Modelling and Verifying Distributed Systems with Aneris

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24. October 2022 Aarhus University

Distributed systems are a suitable target for formal verification

- ▶ More relevant than ever: Cloud Computing, Internet of Things, Mobile devices.
- Hard to get right: Even simple programs can have non-trivial bugs
- ▶ Important to get right: Even minor bugs can have large implications

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 - Unreliable: Messages can be dropped, duplicated, and reordered

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- Distributed Semantics
- Distributed Program Logic

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- ▶ Distributed Program Logic: **Aneris**, a program logic for AnerisLang in Iris

Overview

The AnerisLang Distributed Semantics

- ► Modelling unreliable distributed networks
- Examples of distributed programs
- Pitfalls of unreliable communication

The Aneris Distributed Program Logic

- ▶ Properties of a distributed program logic
- Modular reasoning principles of unreliable distributed systems
- Examples of verification with the logic

- 1. The semantics of the individual nodes
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- 2. The semantics of the network connectives
 - Socket allocation and binding
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- 3. The semantics of the (unreliable) network
 - Delivery of messages
 - Dropping, duplication, and reordering of messages
- 4. A notion of safety
 - e.g. *e* is safe if it never gets stuck

Node-local semantics designed to be as close to OCaml as possible:

```
v \in Val ::= () | b | i | s | \ell | rec f x = e | ...

e \in Expr ::= v | x | rec f x = e | e_1 | e_2 | ref(e) | ! e | e_1 | e_2 |

if e_1 then e_2 else e_3 | assert e | fork (e) | ...
```

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if e_1 then e_2 else e_3 | assert e | fork (e) | ...

Socket semantics inspired by UDP sockets:

```
v \in Val ::= \ldots \mid sh \mid sa \mid \ldots
e \in Expr ::= \ldots \mid socket \mid socketbind e_1 e_2 \mid send e_1 e_2 e_3 \mid recv e \mid \ldots
```

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v \in Val ::= () | b | i | s | \ell | rec f x = e | ...

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Network semantics are unreliable:

- Network arbitrarily takes steps alongside nodes
- Network steps may drop, duplicate, or reorder messages in transit

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Safety defined as programs not getting stuck

The server exposes a ping pong service on the address sa_{pong} . The client uses the service once by sending "ping" and awaiting "pong".

```
\operatorname{clt_{pong}} sa \triangleq s
\operatorname{let} sh = \operatorname{socket} \operatorname{in}
\operatorname{socketbind} sh sa;
\operatorname{send} sh \text{ "Ping" } sa_{\operatorname{pong}};
\operatorname{let} m = \operatorname{recv} sh \operatorname{in}
\operatorname{assert} (\operatorname{fst} m = \operatorname{"Pong"})
```

```
srvpong ≜
let sh = socket in
socketbind sh sapong;
rec go =
(let m = recv sh in
if fst m = "Ping"
then send sh "Pong" (snd m); go ()
else assert false) ()
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It this safe?

What if messages are dropped?

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- ▶ What if messages are dropped?
- ▶ What if messages are duplicated?

The server exposes a ping pong service on the address sa_{pong} . The client uses the service once by sending "ping" and awaiting "pong".

```
 \begin{array}{lll} \operatorname{clt}_{\operatorname{pong}} sa & & \operatorname{srv}_{\operatorname{pong}} & \\ & \operatorname{let} sh = \operatorname{socket} \operatorname{in} & & \operatorname{let} sh = \operatorname{socket} \operatorname{in} \\ & \operatorname{socketbind} sh \, sa; & & \operatorname{socketbind} sh \, sa_{\operatorname{pong}}; \\ & \operatorname{send} sh \; \text{"Ping"} \, sa_{\operatorname{pong}}; & & \operatorname{rec} go_- = \\ & \operatorname{let} m = \operatorname{recv} sh \operatorname{in} & & & \operatorname{if} \operatorname{fst} m = \operatorname{"Ping"} \\ & & \operatorname{assert} \left(\operatorname{fst} m = \operatorname{"Pong"}\right) & & \operatorname{if} \operatorname{fst} m = \operatorname{"Ping"} \\ & & \operatorname{then} \operatorname{send} sh \; \operatorname{"Pong"} \left(\operatorname{snd} \, m\right); go \left(\right) \\ & & \operatorname{else} \operatorname{assert} \, \operatorname{false} \right) \left(\right) \\ \end{array}
```

- ▶ What if messages are dropped?
- ▶ What if messages are duplicated?
- ▶ What if messages are reordered?

The server exposes a ping pong service on the address $sa_{\rm pong}$. The client uses the service once by sending "ping" and awaiting "pong".

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 \begin{array}{lll} \operatorname{clt_{pong}} sa \triangleq & \operatorname{srv_{pong}} \triangleq \\ & \operatorname{let} sh = \operatorname{socketin} & \operatorname{let} sh = \operatorname{socketin} \\ & \operatorname{socketbind} sh \, sa; & \operatorname{socketbind} sh \, sa_{\operatorname{pong}}; \\ & \operatorname{send} sh \, \text{"Ping"} \, sa_{\operatorname{pong}}; & \operatorname{rec} go_- = \\ & \operatorname{let} m = \operatorname{recv} sh \operatorname{in} & \operatorname{if} \operatorname{fst} \, m = \operatorname{"Ping"} \\ & \operatorname{assert} \left( \operatorname{fst} \, m = \operatorname{"Pong"} \right) & \operatorname{if} \operatorname{fst} \, m = \operatorname{"Ping"} \\ & \operatorname{then} \operatorname{send} \, sh \, \operatorname{"Pong"} \left( \operatorname{snd} \, m \right); go \left( \right) \\ & \operatorname{else} \operatorname{assert} \, \operatorname{false} \right) \left( \right) \\ \end{array}
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- ▶ What if messages are dropped? (safe, but loops
- ► What if messages are duplicated?
- ▶ What if messages are reordered?

The server exposes a ping pong service on the address sa_{pong} . The client uses the service once by sending "ping" and awaiting "pong".

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\begin{array}{lll} \operatorname{clt_{pong}} sa \triangleq & \operatorname{srv_{pong}} \triangleq \\ & \operatorname{let} sh = \operatorname{socketin} & \operatorname{let} sh = \operatorname{socketin} \\ & \operatorname{socketbind} sh sa; & \operatorname{socketbind} sh sa_{\operatorname{pong}}; \\ & \operatorname{send} sh \text{ "Ping" } sa_{\operatorname{pong}}; & \operatorname{rec} go_- = \\ & \operatorname{let} m = \operatorname{recv} sh \operatorname{in} & \operatorname{(let} m = \operatorname{recv} sh \operatorname{in} \\ & \operatorname{assert} \left( \operatorname{fst} m = \text{ "Pong"} \right) & \operatorname{if} \operatorname{fst} m = \text{ "Ping"} \\ & \operatorname{then} \operatorname{send} sh \text{ "Pong"} \left( \operatorname{snd} m \right); go \left( \right) \\ & \operatorname{else} \operatorname{assert} \operatorname{false} \right) \left( \right) \end{array}
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- ▶ What if messages are dropped? (safe, but loops ✓)
- ▶ What if messages are duplicated? (safe, as server just keeps responding ✓)
- ▶ What if messages are reordered?

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```

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- ▶ What if messages are duplicated? (safe, as server just keeps responding ✓)
- ▶ What if messages are reordered? (safe, as all directed messages are the same ✓)

The server exposes an echo service on the address sa_{echo} . The client uses the service twice, first sending "Hello" and then "World".

```
cltecho sa \triangleq
let sh = socket in
socketbind sh sa;
send sh "Hello" sa<sub>echo</sub>;
send sh "World" sa<sub>echo</sub>;
let m_1 = \text{recv sh in}
let m_2 = \text{recv sh in}
assert (fst m_1 = "Hello");
assert (fst m_2 = "World")
```

```
srv_{echo} \triangleq 1et sh = socket in socketbind sh sa_{echo};
rec go_{-} = (1et m = recv sh in send sh (fst m) (snd m);
go())()
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Is this safe?

