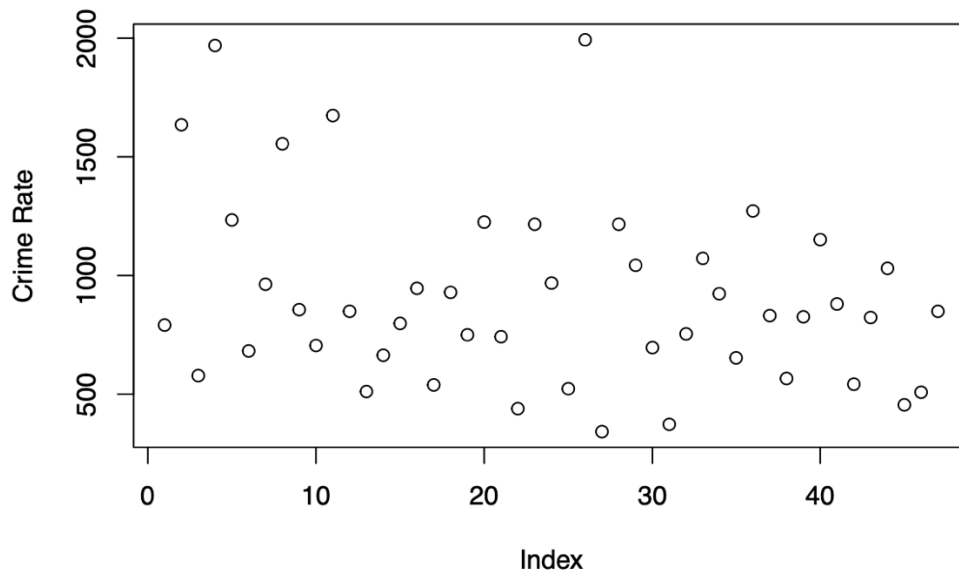
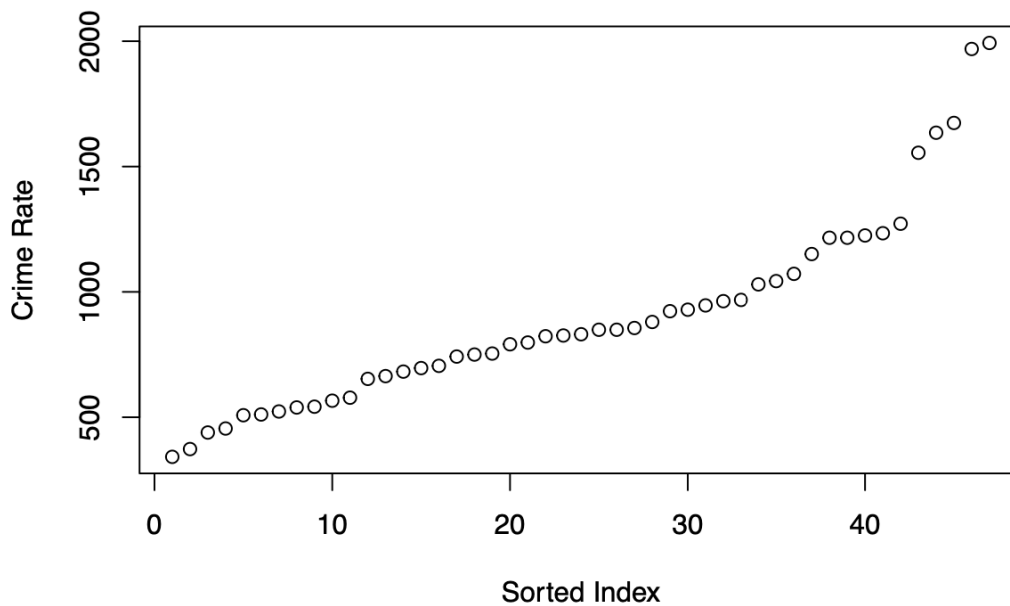


Question 5.1



At first, I plotted the data, and then the data was arranged in ascending order and plotted to visually check for outliers.



We see from the second graph that a straight line appeared on the Q-Q plot for totally normal data. On the right tail, this Line departs from a straight line quite a bit. We'll conduct a test to ensure normality. Using the *grubbs.test* I analyzed the lowest and the highest value to verify if they are outliers. From the graph above, although it is unclear just which outliers exist at the highest crime rates, it certainly appears that there are some.

The highest-crime city might be an outlier($p=0.079$), and if we remove it, the second-highest-crime city also appears to be an outlier($p=0.028$). therefore, we conclude that there are outliers within this data set and they are located near the highest values.

Meanwhile, the lowest crime rate does not seem to be an outlier based on this figure. The two points with the highest crime rates are 1969 and 1993, which are much above the cluster. Based on the *grubbs.test*, a p-value of 1 indicates, according to the findings of this test, that the lowest values in the "Crime" column are not outliers and fall within the predicted standard deviation.

The box-and-whisker plot below shows the data more clearly.



