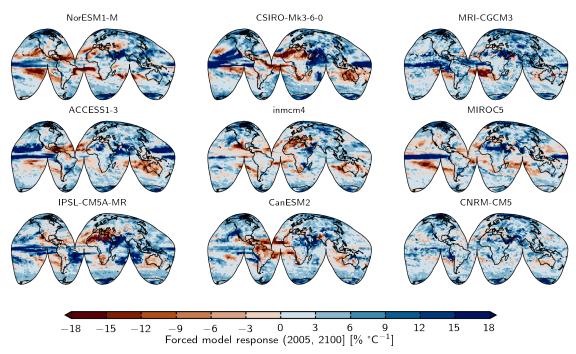
## Contents of this file

Figures S1 to S3 Table S1

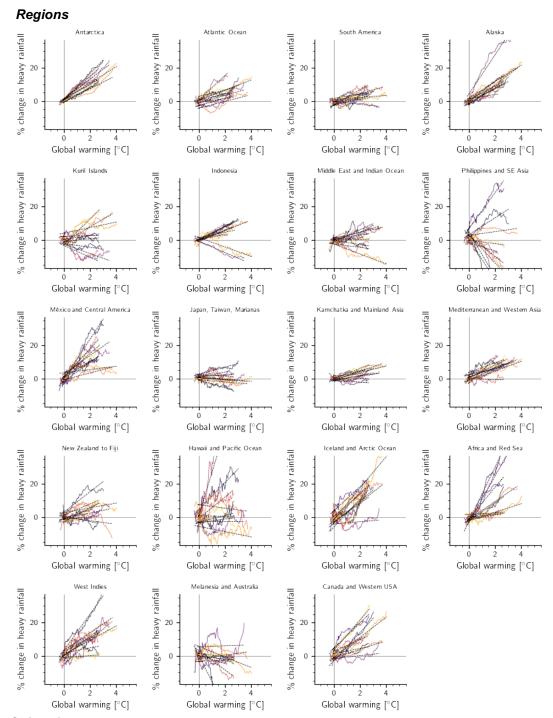
## Introduction

This supplementary material shows forced model response for all models studied (**Fig. S1**); the forced model response for each individual region and subregion for all GCMs (**Fig. S2**); and per-month distribution of large eruptions at two volcanoes (**Fig. S3**). Details of models used are given in **Tab. S1**. Data were processed as described in the main text.

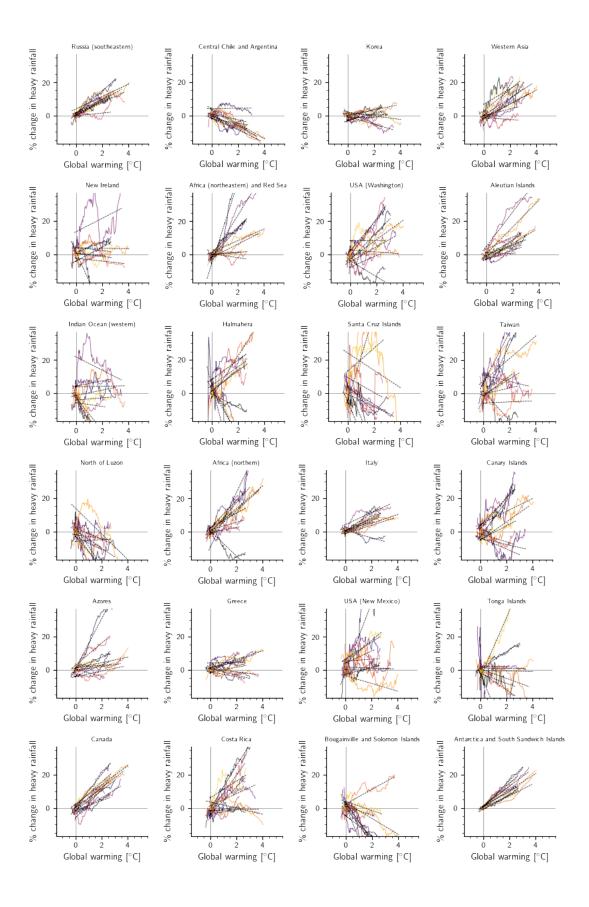
To retrieve the data shown in **Figure S3**, the Global Volcanism Program database (Global Volcanism Program 2013) was filtered to include only "Confirmed" and "Observed" historical eruptions at Reventador and Vesuvius with a Maximum Explosivity Index of 3 or greater. As an additional filter, only eruptions with a "Start Date Day Uncertainty" of  $\leq 5$  were included, resulting in 10 eruptions at Reventador and 26 eruptions at Vesuvius. Full details may be found in the accompanying code.

