User program

CPU 2

CPU 1

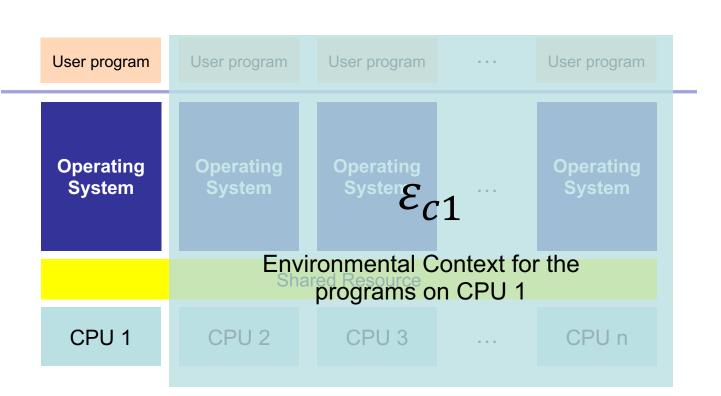


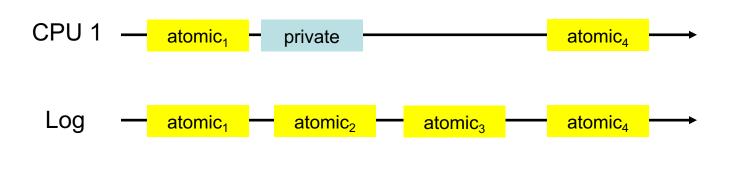
CPU 3

CPU n

User program	User program	User program	 User program	
Operating System	Operating System	Operating System	 Operating System	
CPU 1	CPU 2	CPU 3	 CPU n	

User program	User program	User program		User program		
Operating System	Operating System	Operating System		Operating System		
Shared Resource						
CPU 1	CPU 2	CPU 3		CPU n		