Question 6.1

An example of where Change Detection may be applied is for farmers to decide when will be the best time of the year to harvest their products based on environmental changes. Having the ability to weed out extreme climates of the year, the growers may harvest when the fruits are at their ideal sugar level based on temperature readings (or outliers).

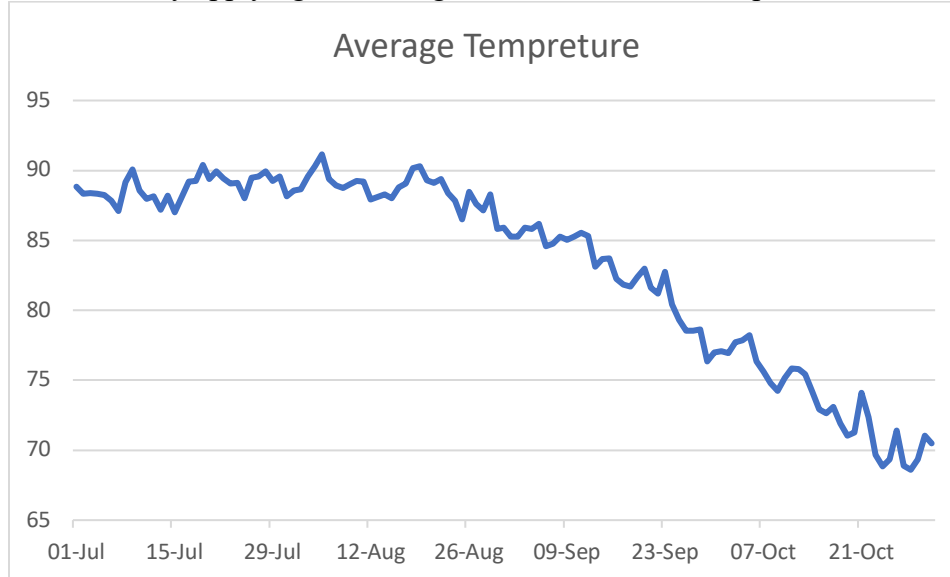
Average temperatures from previous years that were recorded would make a reasonable threshold. The optimal sugar concentration for the month and year can be detected between the highest and lowest limits to endure outliers are spotted.

The ideal harvesting time can be determined by choosing a large critical value, which helps avoid readings with extensive temperature variations. On the other hand, if there are no extreme outliers from the previous years, we could apply a lower C value to calculate the data.

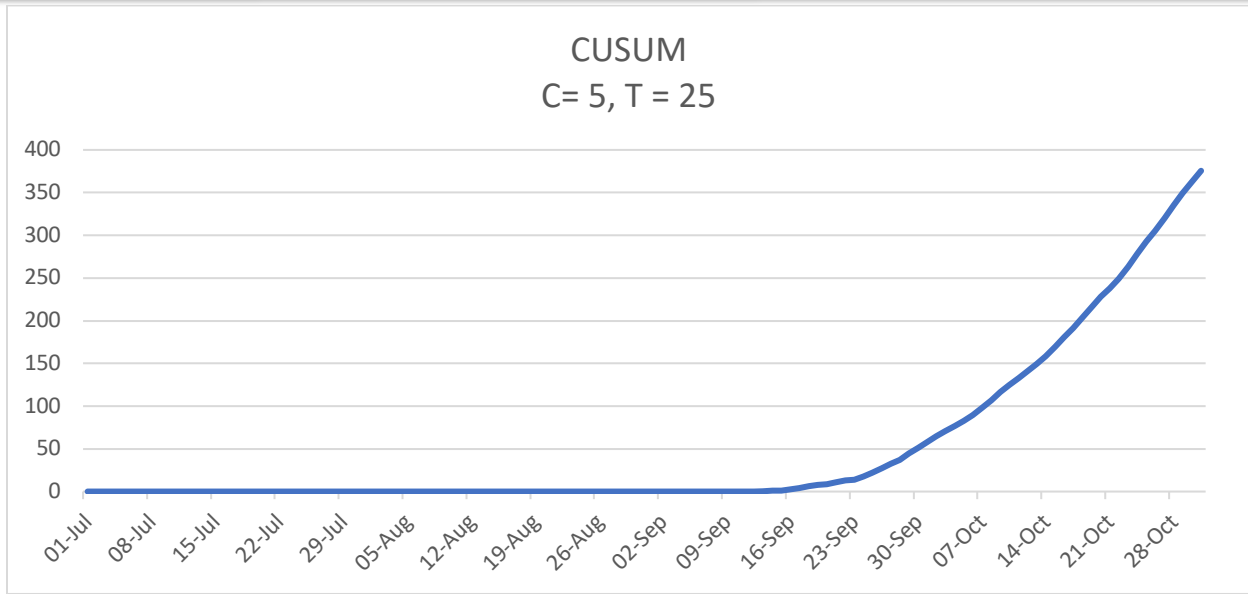
Question 6.2.1

The first step to solving this question is to import the data into Excel. When you import temps.txt into an Excel worksheet, you get a spreadsheet containing 124 rows for the days between July 1 and October 31 and 21 columns for day labels and 20 years' worth of Fahrenheit temperature readings.