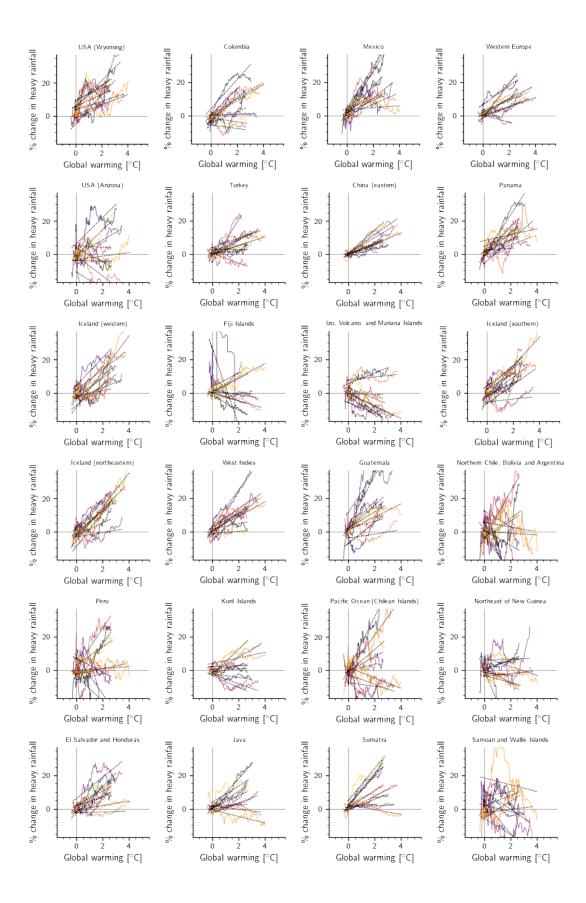


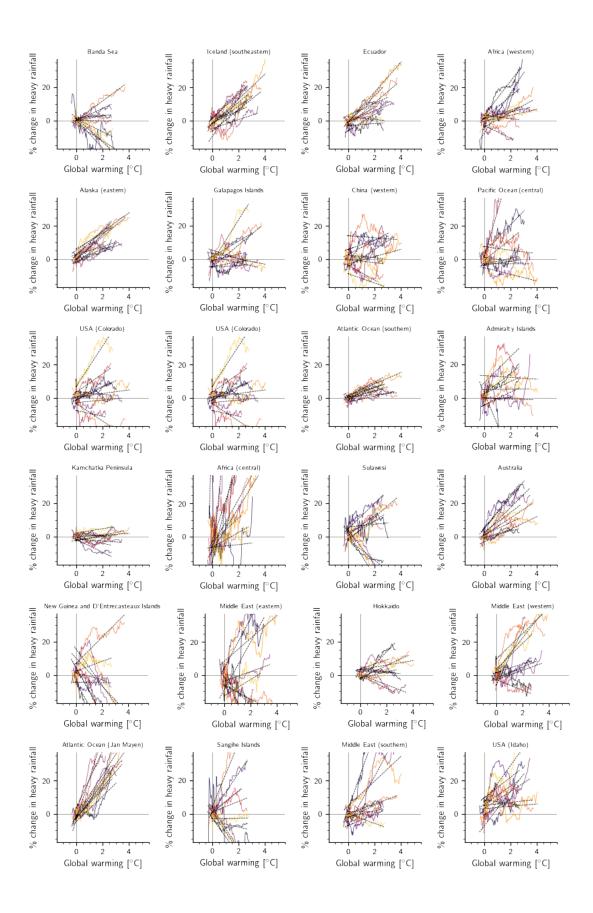
**Figure S1**. Forced model response for all compared models. GCM codes (as listed in Table 1, Methods) are shown above the corresponding map. Forced model response (FMR) as **RX** versus  $\langle T \rangle$  over the timeframe from 2005 or 2006 to 2100, normalized to 2006. Blue tones represent an increase in extreme rainfall with increased global warming, red tones represent a decrease.

