

# **Lecture 14**

## **TRANSFORMER TESTS AND THREE PHASE TRANSFORMER BASICS**

### **Agenda**

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How to get the parameters for the transformer model?



# Lecture Outcomes

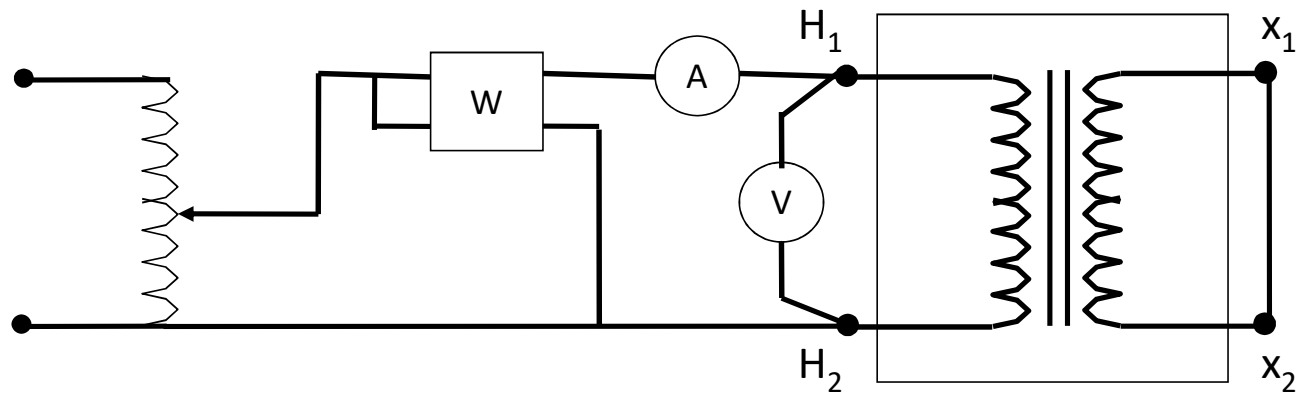
at the end of the lecture, the student must be able to ...

- Apply the open and short circuit tests to derive transformer parameters
- Explain how a three-phase Transformer works.

# Transformer Tests: Short-Circuit Test

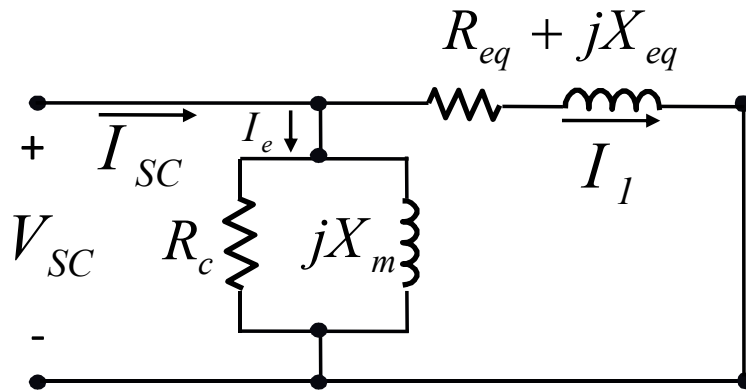
Conducted to determine series impedance

With the secondary (Low-voltage side) short-circuited, apply a primary voltage (usually 2 to 12% of rated value) so that full load current flows.