After loading the data, I calculated the average temperature each year over the 20-year period 1996-2015 by applying the average function in Excel and plotted the line graph as follows:

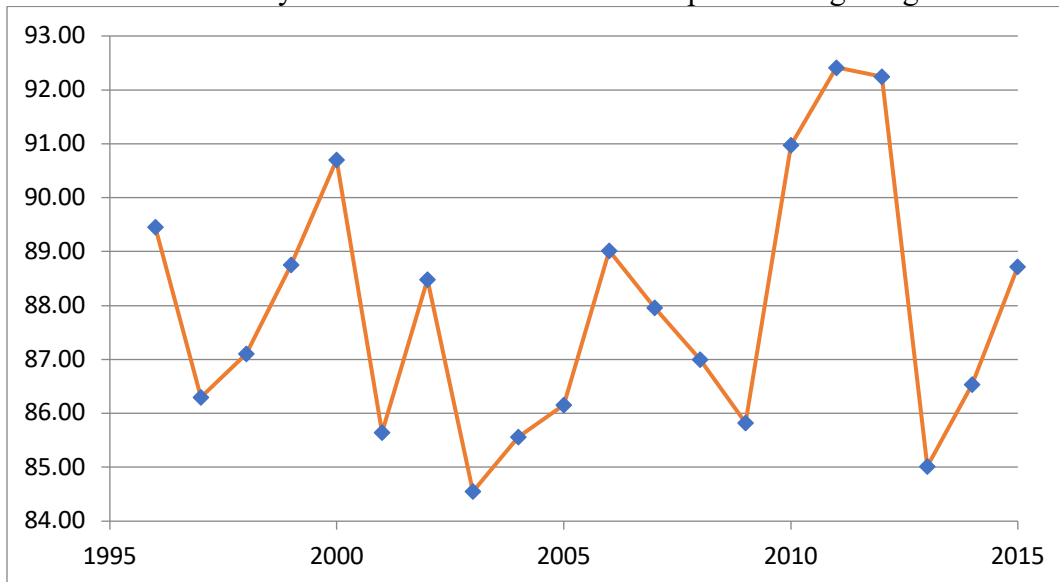


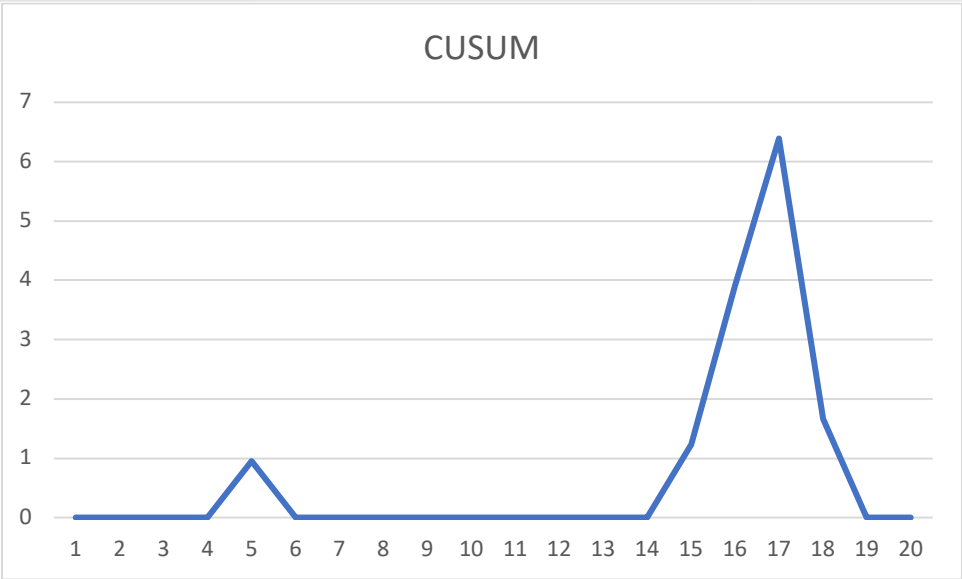
Further, I calculated the max of July averages, min of July averages, and standard deviation of July averages. I used the average July temperature as the Mu. The C value and T value were determined as $C = 5$ and $T = 25$. I calculated the CUSUM using the formula ($St = \text{MAX}(0, St(\text{previous day}) + ([\text{temp on day}(x)/\text{year}(y)] - \text{Mu} - C))$) and is plotted as follows. I would conclude that based on the two graphs, the temperature seems to be dropping around the beginning of September and then drastically decreasing.



Question 6.2.2

For this question, we are essentially trying to figure out how long is summer and are those days getting hotter. Based on the previous question, we can determine the change date of each year and then calculate the average year temperature until that date as shown below. I have also plotted the CUSUM graph to show the difference. We can see that there are fluctuations in between each year and there are significant changes in 2011-2013, however, we also see that temperature drops back in 2014. Therefore, we can conclude that summer temperature changes and it is hard to firmly conclude that the summer temperature is getting warmer.