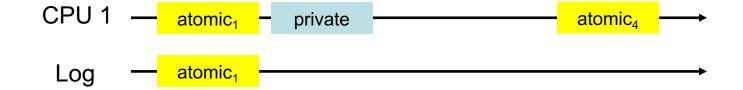


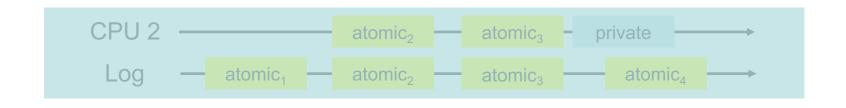
atomic₂

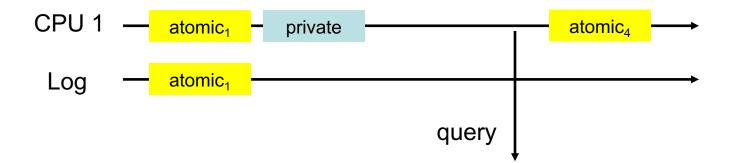
atomic₃

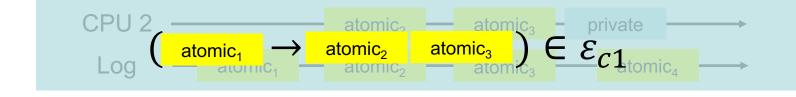
private

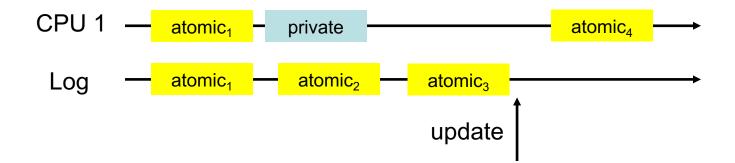
CPU 2

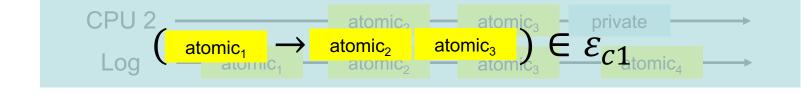




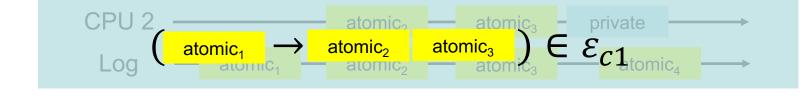


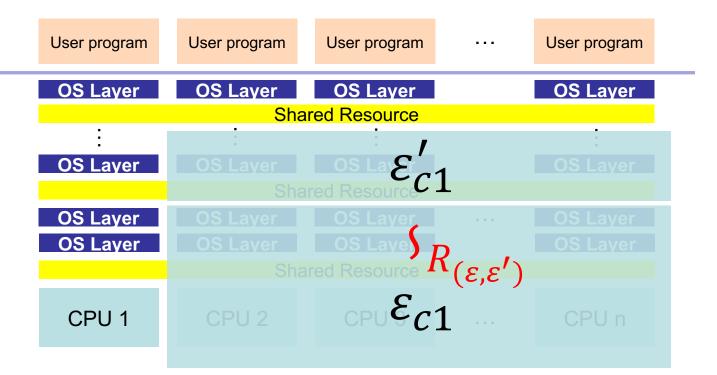






CPU 1 —
$$\frac{1}{\text{atomic}_1}$$
 — $\frac{1}{\text{private}}$ — $\frac{1}{\text{atomic}_2}$ — $\frac{1}{\text{atomic}_3}$ — $\frac{1}{\text{atomic}_4}$ — $\frac{1}{\text{atomic$

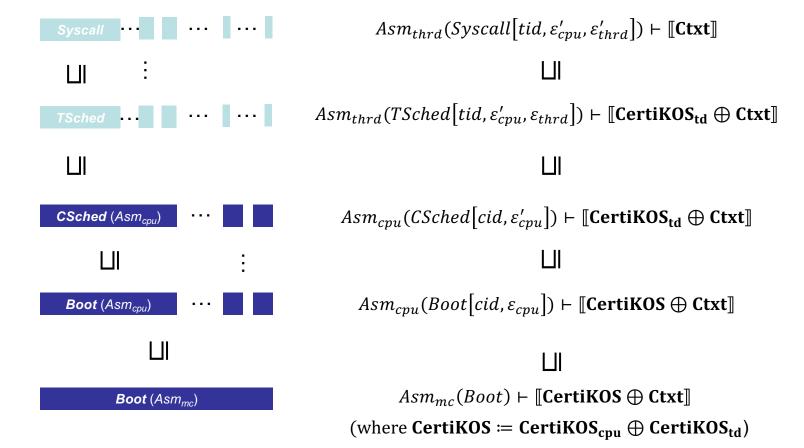




User program	User program	User program		User program				
OS Layer	OS Layer	OS Layer red Resource		OS Layer				
:	• Shared Resource							
:								
OS Layer		OS La Er						
	OS Layer OS Layer OS Layer OS Layer Shared Resource C1							
OS Layer								
OS Layer								
	Shared Resource							
CPU 1		CPU $arepsilon_{c_1}$						

 $Asm_{mc}(Boot) \vdash [[CertiKOS \oplus Ctxt]]$

 $Asm_{thrd}(Syscall[tid,\varepsilon_{cpu}',\varepsilon_{thrd}']) \vdash \llbracket \mathbf{Ctxt} \rrbracket$



 $Asm_{cpu}(Boot[cid, \varepsilon_{cpu}]) \vdash \llbracket \mathbf{CertiKOS} \oplus \mathbf{Ctxt} \rrbracket$ \square $Boot(Asm_{mc})$ $Asm_{mc}(Boot) \vdash \llbracket \mathbf{CertiKOS} \oplus \mathbf{Ctxt} \rrbracket$

- Environment
 - Fixed number of CPUs
 - Fixed initial state for all CPUs
 - Fairness assumptions
- Things to solve
 - Hide non-determinism 1
 - Build environmental context for each CPU 2
 - Prove compositionality of multiple per-CPU machines
 - Provide simple environmental context for per-CPU machines

 $\operatorname{Mach}_{\operatorname{LAsm}}(C, L[\operatorname{cid}, \varepsilon_{\operatorname{cpu}}]) \vdash \llbracket \operatorname{\mathbf{Prog}} \rrbracket$

