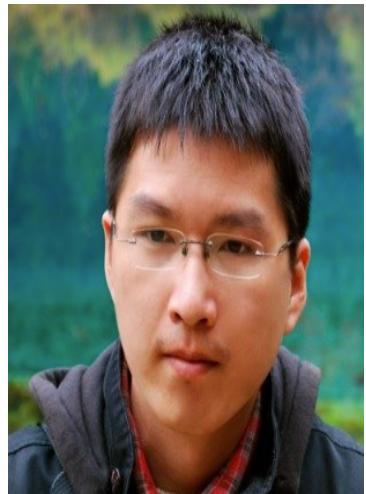
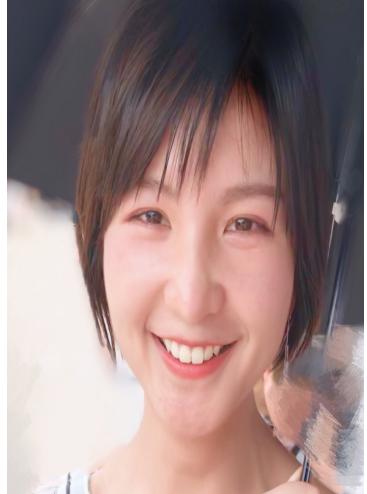
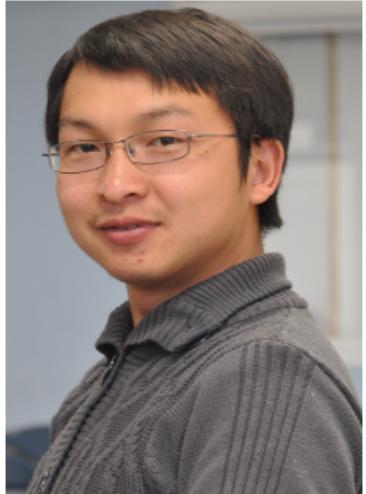


DeepDrawing: A Deep Learning Approach to Graph Drawing



Yong Wang¹.

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Qianwen Wang¹

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Tengfei Ma³.

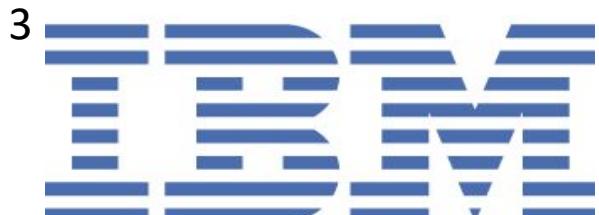
Huamin Qu¹

<http://yong-wang.org/proj/deepDrawing.html>



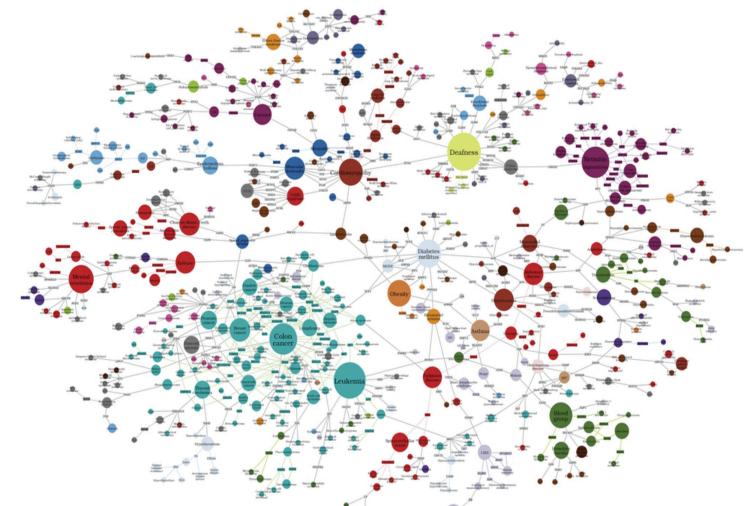
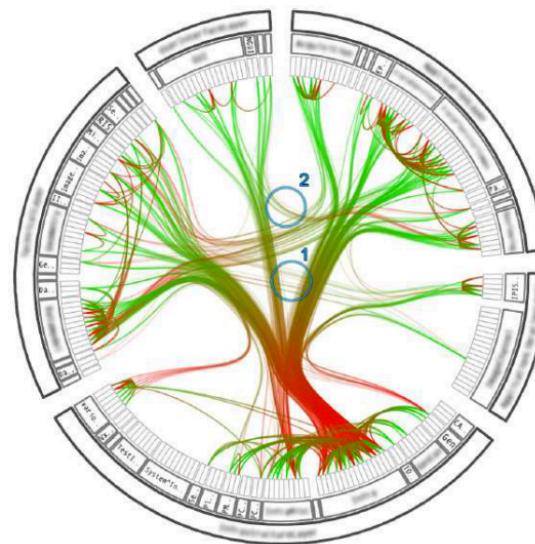
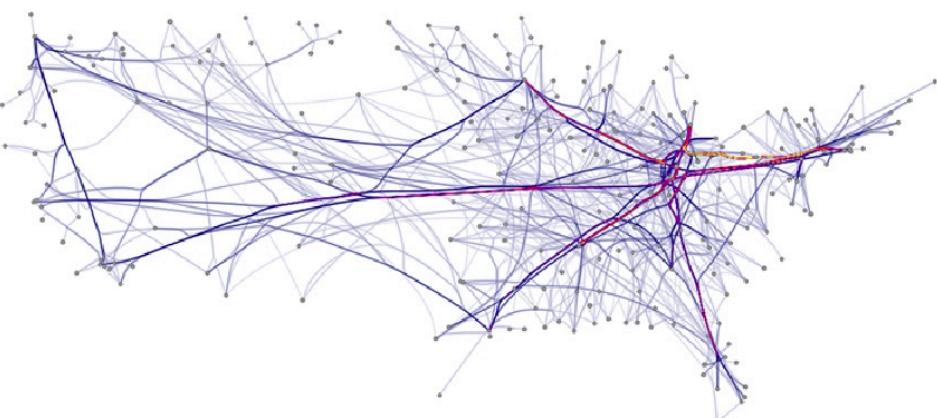
香港科技大學
THE HONG KONG
UNIVERSITY OF SCIENCE
AND TECHNOLOGY