What if message are dropped?

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  let sh = socket in
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  send sh "Hello" saecho;
  send sh "World" saecho:
  let m_1 = \operatorname{recv} sh in
  let m_2 = recv shin
  assert (fst m_1 = \text{"Hello"});
  assert (fst m_2 = "World")
```

- Is this safe?
 - ► What if message are dropped?
 - ► What if messages are duplicated?
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  let sh = socket in
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     go ()) ()
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                                       srv<sub>echo</sub> ≜
  let sh = socket in
                                         let sh = socket in
  socketbind sh sa:
                                         socketbind sh saecho;
  send sh "Hello" saecho;
                                         recgo_{-}=
  send sh "World" saecho:
                                           (let m = recv shin)
                                            send sh(fst m)(snd m);
  let m_1 = recv shin
  let m_2 = recv shin
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clt_{acho} sa \triangleq
  let sh = socket in
                                           let sh = socket in
  socketbind sh sa:
                                            socketbind sh saecho;
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                                           recgo_{-}=
                                              (let m = recv sh in
  send sh "World" saecho:
                                               send sh (fst m) (snd m);
  let m_1 = \operatorname{recv} sh in
  let m_2 = recv shin
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- ► What if message are dropped? (safe, but loops ✓)
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let sh = socket in

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srv_{echo} \triangleq 1et sh = socket in socketbind sh sa_{echo};
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```
The server exposes an echo service on the address sa_{echo}.
The client uses the service twi
                              recyfresh sh ms ≜
     clt<sub>echo</sub> sa ≜
                                recgo_=
       let sh = socket in 	 (let m = recv sh in
       socketbind sh sa; if mem m ms then go () else m) ()
       send sh "Hello" saechoi
                                              recgo_=
                                                41et m = recv shin
       send sh "World" saecho:
                                                 send sh(fst m)(snd m);
       let m_1 = \operatorname{recv} shin
       let m_2 = \text{recvfresh } sh [m_1] in
                                                 go ()) ()
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Is this safe?
```

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  send sh "World" saecho;
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  let m_1 = recv sh in
  let m_2 = \text{recvfresh } sh [m_1] in
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- ▶ What if message are dropped? (safe, but loops ✓)
- ▶ What if messages are duplicated? (safe, as we wait for a fresh second message ✓)
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  let sh = socket in
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  socketbind sh sa:
                                            socketbind sh saecho;
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  let m_1 = \operatorname{recv} sh in
                                               send sh (fst m) (snd m);
  send sh "World" saecho;
  let m_2 = \text{recvfresh } sh [m_1] in
                                               go ()) ()
  assert (fst m_1 = \text{"Hello"});
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```

- ▶ What if message are dropped? (safe, but loops ✓)
- ▶ What if messages are duplicated? (safe, as we wait for a fresh second message ✓)
- ▶ What if messages are reordered? (safe, as we can only receive "Hello" first ✓)

We must be able to reason about:

- 1. Non-distributed internal node reductions
- 2. Allocation and binding of sockets
- 3. Message passing (and resource transfer)

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We want to guarantee safety

▶ No node in the distributed system will ever get stuck

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- 1. Non-distributed internal node reductions
- 2. Allocation and binding of sockets
- 3. Message passing (and resource transfer)

We want to guarantee safety

▶ No node in the distributed system will ever get stuck

We want to obtain **abstraction** and **modularity**:

- ▶ **Abstraction:** abstract over unreliable network layer
- Modularity: reason about nodes individually

Aneris: Distributed Separation Logic

Distributed Program Logic for AnerisLang, built on top of Iris, with:

- ▶ Node-local Hoare triple rules for non-distributed expressions
- ► Node-local Hoare triple rules for sockets
- Node-local Hoare triple rules for message passing

Aneris: Distributed Separation Logic

Distributed Program Logic for AnerisLang, built on top of Iris, with:

- ▶ Node-local Hoare triple rules for non-distributed expressions
- ► Node-local Hoare triple rules for sockets
- Node-local Hoare triple rules for message passing

Aneris inherits Iris's safety guarantees (which are foundationally certified in Coq)

Node-local rules for non-distributed expressions

Standard rules decorated with an ip identifier:

$$\begin{array}{c} \tau,\sigma ::= x \mid 0 \mid 1 \mid B \mid \mathbb{N} \mid Z \mid \mathsf{Type} \mid \forall x : \tau.\,\sigma \mid \mathit{Loc} \mid \mathit{Val} \mid \mathit{Expr} \mid \mathsf{Prop} \mid \mathit{Ip} \mid \ldots \\ t,u,P,Q ::= \mathsf{True} \mid \mathsf{False} \mid P \land Q \mid P \lor Q \mid P \Rightarrow Q \mid \qquad \qquad (\mathsf{Propositional \ logic}) \\ \forall x : \tau.\,P \mid \exists x : \tau.\,P \mid t = u \mid \qquad \qquad (\mathsf{Higher-order \ logic \ with \ equality}) \\ P * Q \mid P \twoheadrightarrow Q \mid \ell \stackrel{\mathit{ip}}{\mapsto} v \mid \{P\} \, \langle \mathit{ip}; \ e \rangle \, \{v.\,Q\} \mid \qquad \qquad (\mathsf{Separation \ logic}) \\ \triangleright P \mid \boxed{P} \mid P \Rrightarrow Q \mid \ldots \qquad \qquad (\mathsf{Ghost \ state \ and \ invariants}) \end{array}$$

Node-local rules for non-distributed expressions

Standard rules decorated with an ip identifier:

$$\tau,\sigma ::= x \mid 0 \mid 1 \mid \mathsf{B} \mid \mathbb{N} \mid \mathsf{Z} \mid \mathsf{Type} \mid \forall x : \tau. \sigma \mid \mathsf{Loc} \mid \mathsf{Val} \mid \mathsf{Expr} \mid \mathsf{Prop} \mid \mathsf{Ip} \mid \dots$$

$$t,u,P,Q ::= \mathsf{True} \mid \mathsf{False} \mid P \land Q \mid P \lor Q \mid P \Rightarrow Q \mid \qquad \qquad (\mathsf{Propositional logic})$$

$$\forall x : \tau. P \mid \exists x : \tau. P \mid t = u \mid \qquad (\mathsf{Higher-order logic with equality})$$

$$P * Q \mid P \twoheadrightarrow Q \mid \ell \stackrel{ip}{\longmapsto} v \mid \{P\} \langle ip; e \rangle \{v. Q\} \mid \qquad (\mathsf{Separation logic})$$

$$\triangleright P \mid \boxed{P} \mid P \Rightarrow Q \mid \dots \qquad (\mathsf{Ghost state and invariants})$$

Example: rules for references:

HT-ALLOC HT-LOAD
$$\{\mathsf{True}\} \, \langle i \! p; \, \mathtt{ref}(v) \rangle \, \{w. \, \exists \ell. \, w = \ell * \ell \stackrel{ip}{\mapsto} v \} \qquad \{\ell \stackrel{ip}{\mapsto} v\} \, \langle i \! p; \, ! \, \ell \rangle \, \{w. \, w = v * \ell \stackrel{ip}{\mapsto} v \}$$

HT-STORE
$$\{\ell \stackrel{ip}{\mapsto} v\} \langle ip; \ell \leftarrow w \rangle \{\ell \stackrel{ip}{\mapsto} w\}$$