HW3

2022-09-13

Question 5.1

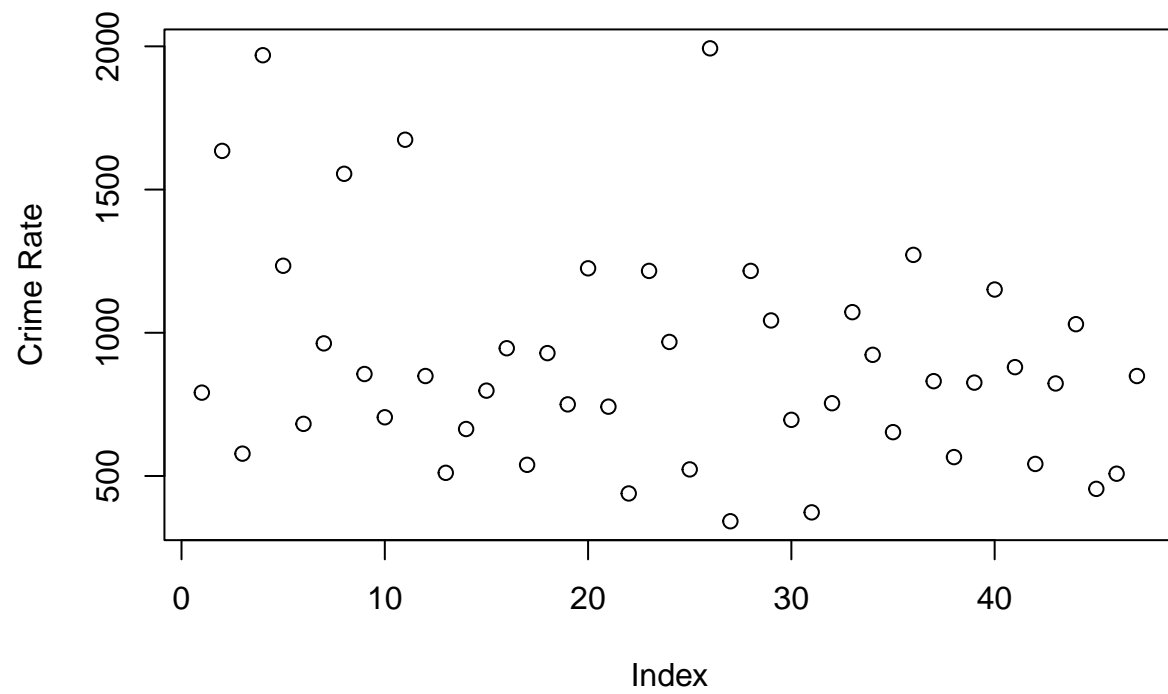
```
library(outliers)

# Clear the enviroment
rm(list = ls())

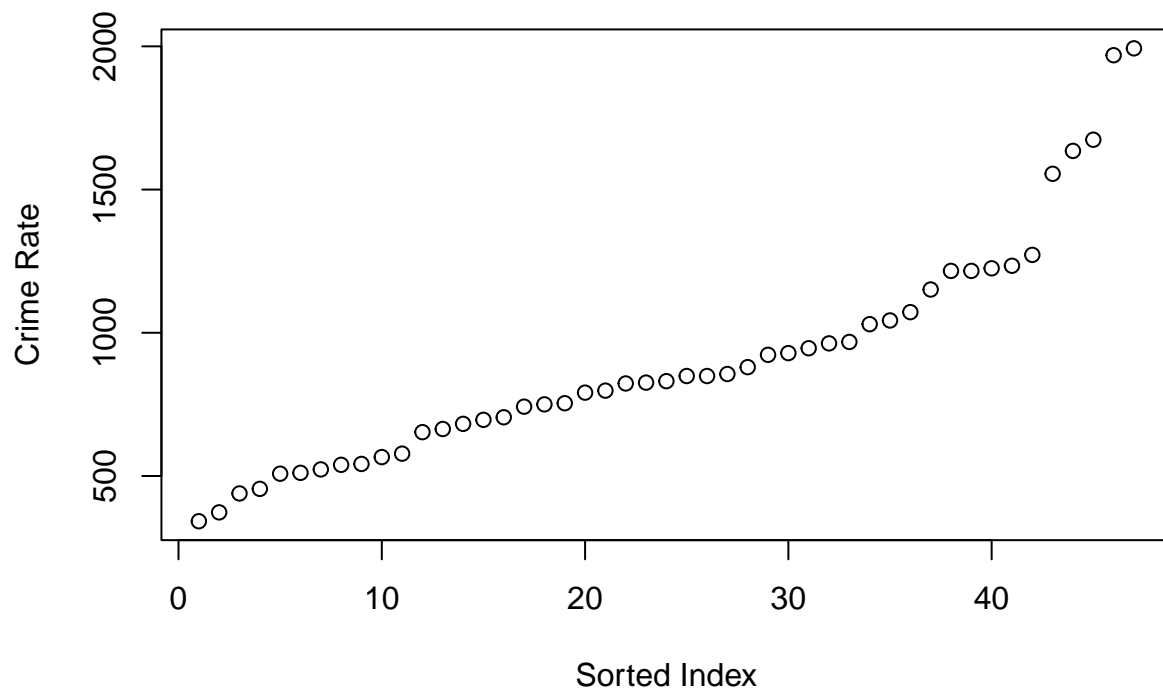
# Comment in set.seed(33) to repeat results across different values of k
set.seed(33)
library(outliers)

# Load crime data into a data frame
uscrime_df <- read.table("/Users/xiaofanjiao/Desktop/uscrime.txt", header=TRUE)
sort = t(uscrime_df$Crime[order(uscrime_df$Crime)]) #sort the Crime data for easier plotting

plot(seq(1:length(uscrime_df$Crime)),
      uscrime_df$Crime,
      xlab = "Index",
      ylab = "Crime Rate") #Plots the crime data
```



```
plot(seq(1:length(sort)), sort, xlab = "Sorted Index", ylab = "Crime Rate") #Plots the sorted crime data
```



```
# Use grubbs.test to check if lowest and highest value are two outliers on opposite tails of sample
grubbs.test(uscrime_df$Crime, type = 11, opposite = FALSE, two.sided = TRUE)
```

```
##
## Grubbs test for two opposite outliers
##
## data: uscrime_df$Crime
## G = 4.26877, U = 0.78103, p-value < 2.2e-16
## alternative hypothesis: 342 and 1993 are outliers
```

```
# Use grubbs.test to check if highest value is an outlier
grubbs.test(uscrime_df$Crime, type = 10, opposite = FALSE, two.sided = FALSE)
```

```
##
## Grubbs test for one outlier
##
## data: uscrime_df$Crime
## G = 2.81287, U = 0.82426, p-value = 0.07887
## alternative hypothesis: highest value 1993 is an outlier
```

```
# Use grubbs.test to check if lowest value is an outlier
grubbs.test(uscrime_df$Crime, type = 10, opposite = TRUE, two.sided = FALSE)
```

```
##
```



```
## Grubbs test for one outlier
##
## data:  uscrime_df$Crime
## G = 1.45589, U = 0.95292, p-value = 1
## alternative hypothesis: lowest value 342 is an outlier
```

```
# Plot usdata_df$crime as a boxplot
boxplot(uscrime_df$Crime,data=uscrime_df$Crime, main="US Crime Rate per 100k")
```



