1.FUN WITH VECTOR CALCULUS

1. Assume we have n real-valued scalar data points $x_1, x_2, ..., x_n$. Analytically derive constant μ for which, $\sum_{i=1}^{n} (x_i - \mu)^2$ is minimized.

Here we set it as the loss function $L(\mu)$

$$L(\mu) = \sum_{i=1}^{n} (x_i - \mu)^2$$

In order to get the minimum, we set $\nabla L(\mu) = 0$

$$\nabla L(\mu) = 2\sum_{i=1}^{n} (x_i - \mu) = 0$$

$$\sum_{i=1}^{n} (x_i - \mu) = 0$$

$$\sum_{i=1}^{n} x_i - n\mu = 0$$

$$\mu = \frac{1}{n} \sum_{i=1}^{n} x_i$$

Thus, when μ is the mean of x_1, x_2, \dots, x_n , the loss function is minimized.

2. Assume we have n data points are real d-dimensional vectors. Analytically derive a constant μ for which, $\sum_{i=1}^{n} ||x_i - \mu||_2^2$ is minimized.

We can easily know that μ is also a d-dimensional vector. Here we set it as the loss function $L(\mu)$

$$L(\mu) = \sum_{i=1}^{n} ||x_i - \mu||_2^2 = \sum_{i=1}^{n} \sum_{j=1}^{d} \sqrt{(x_{ij} - \mu_j)^2}^2 = \sum_{i=1}^{n} \sum_{j=1}^{d} (x_{ij} - \mu_j)^2$$

In order to get the minimum, we need to let the derivative of every $\mu_j (j \in (1, ..., d))$ equals to zero so as to get the derivative of μ equals to zero.

$$\frac{\partial L(\mu)}{\partial \mu_j} = -2\sum_{i=1}^n (x_{ij} - \mu_j) = 0$$

$$\mu_j = \frac{1}{n} \sum_{i=1}^n x_{ij}$$

Thus, we can get the value of μ ,

$$\mu = \left[egin{array}{c} rac{\sum_{i=1}^n x_{i1}}{\sum_{i=1}^n x_{i2}} \ rac{\sum_{i=1}^n x_{id}}{n} \ rac{\sum_{i=1}^n x_{id}}{n} \end{array}
ight]$$

Thus, when μ is the mean vector of x_1, x_2, \dots, x_n , the function is minimized.

2.LINEAR REGRESSION WITH NON-STANDARD LOSSES

1. Using matrix/vector notation, write down a loss function that measures the training error in terms of the l_1 -norm.

Assuming there are m data points. For each data point x, the number of its features is n:

$$x^{(i)} = \begin{bmatrix} x_0^{(i)} \\ x_1^{(i)} \\ \vdots \\ x_n^{(i)} \end{bmatrix}$$

For every data point, the $x_0 = 1$ so as to serve the bias. From the question we know that X is the matrix of training data points (stacked row-wise)

$$X = \begin{bmatrix} x_0^{(i)T} \\ x_1^{(i)T} \\ \vdots \\ x_m^{(i)T} \end{bmatrix} = \begin{bmatrix} 1 & x_1^{(i)} & x_2^{(i)} & \cdots & x_n^{(1)} \\ 1 & x_1^{(2)} & x_2^{(2)} & \cdots & x_n^{(2)} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_1^{(i)} & x_2^{(m)} & \cdots & x_n^{(m)} \end{bmatrix}$$

For each data point x_i , it has a label y_i

$$y = \begin{bmatrix} y_1 \\ y_2 \\ \dots \\ y_m \end{bmatrix}$$

We set the weight as ω :

$$\pmb{\omega} = \left[egin{array}{c} \pmb{\omega}_0 \ \pmb{\omega}_1 \ \dots \ \pmb{\omega}_m \end{array}
ight]$$

