

$\Rightarrow$  Reduce the "flowsto" Over-approximate

## I: eliminate Useless Data-Control Flow:

## ① Redundant If Branch.

case 1: Normalized Boolean Expr in Guard is constant.

 $\Rightarrow$  Remove another Block. $\Rightarrow$  Remove the data-control "flowsto"

of variables assigned inside the Block on Variables in guard.

case 2: 2 Blocks in two Branches are syntactically identity.

 $\Rightarrow$  Remove another Block. $\Rightarrow$  Remove the data-control "flowsto" from all Variables in guard.

to variables assigned inside the Block.

 $x \leftarrow 0.$  $\text{if}(x < 3, [y=1], [y=2])$  $\exists v, \forall c, < c, b > \Downarrow v$  $\text{if } c \in b, [y=1], [y=2].$ 

so branches are the same

## ② Redundant While loop.

Case 1: Normalized Boolean Expr in Guard is constant false.

 $\Rightarrow$  Remove the Block of the while Body $\Rightarrow$  Remove the data-control "flowsto" from all Variables in guard.

to variables assigned inside the Block.

 $x \leftarrow 0$ while  $x > 0,$  $y = 1.$ Same as if-case 1.  $\exists v, \forall c, < c, b > \Downarrow v.$ 

## ③ Redundant variables in Guard.

Forb of guard in every if and while command.

 $\forall x \in \text{VAR}(b), x \notin \text{VAR}(\text{NF}(b)).$ remove all the data-control "flowsto" from  $x$  to variables in the Body Block $x \leftarrow g(0)$  $\text{if } c [x = 0], [y=1], [y=2].$ Variable disappeared from  $\text{VAR}(b)$ , or  $\text{VAR}(e)$  or  $\text{VAR}(a)$  by normalization $x \leftarrow g(0)$  $y \leftarrow g(x - x).$ 

same as boolean expression.

remove dependency after normalization.

## II. Remove redundant data-value "flowsto".

for the  $e$  and  $\psi$  in every assignment command.  $y \leftarrow e$  and  $y \leftarrow \psi$  $\forall x \in \text{VAR}(e), x \in \text{VAR}(\text{NF}(e)), \text{ or } x \in \text{VAR}(\psi) \wedge x \notin \text{VAR}(\text{NF}(\psi))$ Remove the data-value "flowsto" from  $x$  to  $y$ III. Non-trivial liveness Analysis.  $\Rightarrow$  variable Dead. $\Rightarrow$  Cannot further Optimize.

example 2: Event Rewriting occurs in a longer adaptivity chain,

and removing the other vertex is safe, keeping both flow doesn't lead to over-approximation.

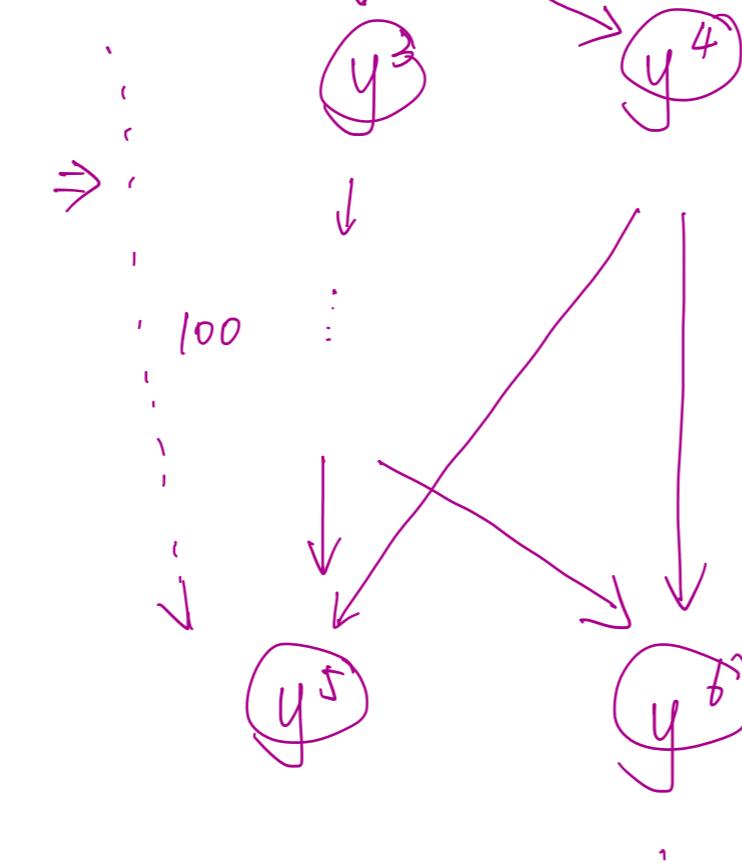
V.

eg:  $z \leftarrow g(0)$        $\xrightarrow{z^1} y^2 \Rightarrow$  Expected Adapt = 2  
 $y \leftarrow 0$        $\downarrow$   
 $x \leftarrow y+1$        $\xrightarrow{x^4} x^3$ . $\Rightarrow$  liveness refined  $\Rightarrow$   $\xrightarrow{z^1} y^2 \Rightarrow$  Adapt = 2.

No over-approximation

## IV: Non-trivial Over-Approximation:

path Sensitive syntactically but not semantically:

 $\Rightarrow$  2 if command have the same guard, they take the same branch always.the adaptivity Expected by  $\max \left\{ \begin{array}{l} \text{Adap}_{\text{truebranch1}} + \text{Adap}_{\text{truebranch2}} \\ \text{Adap}_{\text{f-branch1}} + \text{Adap}_{\text{f-branch2}} \end{array} \right\}$ the Adapt program =  $\max \left\{ \begin{array}{l} \text{Adap}_{\text{truebranch1}} + \text{Adap}_{\text{truebranch2}} \\ \text{Adap}_{\text{f-branch1}} + \text{Adap}_{\text{f-branch2}} \\ \text{Af-branch1} + \text{Af-branch2} \\ \text{Af-branch1} + \text{Af-branch2} \end{array} \right\}$ eg: input a:  $y \leftarrow g(0)$   
 $\text{if } a > 0$   
 $y \leftarrow g^{100}(y)$   
 $\text{else}$   
 $y \leftarrow g(y).$ if  $a > 0$ :  
 $y \leftarrow g(y)$   
 $\text{else}$   
 $y \leftarrow g^{100}(y).$ longest path : 201.      if  $100 = n \Rightarrow 2n+1$ Expected Adapt: 102.       $\Rightarrow n+2.$