print(i, j)
                                                        Line of Attack
 map(func, iterable, ...)
 map(lambda x: x*2, [1, 2, 3])
# returns iterator on resultant list
                                                             Eye power, intuition
                                                             Iteration, recursion (break into subproblems)
 >>> print(map(lambda x: x*2, [1, 2, 3]))
                                                             Get hints from previous functions in the same
 <map object at 0x7fa31936dc70>
 list(map(lambda x: x*2, [1, 2, 3]))
                                                             problem; Inspect arguments & return value
                                                             Exploit other values
 filter(func, iterable)
                                                             Lambda (particularly when # of args doesn't fit
 >>> filter(lambda x: x % 2 == 0, [1, 2, 3, 4])
 <filter object at 0x7fdb8bc52c10>
                                                             or need a placeholder), double lambda;
 # returns iterator on resultant list
                                                             Arguments can be functions too!
 list(filter(lambda x: n%x==0, range(1, n+1)))
                                                             Look at lambda variants below
 reduce(lambda, iterable)
                                                             Recursion ( str is sort of recursive)
 from functools import reduce
                                                             Whack, try test cases, whatever works
 total = reduce(lambda a, b: a+b, [1, 2, 3, 4])
                                                             Check and verify examples
        fstring (Do NOT mix ' and '')
                                                             Generators (for and list comprehensions)
 return f'Current {self.item} stock: {self.stock}'
                                                        Final Checks
 λ Functions
                                                             n // 10 vs n / 10
        2 Recursive
                                                             float("-inf")
 def d(f):
     def g(i):
                                                             print(str(i) + " this is a number")
         # logic
                                                             pow() returns float when any argument is float, use
         # calls parent function with args
                                                             round()
         # i == x is memorized
                                                             range(x, y) is exclusive
         return (lambda x: f(x) or i == x)
                                                             Check base cases ([[]] in 19 Summer)
     return a
                                                             self.var / label() VS label
        3-recursive (typically consists of
                                                             Read doc tests and problem statement
        initiation function, then a 2-recursive)
                                                             Check all methods and variables of objects (what's
                                                             their purpose?)
 def maxer(smoke):
     # initiation function
                                                             Did you remember to recursive call? (dfs(*it))
     def fire(y):
                                                             Check args and RV: Is the argument a list? What
         # 2-recursive parent
                                                             does function return? Boolean? (Midterm 2)
        def haze(z):
            # 2-recursize child
                                                             .append and .extend returns None
            # logic
            return fire(z);
                                                               Multiple lambdas
        return haze
     return fire
                                                        def multiadder(n):
 def compose(n):
```

# returns g(x) = f1(f2(...fn(x)...))

return compose(n - 1)(lambda x: f(g(x)))

return lambda f: f

if n == 1:

def call(f):

return call

def on(q):

return on

```
# >>> multiadder(3)(5)(6)(7)
# 18
        if n == 1:
                return lambda x: x
        else:
                # essentially lambda, since one
argument given
                return lambda x: lambda y: multiadder(n
-1)(x + y)
zipper = lambda x: x
helper = lambda f, g: lambda x: f(g(x))
zipper = helper(f1, zipper)
```