Connect Local Layer Interface⁽⁵⁾

Connect Local Layer Interface

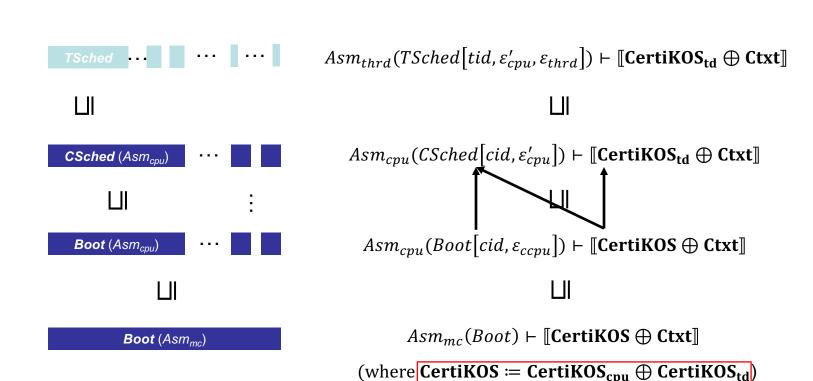
Optimize environmental context

Introduce per-CPU machine

Introduce partial machine and prove linking theorem

Introduce hardware scheduler

```
\operatorname{Mach}_{\operatorname{LAsm}}(\operatorname{MBoot}[\operatorname{cid}, \varepsilon_{\operatorname{cpu}}]) \vdash \llbracket \operatorname{CertiKOS} \oplus \operatorname{Ctxt} \rrbracket
                  \operatorname{Mach}_{\operatorname{sep}}(\operatorname{MBoot}[\operatorname{cid}, \varepsilon_{\operatorname{sep}}]) \vdash [\operatorname{CertiKOS} \oplus \operatorname{Ctxt}]
           \mathsf{Mach}_{\mathsf{reorder}}(\mathsf{MBoot}[\mathit{cid}, \varepsilon'_{\mathit{reorder}}]) \vdash \llbracket \mathbf{CertiKOS} \oplus \mathbf{Ctxt} \rrbracket
           Mach_{reorder}(MBoot[cid, \varepsilon_{reorder}]) \vdash [CertiKOS \oplus Ctxt]]
                    Mach_{split}(MBoot[cid, \varepsilon]) \vdash [CertiKOS \oplus Ctxt]
                   Mach_{si\_big'}(MBoot[cid, \varepsilon]) \vdash [CertiKOS \oplus Ctxt]
                    Mach_{si\_big}(MBoot[cid, \varepsilon]) \vdash [CertiKOS \oplus Ctxt]
                       Mach_{si}(MBoot[cid, \varepsilon]) \vdash [CertiKOS \oplus Ctxt]
                     Mach_{env}(MBoot[\mathit{cid}, \varepsilon]) \vdash [CertiKOS \oplus Ctxt]
Mach_{env}(\|_{i \in CoreSet} \ MBoot[CoreSet, \varepsilon_{CoreSet}]) \vdash [CertiKOS \oplus Ctxt]]
                 Mach_{oracle}(MBoot[\varepsilon_{CoreSet}]) \vdash [CertiKOS \oplus Ctxt]]
                             Mach_{mc}(MBoot) \vdash [CertiKOS \oplus Ctxt]
```



$$TSched \big[tid, \varepsilon'_{cpu}, \varepsilon_{thrd} \big] (yield) - (lst, log) \rightarrow (lst, log')$$

$$TSched \cdots \cdots \cdots Asm_{thrd} (TSched \big[tid, \varepsilon'_{cpu}, \varepsilon_{thrd} \big]) \vdash [\![CertiKOS_{td} \oplus Ctxt]\!]$$

 $Asm_{cnu}(CSched[cid, \varepsilon'_{cnu}]) \vdash [[CertiKOS_{td} \oplus Ctxt]]$

 $CSched[cid, \varepsilon'_{ci}]$ contains software scheduler primitives

- spawn / yield / sleep / wakeup

CSched (Asm_{cpu})

 $CSched[cid, \varepsilon'_{ci}](yield) - (lst, log) \rightarrow (lst/[tid = \cdots, \rho = \cdots, \cdots], log')$

- Environment
 - Arbitrary active or available thread set on the CPU
 - Dynamic initial states
- Things to solve
 - Hide context switching between threads 1
 - Build environmental context for each thread
 - Assign proper initial states for each thread
 - Prove compositionality of multiple per-thread machines
 - Use the same compiler for per-CPU/thread machines