	1986	1987	1988	1989	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	Average	CUSUM	
01-Jul	88	86	91	84	89	84	90	73	82	81	93	85	95	87	82	105	82	90	85												86.3	0	min of July averages
02-Jul	97	90	88	82	91	87	90	81	81	89	93	85	87	90	84	94	93	85	93	87											88.35	0	min of July averages
03-Jul	97	93	91	87	93	87	87	87	86	86	93	82	91	89	83	95	99	76	87	79											88.4	0	min of July averages
04-Jul	90	91	88	95	84	89	86	88	86	86	89	80	85	92	98	77	84	85													88.25	0	std of July averages
05-Jul	89	84	91	90	96	86	93	80	90	82	90	88	90	88	90	100	83	86	84												88.25	0	std of July averages
06-Jul	93	84	89	91	96	87	93	84	90	82	81	87	82	87	89	90	98	83	87	84											87.85	0	std of July averages
07-Jul	93	75	93	82	96	87	89	87	89	76	80	82	88	86	94	94	79	89	80												87.1	0	std of July averages
08-Jul	91	87	95	86	91	89	90	87	88	82	82	90	82	87	94	95	88	90	90												88.15	0	std of July averages
09-Jul	93	84	95	87	96	91	90	89	88	89	84	89	84	96	91	97	88	90	91												90.05	0	std of July averages
10-Jul	93	87	91	87	99	87	91	84	89	78	84	86	87	84	90	92	95	87	87	93											88.55	0	std of July averages
11-Jul	90	84	91	82	96	90	84	84	90	83	90	85	89	86	93	95	90	80	85	92											87.85	0	std of July averages
12-Jul	91	88	86	77	93	90	77	86	89	86	91	87	93	90	90	95	84	87	90	93											88.15	0	std of July averages
13-Jul	93	86	88	73	91	86	82	87	91	84	91	86	85	84	91	97	90	78	89	92											87.2	0	std of July averages
14-Jul	93	90	87	81	93	82	88	84	91	87	91	84	88	89	91	90	85	90	90												88.2	0	std of July averages
15-Jul	82	91	91	81	93	82	91	86	84	84	91	81	89	89	94	80	90	86	89												87	0	std of July averages
16-Jul	91	91	87	86	93	84	93	88	84	85	91	86	89	90	89	85	92	87	83	88											88.1	0	std of July averages
17-Jul	96	89	90	82	91	87	93	88	84	89	93	89	88	87	93	91	86	93													89.2	0	std of July averages
18-Jul	95	89	91	87	97	88	93	88	87	90	89	90	82	83	89	83	87	82	92												89.25	0	std of July averages
19-Jul	96	89	95	88	100	90	93	88	84	89	96	88	91	80	90	94	91	90	85	91											90.4	0	std of July averages
20-Jul	99	90	91	90	99	87	91	88	88	89	93	86	94	82	91	84	86	76	93												89.4	0	std of July averages
21-Jul	91	89	91	90	93	84	95	89	89	90	93	86	95	86	94	92	90	87	93												89.95	0	std of July averages
22-Jul	95	84	89	91	96	87	91	86	89	91	91	79	92	84	95	94	95	85	83	92											89.45	0	std of July averages
23-Jul	91	87	91	93	87	90	89	81	93	91	86	82	87	87	92	92	97	84	88	88											89.05	0	std of July averages
24-Jul	93	88	91	93	82	84	87	82	95	90	87	87	88	88	94	92	97	86	87	91											89.1	0	std of July averages
25-Jul	84	89	86	91	75	82	84	84	89	92	88	87	89	90	95	90	98	89	88	90											89	0	std of July averages
26-Jul	84	89	88	93	82	88	86	87	87	94	93	87	92	95	94	98	86	89	91												89.15	0	std of July averages
27-Jul	82	91	80	93	88	90	89	87	84	92	95	90	90	90	93	94	97	82	92	92											89.55	0	std of July averages
