A Big Data Analytics Framework for Supporting Multidimensional Mining over Big Healthcare Data

Mario Bochicchio

DIE Department
University of Salento
Lecce, Italy
mario.bochicchio@unisalento.it

Alfredo Cuzzocrea
DIA Department, University of
Trieste & ICAR-CNR
Trieste, Italy
alfredo.cuzzocrea@dia.units.it

Lucia Vaira
DIE Department
University of Salento
Lecce, Italy
lucia.vaira@unisalento.it

Abstract— Nowadays, a great deal of attention is being devoted to big data analytics in complex healthcare environments. Fetal growth curves, which are a classical case of big healthcare data, are used in prenatal medicine to early detect potential fetal growth problems, estimate the perinatal outcome and promptly treat possible complications. However, the currently adopted curves and the related diagnostic techniques have been criticized because of their poor precision. New techniques, based on the idea of customized growth curves, have been proposed in literature. In this perspective, the problem of building customized or personalized fetal growth curves by means of big data techniques is discussed in this paper. The proposed framework introduces the idea of summarizing the massive amounts of (input) big data via multidimensional views on top of which well-known Data Mining methods like clustering and classification are applied. This overall defines a multidimensional mining approach, targeted to complex healthcare environments. A preliminary analysis on the effectiveness of the framework is also proposed.

Keywords—Mining Big Data; Big Healthcare Data; Healthcare Systems.

I. INTRODUCTION

Big data analytics in complex healthcare environments (e.g., [13], [14], [15], [16], [17]) are of high interest at now, by following well-known principles of big data management and mining (e.g., [18], [19], [20]). Here, the main problem consists in devising models, techniques and algorithms focused to extract useful knowledge from enormous amounts of (big) data, with the goal of implementing so-called big data intelligence, i.e. deriving decisions, decision processes, guidelines and policies devoted to improve the target healthcare system (e.g., [13]). Fetal growth curves, which are a classical case of big healthcare data, are very important in prenatal medicine for fetal well-being evaluation. Indeed, they represent a mature and well-established practice to early detect potential fetal growth restriction, to estimate the perinatal outcome and promptly treat possible complications. The general idea underlying this test is very simple and effective: fetuses grow up showing a regular trend as a function of the gestational age. Therefore, their wellbeing can be assessed by tracking their sizes over the time and by comparing them with a reference growth curve known as "good". The implementation of the idea, based on ultrasounds pictures of the maternal abdomen, is quite simple, non-invasive and inexpensive.

In the clinical routine, fetal biometric parameters coming from this test are compared with a set of reference parameters, which are usually provided by the same test equipment. When results are too large or too small for the gestational age, they are classified as "potentially pathologic" and supplementary clinical tests are required/performed. A very problematic aspect in this practice is that several sets of fetal growth curves are reported in literature and the adoption of the right one is crucial to avoid errors (e.g., to avoid wrong classifications of fetuses as pathologic or non-pathologic) [5]. This is a hot topic for the obstetrics and gynecologist community [1], since the currentlyadopted references lack of several mother-related aspects, such as ethnic group, food, drugs and smoke. Indeed, it has been recognized that these and other factors have a non-negligible influence on the actual growing trends of fetuses and, then, on the overall number of false-positives/negatives, and further unnecessary tests. In the current practice, failure rates as high as 46% are reported in literature [3], even considering the standard defined by the World Health Organization (WHO), so that, in several cases, it is hard to decide whether the fetus has to be considered pathologic or not. For this reason, customized fetal growth charts [1] have been proposed as an alternative to "literature-based" growth curves. The increasing acceptance of this best practice suggests for a new and ambitious perspective: the creation of an online service able to collect and analyze the world production of fetal growth data [2], in order to support obstetricians in the production of customized/personalized fetal growth curves. The clinical understanding of the phenomenon described by such a large amount of data is extremely intriguing. because of the underlying idea of finally grabbing a total understanding of the fetal growth processes. On the other hand, it is also challenging, due to both technical and medical reasons. These aspects are discussed in the remaining part of the paper. The main goal of the paper is that of assessing the feasibility of such online service. To this end, the paper proposes a big data analytics framework for building customized or personalized fetal growth curves by means via innovative big data techniques. The proposed framework introduces the idea of summarizing the massive amounts of (input) big data via multidimensional views [21] on top of which well-known Data Mining methods like clustering and classification are applied. This overall defines a multidimensional mining approach, targeted to complex healthcare environments. A preliminary analysis on the effectiveness of the framework is also proposed.