Node-local rules for sockets

```
\tau,\sigma ::= \dots \mid Socket \mid Address \mid \dots \\ t,u,P,Q ::= \dots \mid sh \stackrel{ip}{\hookrightarrow} o \mid \mathsf{FreeAddr}(sa) \mid \dots \\ \mathsf{Ht-Newsocket} \qquad \qquad \mathsf{Ht-socketBind} \\ \{\mathsf{True}\} \qquad \qquad \left\{sh \stackrel{sa.ip}{\hookrightarrow} \mathsf{None} * \mathsf{FreeAddr}(sa)\right\} \\ \langle \mathit{ip}; \, \mathsf{socket}() \rangle \qquad \qquad \langle \mathit{sa.ip}; \, \mathsf{socketbind} \, \mathit{sh} \, \mathit{sa} \rangle \\ \{w. \, \exists \mathit{sh}. \, w = \mathit{sh} * \mathit{sh} \stackrel{ip}{\hookrightarrow} \mathsf{None}\} \qquad \left\{w. \, w = () * \mathit{sh} \stackrel{sa.ip}{\hookrightarrow} \mathsf{Some}(sa)\right\}
```

Node-local rules for sockets

```
\tau,\sigma ::= \dots \mid Socket \mid Address \mid \dots
t,u,P,Q ::= \dots \mid sh \stackrel{ip}{\hookrightarrow} o \mid \mathsf{FreeAddr}(sa) \mid \dots
\mathsf{HT-NEWSOCKET} \qquad \qquad \mathsf{HT-SOCKETBIND} \\ \{\mathsf{True}\} \qquad \qquad \left\{sh \stackrel{sa.ip}{\hookrightarrow} \mathsf{None} * \mathsf{FreeAddr}(sa)\right\} \\ \langle ip; \ \mathsf{socket}() \rangle \qquad \qquad \langle sa.ip; \ \mathsf{socketbind} \ sh \ sa \rangle \\ \{w. \exists sh. \ w = sh * sh \stackrel{ip}{\hookrightarrow} \mathsf{None}\} \qquad \qquad \{w. \ w = () * sh \stackrel{sa.ip}{\hookrightarrow} \mathsf{Some}(sa)\}
```

Sockets are treated simlarly to references

- ▶ We assume an infinite range, so we can always allocate a fresh one
- Deallocation assumed to be handled by the runtime

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Sockets are treated simlarly to references

- ▶ We assume an infinite range, so we can always allocate a fresh one
- Deallocation assumed to be handled by the runtime

All addresses are considered free on node startup

- ▶ i.e. the FreeAddr(sa) resource is obtained for any sa for free
- ► FreeAddr(sa) guarantees that addresses are only bound once

Many ways of reasoning about unreliable communication; we want to:

- ► Transfer (Iris) resources along with messages (to facilitate modularity)
- ▶ Abstract over the unreliable semantics (dropping, duplication, and reordering)

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 - ► $Message \triangleq Address * String * Address$
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Many ways of reasoning about unreliable communication; we want to:

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- Treat messages logically as a triple of the source, string, and destination
 - ► $Message \triangleq Address * String * Address$
 - ▶ We often write *m*.src, *m*.str, and *m*.dst for the message components
- Associate each socket address with a protocol $\Phi: Message \rightarrow iProp$ that all received messages must satisfy
 - ▶ Abstracts over reordering, as the order no longer matters
- ightharpoonup Acquire resources specificed by Φ m only when receiving a fresh m
 - ▶ Abstracts over duplication, as duplicate messages dont result in duplicate resources
- ightharpoonup Require giving up resources specified by Φ m only when sending a fresh m
 - Abstracts over dropping, as dropped messages can be retransmitted for free

```
\tau, \sigma ::= \dots \mid \textit{Message} \mid \dots
t, u, P, Q ::= \dots \mid \textit{sa} \leadsto (R, T) \mid \textit{sa} \bowtie \varPhi \mid \dots
\text{HT-SEND} \begin{cases} \textit{sh} \xrightarrow{\textit{sa.ip}} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (R, T) * \textit{dst} \bowtie \varPhi * \\ \{(\textit{sa}, \textit{str}, \textit{dst}) \notin T \Rightarrow \varPhi (\textit{sa}, \textit{str}, \textit{dst})\} \end{cases} \qquad \text{HT-RECV} \\ \{\textit{sh} \xrightarrow{\textit{sa.ip}} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (R, T) * \textit{sa} \bowtie \varPhi \} \\ \{\textit{sh} \xrightarrow{\textit{sa.ip}} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (R, T) * \textit{sa} \bowtie \varPhi \} \end{cases} \\ \langle \textit{sa.ip}; \ \textit{send} \ \textit{sh} \ \textit{str} \ \textit{dst} \rangle \\ \{\textit{sa.ip}; \ \textit{recv} \ \textit{sh} \rangle \\ \{\textit{sa.ip}; \ \textit{recv} \ \textit{sh} \rangle \} \\ \{\textit{sa.ip}; \ \textit{recv} \ \textit{sh} \rangle \end{cases} 
\begin{cases} \textit{w. w} = () * \textit{sh} \xrightarrow{\textit{sa.ip}} \mathsf{Some}(\textit{sa}) * \\ \textit{sa} \leadsto (R, T \cup \{(\textit{src}, \textit{str}, \textit{sa})\}, T) * \\ \{\textit{sh} \xrightarrow{\textit{sa.ip}} \mathsf{sh} \xrightarrow{\textit{sa.ip}} \mathsf{sh} \Rightarrow \varPhi (\textit{src}, \textit{str}, \textit{sa}) \end{cases} \}
```

All addresses have empty histories on node startup

▶ i.e. the $sa \leadsto (\emptyset, \emptyset)$ resource is obtained for any sa for free

```
\tau, \sigma ::= \dots \mid \textit{Message} \mid \dots
t, u, P, Q ::= \dots \mid \textit{sa} \leadsto (R, T) \mid \textit{sa} \Rightarrow \varPhi \mid \dots
\text{HT-SEND} \begin{cases} \textit{sh} \xrightarrow{\textit{csa.ip}} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (R, T) * \textit{dst} \Rightarrow \varPhi * \\ \{(\textit{sa}, \textit{str}, \textit{dst}) \notin T \Rightarrow \varPhi (\textit{sa}, \textit{str}, \textit{dst})) \end{cases} \begin{cases} \mathsf{HT-RECV} \\ \textit{sh} \xrightarrow{\textit{csa.ip}} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (R, T) * \textit{sa} \Rightarrow \varPhi \end{cases} \\ \langle \textit{sa.ip}; \ \textit{send} \ \textit{sh} \ \textit{str} \ \textit{dst} \rangle \\ \langle \textit{sa.ip}; \ \textit{send} \ \textit{sh} \ \textit{str} \ \textit{dst} \rangle \\ \{\textit{w. } \exists \textit{str}, \textit{src.} \ \textit{w} = (\textit{str}, \textit{src}) * \textit{sh} \xrightarrow{\textit{csa.ip}} \mathsf{Some}(\textit{sa}) * \\ \textit{sa} \leadsto (R, T \cup \{(\textit{sa}, \textit{str}, \textit{dst})\})\} \end{cases} \end{cases} \end{cases} \begin{cases} \mathsf{w.} \ \exists \textit{str}, \textit{src.} \ \textit{w} = (\textit{str}, \textit{src}) * \textit{sh} \xrightarrow{\textit{csa.ip}} \mathsf{Some}(\textit{sa}) * \\ \textit{sa} \leadsto (R \cup \{(\textit{src}, \textit{str}, \textit{sa})\}, T) * \\ ((\textit{src}, \textit{str}, \textit{sa}) \notin R \Rightarrow \varPhi (\textit{src}, \textit{str}, \textit{sa})) \end{cases}
```

All addresses have empty histories on node startup

- ▶ i.e. the $sa \rightsquigarrow (\emptyset, \emptyset)$ resource is obtained for any sa for free
- Protocols $(sa \Rightarrow \Phi)$ are considered either static (for servers) or dynamic (for clients)
 - Static protocols are obtained by all nodes on startup