28-Jul	79	91	88	93	91	84	91	89	89	90	96	89	93	89	90	90	97	86	90	94											89.95	0	std of July averages
29-Jul	90	89	89	93	89	89	91	88	87	83	91	87	82	85	84	93	84	86	82	93											89.25	0	std of July averages
30-Jul	91	88	90	97	87	89	88	84	89	78	91	92	90	82	95	96	96	90	84	94											89.55	0	std of July averages
31-Jul	87	72	86	99	86	87	90	88	90	84	94	90	88	85	95	96	88	80	85	93											88.15	0	std of July averages
01-Aug	86	80	86	96	86	84	93	84	91	82	95	92	89	86	91	87	81	89													88.35	0	std of July averages
02-Aug	90	84	82	93	81	84	91	84	90	86	95	92	92	83	84	96	99	89	84	94											88.65	0	std of July averages
03-Aug	84	88	84	88	84	84	91	84	91	88	97	94	91	90	92	97	94	88	88	94											89.55	0	std of July averages
04-Aug	91	89	86	89	88	95	82	91	98	97	93	95	95	95	87	90	90	97													90.3	0	std of July averages
05-Aug	93	88	90	91	91	88	93	84	90	88	96	96	92	92	93	96	90	88	89	95											91.15	0	std of July averages
06-Aug	88	84	89	93	91	84	97	82	84	86	89	98	94	89	93	93	86	88	92	88											89.4	0	std of July averages
07-Aug	91	84	89	93	91	86	87	84	81	80	87	98	90	91	91	93	84	86	95	88											88.95	0	std of July averages
08-Aug	84	80	86	93	91	88	87	84	82	82	96	100	86	92	93	94	92	83	90	92											88.75	0	std of July averages
09-Aug	90	73	82	91	96	87	86	86	84	85	95	103	85	93	94	91	88	89	89	93											89	0	std of July averages
10-Aug	89	87	90	75	88	87	75	83	96	103	85	93	94	95	87	90	86	84													89.05	0	std of July averages
11-Aug	88	86	88	96	89	86	89	84	82	87	88	100	88	95	95	94	85	90	83	91											89.2	0	std of July averages
12-Aug	86	88	84	98	89	86	91	80	88	84	90	81	86	95	95	88	90	88	90												87.9	0	std of July averages
13-Aug	84	88	86	97	89	81	83	87	77	86	81	100	81	90	96	95	98	89	84	89											88.1	0	std of July averages
14-Aug	86	87	80	88	89	87	86	89	82	90	87	99	84	90	94	83	85	90													88.3	0	std of July averages
15-Aug	89	88	82	93	94	84	88	90	82	92	86	102	87	90	90	88	85	73	87	90											89	0	std of July averages
16-Aug	90	91	86	93	97	90	90	86	84	89	89	101	86	88	90	90	91	67	90												88.8	0	std of July averages
17-Aug	91	84	96	99	91	91	89	86	86	101	85	87	91	92	87	66	89	89													89.05	0	std of July averages
18-Aug	91	89	87	98	101	91	93	90	86	90	88	97	86	88	93	94	87	77	89	88											90.15	0	std of July averages
19-Aug	90	89	90	98	101	87	91	90	89	89	88	95	90	90	92	96	84	82	86	89											90.3	0	std of July averages
20-Aug	89	79	89	97	86	93	87	88	92	93	96	90	88	93	93	84	84	89	88												89.3	0	std of July averages
21-Aug	90	82	84	91	87	88	93	88	82	94	91	99	85	88	93	94	88	84	92	89											89.1	0	std of July averages
22-Aug	91	79	87	91	86	90	91	88	84	93	88	104	82	85	94	98	84	88	93	92											89.4	0	std of July averages
23-Aug	91	81	87	90	88	88	90	84	87	87	98	78	81	93	92	88	93	87													89.7	0	std of July averages
24-Aug	91	82	88	80	92	93	93	89	87	85	83	95	83	86	90	93	86	84	88	89											87.85	0	std of July averages
25-Aug	84	90	84	90	82	92	90	91	88	82	84	85	94	78	87	89																	