The remaining part of the paper is organized as follows. Section II contains the background knowledge that represents the foundations of our research. In Section III, we provide related work of our research, which is mainly centered on the issue of managing and mining big data. Section IV provides principles and definitions of the proposed big data analytics framework for supporting multidimensional mining in complex healthcare environments. In Section V, we describe implementation and preliminary results of the proposed framework, along with some preliminary analysis to proof the effectiveness of this framework, on the basis of real-life big healthcare data coming from a government/university research project. Finally, we draw conclusions and discuss our future work in Section VI.

II. BACKGROUND KNOWLEDGE

In this Section, we provide the background knowledge that represents the foundations of our research. Several population-specific fetal growth curves have been proposed in literature, but the problem of defining a widely-accepted model for fetal growth is far from being solved [1], [5], since ethnicity is not the only parameter to be taken into account. Maternal height, weight, parity and the gender of the fetus have all been found to be significantly associated with normal variation in birth weight. Cigarette smoking, fetus gender, genetic syndromes, congenital anomalies and placental failure can also affect the fetal growth.

In the huge amount of scientific literature discussed in [5], several population-specific fetal growth studies are reported. Also, critical issues of these proposals are identified by the following axioms:

- number of involved patients (some hundreds or at the least some thousand) is low with respect to the total number of newborn per year (about 160 million in the world);
- patients that are considered in the studies are not representative of the variety of anthropometrical factors related to ethnicity, familial aspects and to other relevant internal and external factors;
- commonly-used growth curves are up to five decades old, they are not updated with respect to the current population and they are not suitable to investigate temporal trends and dynamic aspects in fetal growth curves – data, in fact, come from "static" archives and not from the current clinical practice;
- informative resources coming from the different countries are not integrated and analyzed as global resource however, no single country has sufficient data to create growth curves for all newborns; this means that, without a global approach, the statistical significance of the different studies is questionable;
- there is a considerable methodological heterogeneity in the studies of fetal biometry so that it is not feasible to adopt a unique standard among the different hospital centers;
- majority of studies related to fetal growth specify some exclusion criteria (e.g., diseases, twins' delivery etc.) in

order to determine whether a given patient may be included in the study – this is practically equivalent to deny pathologic women of the diagnostic support provided by fetal growth curves.

The impact of the adoption of wrong reference growth curves on fetal diagnoses has been analyzed in [1] and [3]. In the latter, a specific population from the southeast of Italy has been analyzed and compared against the reference curves adopted for Italian [4] and European fetuses. Results show that, for the femur length, which is he most variable among biometric parameters, 26% of analyzed fetuses exceed the 95th percentile (i.e., it is suspected as pathologic) if compared to the Italian standards, while 46% of them exceed the 95th percentile if compared with the European ones. This despite to the fact that, at delivery time, all babies were healthy and without biometric problems. Such result, among several others, confirm the necessity of carefully re-defining the concept of "reference growth curves".

To this end, a challenging and stimulating alternative is the (prospective) complete collection and analysis of the world production of fetal growth data, as outlined in Section I. In order to achieve this, a massive amount of data coming from heterogeneous sources should be processed with machine learning algorithms for both diagnostic and research purposes. Among others, classification and clustering algorithms are relevant for our research. Hence, according to a recent survey of clustering algorithms for medical applications [12], we observed that clustering algorithms perform better with uniform data distributions, while their performance as well as the quality of the extracted knowledge tend to decrease in non-uniform collections. Moreover, clustering medical data requires to deal with some critical issues that usually characterize medical datasets, such as outliers, incompleteness and the fact that the expected number of clusters can be hardly guessed a-priori. For these reasons, density-based clustering [11] and Expectation Maximization (EM) clustering [8] have been selected among others in our research. Indeed, density-based algorithms don't need to specify the number of clusters in advance, but their main disadvantage is that they don't handle the data points with varying densities and results depend on the distance measures. EM algorithms, instead, have been considered because of the nature of the fetal growth phenomenon which, for homogeneous groups of mothers, is modeled in literature as a Gaussian distribution of biometric fetal sizes. A good extension of this concept to populations composed by a large number of mothers belonging to an unknown number of homogeneous groups is given by the mixture model (e.g., [22]) and the related EM algorithm.

III. RELATED WORK

The problem of managing and mining big data (e.g., [18], [19], [20]) has received a big deal of attention from the research community, in particular in the healthcare management setting, also stirred-up by emerging *Cloud computing technologies* (e.g., [26]). Actual literature comprises a wide collection of proposals. In this Section, we provide an overview on the most noticeable ones.

[13] proposes a composite big data analytics framework, called *SmartHealth*, for attacking major challenges of healthcare systems via ICT technologies. Indeed, they correctly recognize

that, with the increasing volumes of information gathered via patient monitoring systems, physicians have been put on increasing pressure for making *sophisticated analytical decisions* that exploit the various types of data that is being gathered per patient. The deriving continuously growing datasets delineates a phenomenon that is now recognized in the business community as the *Big Data challenge*. To deal with this emerging challenge, *SmartHealth* comprises a collection of innovative ICT technologies, such as: sensing technologies, Cloud computing, *Internet-of-Things* (e.g., [27]) and big data analytics systems. Several applications of *SmartHealth* in the healthcare domain are also described.

[14] considers *mobile healthcare services* and proposes *an innovative healthcare service architecture* enriched by *a database-management-oriented data acquisition scheme* that also supports *query facilities*. Authors experimentally prove that the proposed architecture effectively bridges the gap between the healthcare application domain and the acquisition of physical data.

[15] moves the attention on real-time discovery services over large, heterogonous and complex healthcare datasets by means of schema-less and column-oriented methods. Particularly, authors introduce a service platform for supporting the exploration of data and discovery of patient-related statistics from healthcare datasets. The architecture of this platform is motivated by the need for fast, schema-less, and flexible approaches to SQL-based exploration and discovery of information embedded in the common, heterogeneously structured healthcare datasets and supporting components such as electronic health records, practice management systems, and so forth. They also apply the proposed service platform to clinical trials candidate discovery, and the analysis of the effectiveness of their related treatments. Key features and software architecture of the proposed platform are discussed in details, as well as its runtime profiles and performance characteristics.

[16] describes an effective, scalable and distributable MapReduce-based algorithms for finding patient similarities in huge healthcare networks. Authors recognize that, in healthcare management systems and, in particular, healthcare network systems, it is necessary to adapt a "big data solution" for addressing fundamentals healthcare problems. Among these, they recognize the problem of finding patient similarities, and they argue that current methods are not adaptive and do not support the complete target data sources. In addition to this, they cannot fulfill user requirements within the scope a query tool. To solve this main drawback, they propose ScaDiPaSi, a scalable and distributable method for finding patient similarities over the well-known MapReduce framework [28]. The enclosed experimental evaluation shows that ScaDiPaSi runs with high confidence and low execution time.

Finally, [17] introduces a semantic big data platform for integrating heterogeneous wearable data in healthcare. Authors focus on wearable computing systems that represent one of the most plunge areas used to transform traditional healthcare systems into active systems able to continuously monitor and control the patients' health. However, authors recognize that the proliferation of such systems creates challenges related to data

management and integration aspects. In response to this emerging issue, they propose a semantic big data architecture based on the "Knowledge as a Service" approach, in order to cope with heterogeneity and scalability challenges. In particular, they enrich the NIST Big Data model with semantics in order to smartly understand the collected data, and generate more accurate and valuable information by correlating scattered medical data stemming from multiple wearable devices or/and from other distributed data sources.

IV. BUILDING CUSTOMIZED FETAL GROWTH CURVES BY MEANS OF BIG DATA ANALYSIS TECHNIQUES

In this Section, we provide the main contribution of our research, i.e. principles and definitions of a big data analytics framework for supporting multidimensional mining in complex healthcare environments. The idea of developing an online service to collect and analyze large datasets about maternal/fetal wellbeing and fetal growth, and supporting gynecologists and obstetricians in diagnoses of fetal growth restrictions has been considered valuable by several authors [1],[3]. Actually, scaling this approach up to the worldwide production of fetal-maternal data could drive the medical community toward a deeper understanding of fetal pathologies, but several aspects have to be considered.

From a technical point of view, due to the volume of data to collect and analyze, the variety of descriptors associated to each mother/fetus and the velocity inherent to the phenomenon, Big Data techniques must be adopted. Indeed, every year there are about 160 millions of newborns in the world: on average this is equivalent to about 300 newborns per second. Considering that, according to international guidelines, for each healthy woman, about 10 clinical test (3 for growth tracking) are performed during pregnancy, and that for pathologic fetuses this number is significantly higher, the global production of data on the phenomenon can be estimated in a continuous stream of 1,000 – 10,000 new medical records per second, with an overall volume of 1 to 10 Petabytes per year. For the purposes of this paper, a more realistic scenario including 10% to 20% of fetal-growth data from at least two European countries is sufficient to test the proposed framework and tune it for further extension.

According to current methods adopted in the clinical practice for fetal-maternal wellbeing assessment, the main algorithms to analyze this stream would be based on: (i) least-square method, (ii) multidimensional analysis, (iii) clustering and classification techniques. The overall computational load is hard to estimate because of the problem is still under investigation, but distributed approaches and parallelization techniques are likely to be adopted. Moreover, the variety of data types (both structured and unstructured) is one of the main characteristics of this research field, because of the elements affecting fetal growth are not completely known and, every year, new variables come from the influence of new pathologies, medicines, therapies, pollutants etc. This heterogeneity is problematic to manage, but it is an important and unavoidable characteristic of the problem.

Referring to the algorithmic part, the possibility of constructing dynamic and customized fetal growth curves is mainly based on the following aspects:

- the application of multidimensional analysis techniques, which allow to both summarize the massive amounts of (input) big data via multidimensional and identify groups of patients (fetuses, in our case) who share similar growth patterns over the time;
- the possibility of searching for possible *correlation* of fetal growths vs parameters like ethnic group, maternal age, fetal gender, and so on.

The hypothesis is that fetuses at the same gestational age, with similar genetic make-up (e.g., ethnicity, familial aspects, and so forth) and in similar environmental conditions (e.g., food, smoke, drugs, and so forth), are subject to similar growth curves. This kind of fetuses will be referred, in the following of the paper as *Homogeneous Patient Groups* (HPG). This allows to identify patients who share common profiles in order to determine if a given fetus is potentially pathologic or not, when his/her growth parameters are different from those of the HPG to which he/she belongs. The membership to a specific group is established at run-time and a specific fetus can belong to one or more groups simultaneously, according to the analyzed features.

The diagnostic process is based on the following three main steps:

- a) build the summarizing multidimensional view of the target experiment;
- b) initially, the HPG of each mother/fetus is not known; it can be identified through anamnesis or specific tests and exams:
- c) the wellbeing of each new fetus is assessed by comparing its actual sizes with the reference charts of the HPG identified by the previous step.

In terms of multidimensional analysis, patients can be represented as multidimensional points, and HPGs as regions, of a multidimensional space whose dimensions are all parameters affecting the fetal growth (ethnicity, maternal weight, height, familial aspects, foods, and so forth), and whose measures of analysis are the biometric parameters of the fetus. In this sense, step b) corresponds to identifying the patient's nearest HPG according to some distance measure, while step c) requires to compute the average size, the variance, and the corresponding percentile on a purposely defined (sufficiently-wide and updated) subset of elements of the same HPG. Moreover, HPGs can be periodically updated (e.g., every four to six months, considering that growth variations are not expected to emerge on shorter periods) by means of a suitable clustering algorithm, according to the guidelines s outlined in Section II. Considering that clustering algorithms are computationally intensive and cannot be repeated at the arrival of every new biometric fetal measure, a suitable classification algorithm must be exploited in order to decide to which precomputed clusters the new sample belong [10].

The innovative aspects of this method with respect to other approaches known in literature can be summarized as follows:

- HPGs are periodically updated rather than statically defined by means of standardized growth curves;

- reference growth curves are associated to each HPG (hundreds or thousands) rather than on few ethnic groups;
- fetal growth curves are continuously updated with the data coming from patients under examination, thus also revealing the long-term population trends in patient's growth.

V. IMPLEMENTATION, PRELIMINARY RESULTS AND DISCUSSION

We conducted some preliminary analysis to proof the effectiveness of our proposed framework, on the basis of real-life big healthcare data coming from a government/university research project. This Section describes the outcome of this task of our research.

In order to explore the implementation details of the proposed big data analytics framework for building customized fetal growth curves, we decided to collect and analyze an actual sample of fetal-maternal data coming from two facilities locate in the Apulia region in south Italy, namely: a university clinic, also involved in research about malformation and diabetes in pregnancy, and a general hospital. The facilities serve a basin of about 1.5 million citizens and assists more than 10,000 pregnant women per year. The sample, concerning about 500 pregnant women under assistance by 8 medical doctors, consists of a quite sparse table with about 2,500 records and 60 attributes grouped into 9 main categories (having obvious meaning):

- Personal Data;
- Parity;
- Fetal Biometry;
- Diabetic Profile;
- Maternal Biometry;
- Familiarity;
- *Glycemic Profile*;
- Other Pathologies;
- Delivery Outcome.

