DS-	-GA	-1003	Spring	2020	Final	Exam
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Name and section:	

1 True or False

1.	(1 point) dataset.	Adaboost usually works better than random forests if there are outliers in the
	O True	○ False
2.	(1 point) True	[SKIP] Bagging reduces variance of decision trees. ○ False
3.	(1 point) True	Logistic regression can be kernelized. ○ False
4.	(1 point) True	Perceptron will find a unique solution if the data is linearly separable. ○ False
5.	(1 point) ○ True	SGD will always converge to a local optimum when learning neural networks. \bigcirc False
6.	5. (1 point) Given an SVM with quadratic kernel, the dual form is more efficient at inference time than the primal form, assuming the number of support vectors is smaller than the input feature dimension.	
	O True	○ False
	Solutio	
7.		011:
•	(1 point) proaches.	The concepts of bias and variance exist in both Bayesian and frequentist ap-
••	` - /	
	proaches. True (1 point)	The concepts of bias and variance exist in both Bayesian and frequentist ap-
	proaches. True (1 point)	The concepts of bias and variance exist in both Bayesian and frequentist ap— O False Random forest is more efficient than gradient boosted trees because it can be
8.	proaches. True (1 point) parallelize True	The concepts of bias and variance exist in both Bayesian and frequentist ap— False Random forest is more efficient than gradient boosted trees because it can be ed during training.

10.	(1 point) L1 regularization can be used for feature selection. (True
11.	(1 point) Multiclass SVMs use the same weight vector for all classes. O True O False
	Solution:
12.	(1 point) In bagging, increasing bootstrap sample size can reduce variance. O True O False
13.	(1 point) Absolute loss is more robust to outliers than squared loss for regression. O True O False
14.	(1 point) Backpropagation uses dynamic programming.True
15.	(1 point) Given a dataset $\{x_1, x_2, \dots, x_n\}$ sampled from a data generating distribution P, x_1 is an unbiased estimate of the mean of the distribution. \bigcirc True \bigcirc False
2	Multiple Choices
	te: There can be more than one correct answers; select all that apply! No partial credits: correct answers must be checked.
1.	(3 points) Which of the following models can be learned by MLE?
	O Perceptron O Ridge regression O SVMs O Logistic regression
	Solution:
2.	(3 points) If we find our learned model is overfitting, what should we do? (Increase model complexity. (Increase regularization.
	Add more data. Training for a longer period of time.
3.	(3 points) Which of the following is true about support vectors?
	 Support vectors are the examples closest to the decision boundary. Removing support vectors during training will not change the decision boundary. Support vectors are the only examples needed for inference. There are at least two support vectors.

	Solution:
4.	(3 points) In a classification setting, which of the following are usually used as weal learners for boosting?
	 A classifier that always predict the majority class. A decision stump. A classifier that uniformly predicts a class at random. Perceptron.
	Solution:
5.	(3 points) Which of the following description is true about kernels?
	\bigcirc A kernel defines a feature map ϕ that maps x to an infinite-dimensional space. \bigcirc The kernel function k can be considered as a similarity function for two data points \bigcirc The kernel trick provides an efficient way to compute inner products in high dimen sional space. \bigcirc A valid kernel function must produce a positive semi-definite kernel matrix.
6.	(3 points) Which of the following are appropriate activation functions for neural net works?
	$\bigcirc 2x \bigcirc \max(x,0) \bigcirc \begin{cases} 1 & x > 0 \\ 0 & x \le 0 \end{cases} \bigcirc \begin{cases} x & x > 0 \\ 0.01x & x \le 0 \end{cases}$
	Solution:
7.	(3 points) Which of the following can reduce variance of a learning algorithm?
	 Increase the maximum depth of a decision tree. Increase the variance of a zero-mean Gaussian prior of the parameters. Increase the step size (shrinkage) in gradient boosting. Increase λ (weight on the penalty term) in ridge regression.
8.	(3 points) Which of the following loss functions is an upper bound of the 0-1 loss function? (Let $y \in \{1, -1\}$ be the gold label and $f(x) \in \mathbb{R}$ be the predictor output.)
	$\bigcirc (1 - yf(x))^2 \bigcirc \max(0, -yf(x)) \bigcirc e^{-yf(x)} \bigcirc \log(1 + e^{-yf(x)})$
	Solution:

	
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-1	
-1	
9.	(3 points) Consider a small XOR dataset:
	Which of the following model can achieve zero training error?
	A decision tree with depth 1.
	A decision tree with depth 2.
	A two-layer neural network with 2 hidden units and ReLU activation function.
	Chinear soft-margin SVM.
10	(2) If il 1 (1' * 1
10.	(3 points) If the solution of linear regression on a dataset is w^* , what solution would you
	get if you scale all features by a factor of c (i.e. replace x by cx) before doing regression?
	$\bigcirc w^* \bigcirc \frac{w^*}{c} \bigcirc \frac{w^*}{c^2} \bigcirc cw^* \bigcirc c^2w^*$
11	(3 points) Assuming that we can always obtain the optimal solution, adding a regular-
11.	ization term to the objective function of logistic regression can
	•
	O Decrease training error O Increase training error
	O Decrease validation error O Increase validation error
12.	(3 points) Which of the following model will always have a unique optimum regardless of the data?
	