(5) Link per-CPU machine compiler with per-thread machine (1, 2, 3)Introduce per-thread machine (1, 2, 3, 4)Introduce multithreaded machine and prove linking theorem

between two layers

 $Mach_{HAsm}(C, TSched[tid, \varepsilon_{thrd}]) \vdash [Prog]$

multithreaded machine and prove linking theorem

Mach_{EAsm}(C, $\parallel_{ti \in TSet}$ TLink $[cid, \varepsilon'_{cpu}]$) \vdash $\llbracket Prog \rrbracket$ Mach_{EAsm}(C, CSched $[cid, \varepsilon'_{cpu}]$) \vdash $\llbracket Prog \rrbracket$ C: thread configuration

AbsRelC

abstract relations

Mach_{EAsm}(C, $\parallel_{ti \in TSet}$ TLink $[cid, \varepsilon'_{cpu}]$) \vdash $\llbracket Prog \rrbracket$ (Context switching incl.)

AbsRelT -

CSched: arbitrary layer with scheduling primitives (context switching incl.)

TLink: arbitrary layer for intermediate machines (scheduling primitives are defined in the machine itself)

TSched: arbitrary layer with scheduling primitives (Scheduling has a identity behavior)

Link per-CPU machine compiler with per-thread machine

- Introduce
- per-thread machine
- Introduce multithreaded machine and prove linking theorem

$$\begin{split} \operatorname{Mach_{HAsm}}(\operatorname{PHThrd}[tid,\varepsilon_{thrd}]) &\vdash \llbracket \operatorname{CertiKOS_{thrd}} \oplus \operatorname{Ctxt} \rrbracket \\ & \qquad \qquad \bigsqcup \rrbracket \\ \operatorname{Mach_{TAsm}}(\operatorname{PHBThrd}\left[tid,\varepsilon_{T_{[cid]}}^{zip}\right]) &\vdash \llbracket \operatorname{CertiKOS_{thrd}} \oplus \operatorname{Ctxt} \rrbracket \end{split}$$

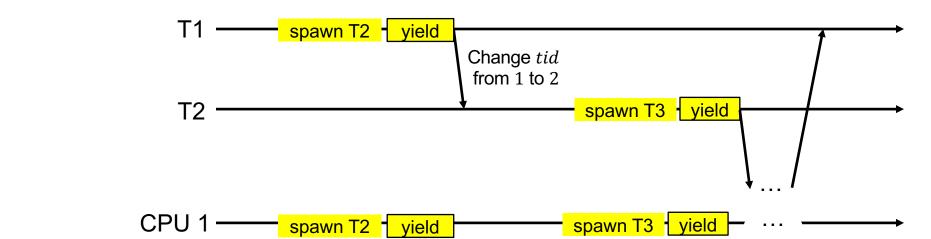
 $\bigsqcup | \\ \mathsf{Mach}_{\mathsf{IEAsm}}(\mathsf{PHBThrd}\left[\mathit{tid}, \varepsilon'_{\mathit{cpu}}, \varepsilon_{T_{[\mathit{cid}]}}\right]) \vdash \llbracket \mathsf{CertiKOS}_{\mathsf{thrd}} \oplus \mathsf{Ctxt} \rrbracket$

 $\begin{aligned} \operatorname{Mach}_{\operatorname{IEAsm}}(\|_{ti \in TSet} \ \operatorname{PHBThrd}[\operatorname{cid}, \varepsilon'_{cpu}]) &\vdash \llbracket \operatorname{CertiKOS_{thrd}} \oplus \operatorname{Ctxt} \rrbracket \\ & \qquad \qquad \bigsqcup \rrbracket \\ \operatorname{Mach}_{\operatorname{EAsm}}(\|_{ti \in TSet} \ \operatorname{PHBThrd}[\operatorname{cid}, \varepsilon'_{cpu}]) &\vdash \llbracket \operatorname{CertiKOS_{thrd}} \oplus \operatorname{Ctxt} \rrbracket \end{aligned}$