02-Jul	98	86	91	84	89	84	90	79	82	91	93	95	85	93	87	92	105	82	90	85
03-Jul	97	90	88	82	91	87	90	81	81	89	93	85	87	90	84	94	93	85	93	87
04-Jul	97	93	91	87	93	87	87	86	86	86	91	82	91	89	91	82	91	89	79	79
05-Jul	90	91	91	88	95	84	89	86	88	86	95	86	90	91	85	92	98	77	84	85
06-Jul	89	91	90	96	85	93	85	92	89	90	85	92	89	89	90	93	92	90	84	85
07-Jul	93	84	89	91	96	87	93	84	90	82	82	82	87	82	87	89	90	98	83	87
08-Jul	93	75	93	82	96	89	87	89	87	89	76	86	87	76	86	82	84	93	79	79
09-Jul	92	87	95	86	91	89	89	90	87	88	82	82	82	90	82	97	94	95	88	90
10-Jul	93	84	89	87	96	92	90	84	88	89	90	84	88	90	92	90	92	90	82	89
11-Jul	93	87	91	87	99	87	92	84	89	78	84	86	87	84	90	92	95	87	87	93
12-Jul	90	84	91	82	90	84	86	86	86	86	90	82	89	89	90	90	90	89	86	92
13-Jul	91	88	86	77	93	90	77	86	89	86	91	87	93	90	90	95	84	87	90	93
14-Jul	91	90	89	71	91	82	82	84	91	87	91	84	88	84	91	90	90	76	89	90
15-Jul	82	91	91	81	93	82	91	86	84	84	91	81	89	89	94	80	90	86	86	89
16-Jul	91	91	87	86	93	93	93	84	85	89	90	85	92	87	93	82	87	83	88	93
17-Jul	96	89	90	87	91	87	93	88	84	89	93	89	88	88	87	87	93	91	86	93
18-Jul	95	89	91	87	88	93	93	88	87	90	87	90	82	89	93	87	93	87	92	89
19-Jul	99	89	95	88	100	90	93	88	84	89	96	88	91	80	90	94	91	90	85	91
20-Jul	99	90	91	90	89	87	91	88	89	94	88	94	82	91	81	84	86	76	93	92
21-Jul	91	89	91	90	93	84	95	89	89	90	93	86	95	86	94	92	90	87	82	93
22-Jul	95	84	89	91	96	87	91	86	89	91	91	79	92	84	95	92	94	85	83	92
23-Jul	91	87	91	93	87	90	89	81	93	91	80	82	87	87	97	92	97	84	88	88
24-Jul	93	88	91	93	82	84	87	82	95	90	87	87	88	84	92	97	86	87	91	92
25-Jul	84	89	86	91	75	82	84	84	89	92	88	87	89	90	95	90	98	89	88	90
26-Jul	84	89	88	93	82	88	86	87	87	94	93	87	92	95	94	98	96	89	92	92
27-Jul	82	91	80	93	88	90	89	87	84	92	95	90	90	93	94	97	97	82	92	92
28-Jul	79	91	88	93	91	84	91	83	89	90	96	89	92	99	90	97	86	90	84	94
29-Jul	90	89	89	93	89	89	91	88	87	83	91	87	92	85	94	93	94	86	82	93
30-Jul	80	80	86	96	86	84	93	84	91	82	95	80	89	96	91	94	87	81	89	90
31-Jul	87	72	86	99	86	87	90	88	90	84	90	88	85	95	96	88	80	85	93	89
01-Aug	90	84	82	93	81	84	92	84	90	86	95	92	92	83	84	96	99	89	84	94
02-Aug	91	88	84	88	84	84	91	84	91	91	97	94	91	90	92	97	94	90	88	84
03-Aug	91	89	86	89	88	86	91	82	91	98	97	91	92	95	85	87	84	90	90	97
04-Aug	93	88	90	91	91	88	93	84	88	88	96	96	92	92	93	96	90	88	89	95
05-Aug	88	88	89	93	91	84	97	87	84	86	89	84	89	94	93	93	82	88	91	88
06-Aug	91	84	89	91	91	86	87	84	81	80	97	98	90	91	91	93	84	86	95	88
07-Aug	84	80	89	93	91	87	87	84	82	82	93	93	94	94	92	83	90	92	83	88
08-Aug	93	73	82	91	96	87	86	86	84	85	95	103	85	93	94	91	88	89	93	93
09-Aug	89	80	87	90	95	88	88	87	75	83	93	103	85	93	94	95	87	90	86	84
10-Aug	88	86	88	96	89	86	89	84	82	87	88	100	88	95	95	94	85	90	83	91
11-Aug	86	88	84	86	89	81	91	91	81	80	88	86	85	91	86	95	81	86	85	84