# Short-Circuit Test

## Short-Circuit Test



$$I_e \approx 0$$

$$I_{sc} = I_l$$

$$R_{eq} = \frac{P_{SC}}{I_{SC}^2}$$

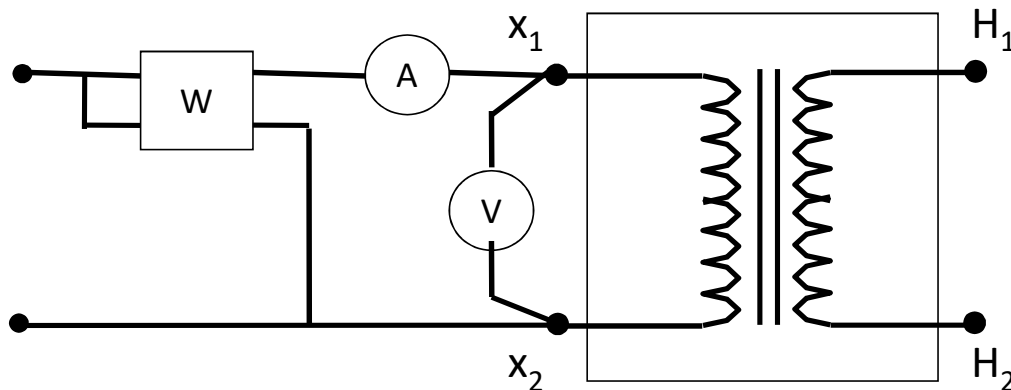
$$Z_{eq} = \frac{V_{SC}}{I_{SC}}$$

$$X_{eq} = \sqrt{Z_{eq}^2 - R_{eq}^2}$$

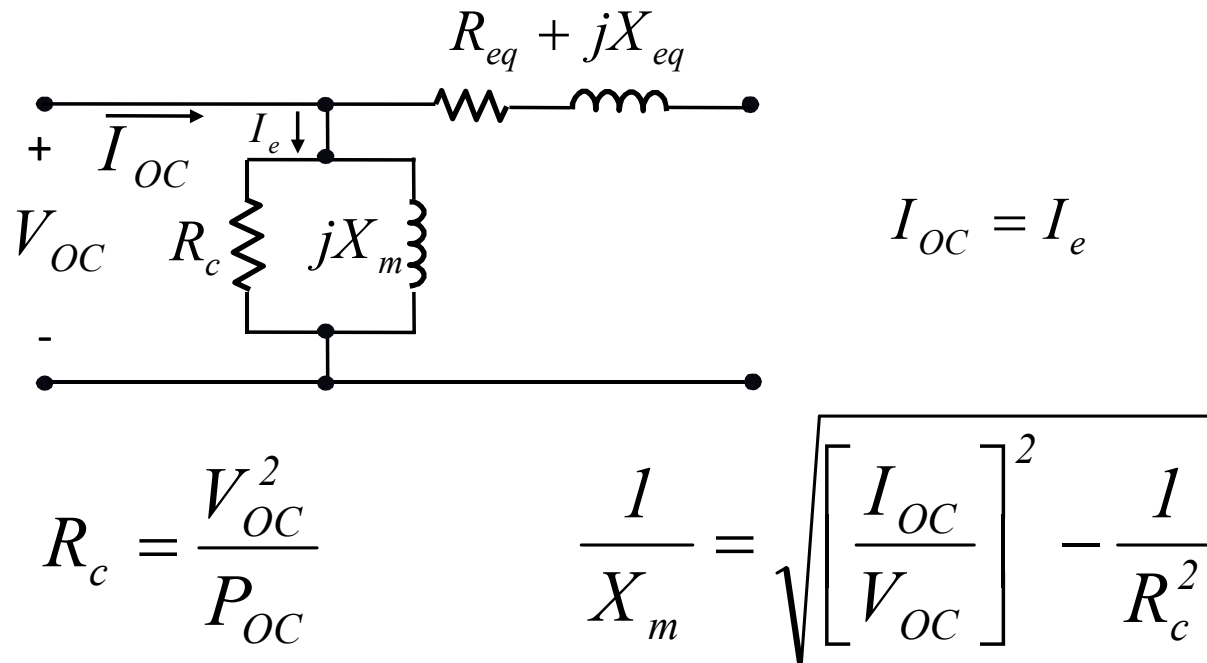
# Transformer Tests: Open-Circuit Test

Conducted to determine shunt impedance

With the secondary (High-voltage side) open-circuited, apply rated voltage to the primary.



# Open-Circuit Test



# Short-Circuit and Open-Circuit Tests

Example:

50 kVA, 2400/240V, single-phase transformer

Short-Circuit Test: HV side energized

$$V_{SC} = 48 \text{ volts} \quad I_{SC} = 20.8 \text{ amps} \quad P_{SC} = 617 \text{ watts}$$

Open-Circuit Test: LV side energized

$$V_{OC} = 240 \text{ volts} \quad I_{OC} = 5.41 \text{ amps} \quad P_{OC} = 186 \text{ watts}$$

Determine the Series and Shunt Impedance of the transformer.  
What is %Z and X/R of the transformer?



