

Lab3: Primality Testing

Part 1

Implement the **modexp** function in Figure 1.4 (pg 19 of the text book) for modular exponentiation. It should take as input three integers x , y , and N and return $x^y \bmod N$

Part 2

Implement the randomized primality testing algorithm in Fig 1.8 (page 27 of the text book) using the **modexp** from part 1 as a subroutine. Given inputs N and k , you should determine whether N is prime or not using k trials. Print N "is prime" or N "is not prime".

What to turn in

You can test your code on arbitrary integers N to test if they are prime or not. In general, with k trials the probability of returning a wrong answer is $1/2^k$. However, Carmichael numbers are composite numbers that pass Fermat's little theorem for all integers a relatively prime to N .

For each of the following Carmichael numbers determine the probability of failure in k trials, using $k=1000$. That is, the probability that the number is determined to be a prime when in fact it is not.

The first 32 Carmichael numbers are: 561, 1105, 1729, 2465, 2821, 6601, 8911, 10585, 15841, 29341, 41041, 46657, 52633, 62745, 63973, 75361, 101101, 115921, 126217, 162401, 172081, 188461, 252601, 278545, 294409, 314821, 334153, 340561, 399001, 410041, 449065, 488881.

Verify that these probabilities are much higher than $1/2^k$.