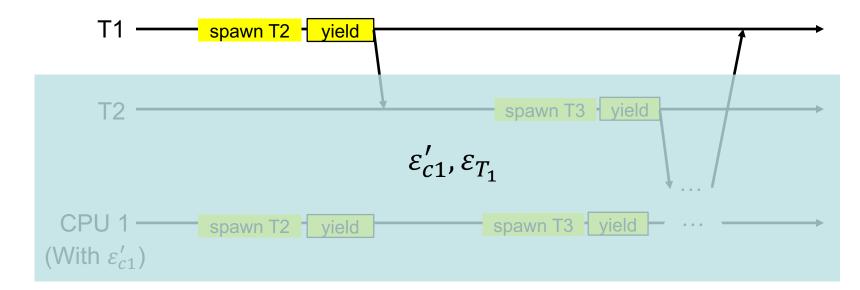
 $\mathsf{Mach}_{\mathsf{LAsm}}(\mathsf{PBThrd}[\mathit{cid}, \varepsilon'_{cpu}]) \vdash \llbracket \mathsf{CertiKOS}_{\mathsf{thrd}} \oplus \mathsf{Ctxt} \rrbracket$

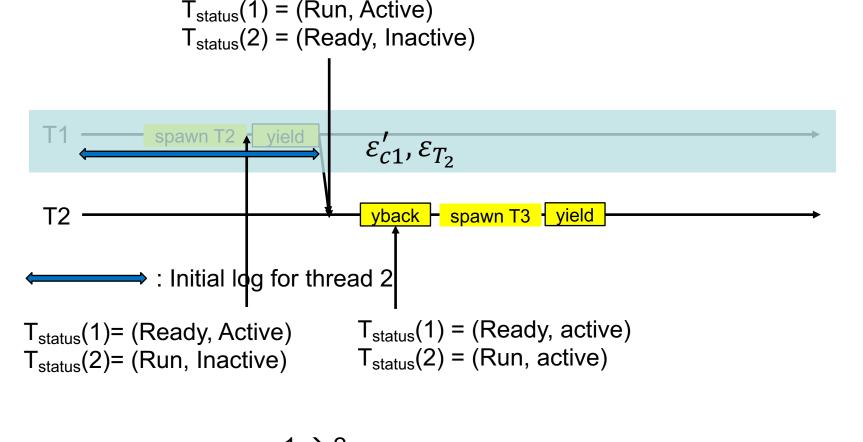
$$st_{TSet} := (tid, \{ti \mapsto lst_{ti}\}, log) \ (\forall ti, ti \in TSet)$$

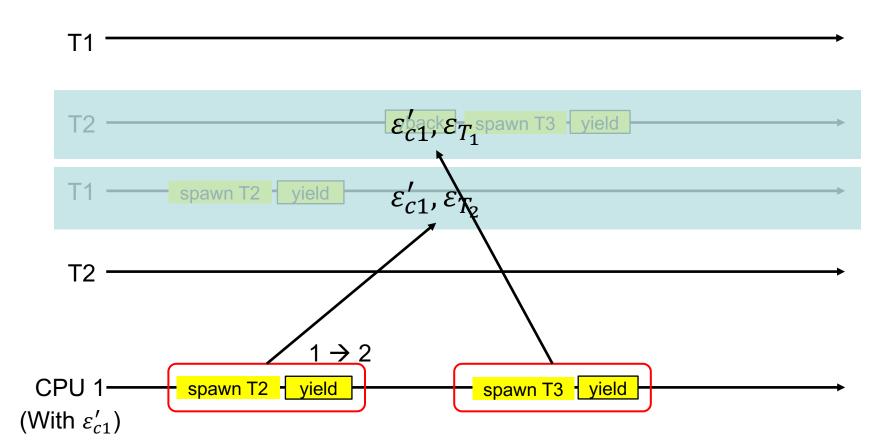
(With ε'_{c1})