So the predictions of the data points should be:

$$\begin{bmatrix} \omega_0 x_0^{(1)} + \omega_1 x_1^{(1)} + \dots + \omega_n x_n^{(1)} \\ \dots \\ \dots \\ \omega_0 x_0^{(m)} + \omega_1 x_1^{(m)} + \dots + \omega_n x_n^{(m)} \end{bmatrix} = X \omega$$

Thus the loss should be the l_1 -norm difference between labels Y and predictions:

$$L(\omega) = \sum_{i=1}^{m} |y_i - \sum_{j=1}^{n} \omega_j x_j^{(i)}| = \sum_{i=1}^{m} |y_i - \omega^T x^{(i)}|$$

For conciseness, we write this as:

$$L(\boldsymbol{\omega}) = ||X\boldsymbol{\omega} - \mathbf{y}||_1$$

2. Can you write down the optimal linear model in closed form? If not, why not? So we can't write down the optimal linear model in closed form.

No, because the l_1 loss function is not a continuous derivative function.

From the Figure 1, we can easily know that when $X\omega - Y = 0$, the loss is the minima. However, this point doesn't have derivative. Thus, we cannot find the minima by finding the point whose derivative is zero.

3. If the answer to b is no, can you think of an alternative algorithm to optimize the loss function? Comment on its pros and cons.

Although using gradient descent we can get a comparatively small value closed to the optimal of 11 loss function, it might be hard to reach the optimal(minima). The gradient of the 11 loss

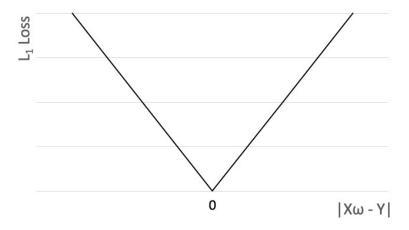


Figure 1. L1 loss function

function only have two values, thus when it is in neighborhood of the optimal, it might still have a comparatively large gradient, thus it might miss the optimal and jump around the minima.

However, in other words, if we try to minimize l_1 loss (a.k.a MAE), that prediction would be the median of all observations. Here's how to prove it: Assuming we have $y_1, y_2, ..., y_n$ and β is the prediction.

$$L_1 = \sum_{i=1}^n |y_i - \beta|$$

$$\frac{\partial L_1}{\partial \beta} = -\sum_{i=1}^n sgn(y_i - \beta)$$

$$sgn(y_i - \beta) = \begin{cases} 1 & \text{if } y_i > \beta \\ -1 & \text{if } y_i < \beta \end{cases}$$

Thus, the derivative equals to 0 when there is the same number of positive and negative terms among the $y_i - \beta$, which means β should be the median of y_i

Pros:

a. More robust to outliers compared to L2 loss;

b. Easy to understand and implement.

Cons

a. The complexity for finding median would be high when the data set is huge;

b. Median can be a bit jumpy in small samples made up of discrete values;

c. When data points are a bit of clustered, using median might not a good choice.

3.HARD CODING A MULTI-LAYER PERCEPTRON

The multi-layer perceptron network structure is shown in figure 2: for Perceptron $1 P_1$:

$$f(x) = \begin{cases} 1 & \text{if } x_2 - x_1 > 0 \\ 0 & \text{otherwise} \end{cases}$$

for Perceptron 1 P_2 :

$$f(x) = \begin{cases} 1 & \text{if } x_3 - x_2 > 0 \\ 0 & \text{otherwise} \end{cases}$$

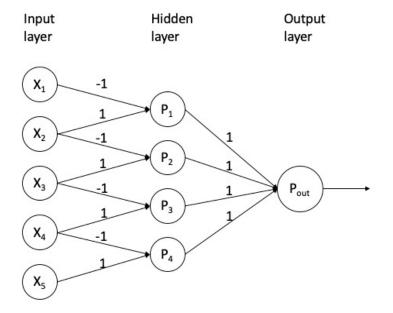


Figure 2. structure of the neural network.