HT-DYNAMIC

All addresses have empty histories on node startup

- ▶ i.e. the $sa \rightsquigarrow (\emptyset, \emptyset)$ resource is obtained for any sa for free
- Protocols ($sa \Rightarrow \Phi$) are considered either static (for servers) or dynamic (for clients)
 - ▶ Static protocols are obtained by all nodes on startup
 - ▶ Dynamic protocols are obtained via dyn sa, given to respective nodes on startup

```
clt_{pong} sa \triangleq 
let sh = socket in
socketbind sh sa;
send sh "Ping" sa_{pong};
let m = recv sh in
assert (fst m = "Pong");
```

```
\operatorname{srv_{pong}} \triangleq 1 \operatorname{et} sh = \operatorname{socket} \operatorname{in}
\operatorname{socketbind} sh sa_{\operatorname{pong}};
\operatorname{rec} go_{-} = (\operatorname{let} m = \operatorname{recv} sh \operatorname{in})
\operatorname{if} \operatorname{fst} m = \operatorname{"Ping"}
\operatorname{then} \operatorname{send} sh \operatorname{"Pong"} (\operatorname{snd} m); go()
\operatorname{else} \operatorname{assert} \operatorname{false}()
```

```
cltpong sa ≜
  let sh = socket in
  socketbind sh sa;
  send sh "Ping" sapong;
  let m = recv sh in
  assert (fst m = "Pong");
```

```
srv_{pong} \triangleq 1et sh = socket in
socketbind sh sa_{pong};
rec go_{-} = (1et m = recv sh in if fst m = "Ping" then send sh "Pong" (snd m); go () else assert false) ()
```

Socket protocols:

```
\Phi_{clt} \triangleq \lambda m. \dots 

\Phi_{srv} \triangleq \lambda m. \dots
```

```
clt_{pong} sa \triangleq 
let sh = socket in
socketbind sh sa;
send sh "Ping" sa_{pong};
let m = recv sh in
assert (fst m = "Pong");
```

```
srv_{pong} \triangleq 
let sh = socket in
socketbind sh sa_{pong};
rec go_{-} = 
(let m = recv sh in
if fst m = "Ping"
then send sh "Pong" (snd m); go ()
else assert false) ()
```

Socket protocols:

```
\Phi_{\textit{clt}} \triangleq \lambda \textit{m}. \ldots

\Phi_{\textit{srv}} \triangleq \lambda \textit{m}. \textit{m.str} = \text{"Ping"} * \ldots
```

```
\mathtt{srv}_{\mathtt{pong}} \triangleq
  clt_{pong} sa \triangleq
     let sh = socket in
                                                      let sh = socket in
                                                      socketbind sh sa<sub>pong</sub>;
     socketbind sh sa;
     send sh "Ping" sapong;
                                                      recgo_- =
     let m = recv shin
                                                         (let m = recv shin)
     assert (fst m = "Pong"):
                                                          if fst m = "Ping"
                                                          then send sh "Pong" (snd m); go ()
                                                          else assert false)()
Socket protocols:
\Phi_{clt} \triangleq \lambda m. \dots
\Phi_{\mathsf{env}} \triangleq \lambda \mathsf{m}.\,\mathsf{m.str} = \text{"Ping"} * \exists \psi.\,\mathsf{m.src} \Rightarrow \psi * \dots
```

```
\mathtt{srv}_{\mathtt{pong}} \triangleq
  clt_{pong} sa \triangleq
      let sh = socket in
                                                            let sh = socket in
      socketbind sh sa;
                                                            socketbind sh sa<sub>pong</sub>;
      send sh "Ping" sapong;
                                                            recgo_- =
      let m = recv shin
                                                               (let m = recv shin)
      assert (fst m = "Pong"):
                                                                if fst m = "Ping"
                                                                 then send sh "Pong" (snd m); go ()
                                                                 else assert false)()
Socket protocols:
\Phi_{clt} \triangleq \lambda m. \dots
\Phi_{\mathsf{srv}} \triangleq \lambda \mathsf{m}.\,\mathsf{m}.\mathsf{str} = \text{"Ping"} * \exists \psi.\,\mathsf{m}.\mathsf{src} \Rightarrow \psi * (\forall \mathsf{m'}.\,\mathsf{m'}.\mathsf{str} = \text{"Pong"} * \psi \;\mathsf{m'})
```

```
\mathtt{srv}_{\mathtt{pong}} \triangleq
  clt_{pong} sa \triangleq
      let sh = socket in
                                                       let sh = socket in
      socketbind sh sa;
                                                       socketbind sh sa<sub>pong</sub>;
      send sh "Ping" sapong;
                                                       recgo_- =
      let m = recv shin
                                                          (let m = recv shin)
      assert (fst m = "Pong"):
                                                           if fst m = "Ping"
                                                            then send sh "Pong" (snd m); go ()
                                                            else assert false)()
Socket protocols:
\Phi_{clt} \triangleq \lambda m. m. str = "Pong"
\Phi_{\mathsf{srv}} \triangleq \lambda m. \, m.\mathsf{str} = \text{"Ping"} * \exists \psi. \, m.\mathsf{src} \Rightarrow \psi * (\forall m'. \, m'.\mathsf{str} = \text{"Pong"} - * \psi \, m')
```

```
 \begin{split} & \big\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} & \hspace{0.5em} \mapsto \varPhi_{\mathit{srv}} \big\} \\ & \langle \mathit{sa}.\mathtt{ip}; \mathtt{clt}_{\mathsf{pong}} \; \mathit{sa} \rangle \\ & \big\{ \mathsf{True} \big\} \end{split}
```

```
 \left\{ \begin{aligned} & \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{\text{pong}} \mapsto \varPhi_{srv} \right\} \\ & \text{let } sh = \text{socket in} \\ & \text{socketbind } sh \; sa; \\ & \text{send } sh \; \text{"Ping" } sa_{\text{pong}}; \\ & \text{let } m = \text{recv } sh \text{ in} \\ & \text{assert } (\text{fst } m = \text{"Pong"}) \\ & \text{\{True\}} \end{aligned}
```

```
 \left\{ \begin{aligned} & \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{\text{pong}} & \mapsto \varPhi_{\textit{srv}} \right\} \\ & \text{let } sh = \texttt{socketin} \\ & \text{socketbind } sh \; sa; \\ & \text{send } sh \; \text{"Ping"} \; sa_{\text{pong}}; \\ & \text{let } m = \texttt{recv} \; sh \; \text{in} \\ & \text{assert} \; (\texttt{fst} \; m = \; \text{"Pong"}) \\ & \text{\{True\}} \end{aligned}
```

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longrightarrow} \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \mathsf{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \mathsf{let} \; \mathit{m} = \mathtt{recv} \; \mathit{sh} \; \mathsf{in} \\ & \mathsf{assert} \; (\mathtt{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
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```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\hookrightarrow} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\hookrightarrow} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \text{let} \; \mathit{m} = \mathtt{recv} \; \mathit{sh} \; \mathsf{in} \\ & \text{assert} \; (\mathtt{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

```
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```

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \mathsf{let} \; \mathit{m} = \mathsf{recv} \; \mathit{sh} \; \mathsf{in} \\ & \mathsf{assert} \; (\mathsf{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

```
HT-SEND \{sh \stackrel{\text{sa.ip.}}{\longrightarrow} \text{Some}(sa) * sa \rightsquigarrow (R, T) * dst \mapsto \Phi * ((sa, str, dst) \notin T \Rightarrow \Phi (sa, str, dst))\} \langle sa.ip; send sh str dst \rangle \{w.w = () * sh \stackrel{\text{sa.ip.}}{\longrightarrow} \text{Some}(sa) * sa \rightsquigarrow (R, T) \cup \{(sa, str, dst)\}\}
```

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & 1 \in \mathsf{t} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \  \  \, \mathtt{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \  \  \, \mathtt{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & 1 \in \mathsf{t} \; \mathit{m} = \mathsf{recv} \; \mathit{sh} \; \mathsf{in} \\ & \  \  \, \mathtt{assert} \; (\mathsf{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

 $\varPhi_{\mathit{srv}} \; (\mathit{sa}, \, \text{``Ping''}, \mathit{sa}_{\mathtt{pong}})$

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \mathsf{let} \; \mathit{m} = \mathsf{recv} \; \mathit{sh} \; \mathsf{in} \\ & \mathsf{assert} \; (\mathsf{fst} \; \mathit{m} = \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

```
\text{"Ping"} = \text{"Ping"} * \exists \psi. \textit{sa} \mapsto \psi * (\forall \textit{m'}. \textit{m'}. \mathsf{str} = \text{"Pong"} \twoheadrightarrow \psi \textit{m'})
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    let sh = socket in
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
    socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \rightsquigarrow (\emptyset, \emptyset) * \mathsf{dyn} \; sa * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    send sh "Ping" sapong;
    let m = \text{recy } sh in
                                                                                                    HT-DYNAMIC
    assert (fst m = "Pong")
                                                                                                     \{P * sa \Rightarrow \Phi\} \langle ip; e \rangle \{Q\}
{True}
                                                                                                     \{P * dyn sa\} \langle ip; e \rangle \{Q\}
```

"Ping" = "Ping"
$$*\exists \psi. sa \Rightarrow \psi * (\forall m'. m'. str = "Pong" - * \psi m')$$

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    let sh = socket in
\{sh \stackrel{sa.ip}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \rightsquigarrow (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
    socketbind sh sa:
\{sh \stackrel{sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} \}
    send sh "Ping" sapong;
    let m = \text{recy } sh in
                                                                                                HT-DYNAMIC
    assert (fst m = "Pong")
                                                                                                \{P * sa \Rightarrow \Phi\} \langle ip; e \rangle \{Q\}
{True}
                                                                                                 \{P * dyn sa\} \langle ip; e \rangle \{Q\}
```

"Ping" = "Ping"
$$*\exists \psi. sa \Rightarrow \psi * (\forall m'. m'. str = "Pong" - * \psi m')$$

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \text{let} \; \mathit{m} = \mathtt{recv} \; \mathit{sh} \; \mathsf{in} \\ & \text{assert} \; (\mathtt{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

$$(\forall m'. m'. \mathsf{str} = \text{"Pong"} \twoheadrightarrow \Phi_{\mathsf{clt}} m')$$

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{cs.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \text{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \text{let} \; \mathit{m} = \mathtt{recv} \; \mathit{sh} \; \mathsf{in} \\ & \text{assert} \; (\mathtt{fst} \; \mathit{m} = \; \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

```
(\forall \textit{m}'.\,\textit{m}'.\mathsf{str} = \text{``Pong''} \, \twoheadrightarrow \, \textit{m}'.\mathsf{str} = \text{``Pong''})
```

```
 \left\{ \begin{aligned} & \left\{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{let} \; \mathit{sh} = \mathtt{socketin} \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{None} * \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{socketbind} \; \mathit{sh} \; \mathit{sa}; \\ & \left\{ \mathit{sh} \overset{\mathit{sa.ip}}{\longmapsto} \; \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \right\} \\ & \mathsf{send} \; \mathit{sh} \; \text{"Ping"} \; \mathit{sa}_{\mathsf{pong}}; \\ & \mathsf{let} \; \mathit{m} = \mathsf{recv} \; \mathit{sh} \; \mathsf{in} \\ & \mathsf{assert} \; (\mathsf{fst} \; \mathit{m} = \text{"Pong"}) \\ & \left\{ \mathsf{True} \right\} \end{aligned}
```

```
\{\operatorname{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \operatorname{dyn} sa * sa_{\operatorname{pong}} \Longrightarrow \Phi_{srv} \}
    let sh = socket in
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \rightsquigarrow (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
    socketbind sh sa:
\{sh \stackrel{sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} \}
    send sh "Ping" sapong;
\{sh \stackrel{ss.1R}{\longrightarrow} Some(sa) * sa \leadsto (\emptyset, \{(sa, "Ping", sa_{pong})\}) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} \}
    let m = \text{recy } sh in
    assert (fst m = "Pong")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    let sh = socket in
\{sh \stackrel{sa.ip}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \rightsquigarrow (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
    socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * sa \mapsto \Phi_{clt} * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    send sh "Ping" sapong;
\{sh \stackrel{ss.1R}{\longrightarrow} Some(sa) * sa \leadsto (\emptyset, \{(sa, "Ping", sa_{pong})\}) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} \}
    let m = \text{recy } sh in
    assert (fst m = "Pong")
{True}
```

```
HT-RECV
{FreeAdd
                                \{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (R, T) * sa \Longrightarrow \Phi\}
    let.sh
                                    \langle sa.ip: recv sh \rangle
\{sh \stackrel{sa.ip}{\longleftrightarrow}
                                  (w. \exists str, src. w = (str, src) * sh \stackrel{csa.ip}{\longrightarrow} Some(sa) *
    socke
                                       sa \rightsquigarrow (R \cup \{(src, str, sa)\}, T) *
\{sh \stackrel{sa.ip}{\hookrightarrow}
                                       ((src. str. sa) \notin R \Rightarrow \Phi (src. str. sa))
    send
\{sh \stackrel{sa.1P}{\longrightarrow} Some(sa) * sa \leadsto (\emptyset, \{(sa, "Ping", sa_{pong})\}) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} \}
    let m = \text{recy } sh in
    assert (fst m = "Pong")
{True}
```

```
HT-RECV
{FreeAdd
                                      \{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (R, T) * sa \Longrightarrow \Phi\}
     let.sh
                                           \langle sa.ip: recv sh \rangle
\{sh \stackrel{sa.ip}{\longleftrightarrow} \}
                                       (w. \exists str, src. w = (str, src) * sh \stackrel{ss.ip}{\longrightarrow} Some(sa) *
     socke
                                             sa \rightsquigarrow (R \cup \{(src, str, sa)\}, T) *
\{sh \stackrel{sa.ip}{\longleftrightarrow}
                                             ((src. str. sa) \notin R \Rightarrow \Phi (src. str. sa))
     send
\{sh \stackrel{sa.ip}{\longrightarrow} Some(sa) * sa \leadsto (\emptyset, \{(sa, "Ping", sa_{pong})\}) * sa \mapsto \overline{\Phi}_{clt} * sa_{pong} \mapsto \overline{\Phi}_{srv}\}
     let m = \text{recy } sh in
 \begin{cases} sh \xrightarrow{sa.ip} \mathsf{Some}(sa) * sa \leadsto (\{(src, str, sa)\}, \{(sa, \text{"Ping"}, sa_{pong})\}) * \\ sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} * m = (str, src) * \Phi_{clt} (src, str, sa) \end{cases}
    assert (fst m = "Pong")
{True}
```

```
\{\operatorname{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \operatorname{dyn} sa * sa_{\operatorname{pong}} \Longrightarrow \Phi_{srv} \}
     let sh = socket in
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
     socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * sa \mapsto \Phi_{clt} * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     send sh "Ping" sapong;
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \{(sa, \text{"Ping"}, sa_{pong})\}) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv}\}
     let m = \text{recy } sh in
 \begin{cases} sh \stackrel{sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(src, str, sa)\}, \{(sa, \text{"Ping"}, sa_{pong})\}) * \\ sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} * m = (str, src) * \Phi_{clt} (src, str, sa) \end{cases}
     assert (fst m = "Pong")
{True}
```

```
\{\operatorname{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \operatorname{dyn} sa * sa_{\operatorname{pong}} \Longrightarrow \Phi_{srv} \}
     let sh = socket in
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
     socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * sa \mapsto \Phi_{clt} * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     send sh "Ping" sapong;
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \{(sa, \text{"Ping"}, sa_{pong})\}) * sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv}\}
     let m = \text{recy } sh in
 \begin{cases} sh \stackrel{sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(src, str, sa)\}, \{(sa, \text{"Ping"}, sa_{pong})\}) * \\ sa \mapsto \Phi_{clt} * sa_{pong} \mapsto \Phi_{srv} * m = (str, src) * str = \text{"Pong"} \end{cases}
     assert (fst m = "Pong")
{True}
```

```
clt_{echo} sa \triangleq
                                          srv<sub>echo</sub> ≜
  let sh = socket in
                                             let sh = socket in
  socketbind sh sa:
                                             socketbind sh saecho;
  send sh "Hello" sa<sub>echo</sub>;
                                             recgo_{-} =
  let m_1 = recv sh in
                                               (let m = recv shin)
  send sh "World" saecho:
                                                send sh (fst m) (snd m);
  let m_2 = \text{recvfresh } sh [m_1] \text{ in }
                                                go ()) ()
  assert (fst m_1 = \text{"Hello"});
  assert (fst m_2 = "World")
```

```
clt_{echo} sa \triangleq
                                                      srv<sub>echo</sub> ≜
         let sh = socket in
                                                         let sh = socket in
         socketbind sh sa:
                                                         socketbind sh saecho;
         send sh "Hello" saecho;
                                                         recgo_{-} =
         let m_1 = recv sh in
                                                            (let m = recv shin)
         send sh "World" saecho:
                                                             send sh (fst m) (snd m);
         let m_2 = \text{recvfresh } sh [m_1] \text{ in }
                                                             go ()) ()
         assert (fst m_1 = \text{"Hello"});
         assert (fst m_2 = "World")
Socket protocols:
\Phi_{clt} \triangleq \lambda m. \dots
\Phi_{\mathsf{srv}} \triangleq \lambda \mathsf{m} \ldots
```

```
clt_{echo} sa \triangleq
                                                           srv<sub>echo</sub> ≜
          let sh = socket in
                                                              let sh = socket in
          socketbind sh sa:
                                                              socketbind sh saecho;
          send sh "Hello" saecho;
                                                              recgo_{-} =
          let m_1 = recv sh in
                                                                 (let m = recv shin)
          send sh "World" saecho:
                                                                  send sh (fst m) (snd m);
          let m_2 = \text{recvfresh } sh [m_1] \text{ in }
                                                                  go ()) ()
          assert (fst m_1 = \text{"Hello"});
          assert (fst m_2 = "World")
Socket protocols:
\Phi_{clt} \triangleq \lambda m. \dots
\Phi_{\mathsf{srv}} \triangleq \lambda \mathsf{m}. \, \exists \psi. \, \mathsf{m}.\mathsf{src} \Rightarrow \psi * \dots
```

```
clt_{echo} sa \triangleq
                                                         srv<sub>echo</sub> ≜
          let sh = socket in
                                                            let sh = socket in
          socketbind sh sa:
                                                             socketbind sh saecho;
          send sh "Hello" saecho;
                                                            recgo_{-} =
          let m_1 = recv sh in
                                                               (let m = recv shin)
          send sh "World" saecho:
                                                                send sh (fst m) (snd m);
          let m_2 = \text{recvfresh } sh [m_1] \text{ in }
                                                                go ()) ()
          assert (fst m_1 = \text{"Hello"});
          assert (fst m_2 = "World")
Socket protocols:
\Phi_{clt} \triangleq \lambda m. \dots
\Phi_{\mathsf{srv}} \triangleq \lambda \mathsf{m}. \exists \psi. \mathsf{m.src} \Rightarrow \psi *
                   (\forall m'. m'. str = m. str * \psi m')
```

```
clt_{echo} sa \triangleq
                                                           srv<sub>echo</sub> ≜
          let sh = socket in
                                                              let sh = socket in
          socketbind sh sa:
                                                               socketbind sh saecho;
          send sh "Hello" sa<sub>echo</sub>;
                                                              recgo_{-} =
          let m_1 = recv sh in
                                                                 (let m = recv shin)
          send sh "World" saecho:
                                                                   send sh (fst m) (snd m);
          let m_2 = \text{recvfresh } sh [m_1] \text{ in }
                                                                  go ()) ()
          assert (fst m_1 = \text{"Hello"});
          assert (fst m_2 = "World")
Socket protocols:
\Phi_{clt} \triangleq \lambda m. ???
\Phi_{\mathsf{srv}} \triangleq \lambda \mathsf{m}. \exists \psi. \mathsf{m}.\mathsf{src} \Rightarrow \psi *
                   (\forall m'. m'. str = m. str * \psi m')
```

User-defined ghost state!

$$t, u, P, Q ::= \ldots \mid \mathtt{half}^{\gamma} \times \mid \ldots$$

Half-alloc

Half-agree

$$\vdash \Longrightarrow \exists \gamma. \, \mathtt{half}^{\gamma} \; x * \mathtt{half}^{\gamma} \; x$$

 $\mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ y \vdash x = y$

Half-update

$$\mathtt{half}^{\gamma} x * \mathtt{half}^{\gamma} y \vdash \Longrightarrow \mathtt{half}^{\gamma} z * \mathtt{half}^{\gamma} z$$

$$\Phi_{\textit{clt}} \triangleq \lambda \textit{m}. ???$$

$$\Phi_{\textit{srv}} \triangleq \lambda \textit{m}. \exists \psi. \textit{m}. \textit{src} \Rightarrow \psi *$$

$$(\forall m'.\ m'.\mathsf{str} = m.\mathsf{str} \twoheadrightarrow \psi \ m')$$

User-defined ghost state! $t, u, P, Q ::= \dots \mid \text{half}^{\gamma} \times \mid \dots$ HALF-ALLOC HALF-AGREE $half^{\gamma} x * half^{\gamma} v \vdash x = v$ $\vdash \Longrightarrow \exists \gamma. \mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ x$ HALF-UPDATE $half^{\gamma} x * half^{\gamma} y \vdash \Longrightarrow half^{\gamma} z * half^{\gamma} z$

$$\begin{split} \varPhi_{\textit{clt}} \ \gamma & \stackrel{\triangle}{=} \lambda \textit{m}. \, \text{half}^{\gamma} \ \textit{m}. \text{str} \\ \varPhi_{\textit{srv}} & \triangleq \lambda \textit{m}. \, \exists \psi. \, \textit{m}. \text{src} \Rightarrow \psi * \\ & (\forall \textit{m}'. \, \textit{m}'. \, \text{str} = \textit{m}. \text{str} \twoheadrightarrow \psi \ \textit{m}') \end{split}$$

User-defined ghost state! $t, u, P, Q ::= \dots \mid \text{half}^{\gamma} \times \mid \dots$ HALF-ALLOC HALF-AGREE $half^{\gamma} x * half^{\gamma} v \vdash x = v$ $\vdash \Longrightarrow \exists \gamma. \mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ x$ HALF-UPDATE $half^{\gamma} x * half^{\gamma} y \vdash \Longrightarrow half^{\gamma} z * half^{\gamma} z$

```
\begin{split} \varPhi_{\textit{clt}} \ \gamma &\triangleq \lambda \textit{m}.\, \texttt{half}^{\gamma} \ \textit{m}. \texttt{str} \\ \varPhi_{\textit{srv}} &\triangleq \lambda \textit{m}.\, \exists \psi.\, \exists \gamma.\, \textit{m}. \texttt{src} \Rightarrow \psi * \\ & \left( \forall \textit{m}'.\, \textit{m}'. \texttt{str} = \textit{m}. \texttt{str} * \texttt{half}^{\gamma} \ \textit{m}. \texttt{str} - \!\!\!* \psi \ \textit{m}' \right) \end{split}
```

User-defined ghost state! $t, u, P, Q ::= \dots \mid \text{half}^{\gamma} \times \mid \dots$ HALF-ALLOC HALF-AGREE $half^{\gamma} x * half^{\gamma} v \vdash x = v$ $\vdash \Longrightarrow \exists \gamma. \mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ x$ HALF-UPDATE $half^{\gamma} x * half^{\gamma} y \vdash \Longrightarrow half^{\gamma} z * half^{\gamma} z$

$$\begin{split} \varPhi_{\textit{clt}} \ \gamma & \stackrel{\triangle}{=} \lambda \textit{m}. \, \text{half}^{\gamma} \ \textit{m}. \text{str} \\ \varPhi_{\textit{srv}} & \triangleq \lambda \textit{m}. \, \exists \psi. \, \exists \gamma. \, \text{half}^{\gamma} \ \textit{m}. \text{str} * \textit{m}. \text{src} \\ & \left(\forall \textit{m}'. \, \textit{m}'. \, \text{str} = \textit{m}. \text{str} * \text{half}^{\gamma} \ \textit{m}. \text{str} - \!\!\!* \psi \ \textit{m}' \right) \end{split}$$

User-defined ghost state!

$$t, u, P, Q ::= \ldots \mid \mathtt{half}^{\gamma} \times \mid \ldots$$

Half-alloc

Half-agree

$$\vdash \Longrightarrow \exists \gamma. \, \mathtt{half}^{\gamma} \; x * \mathtt{half}^{\gamma} \; x$$

 $\mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ y \vdash x = y$

Half-update

 $\mathtt{half}^{\gamma} x * \mathtt{half}^{\gamma} y \vdash \Longrightarrow \mathtt{half}^{\gamma} z * \mathtt{half}^{\gamma} z$