12-Aug	93	88	86	97	89	81	91	87	77	86	81	100	81	90	96	95	91	89	84	88
13-Aug	86	87	80	88	89	89	88	89	82	90	87	90	87	89	84	90	90	84	86	86
14-Aug	89	88	82	93	94	84	93	88	90	82	92	86	102	87	90	90	88	85	73	87
15-Aug	90	91	86	93	87	90	90	84	89	93	90	84	101	86	93	90	91	84	86	90
16-Aug	91	91	84	96	99	91	91	89	86	90	86	101	85	87	91	92	87	66	89	89
17-Aug	91	89	87	98	101	93	93	88	88	90	88	97	84	87	94	97	97	86	89	86
18-Aug	90	89	90	98	101	87	91	90	89	89	88	95	90	92	96	84	82	86	89	90
19-Aug	90	89	79	89	87	86	93	88	88	92	86	90	88	92	90	84	84	86	86	86
20-Aug	91	82	84	91	87	88	93	88	82	94	91	99	85	88	93	94	88	84	92	89
21-Aug	91	79	87	88	88	88	90	84	84	84	90	104	82	84	90	92	92	84	86	86
22-Aug	91	81	87	90	88	88	95	90	84	87	87	98	78	81	93	92	88	90	93	87
23-Aug	91	82	88	80	92	93	95	89	87	85	83	95	83	86	90	93	86	84	88	84
24-Aug	84	84	90	82	92	90	92	88	82	84	78	87	84	78	87	91	90	90	82	86
25-Aug	88	87	91	89	90	91	88	89	86	84	88	92	83	90	90	99	90	82	86	86
26-Aug	84	90	89	88	90	91	84	90	88	80	83	89	80	83	90	86	88	80	86	88
27-Aug	88	90	90	90	92	81	82	91	90	86	90	88	86	75	87	95	80	90	91	83
28-Aug	88	91	93	92	86	82	82	89	87	85	88	86	84	89	86	93	86	92	82	82
29-Aug	84	91	93	91	88	81	78	88	88	85	88	89	79	85	90	80	87	88	74	84
30-Aug	82	88	91	84	87	82	77	79	87	85	85	79	89	92	89	90	88	89	86	89
01-Sep	80	88	87	88	79	80	84	88	82	85	85	84	81	71	90	95	91	90	90	87
02-Sep	73	91	84	91	81	75	84	80	80	88	85	78	83	85	86	89	84	86	84	86
03-Sep	97	93	77	84	82	73	89	87	81	87	85	88	73	79	92	95	85	90	92	89
04-Sep	84	81	90	93	87	81	93	87	82	85	87	85	82	81	80	87	85	77	91	84
05-Sep	87	83	91	96	81	90	93	84	84	81	83	89	88	83	85	78	85	89	89	87
06-Sep	89	82	86	86	80	80	87	83	81	82	81	87	81	80	87	81	80	87	81	80
07-Sep	89	86	90	91	86	87	88	75	86	83	80	86	89	84	91	89	92	88	90	85
08-Sep	89	89	93	75	86	87	88	73	75	86	87	73	78	80	87	80	81	84	86	84
09-Sep	91	84	79	77	80	86	91	82	84	86	83	89	88	84	92	81	83	90	84	87
10-Sep	81	80	78	87	84	84	86	84	84	84	84	84	84	84	84	84	84	84	84	84
11-Sep	86	82	81	87	84	87	95	80	84	84	84	89	83	75	96	86	83	83	90	86
12-Sep	88	80	84	87	86	87	84	90	83	93	88	82	86	80	86	80	81	87	86	79
13-Sep	79	87	87	87	86	86	75	82	79	80	80	81	88	82	91	92	83	82	78	77
14-Sep	86	88	87	89	80	77	91	82	73	91	82	79	87	86	87	84	80	80	82	80
15-Sep	82	80	87	81	75	77	88	81	75	88	83	76	80	82	89	72	86	89	86	79
16-Sep	82	81	87	73	81	80	86	81	80	86	81	76	78	69	73	75	79	79	86	83
17-Sep	78	88	82	82	73	82	81	81	79	88	85	79	82	80	91	77	79	78	85	83
18-Sep	79	91	80	79	84	82	80	84	78	90	79	82	74	82	77	81	84	84	87	81
19-Sep	79	95	82	68	87	84	86	87	73	90	73	81	79	81	96	82	79	86	83	89
20-Sep	78	89	82	79	77	86	84	82	75	86	79	78	75	79	95	86	85	79	87	77
21-Sep	81	70	88	72	73	87	77	75	80	86	82	86	84	84	92	80	87	82	82	76
22-Sep	84	80	84	7																