for Perceptron 1 P_3 :

$$f(x) = \begin{cases} 1 & \text{if } x_4 - x_3 > 0 \\ 0 & \text{otherwise} \end{cases}$$

for Perceptron 1 P_4 :

$$f(x) = \begin{cases} 1 & \text{if } x_5 - x_4 > 0 \\ 0 & \text{otherwise} \end{cases}$$

So only when all perceptrons have the output as 1, then it meets the requirement that $x_1 < x_2 < x_3 < x_4 < x_5$. Thus, for Perceptron out P_{out} :

$$f(x) = \begin{cases} 1 & \text{if } x_1 + x_2 + x_3 + x_4 = 4\\ -1 & \text{otherwise} \end{cases}$$

9/18/2020

prefer PyTorch, which is based on an earlier library called Torch (designed for training neural nets via backprop). nets. Training these is a bit more involved, and implementing from scratch requires time and effort. Instead, we just use well-established libraries. I OK, thus far we have been talking about linear models. All these can be viewed as a single-layer neural net. The next step is to move on to multi-layer

```
:[ ] nI
                                 import numpy as np
import torchvision
                import torch
```

Torch handles data types a bit differently. Everything in torch is a tensor.

```
] nI
                           contest of b: tensor([[0.8165, 0.7560, 0.6727],
                                                                                contest of a: [[0.816508
                                                                                                                                     print("contest of b: ", b)
                                                                                                                                                                                          # Q4.1 Display the contents of a, b
                                                                                                                                                             print("contest of a: ", a)
                                                        [0.38200301 0.06110529 0.70656539]]
                                                                                                                                                                                                                                                         Ш
                                                                                                                                                                                                                                                                                 ||
                                                                                                                                                                                                                                               torch.from_numpy(a)
                                                                                                                                                                                                                                                                            np.random.rand(2,3)
[0.3820, 0.0611, 0.7066]], dtype=torch.float64)
                                                                                      0.75597224 0.67269371]
```

The idea in Torch is that tensors allow for easy forward (function evaluations) and backward (gradient) passes.

9/18/2020 hw1prob4

```
] uI
                                                                                                                                       <u>..</u>
                                                                                                                                         ×
                                                                                      У
                                                                                                                 ×
print(x)
           print(x.grad)
                        z.backward()
                                     print(z)
                                                z = y.sum()
                                                            print(y)
                                                                                                                  Ш
                                                                                                                                           Ш
                                                                                         ||
                                                                                      torch.matmul(A,x) + b
                                                                                                                          torch.rand(2,1)
                                                                                                              torch.rand(2,1, requires_grad=True)
                                                                                                                                       torch.rand(2,2)
```

Fashion MNIST dataset, which is a database of grayscale images of clothing items. Notice how the backward pass computed the gradients using autograd. OK, enough background. Time to train some networks. Let us load the

```
In
                                                                                                                                                                               <u>.</u>
                                                                                                                                                                               trainingdata = torchvision.datasets.FashionMNIST('./FashionMNIST/',train=True,download=True,transform
rchvision.transforms.ToTensor())
                                                                                                                    =torchvision.transforms.ToTensor())
                                                          testdata = torchvision.datasets.FashionMNIST('./FashionMNIST/',train=False,download=True,transform=to
```

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-images-idx3-ubyte.gz to ./FashionMNIST/FashionMNIST/raw/train-images-idx3-ubyte.gz

Extracting ./FashionMNIST/FashionMNIST/raw/train-images-idx3-ubyte.gz to ./FashionMNIST/FashionMNIS

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-labels-idx1-ubyte.gz to ./FashionMNIST/FashionMNIST/raw/train-labels-idx1-ubyte.gz

Extracting ./FashionMNIST/FashionMNIST/raw/train-labels-idx1-ubyte.gz to ./FashionMNIST/FashionMNIS