2 Microsoft®
Research
微软亚洲研究院



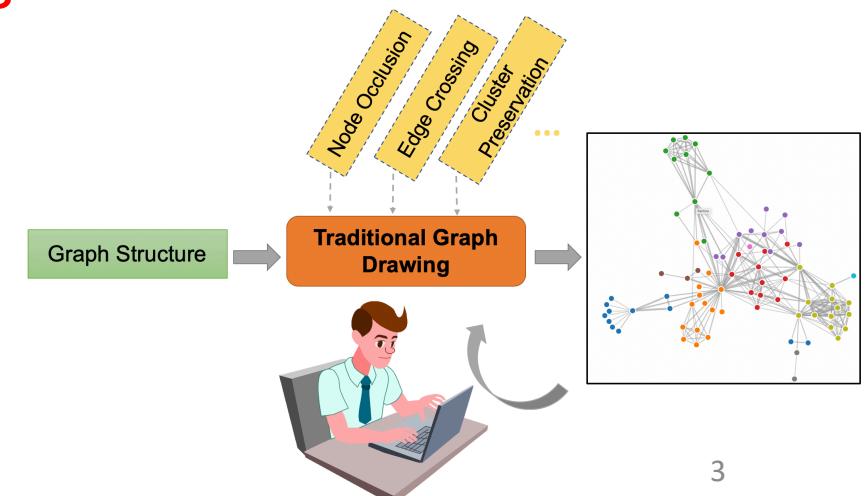
Motivation

- Graph drawing has been extensively studied to facilitate the exploration, analysis and presentation of networks!



Motivation

- Graph drawing has been extensively studied to facilitate the exploration, analysis and presentation of networks!
- However, users often need to find a desirable graph layout through trial-and-error:
 - Tune different algorithm-specific parameters
 - Compare different drawing results



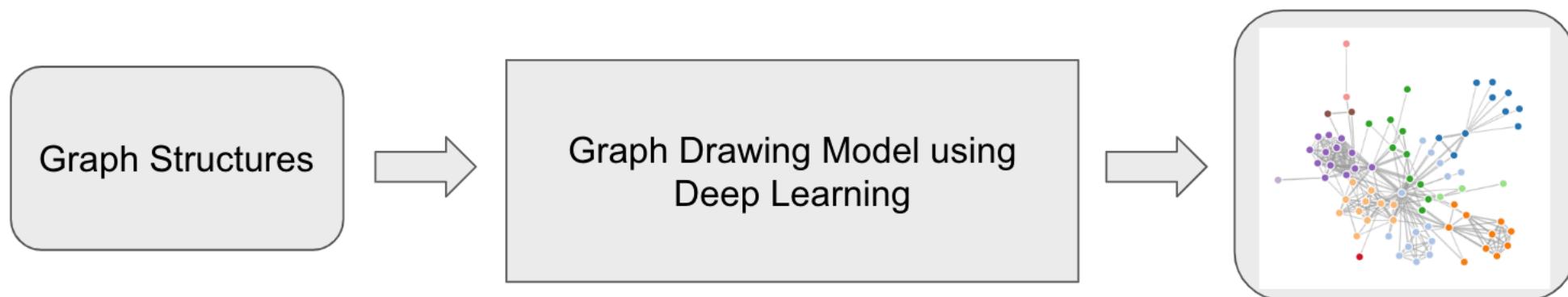
Motivation

- Graph drawing has been extensively studied to facilitate the exploration, analysis and presentation of networks!
- However, users often need to find a desirable graph layout through trial-and-error:

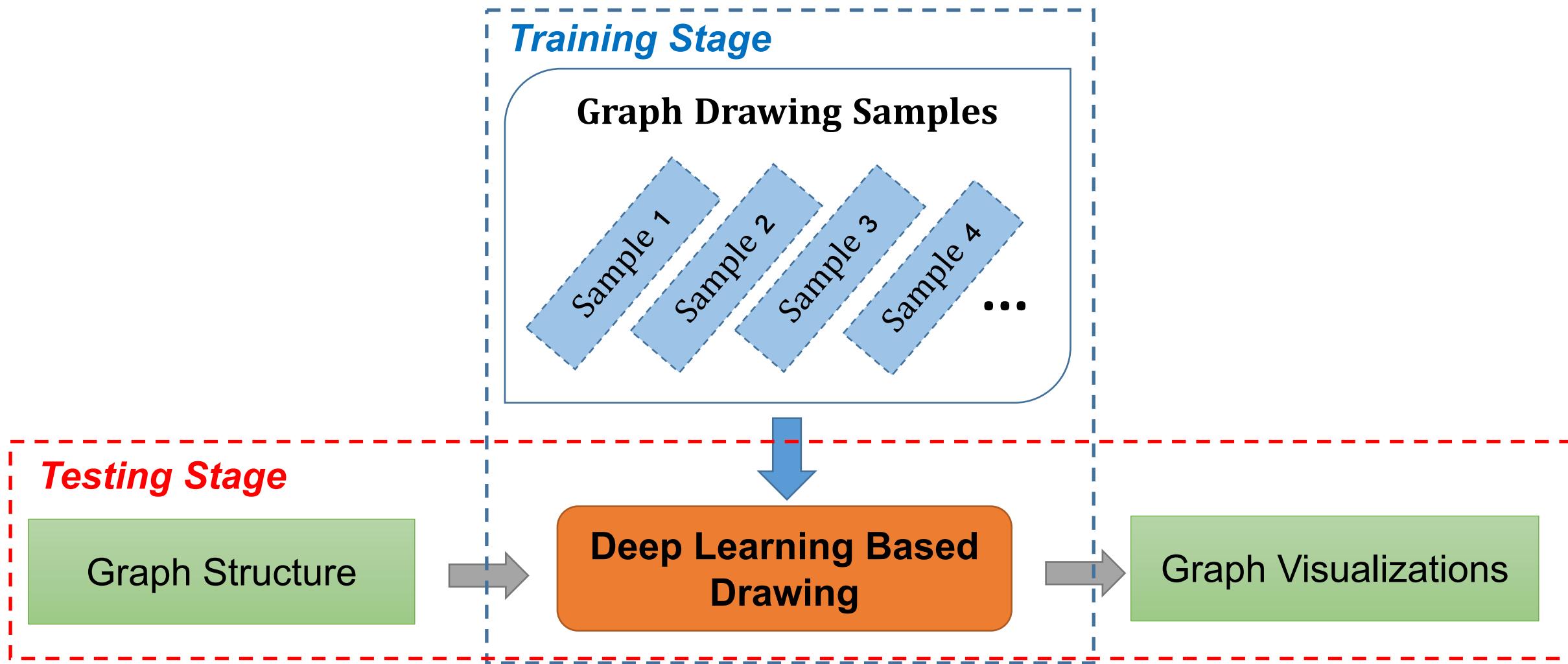
It is time-consuming and not user-friendly, especially for non-expert users!

Research Question

- Deep learning techniques have shown a powerful capability of modelling the training data and further making predictions in many applications
- Can we model graph drawing as a learning and prediction problem and further generate drawings for input graphs directly?



Overall Idea



Challenges

- Model Architecture
- Loss Function Design
- Training Datasets

Challenges

- **Model Architecture**
 - Existing deep learning techniques are mainly applied to the Euclidean data (e.g., images, videos and texts), instead of graphs
 - Recent research on Graph Neural Network mainly targets at node classification and link prediction on a **single graph**, which is much **different** from graph drawing

Challenges

- **Model Architecture**
- **Loss Function Design**
 - How to evaluate whether a drawing for an input graph is "correct" or not?

Challenges

- **Model Architecture**
- **Loss Function Design**
- **Training Datasets**
 - There are no publicly-available high-quality datasets for graph drawing

DeepDrawing

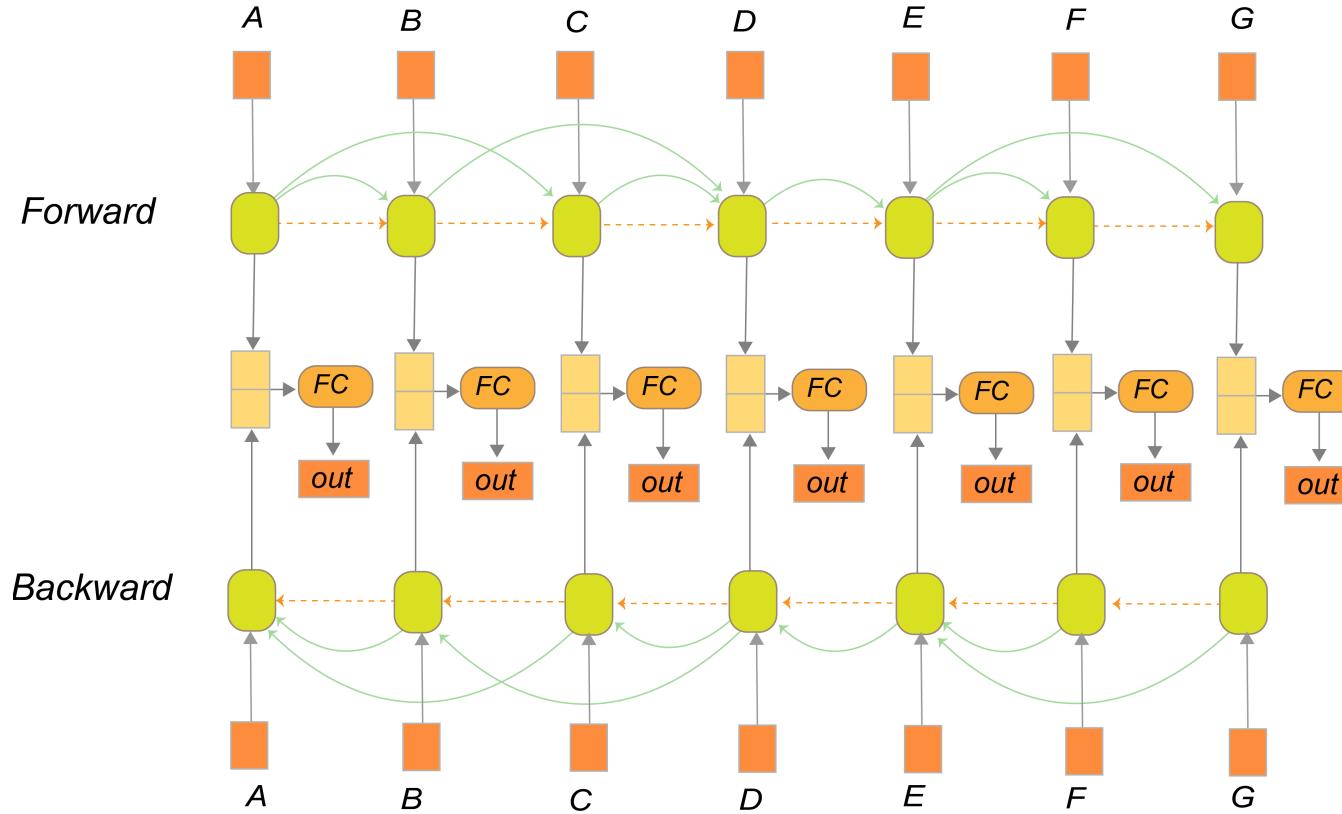
- Model Architecture
- Model Input
- Loss Function Design
- Dataset Generation

DeepDrawing – Model Architecture

- Major Considerations
 - The majority of graph neural networks mainly focus on the learning and prediction tasks for **a single graph**
 - However, a recent study^[1] has shown that **RNNs** are capable of modelling the structure information of multiple graphs

[1] J. You, R. Ying, X. Ren, W. L. Hamilton, and J. Leskovec. Graphrnn: a deep generative model for graphs. In *Proceedings of the 35th International Conference on Machine Learning*, 2018.

DeepDrawing – Model Architecture

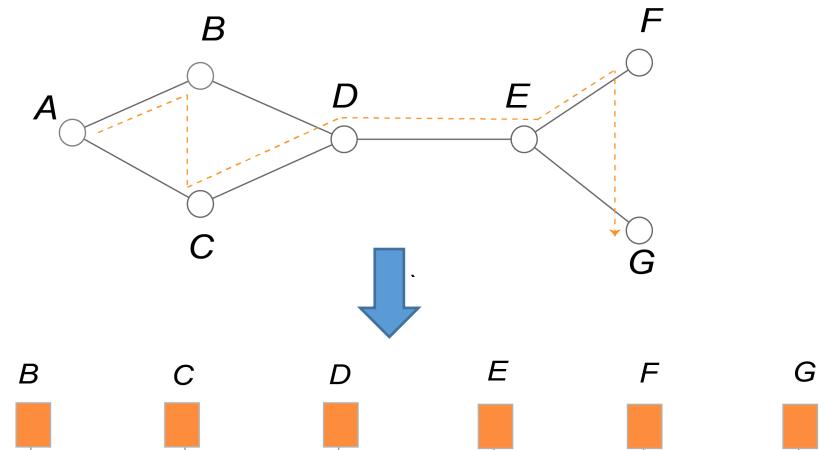


We propose a bi-directional graph-LSTM based model for graph drawing.

DeepDrawing – Model Architecture

- Architecture Details:

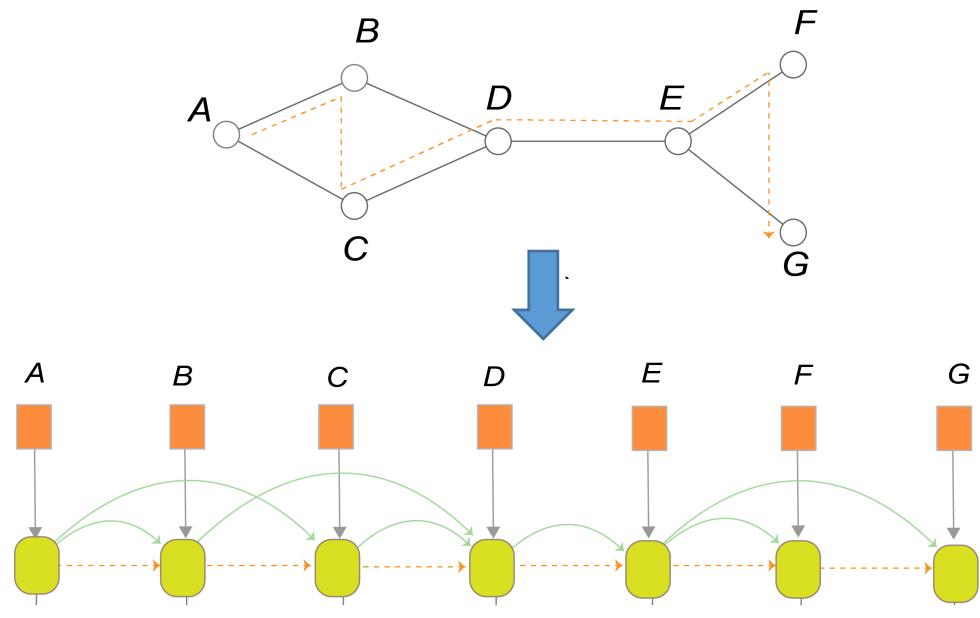
- BFS-ordering of graph nodes



DeepDrawing – Model Architecture

- Architecture Details:

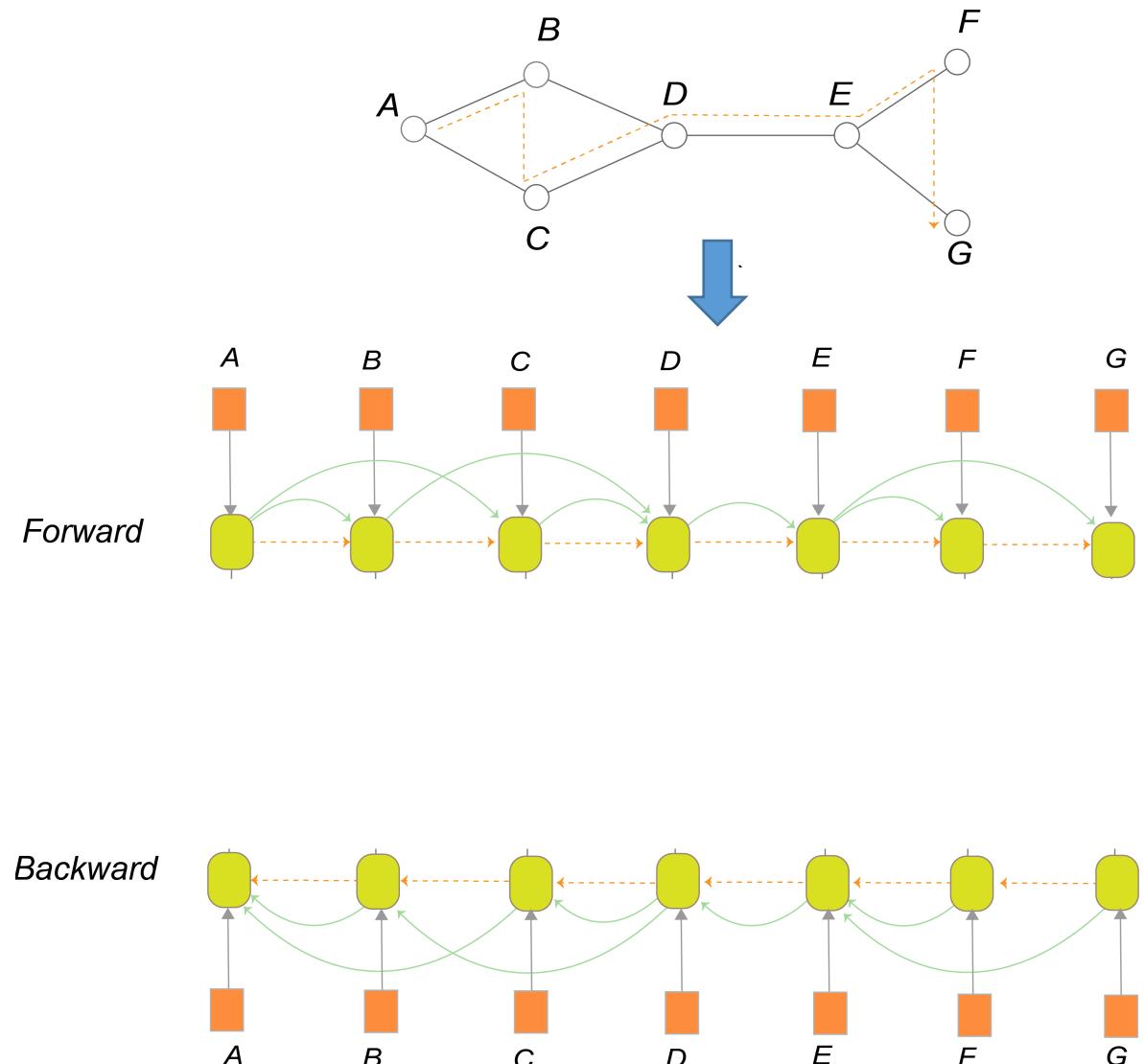
- BFS-ordering of graph nodes
- Fake edges (dotted yellow arrow) and real edges (green arrow)



DeepDrawing – Model Architecture

➤ Architecture Details:

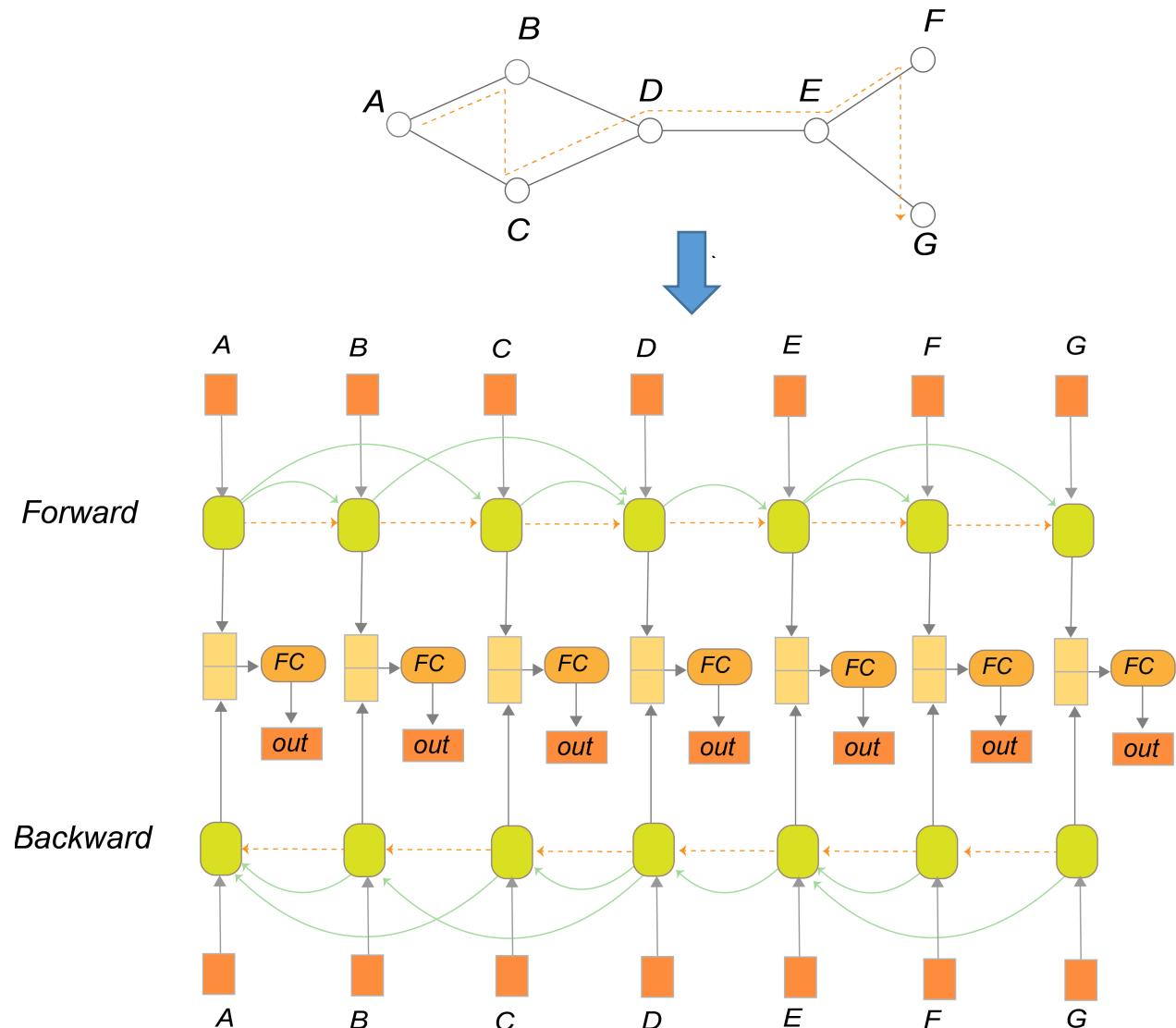
- BFS-ordering of graph nodes
- Fake edges and real edges
- Bi-directional



DeepDrawing – Model Architecture

➤ Architecture Details:

- BFS-ordering of graph nodes
- Fake edges and real edges
- Bi-directional



DeepDrawing – Model Input

- Node Feature Vector
 - Natural choice: node embedding
 - A fixed-length adjacency vector encoding the connection information between the current node and its prior nodes.
- They mainly target at single graphs and are not able to be generalized to multiple graphs^[2]!

[2] M. Heimann and D. Koutra. On generalizing neural node embedding methods to multi-network problems.
In *KDD MLG Workshop*, 2017.

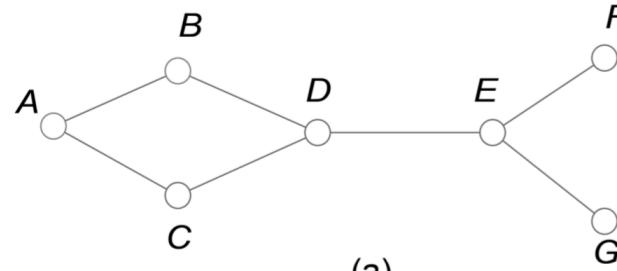
DeepDrawing – Model Input

- Node Ordering
 - Random ordering

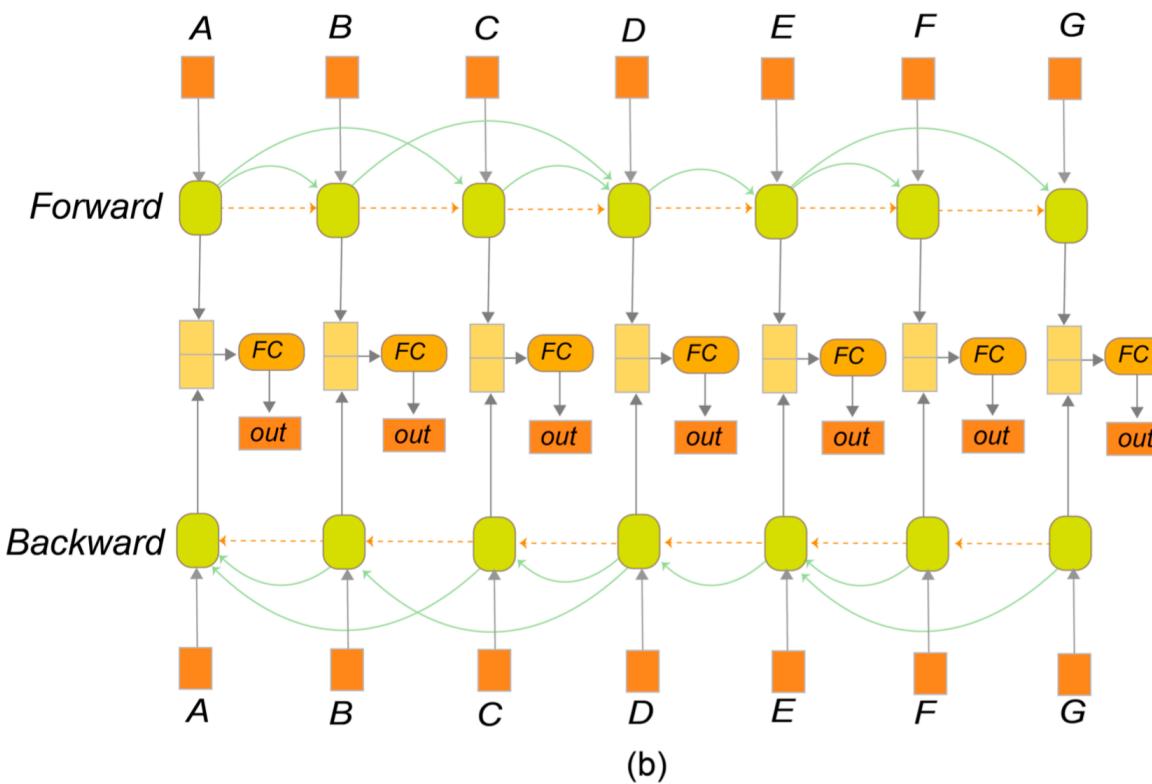
The possible orderings for an input graph can be very large!
 - **BFS ordering**
 - Avoid exhaustively going through all possible node permutations
 - There is **an upper bound** for the possible connection between the current node and its prior furthest nodes along the BFS sequence^[1]!

[1] J. You, R. Ying, X. Ren, W. L. Hamilton, and J. Leskovec. Graphrnn: a deep generative model for graphs. In *Proceedings of the 35th International Conference on Machine Learning*, 2018.

DeepDrawing – Model Input



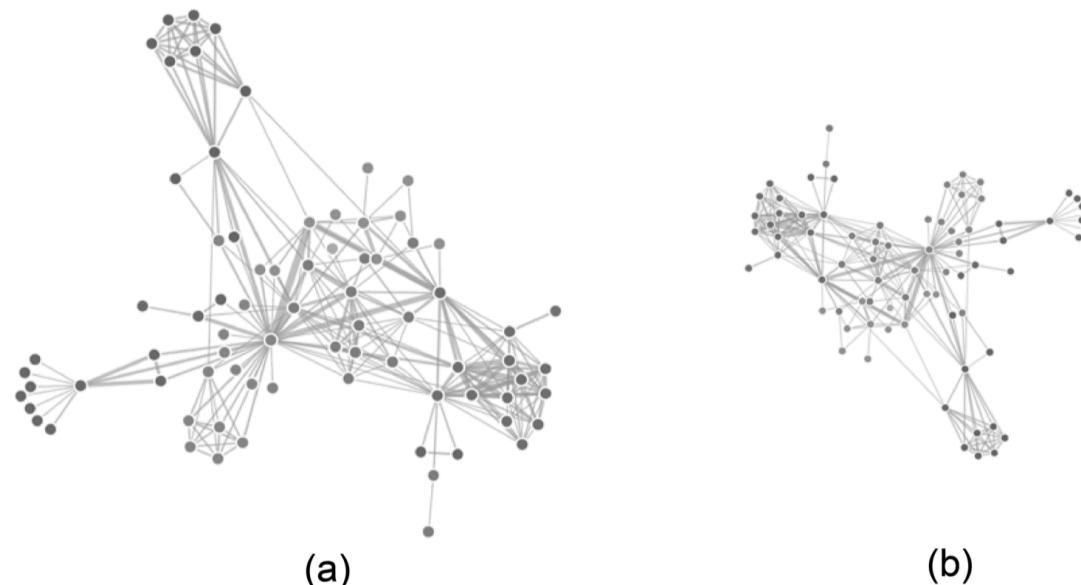
(a)



(b)

DeepDrawing – Loss Function Design

- Design Considerations
 - Make the predicted drawings as **similar** as possible to the drawings of ground-truth
 - The function should be **invariant to translation, rotation and scaling**



DeepDrawing – Loss Function Design

➤ Procrustes Statistic

$$R^2 = 1 - \frac{(tr(C^T \bar{C} \bar{C}^T C)^{1/2})^2}{tr(C^T C) tr(\bar{C}^T \bar{C})}$$

- It is transformation-invariant
- It is between 0 and 1
- Zero means the drawings are exactly the same; while one means they are totally different

DeepDrawing – Dataset Generation

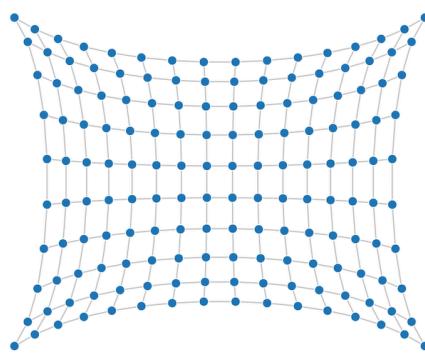
- We generate:
 - Graph data: grid graphs, star graphs, clustered general graphs
 - Graph drawing data: grid layout, star layout, ForceAtlas2, PivotMDS
 - We manually tune the parameters of the drawing algorithms

Evaluations

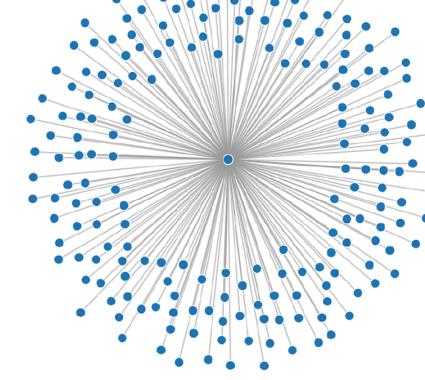
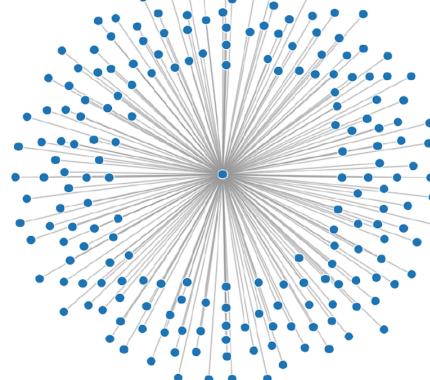
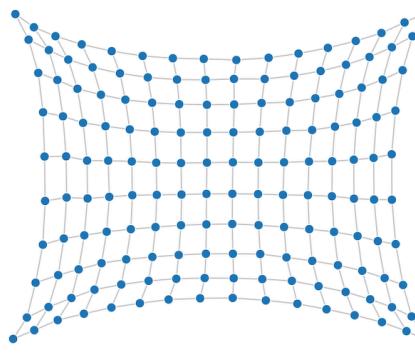
- We extensively evaluated the proposed approach:
 - Qualitative and quantitative evaluations
 - Comparison with the graph truth drawings and those by the baseline model (a 4-layer Bi-LSTM model)

Evaluations – Qualitative Evaluation

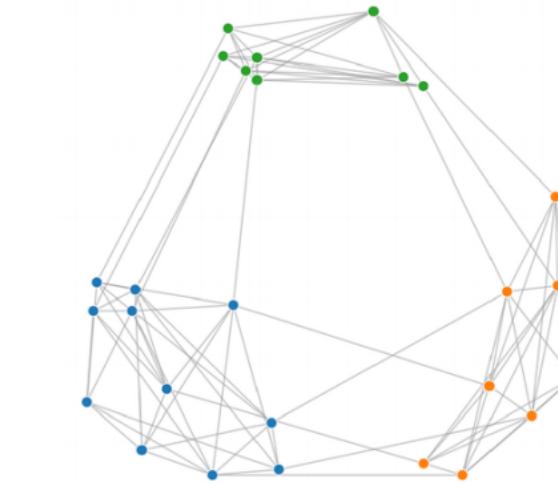
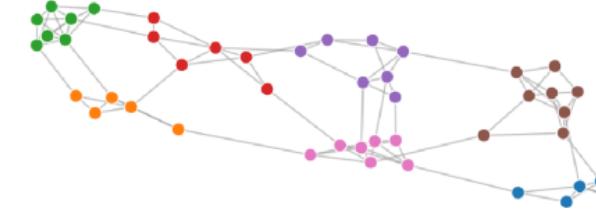
Ground-Truth



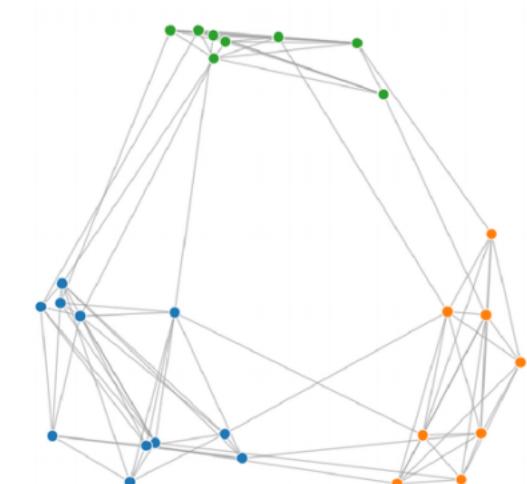
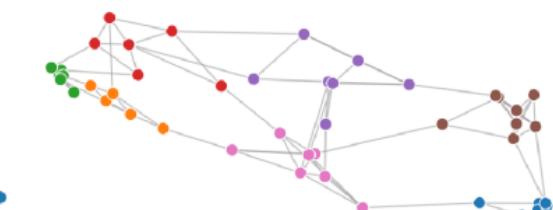
Our Approach