# Short-Circuit and Open-Circuit Tests

Solution:

From the short-circuit test

$$Z_{eq,H} = \frac{48}{20.8} = 2.31 \text{ ohm}$$

$$R_{eq,H} = \frac{617}{(20.8)^2} = 1.42 \text{ ohm}$$

$$X_{eq,H} = \sqrt{2.31^2 - 1.42^2} = 1.82 \text{ ohm}$$

From the open-circuit test

$$R_{cq,L} = \frac{(240)^2}{186} = 310 \text{ ohm}$$

$$\frac{1}{X_m} = \sqrt{\left[\frac{5.41}{240}\right]^2 - \left[\frac{1}{310}\right]^2}$$

$$X_{m,L} = 45 \text{ ohm}$$

# Short-Circuit and Open-Circuit Tests

Referred to the HV side

$$R_{c,H} = a^2 R_{c,L} = 30,968 \text{ ohm}$$

$$X_{m,H} = a^2 X_{m,L} = 4,482 \text{ ohm}$$

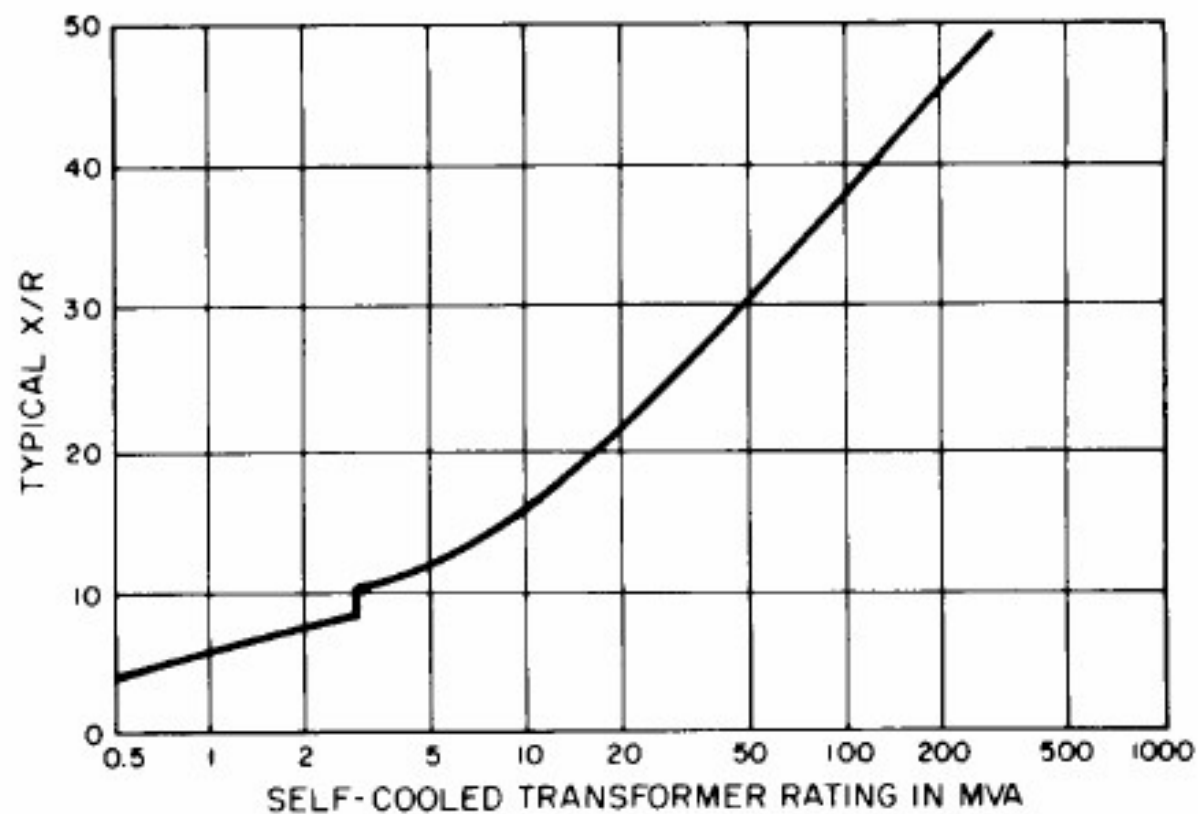
%Z and X/R

$$Z_{BASE} = \frac{[2.4]^2}{50 / 1000} = 115.2 \text{ ohm}$$

$$\%Z = \left( \frac{2.31}{115.2} \right) \times 100 = 2\%$$