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10k-images-idx3-ubyte.gz ./FashionMNIST/FashionMNIST/raw/t10k-images-idx3-ubyte.gz to

Extracting ./FashionMNIST/FashionMNIST/raw/t10k-images-idx3-ubyte.gz to ./FashionMNIST/FashionMNIST/

Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/t10k-labels-idx1-ubyte.gz to ./FashionMNIST/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz

Extracting ./FashionMNIST/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz to ./FashionMNIST/FashionMNIST/

Processing...

c/utils/tensor_numpy.cpp:141.) rning will be suppressed for the rest of this program. (Triggered internally at the array to protect its data or make it writeable before converting it to a ite to the underlying (supposedly non-writeable) NumPy array using the tensor. You may want to copy Py array is not writeable, and PyTorch does not support non-writeable tensors. /usr/local/lib/python3.6/dist-packages/torchvision/datasets/mnist.py:469: UserWarning: The given Num tensor. This type of wa This means you can wr /pytorch/torch/csr

return torch.from_numpy(parsed.astype(m[2], copy=False)).view(*s)

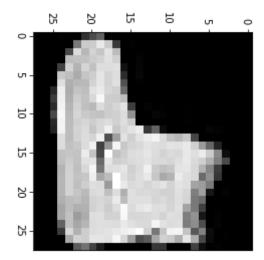
Let us examine the size of the dataset.

```
In [
                                                                                                                                                                                                                                                                   # that means each image has 28*28=784 pixels
                                                                                                                                                                                                                                                                                                                          \#'28*28' means the width and height of each image are both 28 pixels
                                                                                                                                                                                                                                                                                                                                                                           # '1' means each pixel only has one channel, that's grayscale value
print("label for each data is", type(trainingdata[0][1]))
                                                   print("the size of each image data: ", trainingdata[0][0].size())
                                                                                                          print("the size of each data point vector: ", len(trainingdata[0]))
                                                                                                                                                           print("the number of testing data points: "
                                                                                                                                                                                                            print("the number of traning data points: ", len(trainingdata))
                                                                                                                                                                                                                                                                                                                                                                                                                                  The data size of each image is 1*28*28
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  For each data point, we have the image data and the actual label for this
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              What is the number of features in each data point?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         There are 60000 training data points and 10000 testing data points in the
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     How many training and testing data points are
                                                                                                                                                           ', len(testdata))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        there in the dataset?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ımage.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dataset
```

```
the number of traning data points: 60000
the number of testing data points: 10000
the size of each data point vector: 2
the size of each image data: torch.Size([1, 28, 28])
label for each data is <class 'int'>
```

Let us try to visualize some of the images. Since each data point is a tensor (not an array) we need to postprocess to use matplotlib.

```
In [ ]:
                                                                                                                                                                                                                                 import matplotlib.pyplot as plt
plt.show()
                                                                 plt.figure()
                                                                                                                                image, label = trainingdata[0]
                            plt.imshow(image[0], cmap='gray')
                                                                                                  \# Q4.3 Assuming each sample is an image of size 28x28, show it in matplotlib.
                                                                                                                                                                                                      %matplotlib inline
```



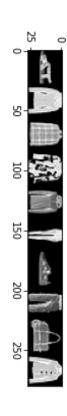
Let's try plotting several images. This is conveniently achieved in PyTorch using a data loader, which loads data in batches

```
In [ ]:
                                                                                                                                                                                                                                                                                                                                                                                                                                                        trainDataLoader = torch.utils.data.DataLoader(trainingdata, batch_size=64, shuffle=True)
                                                                                                                                                                       torch.Size([64, 1, 28, 28]) tensor([5, 4, 6, 6, 2, 1, 7, 1, 8, 4, 8, 8, 1, 6, 8, 8, 0, 8, 7, 4,
                                                                                                                                                                                                                                                                                 print(images.size(), labels)
                                                                                                                                                                                                                                                                                                                                                                                                testDataLoader = torch.utils.data.DataLoader(testdata, batch_size=64, shuffle=False)
                                                                                                                                                                                                                                                                                                                                              images, labels = iter(trainDataLoader).next()
2, 1, 3, 8, 2, 2, 4, 0, 1, 4, 5, 3, 3, 2, 5, 5, 7, 3, 6, 4, 1, 5, 2, 7, 1, 0, 7, 1, 4, 6, 5, 0, 2, 6, 2, 7, 2, 6])
                                                                                                                                                                             2,
```

