

# Assignment 1: Solutions

## IS711: Learning and Planning in Intelligent Systems

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### 1 Question #1

#### 1.1 Answer to Question #1.1

We can formulate the problem with the following definitions:

- **State space:**
  - the top block on the table
- **Initial state:**
  - the top block on the table is the block A
- **Goal state:**
  - the top block on the table is the block C
- **Possible Operators:**
- **Path cost:**

#### 1.2 Answer to Question #1.2

In the initial state con0, we can do the operation moveTo(2,1), moveToTable(2), moveTo(1,2), moveToTable(1), and get different configurations respectively, con1, con2, con3, con4, based on the formula  $f(n) = g(n) + h(n)$ , we can get the estimated the cost of each configuration and

the first four nodes with the search tree are shown below, clearly indicate: the order of expansion of each node; the action corresponding to each edge of the tree; the state,  $f(n)$  value that sum of heuristic value with real cost.

### 2 Question #2

Cutting:40hrs, Assembly:42hrs, Finishing: 25hrs Sofa: 201hrs of cutting, 2hrs of assembly, 1hr of finishing Chair : 30 2 hrs of cutting, 1 hr of assembly, 1 hr of finishing

The calculation is as follows:

- **Variables:** X1 : manufacture one unit of sofa X2: manufacture one unit of chair
- **Constraints:**
- **Objective:**
- **Solution:**

### 3 Question #3

Let's use  $(X,Y)$  represent the value that the first dice is  $X$ , and the second is  $Y$ , total 36 possibilities of the results for  $(X,Y)$  of rolling two fair six-sided dice at one time.

$$P(\text{win \$1 in first round}) = P(1,1) + P(2,3) + P(3,2) + P(1,4) + P(4,1) + P(1,6) + P(6,1) + P(3,4) + P(4,3) + P(2,5) + P(5,2) + P(4,6) + P(6,4) + P(5,5) = 7/18$$

$$P(\text{lose \$1 in first round}) = P(1,5) + P(5,1) + P(3,3) + P(2,4) + P(4,2) + P(6,6) = 1/6$$

$$P(\text{play one more round}) = 1 - 7/18 - 1/6 = 4/9$$

$$P(\text{win \$2 in second round} \mid \text{play one more round}) = P(2,2) + P(1,3) + P(3,1) + P(1,5) + P(5,1) + P(3,3) + P(4,2) + P(2,4) + P(6,1) + P(6,1) + P(3,4) + P(4,3) + P(2,5) + P(5,2) + P(2,6) + P(6,2) + P(3,5) + P(5,3) + P(4,4) = 19/36$$

$P(\text{lose \$1 in second round} \mid \text{play one more round}) = 1 - 17/36 = 5/9$  Expected value of game:  $(7/18)*1 + (1/6)*(-1) + (4/9)*(19/36)*2 + (4/9)*(17/36)*(-1) = 13/27 > 0$   $P(\text{winning}) = P(\text{win \$1 in first round}) + P(\text{play one more round}) * P(\text{win \$2 in second round} \mid \text{play one more round}) = 101/162$  The probability of winning is 101/162 As expected value is much bigger than 0, and win probability is bigger than 0.5, I will play this game.

### 4 Question #4

#### 4.1 Answer to Question #4.1

#### 4.2 Answer to Question #4.2

#### 4.3 Answer to Question #4.3

### 5 Question #5

### 6 Question #6

#### 6.1 Answer to Question #6.a

#### 6.2 Answer to Question #6.b