Ground-Truth

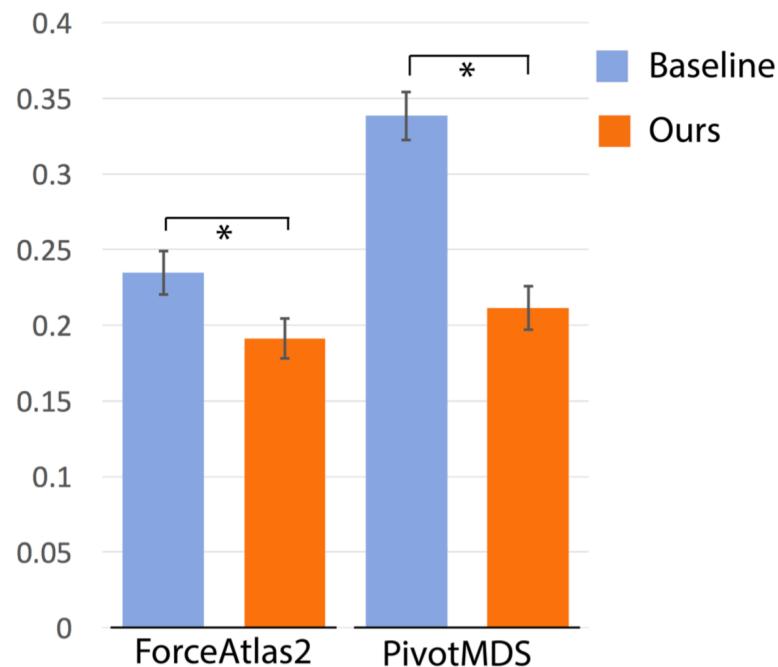


Our Approach



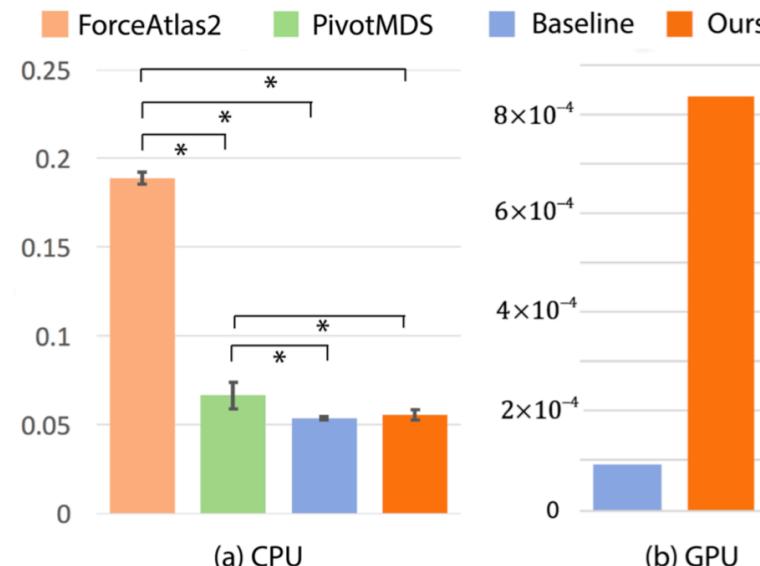
Evaluations – Quantitative Evaluation

- Procrustes Statistic-based similarity:
Our approach is **significantly better** than the baseline model



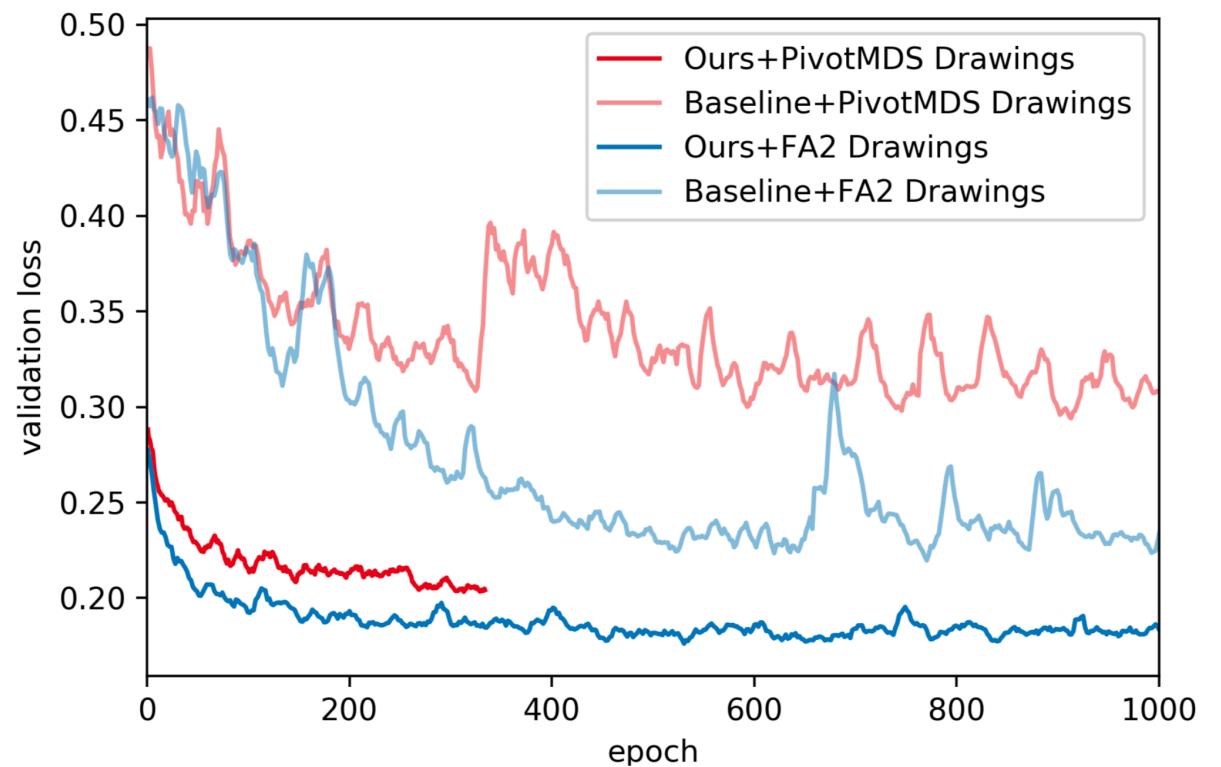
Evaluations – Quantitative Evaluation

- Running Speed
 - CPU: Both our approach and the baseline model is **faster** than the traditional graph drawing methods
 - GPU: Our approach is **slower** than the baseline model on GPU, though **it has 80% less parameters**



Evaluations – Quantitative Evaluation

- Training Convergence Comparison
Our approach can **converge faster** than the 4 layer Bi-LSTM in terms of #Epochs.



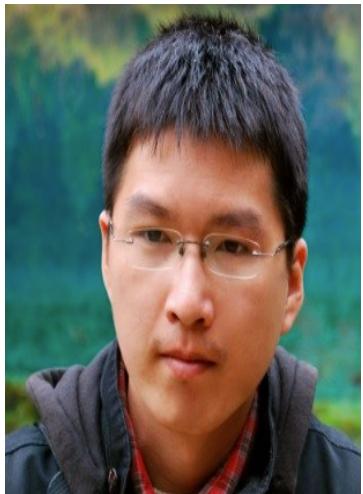
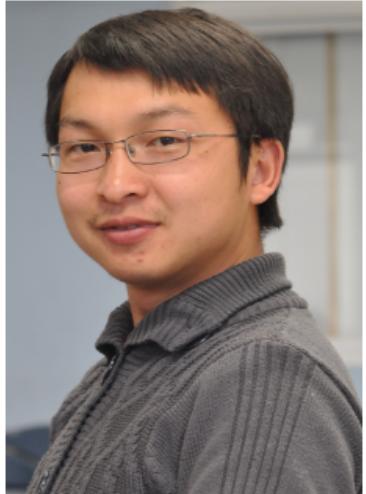
Limitations

- Lack Interpretability
- Our current evaluations mainly focus on small graphs with 20 to 50 nodes
- The performance of DeepDrawing has a dependence on the input node ordering and the structure similarity with the training graphs

Take Home Message

- We propose a graph-LSTM based approach to graph drawing and investigate its effectiveness on small graphs
- It is worth further exploration in terms of good interpretability and better prediction performance on large graphs
- More details: code, video and slides are(or will be) accessible at:
<http://yong-wang.org/proj/deepDrawing.html>

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