	Cognitive regression Chasso regression
	Solution:
13.	(3 points) Which of the following are necessary conditions for the minimum risk of a classification problem using 0-1 loss (i.e. the Bayes error rate) to be zero?
	\bigcirc The distributions $P(X \mid Y)$ don't overlap.
	The training data is linearly separable.
	\bigcirc Cannot tell. It depends on the class prior $P(Y)$.
	\bigcirc X Y follows a Gaussian distribution.
14.	(3 points) Which of the following is true about neural networks?
	The objective function is convex.
	The objective function is convex. Their nonlinearity is due to the nonlinear activation functions.
	They can only be used for classification.
	Yann Lecun won Turing Award because of his contribution to neural networks.

 x_1

 x_2

y

15. (3 points) Consider OvA and AvA for multiclass classification, if the base binary classifier takes $O(N^2)$ time to train, where N is the number of training examples, which method is more efficient in terms of training time (assuming no parallelization)? \bigcirc OvA Equally efficient \bigcirc AvA Solution: 16. (3 points) Assuming that the data is not separable, increasing C in soft-margin SVMs can O Increase margin Reduce margin Reduce training error Increase training error 17. (3 points) Which of the following is true about the Naive Bayes classifier? O It assumes features are independent conditioned on the label. O It only works with categorical features. O It has a linear decision boundary. O It is a generative model. Solution: 18. (3 points) Which model could have generated the decision boundary shown in the figure below?

Solution:

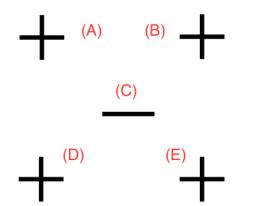
Neural networks

O SVM with Gaussian kernel

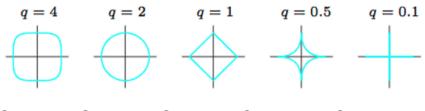
O Logistic regression

Random forest

19. (3 points) Consider training an Adaboost classifier using decision stumps. Given the following 2D dataset, which examples will have their weights increased after the first iteration?



- \bigcirc A \bigcirc B \bigcirc C \bigcirc D \bigcirc E
- 20. (3 points) Consider the regularizer $\ell_q = \left(\sum_{i=1}^d |w_i|^q\right)^{\frac{1}{q}}$. For d=2, which of the following will produce sparse weights?



 $\bigcirc q = 4 \quad \bigcirc q = 2 \quad \bigcirc q = 1 \quad \bigcirc q = 0.5 \quad \bigcirc q = 0.1$

3 Short Questions

- 1. **Optimization.** Consider $f: \mathbb{R} \to \mathbb{R}$, $f(x) = \max(x^2, 2x)$.
 - (a) (1 point) Is f(x) convex? \bigcirc True \bigcirc False
 - (b) (2 points) At which points does the function have non-unique subgradients?

Solution:

(c) (3 points) What is the subgradient at x = 2? Show all valid subgradients if there is more than one.

Solution:

(d) (1 point) How many local minima does f(x) have?

Solution:

2. MLE and Bayesian methods. To estimate the number of visitors to a store (denoted by X) during some fixed time of the day, we assume that X follows a Poisson distribution:

$$p(X = k \mid \lambda) = \text{Poisson}(\lambda) = \frac{\lambda^k e^{-\lambda}}{k!} \quad (\lambda > 0).$$

We then recorded the number of visitors for 10 days and got the following data points:

$$\mathcal{D} = (5, 3, 12, 7, 6, 8, 6, 10, 9, 9).$$

(a) (4 points) What is the maximum likelihood estimate of λ given the observed data?

Solution:

(b) (4 points) Let's put a gamma prior on λ :

$$p(\lambda) = \text{Gamma}(\alpha, \beta) = \frac{\beta^{\alpha}}{\Gamma(\alpha)} \lambda^{\alpha - 1} e^{-\beta \lambda} \quad (\lambda, \alpha, \beta > 0),$$

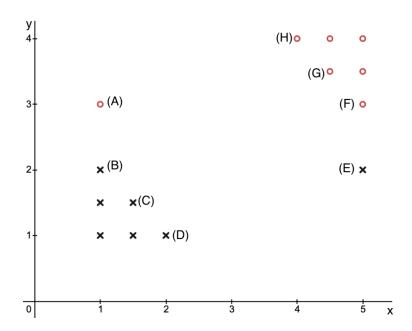
where $\Gamma(\alpha)$ is the gamma function (you can treat it as a constant). If we take the prior Gamma(5, 1), what is the posterior $p(\lambda \mid \mathcal{D})$?

Solution:

- (c) (1 point) Is the Gamma prior conjugate to the Poisson model?
 - True False
- (d) (2 points) Suppose we need to update our estimate of λ as more data arrives, what is the amount of data storage needed if the total number of data points is n?

Solution:

- 3. SVMs. Consider the 2D datasets shown in the figure below. We want to classify the red circles and the black crosses using SVMs.
 - (a) (1 point) Is the data linearly separable?
 - True False
 - (b) Let's first consider using a linear hard-margin SVM.
 - i. (3 points) What's the learned decision boundary?



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ii. (2 points) Select all points that are support vectors.

 \bigcirc A \bigcirc B \bigcirc C \bigcirc D \bigcirc E \bigcirc F \bigcirc G \bigcirc H

iii. (2 points) What's a potential problem of hard-margin SVMs (as demonstrated in this example)?

Solution:

(c) Next, let's consider a linear soft-margin SVM.

i. (3 points) Assuming C is not too extreme (very small or very large), what is a likely decision boundary learned by the soft-margin SVM? (The answer doesn't have to be exact as long as it shows a qualitative difference from the hard-margin SVM.)

Solution:

ii. (2 points) What's the training error rate of the learned SVM?

Solution:

(d) (3 points) Suppose we got the optimal solution w_1 of the hard-margin SVM on the dataset. If we add a new feature to each data points and compute the new optimal solution w_2 , which of the following might be true?

 $\bigcirc \|w_2\|_2 > \|w_1\|_2 \quad \bigcirc \|w_2\|_2 = \|w_1\|_2 \quad \bigcirc \|w_2\|_2 < \|w_1\|_2$

Solution:
