

AA - Experiment 4A - Red Black Tree (Insertion)

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022Experiment 4A: RB InsertionAim: To implement Red black tree (insertion)Theory:

1. RB-tree is a self-balancing BST with each node colored red / Black, satisfying properties:
 - a) Every node is either red / black.
 - b) Root is black.
 - c) Every leaf which is NIL is black.
 - d) If a red node has children, then children are black.
 - e) For each node, all simple paths from node to descendant leaves contains same no. of black nodes.
2. Insertion begins like a standard BST insertion but may violate red black tree properties. It fixes violations through recoloring or rotations, ensuring the tree remains balanced.
3. In RB-tree, after standard BST insertion, the inserted node is colored red. This may violate RB tree properties, especially, the black height properties. To restore the balance, these are the cases:
 - a) If parent of inserted node is black - No Violations.
 - b) If the parent is red, violating the property that a red node cannot have a red parent, there are further cases:

- i) If uncle is red, ~~set~~ recolor node to balance.
- ii) If uncle is black & inserted node is an inside child, perform a rotation & recolor to balance.
- iii) If the uncle is black & inserted node is an outside child, perform double rotation & recolor to balance.

Conclusions: RB Tree insertion maintains balance by recoloring & rotating the nodes, ensuring efficient search & insertion op. Thus we have implemented it.

CODE :

```
class Node:
```

```
    def __init__(self, val, color):
        self.val = val
        self.color = color
        self.left = None
        self.right = None
        self.parent = None
```

```
class RedBlackTree:
```

```
    def __init__(self):
        self.root = None
```

```
    def insert(self, val):
        new_node = Node(val, "RED")
        if not self.root:
            self.root = new_node
            new_node.color = "BLACK"
            return
```

```
        curr = self.root
        parent = None
        while curr:
            parent = curr
            if val < curr.val:
                curr = curr.left
            else:
                curr = curr.right
```

```
        new_node.parent = parent
        if val < parent.val:
            parent.left = new_node
        else:
            parent.right = new_node
```

```
        self._fix_violations(new_node)
```

```
    def _fix_violations(self, node):
        while node.parent and node.parent.color == "RED":
            if node.parent == node.parent.parent.left:
                uncle = node.parent.parent.right
```

```

        if uncle and uncle.color == "RED":
            node.parent.color, uncle.color, node.parent.parent.color = "BLACK", "BLACK",
"RED"
            node = node.parent.parent
        else:
            if node == node.parent.right:
                node = node.parent
                self._left_rotate(node)
                node.parent.color, node.parent.parent.color = "BLACK", "RED"
                self._right_rotate(node.parent.parent)
            else:
                uncle = node.parent.parent.left
                if uncle and uncle.color == "RED":
                    node.parent.color, uncle.color, node.parent.parent.color = "BLACK", "BLACK",
"RED"
                    node = node.parent.parent
                else:
                    if node == node.parent.left:
                        node = node.parent
                        self._right_rotate(node)
                        node.parent.color, node.parent.parent.color = "BLACK", "RED"
                        self._left_rotate(node.parent.parent)

self.root.color = "BLACK"

def _left_rotate(self, node):
    right_child = node.right
    node.right = right_child.left

    if right_child.left:
        right_child.left.parent = node
    right_child.parent = node.parent

    if not node.parent:
        self.root = right_child
    elif node == node.parent.left:
        node.parent.left = right_child
    else:
        node.parent.right = right_child

    right_child.left = node
    node.parent = right_child

def _right_rotate(self, node):
    left_child = node.left

```

```

node.left = left_child.right

if left_child.right:
    left_child.right.parent = node
left_child.parent = node.parent

if not node.parent:
    self.root = left_child
elif node == node.parent.right:
    node.parent.right = left_child
else:
    node.parent.left = left_child

left_child.right = node
node.parent = left_child

def inorder_traversal(self, node, depth=0):
    if node:
        self.inorder_traversal(node.left, depth + 1)
        print(" " * depth + f"{node.val} ({node.color})")
        self.inorder_traversal(node.right, depth + 1)

# Example usage
tree = RedBlackTree()
for val in [8, 18, 5, 15, 17, 25, 40, 80]:
    tree.insert(val)

print("Inorder traversal of Red Black Tree:")
tree.inorder_traversal(tree.root)

```

OUTPUT :

```

PS D:\SEM-6\AA\EXPERIMENTS> python -u "d:\SEM-6\AA\EXPERIMENTS\rb_insertion2.py"
Inorder traversal of Red Black Tree:
 5 (BLACK)
 8 (RED)
15 (BLACK)
17 (BLACK)
18 (BLACK)
25 (RED)
40 (BLACK)
80 (RED)
PS D:\SEM-6\AA\EXPERIMENTS>

```