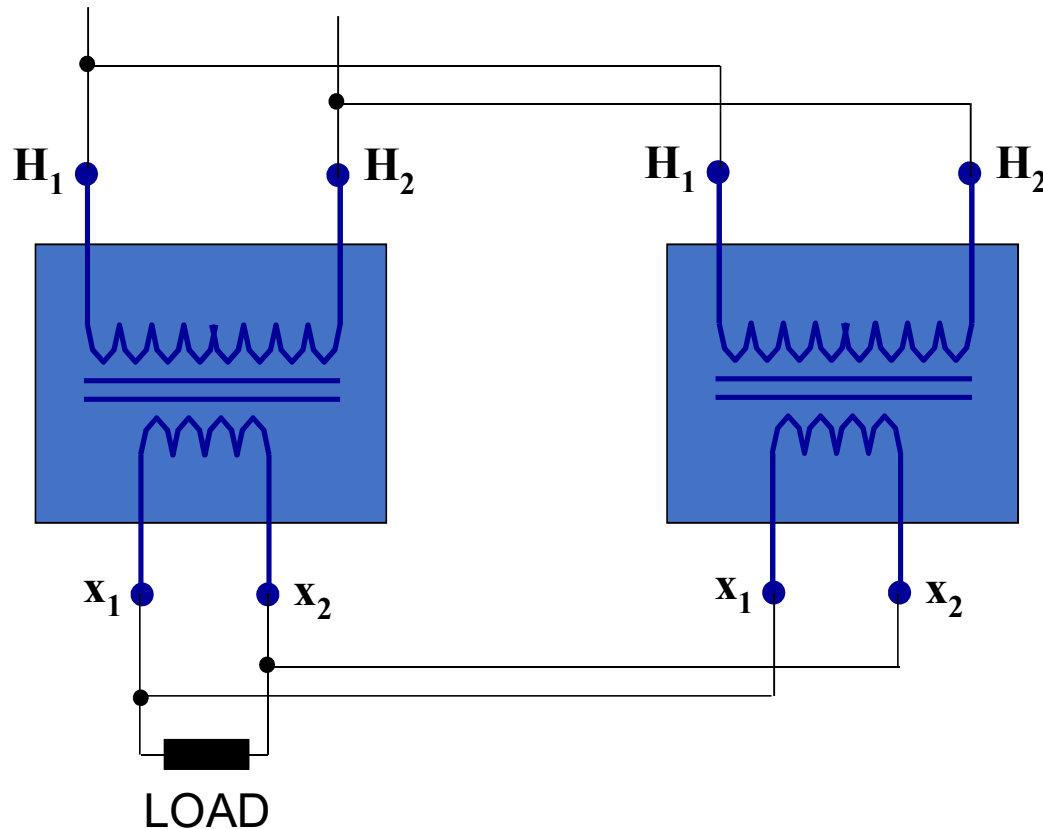
$$X / R = \frac{1.82}{1.42} = 1.28$$

# X/R Ratios of Transformers



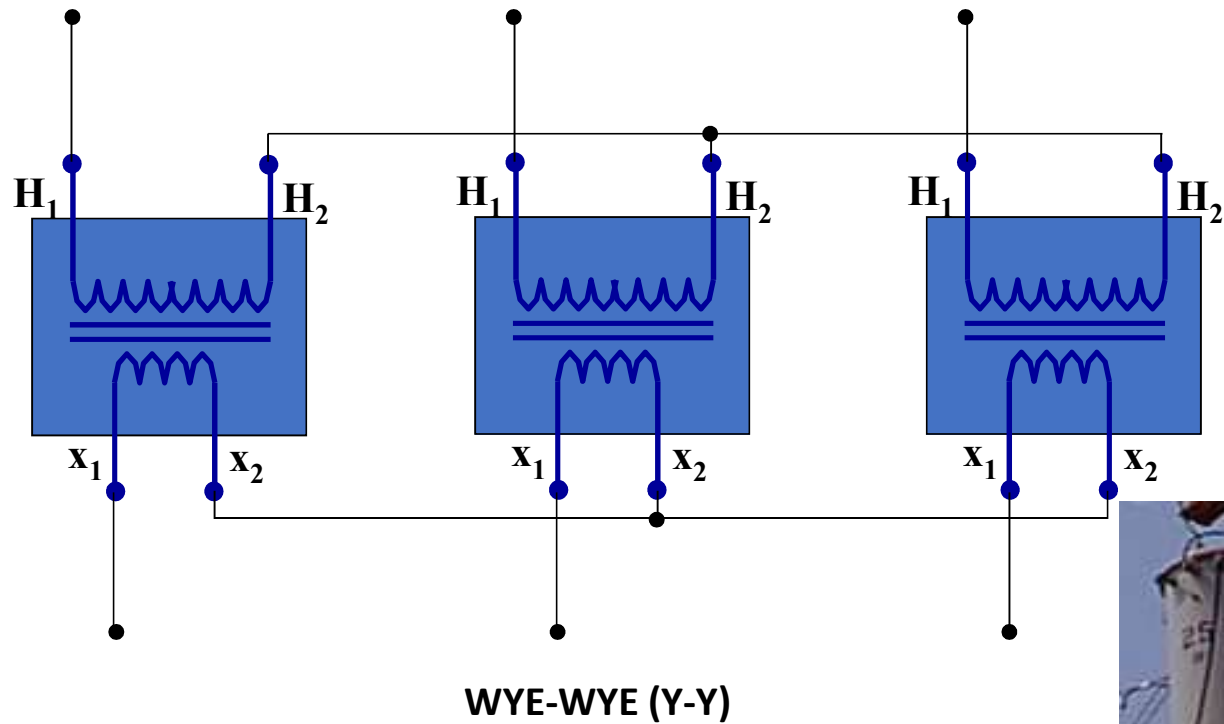
Source: Based on IEEE Std C37.010-1979.

# Transformers in Parallel



- Same turns ratio
- Connected to the same primary phase
- Identical frequency ratings
- Identical voltage ratings
- Identical tap settings
- Per unit impedances within 0.925 to 1.075 of each other

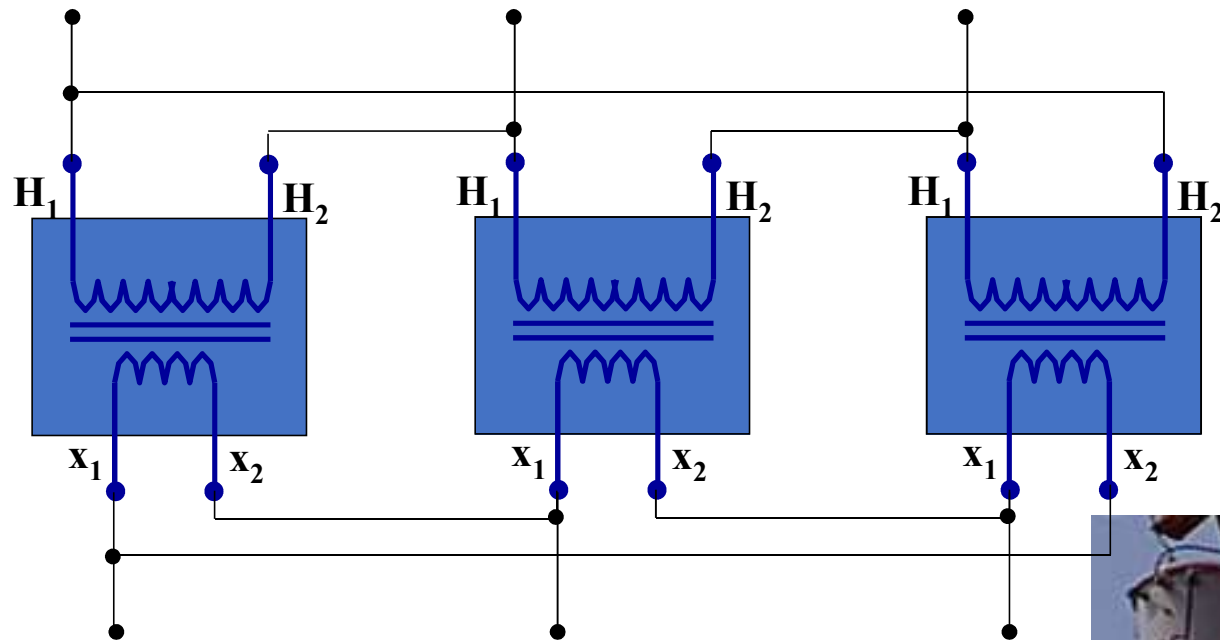
# Three-Phase Transformers



Three Phase Transformer Bank



# Three-Phase Transformers

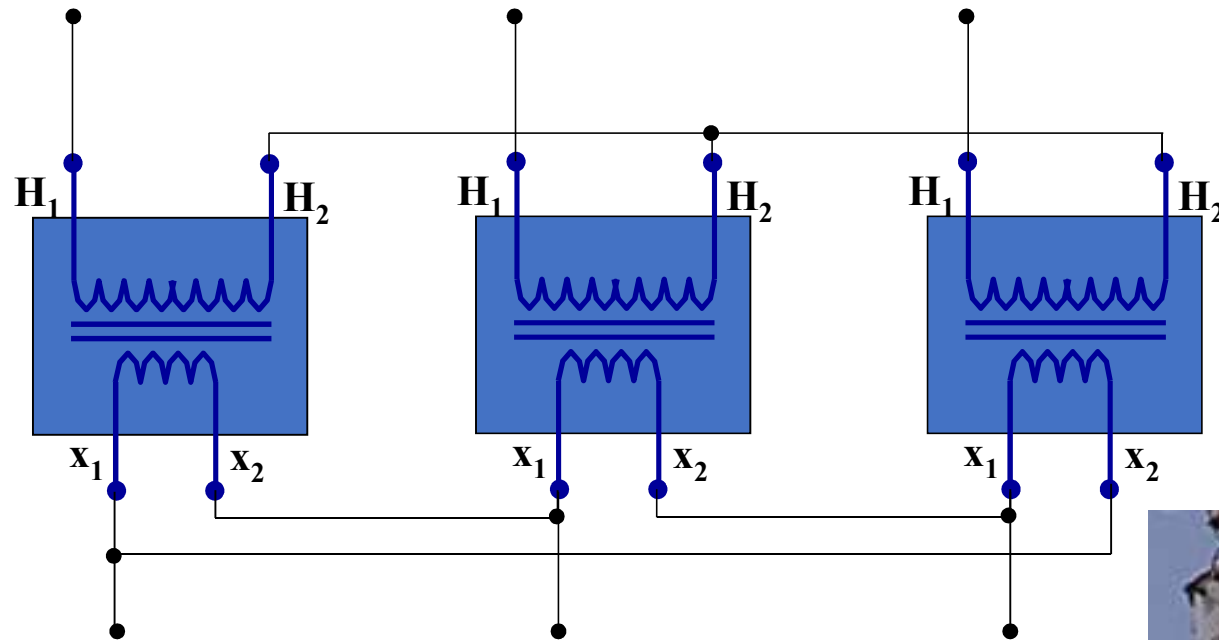


DELTA-DELTA ( $\Delta$ - $\Delta$ )