9/18/2020 hw1prob4

```
] nI
plt.show()
                                     plt.imshow(row, cmap='gray')
                                                                     print("Showing the 10 images in one row:")
                                                                                                               plt.figure()
                                                                                                                                              row = np.concatenate([first_ten_images[i] for i in range(10)], axis=1)
                                                                                                                                                                                   first_ten_images = images[:10, 0,...].numpy()
                                                                                                                                                                                                                                                                    returned by testDataLoader.
                                                                                                                                                                                                                                                                                                       Q4.4 Visualize the first 10 images of the first minibatch
```

Showing the 10 images in one row:



logistic regression (similar to the one discussed in class notes). Now we are ready to define our linear model. Here is some boilerplate PyTorch code that implements the forward model for a single layer network for

```
In [ ]:
                                                                                                                                                                                                                                                                                                                                                      class LinearReg(torch.nn.Module):
optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
                                                       net = LinearReg().cuda()
                            Loss = torch.nn.CrossEntropyLoss()
                                                                                                                                                                                                        def forward(self, x):
                                                                                                                                                                                                                                                                                           super(LinearReg, self).__init_
                                                                                                                  return transformed_x
                                                                                                                                               transformed_x = self.linear(x)
                                                                                                                                                                          x = x.view(-1,28*28)
                                                                                                                                                                                                                                                                  self.linear = torch.nn.Linear(28*28,10)
                                                                                                                                                                                                                                                                                                                             _init_
                                                                                                                                                                                                                                                                                                                         _(self):
```

Cool! Now we have set everything up. Let's try to train the network.

```
In [
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       train_loss_history = []
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   num_of_epochs =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   net = LinearReg().cuda()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #Initiate network
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             test_loss_history = []
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for i in range(num_of_epochs):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Loss = torch.nn.CrossEntropyLoss()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         and print the train/test losses.
                                                                                                                                                                  epoch_test_loss = 0
                                                                                                                                                                                                                                                                                                                           epoch_train_loss /= len(trainingdata)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               epoch_train_loss = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #shuffle training data
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 execute the next code block.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Save them in the variables above. If done correctly, you should be able to
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Q4.5 Write down a for-loop that trains this network for 20 minibatch iterations,
                                                                                                                                                                                                                                                                                    train_loss_history.append(epoch_train_loss)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           #train the net with each minibatch
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        trainDataLoader = torch.utils.data.DataLoader(trainingdata, batch_size=64, shuffle=True)
                                                                                                                           for images, labels in testDataLoader:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for images, labels in trainDataLoader:
                                                                                                                                                                                                            test the net with each minibatch
                                                                                                                                                                                                                                                                                                                                                                            calculate train loss for the epoch
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  optimizer.zero_grad()
epoch_test_loss += batch_images_loss
                                                                                     preds = net(images.cuda())
                                                                                                                                                                                                                                                                                                                                                                                                                                                      optimizer.step()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            batch_images_loss.backward()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        #optimize the network
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  epoch_train_loss += batch_images_loss
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   preds = net(images.cuda())
                                         batch_images_loss = Loss(preds, labels.cuda())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         batch_images_loss = Loss(preds, labels.cuda())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             # calculate train loss of the current minibatch
```