For each category, the percentage of information completeness, defined as the number of not-null records over the total number of records, is represented in Fig. 1.

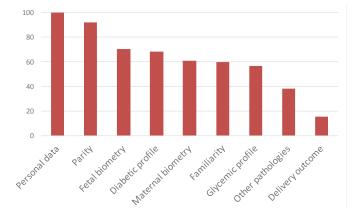


Fig. 1 – Information Completeness

This collection permitted us to better understand the nature and the variability of data involved in maternal and fetal wellbeing monitoring. Moreover, it permitted us to define a set of *Dimensional Fact Models* (DFM) [23] able to describe a typical fetal-maternal test, along with its variable aspects. A simplified version of the main DFM is shown in Fig. 2.

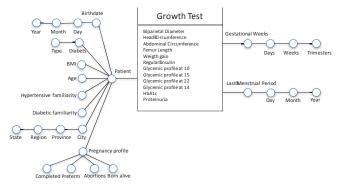


Fig. 2 – DFM of a Fetal-Maternal Test

According to the guidelines of the WHO on fetal growth curves, the available data sample has been also used to extract the reference curves for the target population to be analyzed. The process included a preliminary *normality distribution test* and a *linear regression*. This preliminary step was essential for a quantitative evaluation of the reduction of false positive/negative obtained with the new proposed method.

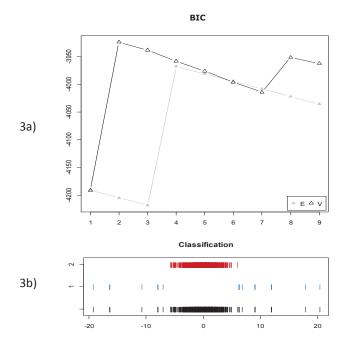


Fig. 3 – Expectation Maximization Clustering: Results

For what concern the clustering analysis, the above-defined multidimensional model has been implemented on top of the OLAP server *Mondrian* [24] and two standard implementations of the density-based and EM clustering techniques (discussed in

Section II) have been provided by the *R environment* [25]. In our preliminary experimentation, we noticed that, while the EM algorithm converges on two overlapped clusters, no clear results come out from the density-based algorithm, probably due to the very non-homogeneous nature of the processed dataset. The results achieved by applying the EM algorithm are represented in fig. 3a (Bayesian Information Criterion, used to estimate the number of clusters in the analyzed sample) and 3b (the original dataset and the two achieved clusters). Indeed, this approach can be improved by overcoming the well-known not-exciting performance of density-based clustering algorithms (e.g., [31]), for instance by adopting a kind of adaptive threshold like in [32].

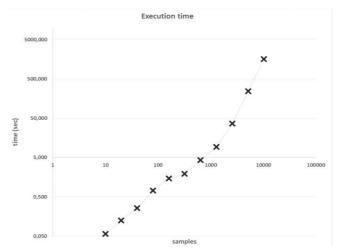


Fig. 4 – EM Clustering: Execution Time vs. Sample Size

Finally, in Fig. 4 it is reported the execution time of the adopted algorithm as a function of the problem size. This parameter is important to decide the maximum size of the clustered sample as well as how frequently it can be updated. The result shows that the execution time increases more than exponentially and that datasets of 5120 fetal sizes can be processed in about 4 minutes on a Pentium Core i5 @ 2.5 GHz, which is compatible with the discussed problem.

The application of these methodologies (i.e., multidimensional summarization and clustering analysis) confirms to us the effectiveness of our proposed framework in dealing with multidimensional mining in complex healthcare environments via big data analytics techniques.

VI. CONCLUSIONS AND FURTHER WORK

In this paper, we have introduced a big data analytics framework targeted to big healthcare data. The framework realizes a multidimensional mining approach for building customized or personalized fetal growth curves. The main idea consists in summarizing the massive amounts of (input) big data via multidimensional views on top of which well-known Data Mining methods like clustering and classification are applied. A preliminary analysis on the effectiveness of the framework has been also proposed.

Future work is mainly oriented towards extending our big data analytics framework by means of innovative computing metaphors such as *adaptiveness* (e.g., [29]) and *uncertainty* (e.g., [30]).

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