

Topic 6 Limitations of Linear Regression Part II
MG20S Econometrics: Theory and Applications
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Last week

- OVB
- Sample selection
- Projection vs. regression
- Non-random sampling
- Unbiasedness.
- Reverse causality

Today

- Take attendance
- What is in there for me to do the formative?
- Recap of theor TG P#.
- AT Will Class Exercises
- Holidays.

L4: Outlying observations.

- Leverage values
- Influential observations / Outliers.
- Correction methods: Leave-one out estimator.
- Outlier \neq typo \neq different units \neq measurement error.

Alternative methods:

- Estimate log model.
- Drop outliers.
- Winsorise.
- Model median, 99th percentile, etc.

LG: Heteroskedasticity.

- Makes inference harder. $\text{Var}(\hat{\beta}_j) = E[\hat{\sigma}^2 - \sigma^2]$

identically, independently distributed
non-heteroskedasticity non-random sampling
 $\text{Var}(e_i | X) = \sigma_i^2$

LS: Measurement error

Dependent $y = y^* + e_0$ $e_0 \sim N(0, \sigma_{e_0}^2)$

Independent $x = x^* + e_1$ $e_1 \sim N(0, \sigma_{e_1}^2)$

$$y = \beta_0 + \beta_1 x + \underbrace{(e_0 - \beta_1 e_1)}_g$$

$$\text{cov}(x, e_1) = E[e_1^2] = \text{var}(e_1)$$

"OVB": special case. Attenuation bias: drives
 $\text{plim}(\hat{\beta}_1) = \beta_1 \cdot \frac{1}{1 + \frac{\text{var}(e_1)}{\text{var}(x^*)}} < \beta_1$ magnitude towards 0.

Q9. $N = 3,000$

admin data

subjective judgement.

$$\widehat{wages} = 3.15 - 0.71 \text{ below}$$

$(0.66) \quad (0.33)$

Measurement error: independent variable
 \Rightarrow attenuation bias.

-0.71 is closer to 0 than it should
w/o bias, it could be -1.75. think in terms of
magnitude

$t = |-2.15| > 1.96$ even with bias.

$$Q10. \log(\widehat{\text{wages}}) = 3.2 + 0.4 \text{ educ } N=2,000.$$

(1.3) (0.2)

a. $H_0: \beta = 0$ vs $H_a: \beta > 0$ = one-tailed test

$$t = 2 > 1.645 \quad \text{w/o abs value.}$$

b. wages dependent variable. would reduce overall variance.

c. education independent variable. attenuation bias.

Still rejected in both cases.

Q11. Some answer as lecture slides.

Feel free to ask for clarification!

Q2. Why measurement error in the independent variable is not "a severe problem"?

Attenuation bias: $\text{plim } (\hat{\beta}_1) = \beta_1 \frac{1}{1 + \frac{\text{var}(e_1)}{\text{var}(x_1)}} < \beta_1$

Magnitude is always lower. Estimate goes to 0.

Lower bound.

Does not affect the sign. Persuasive of the effect.
Bad when you need the point estimate.

$$QB. \text{ profits} = \beta_0 + \beta_1 \log(\text{sales}) + e$$

β_1 : ↑ 1% of sales will increase profits
by $\frac{\hat{\beta}_1}{100}$ millions of dollars.

Heteroskedasticity does not affect point estimates.
Only affect inference.

Q14. Same argument as slides.

Q. and A

Summary

- Measurement error.
- Lower bound
- Attenuation bias
- Non-random sampling
- Heteroskedasticity
- Outlying observations.

See you on January!