

Lab 1: Fibonacci Series

Due Wed 1/18/23

Please attend to your assigned lab section only!

Part 1: Implement two separate programs that generate the n -th Fibonacci number. The programs should both take n as command line input. The first algorithm one should implement the recursive algorithm (fib1 on Page 3 of the textbook), and the second one should implement the iterative algorithm (fib2 on Page 4). You should measure the time it takes for each of these versions (use for example, the time module in python) to calculate the n -th Fibonacci number for the following values of n : 1, 5, 10, 15, 20, 25, 30, 35, 40, 41, 42, 43. Finally, create a table of all your results and plot the time taken to compute the Fibonacci numbers using fib1 and fib2, with n on the x-axis and time on the y-axis.

Part 2: Now verify that fib2 is indeed quadratic time. Run fib2 and record the time on the following values of n : 2^{10} (i.e. 2^{10}), 2^{12} , 2^{14} , 2^{16} , 2^{18} , 2^{19} . If it takes more than 20 mins on your machine to compute 2^{19} , then drop the last value above. For this part you can appreciate the fact that Python has native arbitrary precision integer arithmetic. Otherwise, the values of $F(n)$ would easily exceed the 64 bit word size and cause overflow. Plot the time of fib2 versus n .

Grading: Your code must be implemented in Python. To get full credit, you must show your code, output, and plots to the TA and/or the undergrad mentors. Make sure that your grade is recorded in the official sheet. The lab will be graded according to the rubric outlined on the syllabus. Do not submit your code via email or any other means to the TA/mentors. It will be ignored.