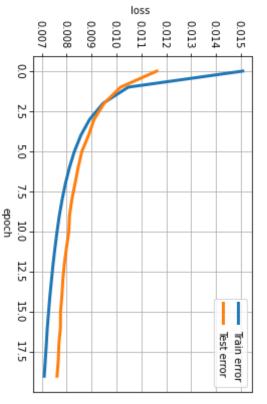
```
print('Epoch: {}, Train Loss: {}, Test Loss: {}'.format(i, epoch_train_loss, epoch_test_loss))
                                                                                                                            test_loss_history.append(epoch_test_loss)
                                                                                                                                                                                            epoch_test_loss /= len(testdata)
                                                                                                                                                                                                                                                            # calculate test loss for the epoch
```

```
Epoch:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Epoch:
                                                                           Epoch:
                                                                                                                                                                                 Epoch:
                                                                                                                                                                                                                                   Epoch:
                                                                                                                                                                                                                                                                                      Epoch:
                                                                                                                                                                                                                                                                                                               Epoch:
                                                                                                                                                                                                                                                                                                                                        Epoch:
                                                                                                                                                                                                                                                                                                                                                                  Epoch
                                                                                                                                                                                                                                                                                                                                                                                           Epoch:
                                                                                                                                                                                                                                                                                                                                                                                                                    Epoch
 Epoch:
                                                    Epoch:
                                                                                                     Epoch:
                                                                                                                               Epoch:
                                                                                                                                                       Epoch:
                                                                                                                                                                                                           Epoch:
                                                                                                                                                                                                                                                                                                                                                                                                                                               Epoch:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Epoch:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Train Loss: 0.010432981885969639,
                                                                                                                                                                                                                                                              Train Loss:
                                                                                                                                                                                                                                                                                                                  Train
                                                                                                                                                                                                                                                                                                                                                                                                                       Train
                                                                                                                                                                                                                                                                                                                                                                                                                                                 Train
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Train
                                                                                                                                                                                                                                                                                         Train Loss:
                                                                                                                                                                                                                                                                                                                                           Train
                                                                                                                                                                                                                                                                                                                                                                     Train
                                                                                                                                                                                                                                                                                                                                                                                              Train
                                                                                                                                                                                                                                Train Loss: 0.007574894465506077, Test Loss: 0.008048789575695992
                                                                                                     Train Loss:
                                                                                                                                                                                                           Train Loss:
 Train Loss:
                            Train
                                                     Train
                                                                                                                                                          Train
                                                                              Train
                                                                                                                                 Train
                                                                                                                                                                                    Train
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Loss: 0.01502606924623251, Test Loss: 0.011578425765037537
                                                                                                                                                                                                                                                                                                                  Loss:
                                                                                                                                                                                                                                                                                                                                           Loss:
                                                                                                                                                                                                                                                                                                                                                                                                                      Loss:
                                                                                                                                                                                                                                                                                                                                                                                                                                                 Loss:
                                                                                                                                                                                                                                                                                                                                                                                              Loss
                                                                                                                                                                                                                                                                                                                                                                     Loss
                                                    Loss:
                                                                              Loss:
                                                                                                                               Loss:
                                                                                                                                                          Loss:
                                                                                                                                                                                  Loss:
                          Loss:
                                                                                                                                                                                                                                                            0.007666518911719322, Test Loss: 0.00807636696845293
                                                                                                                                                                                                                                                                                      0.007779350504279137,
                                                                                                                                                                                                                                                                                                                                        0.00807273667305708, Test Loss: 0.00842297449707985
                                                                                                                                                                                                                                                                                                                                                                                                                    0.008885594084858894,
                                                                                                                                                                                                                                                                                                                                                                                                                                              0.009428427554666996,
                                                                                                                                                                                                                                                                                                               0.007911734282970428, Test Loss: 0.008297959342598915
                                                                                                                                                                                                                                                                                                                                                                  0.008271351456642151, Test Loss: 0.008571295067667961
                                                                                                                                                                                                                                                                                                                                                                                           0.008530200459063053,
                         0.007103899493813515,
                                                                                                                                                       0.0073526217602193356, Test Loss: 0.0078074736520648
                                                                                                                                                                                 0.007416723761707544, Test Loss: 0.007868158631026745
                                                                                                                                                                                                          0.007492510136216879,
0.007061449345201254, Test Loss: 0.007573876064270735
                                                  0.007145352195948362, Test Loss: 0.007648747880011797
                                                                                                     0.007235296536237001, Test Loss: 0.007714950945228338
                                                                                                                              0.007288788910955191, Test Loss: 0.007769959978759289
                                                                           0.0071831876412034035, Test Loss: 0.0077091665007174015
                                                                                                                                                                                                                                                                                      Test Loss: 0.008169146254658699
                                                                                                                                                                                                                                                                                                                                                                                                                    Test Loss: 0.00906306505203247
                                                                                                                                                                                                                                                                                                                                                                                                                                              Test Loss: 0.009466097690165043
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Test Loss: 0.010125137865543365
                                                                                                                                                                                                                                                                                                                                                                                           Test Loss: 0.008839458227157593
                         Test Loss: 0.007626079488545656
                                                                                                                                                                                                          Test Loss: 0.007952781394124031
```