Three Phase Transformer Bank



# Three-Phase Transformers

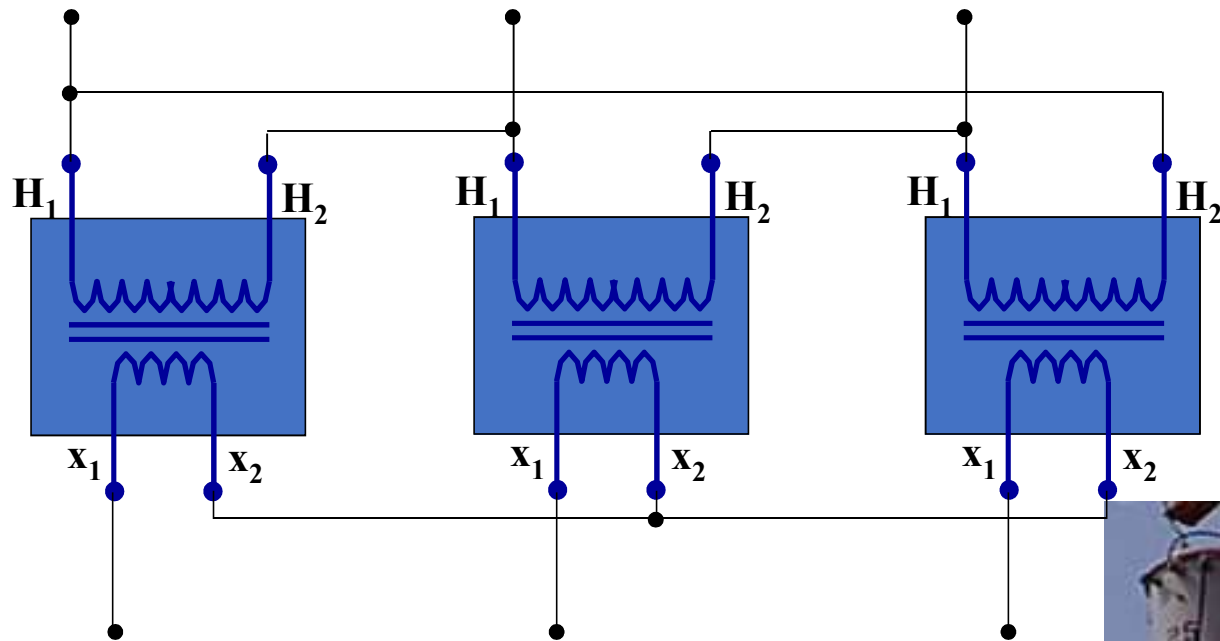


WYE-DELTA (Y- $\Delta$ )

Three Phase Transformer Bank



# Three-Phase Transformers



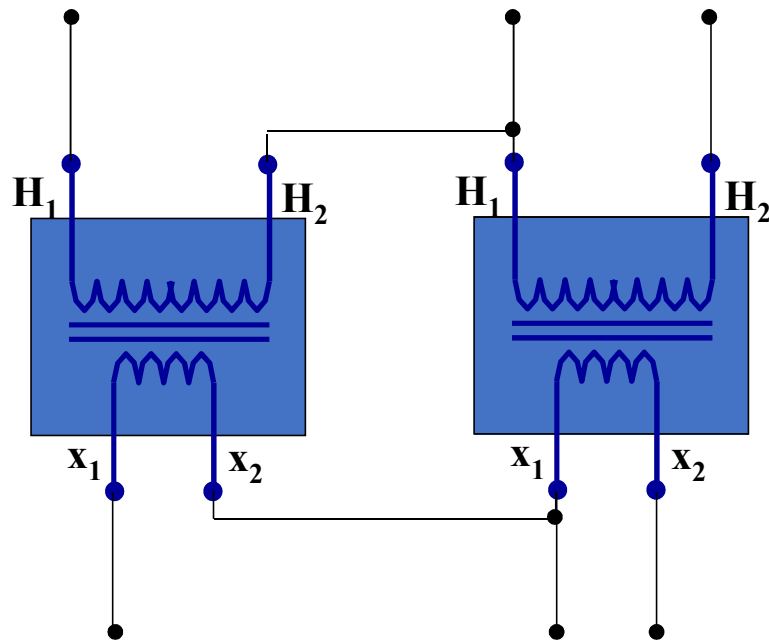
DELTA-WYE ( $\Delta$ -Y)