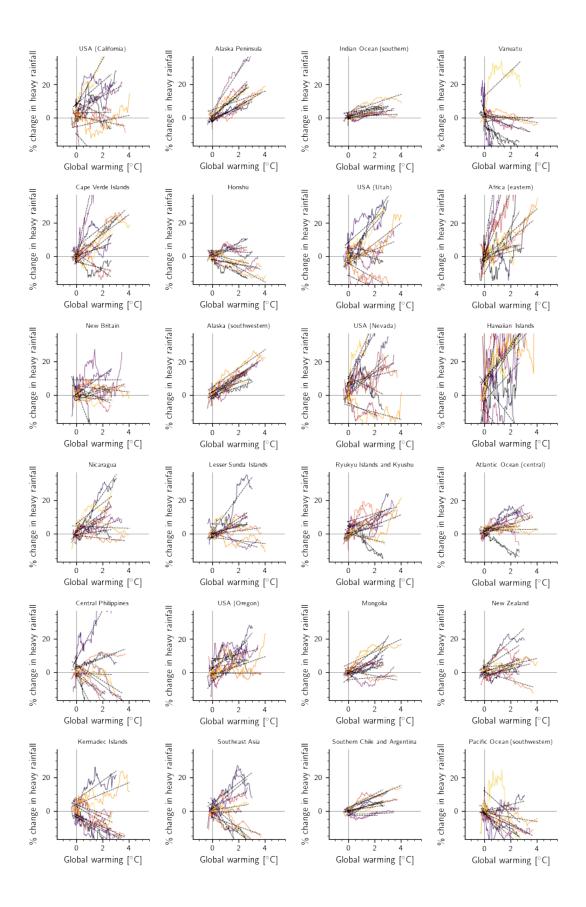


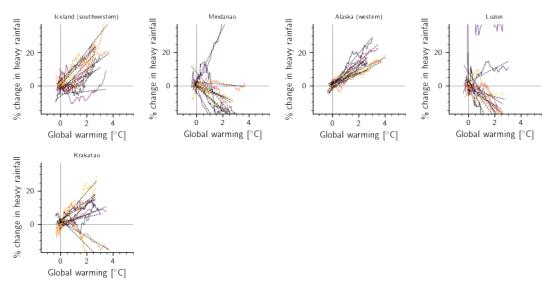
Subregions



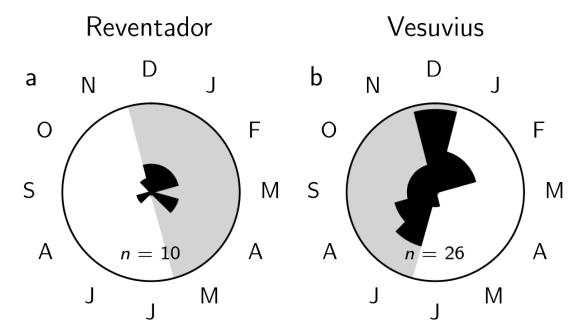








**Figure S2.** Forced model responses at different spatial scales. Percent change in modelled heavy rainfall per degree of global warming, from nine climate models: ACCESS1.3, CNRM-CM5, CSIRO-Mk3.6.0, CanESM2, INM-CM4, IPSL-CM5A-MR, MIROC5, MRI-CGCM3, and NorESM1-M. Data are shown as a 30-yr rolling mean, normalized to January 2021. Dashed black lines are linear regression of response for each model. Data are areal averages, calculated by including model grids that contain a Holocene-active volcano for each of the Global Volcanism Program's defined "Region" and "Subregion" categories (19 and 101 categories, respectively).



**Figure S3.** Distribution of eruptions  $\geq$ VEI 3 for **a** Reventador (Ecuador), and **b** Vesuvius (Italy). In both panels, the labels [J, F, ..., D], correspond to months of the year, and each bar reflects the number of historical eruptions in the GVP database occurring within that month. The total number  $\boldsymbol{n}$  reflects the number of eruptions in the filtered dataset. Grey shaded region indicates the period of the year receiving the most rainfall.

**Table S1.** Nine CMIP5 models used in this study, including their spatial resolutions. Data accessed via Earth System Grid Federation servers, in particular the node hosted by the Lawrence Livermore National Laboratory: https://esgf-node.llnl.gov/search/cmip5/.

Model	Modelling center	Spatial resolution	
		Nodes	Degrees (lat × lon)
ACCESS1.3	CSIRO (Commonwealth Scientific and Industrial Research Organisation, Australia), and BOM (Bureau of Meteorology, Australia)	145 × 192	1.25 × 1.875
CNRM-CM5	Centre National de Recherches Météorologiques/Centre Européen de Recherche et Formation Avancées en Calcul Scientifique	128 × 256	1.4008 × 1.40625
CSIRO-Mk3.6.0	CSIRO (Commonwealth Scientific and Industrial Research Organisation, Australia), and BOM (Bureau of Meteorology, Australia)	96 × 192	1.8653×1.875
CanESM2	Canadian Centre for Climate Modelling and Analysis	64 × 128	2.7906 × 2.8125
INM-CM4	Institute for Numerical Mathematics, Russia	120 × 180	1.5×2
IPSL-CM5A-MR	Institut Pierre-Simon Laplace, France	96×96	1.2676 × 2.5
MIROC5	Atmosphere and Ocean Research Institute (The University of Tokyo), National Institute for Environmental Studies, and Japan Agency for Marine-Earth Science and Technology, Japan	128 × 256	1.4008 × 1.40625
MRI-CGCM3	Meteorological Research Institute, Japan	160 × 320	1.12148×1.125
NorESM1-M	Norwegian Climate Centre, Norway	96 × 144	1.8947 × 2.5