SE 2XB3 Group 4 Report 2

Huang, Kehao 400235182 huangk53@mcmaster.ca L01 $\begin{array}{c} {\rm Jiao,\,Anhao} \\ 400251837 \\ {\rm jiaoa3@mcmaster.ca} \\ {\rm L01} \end{array}$

 $Ye, Xunzhou \\ 400268576 \\ \texttt{yex33@mcmaster.ca} \\ L01$

January 29, 2021

1 Timeing Data

1.1 Analysis of f(n)

f(n) is determined to be growing in the order of $\mathcal{O}(n)$. We started by plotting f(n) on a x-y plane and observed a graph similar to that of a linear function. We formed our speculation on f(n) being linear. A linear regression on the data set was then attempted to further investigate. The resulting coefficient of determination is 0.9992, indicating that there is a high chance that f(n) is indeed a linear function. To confirm our guesses, we plotted a log-log graph for f(n) and performed linear regression on the plot. Both the slope of the trend line and the R^2 value were approximately 0.9994. This is strong evidence that f(n) grows in the order of $\mathcal{O}(n)$.

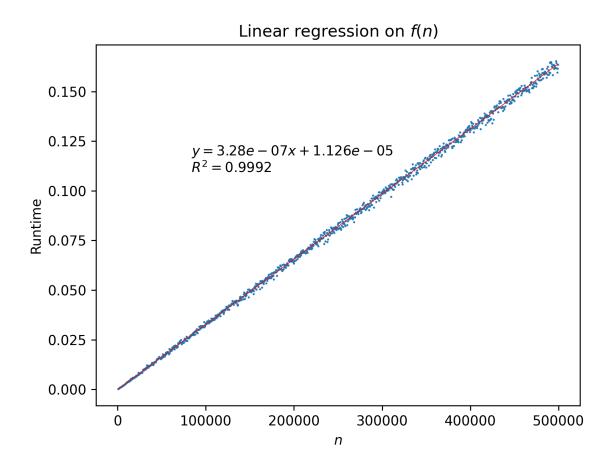


Figure 1: f(n) linear regression

1.2 Analysis of g(n)

By observing the graph of g(n), our guess on the order of growth was polynomial or power. After applying the fitting line and constructed R^2 value, we found that the polynomial

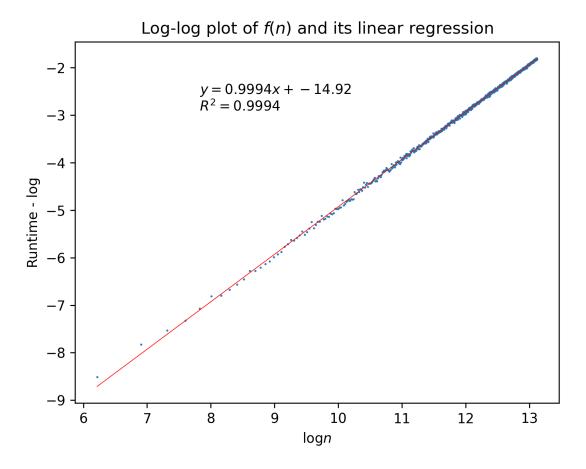


Figure 2: f(n) log linear regression

function with power of 3 fit the dots the most. However, the coefficient of x^3 is relatively smaller than the coefficient of x^2 . To confirm our hypothesis on the growth order, we plotted the log graph and resulted in a linear regression with 2.8548 as the coefficient of x. Because there were nly 43 pairs of data were given for g(n), so the insufficient amount of data ould cause the difference between 2.8548 and 3(the expected growth rate). Overall, with the finite given date set, we concluded that g(n) has a growth order of $\mathcal{O}(x^3)$

1.3 Analysis of h(n)

After plotting the h(n) data set into the graph, our first intuition about the type of growth was linear. However, by the visual contrast with the h(n) (figureh(n)1), we all thought that the fitting line bended too much as a linear function. Therefore, we made the second graph which plotted with log(n) and log(runtime) (figureh(n)2), as the x-axis and the y-axis respectively. Then, we analyzed the coefficient of the term that has the highest power(x). Compared to 1, the oefficient 1.1069 is off by quite a bit. At this point we were uncertain about the intuition we had at the beginning. Because the coefficient is larger than 1 which means it grows faster than linear, however, not as much as polynomial, exponential or power

functions. At this point, we doubted that it could be nlog(n) form. Last but not least, we divided the runtime (nlog(n)) by its number (n) and we got the figure (h(n)3). Our assumption was right and the graph fits as a log function. In conclusion, the h(n) grows in the order of $\mathcal{O}(nlog(n))$