Three Phase Transformer Bank





# Three-Phase Transformers

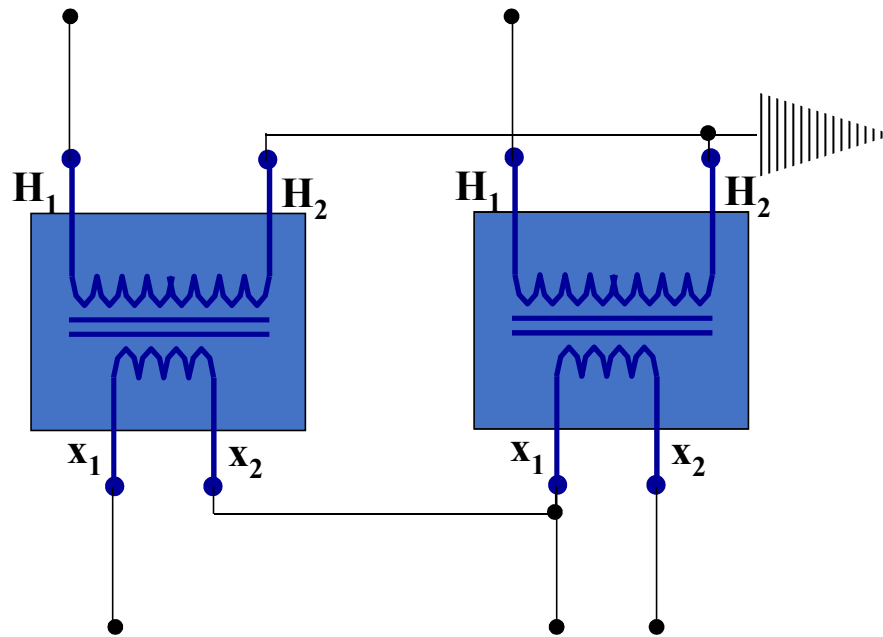


OPEN DELTA – OPEN DELTA

Three Phase Transformer Bank



# Transformer Connection

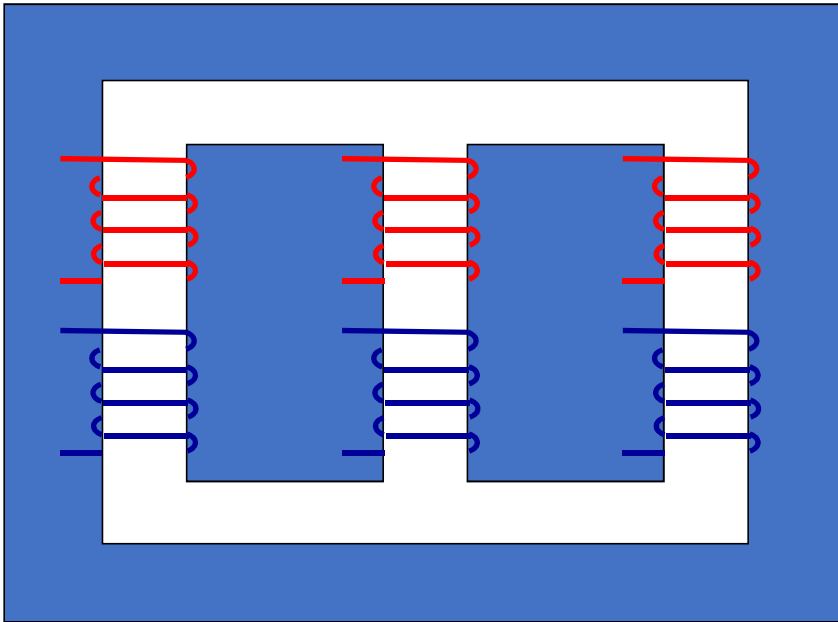


OPEN WYE - OPEN DELTA

Three Phase Transformer Bank



# Three-Phase Transformer



Windings are connected Wye or Delta internally

# HOMEWORK

**Example 2–2.** The equivalent circuit impedances of a 20-kVA, 8000/240-V, 60-Hz transformer are to be determined. The open-circuit test and the short-circuit test were performed on the primary side of the transformer, and the following data were taken:

Open-circuit test (on primary)	Short-circuit test (on primary)
$V_{OC} = 8000 \text{ V}$	$V_{SC} = 489 \text{ V}$
$I_{OC} = 0.214 \text{ A}$	$I_{SC} = 2.5 \text{ A}$
$P_{OC} = 400 \text{ W}$	$P_{SC} = 240 \text{ W}$

Find the impedances of the approximate equivalent circuit referred to the primary side, and sketch that circuit.