9/18/2020 hw1prob4

```
In [ ]:
                                                                                                                                                                      plt.plot(range(20), train_loss_history,'-',linewidth=3,label='Train error')
plt.legend()
                                                                    plt.ylabel('loss')
                              plt.grid(True)
                                                                                                    plt.xlabel('epoch')
                                                                                                                                    plt.plot(range(20),test_loss_history,'-',linewidth=3,label='Test error')
```

Out[]: <matplotlib.legend.Legend at 0x7f243392e710>



output of the neural network model and computing the index corresponding to the maximum activation. Something like Neat! Now let's evaluate our model accuracy on the entire dataset. The predicted class label for a given input image can computed by looking at the

predicted_output = net(images) _, predicted_labels = torch.max(predicted_output,1)

```
In [ ]:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               In [ ]:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          def evaluate(dataloader):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       device='cuda:0', grad_fn=<MaxBackward0>),
indices=tensor([3, 1, 7, 5, 8, 2, 5, 6, 8, 9, 1, 9, 1, 8, 1, 5], device='cuda:0'))
tensor([3, 2, 7, 5, 8, 4, 5, 6, 8, 9, 1, 9, 1, 8, 1, 5])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     predicted_output = net(images.cuda())
  print('Train acc = %0.2f, test acc =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      values=tensor([ 6.1149, 2.9275, 8.9590, 7.8504, 6.6379, 6.2165, 10.2046, 4.3740,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        torch.return_types.max(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          print(labels)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 print(torch.max(predicted_output, 1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   fit = Loss(predicted_output, labels.cuda())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            correct_pred = 0
                                                                                                                                     return correct_pred/num_of_all_images
                                                                                                                                                                                                                                                                                                                                                                                                                                  for images, labels in dataloader:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                num_of_all_images = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             # Here, accuracy is measured by probability of successful classification
                                                                                                                                                                                         num_of_all_images += len(images)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Q4.6 Implement a function here that evaluates training and testing accuracy.
                                                                                                                                                                                                                                        correct_pred += int((preds_diff==0).sum())
                                                                                                                                                                                                                                                                                      preds_diff = labels - predicted_labels.cpu()
                                                                                                                                                                                                                                                                                                                                                                                   predicted_output = net(images.cuda())
                                                                                                                                                                                                                                                                                                                                  _, predicted_labels = torch.max(predicted_output,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        7.0905, 11.6778, 10.4770, 10.4350, 6.6251, 4.7262, 9.3121, 4.5606],
%0.2f' % (evaluate(trainDataLoader), evaluate(testDataLoader)))
```

Train acc

II

0.85,

test acc = 0.83