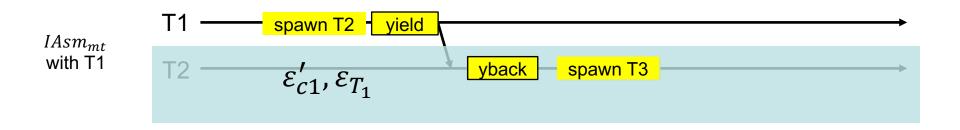


$$st_{TSet} := (tid, \{ti \mapsto lst_{ti}\}, log) \ (\forall ti, ti \in TSet)$$



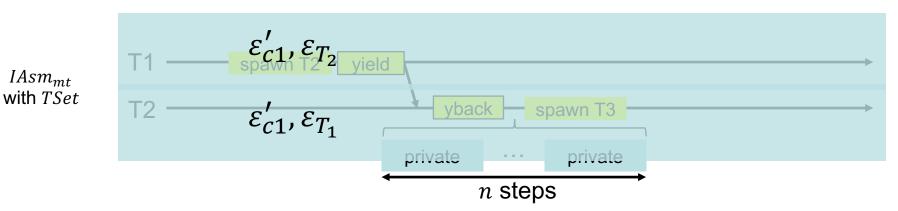


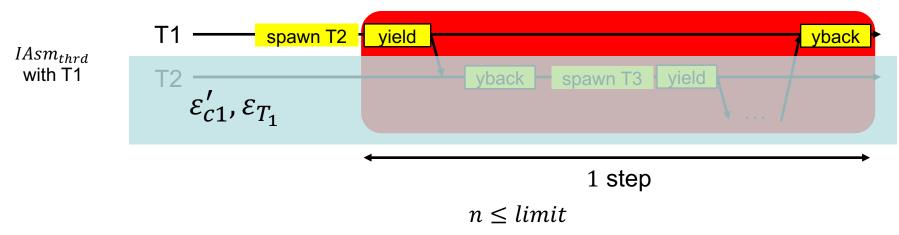




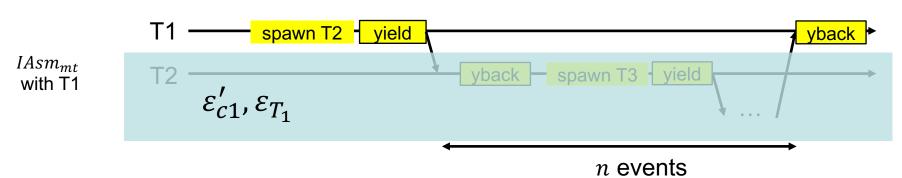
 $IAsm_{mt}$

n < *progress* Every thread will generate at least one event within progress steps





Every thread will be eventually scheduled within $limit \times progress$ steps



Initial state: Calculate initial log to find the proper initial state

Yield rule:
$$TSched[tid, \varepsilon'_{cpu}, \varepsilon_{thrd}](yield) - (lst, log) \rightarrow (lst, log')$$

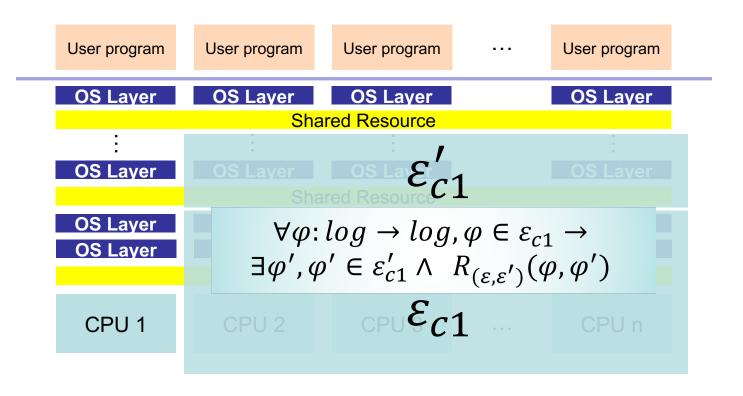
TSched $Asm_{thrd}(TSched[tid, \varepsilon'_{cpu}, \varepsilon_{thrd}]) \vdash [CertiKOS_{td} \oplus Ctxt]$
 \square

CSched (
$$Asm_{cpu}$$
) ... $Asm_{cpu}(CSched[tid, \varepsilon'_{cpu}]) \vdash [CertiKOS_{td} \oplus Ctxt]$

Initial state: Fixed initial state

Yield rule: $\mathit{CSched}\left[\mathit{cid}, \varepsilon'_{cpu}\right](\mathit{yield}) - (\mathit{lst}, \mathit{log}) \rightarrow (\mathit{lst}/[\mathit{tid} = \cdots, \rho = \cdots, \cdots], \mathit{log}')$

Environmental Context Relation



Hide Nondeterminism

 $Asm_{oracle}(Boot[\varepsilon_{CoreSet}]) \vdash [\![CertiKOS \oplus Ctxt]\!]$

Ш

 $Asm_{mc}(Boot) \vdash [[CertiKOS \oplus Ctxt]]$