$$\begin{split} \varPhi_{\textit{clt}} \ \gamma & \stackrel{\triangle}{=} \lambda \textit{m}. \, \text{half}^{\gamma} \ \textit{m.str} \\ \varPhi_{\textit{srv}} & \stackrel{\triangle}{=} \lambda \textit{m}. \, \exists \psi. \, \exists R. \, R*\textit{m.src} \\ & (\forall \textit{m'}. \, \textit{m'}. \text{str} = \textit{m.str} *R \twoheadrightarrow \psi \ \textit{m'}) \end{split}$$

```
 \begin{split} & \{ \mathsf{FreeAddr}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \} \\ & \langle \mathit{sa}.\mathtt{ip}; \mathtt{clt}_{\mathsf{echo}} \; \mathit{sa} \rangle \\ & \{ \mathsf{True} \} \end{split}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
   let sh = socket in
   socketbind sh sa:
   send sh "Hello" saecho:
   let m_1 = recv sh in
   send sh "World" saecho;
   let m_2 = \text{recvfresh } sh [m_1] \text{ in}
   assert (fst m_1 = \text{"Hello"});
   assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
    let sh = socket in
\{sh \stackrel{sa.ip}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
    socketbind sh sa:
    send sh "Hello" sa<sub>echo</sub>;
    let m_1 = \operatorname{recv} sh in
    send sh "World" saecho:
   let m_2 = \text{recvfresh } sh [m_1] in
    assert (fst m_1 = \text{"Hello"});
    assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
    let sh = socket in
\{sh \stackrel{\mathsf{sa.ip}}{\longrightarrow} \mathsf{None} * \mathsf{FreeAddr}(sa) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; sa * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    send sh "Hello" saecho;
    let m_1 = \operatorname{recv} sh in
    send sh "World" saecho;
    let m_2 = \text{recvfresh } sh [m_1] in
    assert (fst m_1 = \text{"Hello"});
    assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
\{sh \stackrel{\mathsf{sa.ip}}{\longrightarrow} \mathsf{None} * \mathsf{FreeAddr}(sa) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
     socketbind sh sa:
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; sa * sa_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}} \}
    send sh "Hello" saecho;
     let m_1 = \operatorname{recv} sh in
     send sh "World" saecho;
                                                                                                     Half-alloc
    let m_2 = \text{recvfresh } sh [m_1] \text{ in}
     assert (fst m_1 = \text{"Hello"});
                                                                                                     \vdash \Longrightarrow \exists \gamma. \, \mathtt{half}^{\gamma} \, x * \mathtt{half}^{\gamma} \, x
     assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
\{sh \stackrel{\mathsf{sa.ip}}{\longrightarrow} \mathsf{None} * \mathsf{FreeAddr}(sa) * \mathsf{sa} \leadsto (\emptyset, \emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathtt{pong}} \mapsto \Phi_{\mathsf{srv}} \}
     socketbind sh sa:
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{dyn} \; \mathit{sa} * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \; \text{"Hello"} * \mathsf{half}^{\gamma} \; \text{"Hello"} \end{cases}
     send sh "Hello" saecho:
     let m_1 = \operatorname{recv} sh in
                                                                                                                     Half-alloc
     send sh "World" saecho:
     let m_2 = \text{recvfresh } sh [m_1] in
                                                                                                                      \vdash \Longrightarrow \exists \gamma. \, \mathsf{half}^{\gamma} \, x * \mathsf{half}^{\gamma} \, x
     assert (fst m_1 = \text{"Hello"});
     assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
\{sh \stackrel{\text{sa.ip}}{\longrightarrow} \text{None} * \text{FreeAddr}(sa) * sa \leadsto (\emptyset, \emptyset) * \text{dyn } sa * sa_{pong} \Rightarrow \Phi_{srv} \}
     socketbind sh sa:
 \begin{cases} \mathit{sh} \xrightarrow{\mathit{sa.ip}} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{"Hello"} * \mathsf{half}^{\gamma} \ \text{"Hello"} \end{cases}
     send sh "Hello" saecho:
     let m_1 = \operatorname{recv} sh in
     send sh "World" saecho:
     let m_2 = \text{recvfresh } sh [m_1] in
     assert (fst m_1 = \text{"Hello"});
     assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
     socketbind sh sa:
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \ * \\ \mathsf{half}^{\gamma} \ \text{"Hello"} * \mathsf{half}^{\gamma} \ \text{"Hello"} \end{cases}
     send sh "Hello" saecho;
     let m_1 = \operatorname{recv} sh in
     send sh "World" saecho;
     let m_2 = \text{recvfresh } sh [m_1] in
     assert (fst m_1 = \text{"Hello"});
     assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
 \begin{cases} \mathit{sh} \overset{\mathsf{csa.ip}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \emptyset) * \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} \ * \\ \mathsf{half}^{\gamma} \ \text{"Hello"} * \mathsf{half}^{\gamma} \ \text{"Hello"} \end{cases} 
      send sh "Hello" saecho;
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{\mathit{echo}})\}) * \\ \mathit{sa} \boxminus \varPhi_{\mathit{clt}} \; \gamma * \mathit{sa}_{\mathit{pong}} \boxminus \varPhi_{\mathit{srv}} * \\ \mathit{half}^{\gamma} \; \text{``Hello''} \end{cases} 
       let m_1 = recv sh in
       send sh "World" saecho:
      let m_2 = \text{recvfresh } sh [m_1] \text{ in}
       assert (fst m_1 = \text{"Hello"});
       assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
      let sh = socket in
      socketbind sh sa:
      send sh "Hello" saecho:
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \mathsf{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \mathsf{``Hello''} \end{cases} 
     let m_1 = \operatorname{recv} sh in
      send sh "World" saecho:
     let m_2 = \text{recvfresh } sh [m_1] \text{ in}
      assert (fst m_1 = \text{"Hello"});
      assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
        let sh = socket in
        socketbind sh sa:
        send sh "Hello" saecho:
\begin{cases} \textit{sh} \overset{\textit{sa.ip}}{\longrightarrow} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (\emptyset, \{(\textit{sa}, \text{"Hello"}, \textit{sa}_\textit{echo})\}) * \\ \textit{sa} \mapsto \varPhi_\textit{clt} \ \gamma * \textit{sa}_\textit{pong} \mapsto \varPhi_\textit{srv} * \\ \texttt{half}^{\gamma} \ \text{"Hello"} \end{cases}
       let m_1 = \operatorname{recv} sh in
 \begin{cases} sh \stackrel{\varsigma \text{s-i.p.}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(\_, str_1, sa)\}, \{(sa, \text{``Hello''}, sa_{echo})\}) * \\ sa \mapsto \varPhi_{clt} \ \gamma * sa_{\mathsf{pong}} \mapsto \varPhi_{srv} * \\ \mathsf{half}^{\gamma} \ \text{``Hello''} * m_1 = (str_1, \_) * \varPhi_{clt} \ \gamma \ (\_, str_1, sa) \end{cases} 
       send sh "World" saecho:
       let m_2 = \text{recvfresh } sh [m_1] \text{ in}
        assert (fst m_1 = \text{"Hello"});
       assert (fst m_2 = "World")
  {\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
\begin{cases} \textit{sh} \overset{\textit{sa.ip}}{\longrightarrow} \mathsf{Some}(\textit{sa}) * \textit{sa} \leadsto (\emptyset, \{(\textit{sa}, \text{"Hello"}, \textit{sa}_\textit{echo})\}) * \\ \textit{sa} \mapsto \varPhi_\textit{clt} \ \gamma * \textit{sa}_\textit{pong} \mapsto \varPhi_\textit{srv} * \\ \texttt{half}^{\gamma} \ \text{"Hello"} \end{cases}
       let m_1 = \operatorname{recv} sh in
 \begin{cases} sh \xrightarrow{csa.ip} \mathsf{Some}(sa) * sa \leadsto (\{(\_, str_1, sa)\}, \{(sa, \text{``Hello''}, sa_{echo})\}) * \\ sa \mapsto \varPhi_{clt} \ \gamma * sa_{pong} \mapsto \varPhi_{srv} * \\ \mathsf{half}^{\gamma} \ \text{``Hello''} * m_1 = (str_1, \_) * \mathsf{half}^{\gamma} \ str_1 \end{cases} 
       send sh "World" saecho:
       let m_2 = \text{recvfresh } sh [m_1] \text{ in}
       assert (fst m_1 = \text{"Hello"});
       assert (fst m_2 = "World")
  {\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
      let sh = socket in
      socketbind sh sa:
      send sh "Hello" saecho:
 \begin{cases} \mathit{sh} \overset{\mathsf{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \mathsf{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \mathsf{``Hello''} \end{cases} 
      let m_1 = \operatorname{recv} sh in
 \left\{ \begin{matrix} sh \overset{csa.ip}{\longleftrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(\_, str_1, sa)\}, \{(sa, \text{``Hello''}, sa_{echo})\}) * \\ sa \mapsto \varPhi_{clt} \ \gamma * sa_{\mathsf{pong}} \mapsto \varPhi_{srv} * \\ \mathsf{half}^{\gamma} \ \text{``Hello''} * m_1 = (str_1, \_) * \mathsf{half}^{\gamma} \ str_1 \end{matrix} \right\} 
      send sh "World" saecho:
                                                                                                                                                   HALE-AGREE
      let m_2 = \text{recvfresh } sh [m_1] in
      assert (fst m_1 = \text{"Hello"});
      assert (fst m_2 = "World")
{\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
 \begin{cases} \mathit{sh} \overset{\mathsf{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \mathsf{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \mathsf{``Hello''} \end{cases} 
       let m_1 = \operatorname{recv} sh in
 \left\{ \begin{array}{l} \mathit{sh} \overset{\mathsf{csa.ip}}{\longleftrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{\mathit{echo}})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathit{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{``Hello''} * \mathit{m}_1 = (\text{``Hello''}, \_) * \mathsf{half}^{\gamma} \ \mathit{str}_1 \end{array} \right\} 
       send sh "World" saecho:
                                                                                                                                                                    HALE-AGREE
       let m_2 = \text{recvfresh } sh [m_1] in
       assert (fst m_1 = \text{"Hello"});
                                                                                                                                                                    \mathtt{half}^{\gamma} \ x * \mathtt{half}^{\gamma} \ y \vdash x = y
       assert (fst m_2 = "World")
 {\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
 \begin{cases} \mathit{sh} \overset{\mathsf{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \mathsf{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \mathsf{``Hello''} \end{cases} 
      let m_1 = \operatorname{recv} sh in
 \left\{ \begin{array}{l} \mathit{sh} \overset{\mathsf{csa.ip}}{\longleftrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{\mathit{echo}})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathit{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{``Hello''} * \mathit{m}_1 = (\text{``Hello''}, \_) * \mathsf{half}^{\gamma} \ \mathit{str}_1 \end{array} \right\} 
      send sh "World" saecho:
                                                                                                                                  HALE-UPDATE
      let m_2 = \text{recvfresh } sh [m_1] \text{ in}
       assert (fst m_1 = \text{"Hello"});
                                                                                                                                   half^{\gamma} x * half^{\gamma} y \vdash \Longrightarrow half^{\gamma} z * half^{\gamma} z
      assert (fst m_2 = "World")
{\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
 \begin{cases} \mathit{sh} \overset{\mathsf{sa.ip}}{\longrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\emptyset, \{(\mathit{sa}, \mathsf{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \mathsf{``Hello''} \end{cases} 
      let m_1 = \operatorname{recv} sh in
 \left\{ \begin{array}{l} \mathit{sh} \overset{\mathsf{csa.ip}}{\longleftrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{\mathit{echo}})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathit{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) * \mathsf{half}^{\gamma} \ \text{``World''} \\ \end{array} \right\} 
      send sh "World" saecho:
                                                                                                                                  HALE-UPDATE
      let m_2 = \text{recvfresh } sh [m_1] in
       assert (fst m_1 = \text{"Hello"});
                                                                                                                                   half^{\gamma} x * half^{\gamma} y \vdash \Longrightarrow half^{\gamma} z * half^{\gamma} z
      assert (fst m_2 = "World")
{\mathsf{True}}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
      let sh = socket in
      socketbind sh sa:
      send sh "Hello" saecho:
      let m_1 = recv sh in
 \begin{cases} \mathit{sh} \overset{\mathit{sa.in}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{\mathit{echo}})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathit{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) * \mathsf{half}^{\gamma} \text{``World''} \end{cases} 
      send sh "World" saecho:
     let m_2 = \text{recvfresh } sh [m_1] \text{ in}
      assert (fst m_1 = \text{"Hello"});
      assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
       let m_1 = \operatorname{recv} sh in
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{pong} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) * \mathsf{half}^{\gamma} \ \text{``World''} \end{cases} 
       send sh "World" saecho:
 \begin{cases} sh \stackrel{\varsigma sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(\_, str_1, sa)\}, \{(sa, \text{``Hello''}, sa_{echo}), (sa, \text{``World''}, sa_{echo})\}) * \\ sa \mapsto \varPhi_{clt} \ \gamma * sa_{pong} \mapsto \varPhi_{srv} \ * \\ \mathtt{half}^{\gamma} \ \text{``World''} * m_1 = (\text{``Hello''}, \_) \end{cases} 
       let m_2 = \text{recvfresh } sh [m_1] \text{ in}
       assert (fst m_1 = \text{"Hello"});
       assert (fst m_2 = "World")
 {True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
     socketbind sh sa:
     send sh "Hello" saecho:
     let m_1 = recv sh in
     send sh "World" saecho;
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip.}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{echo}), (\mathit{sa}, \text{``World''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{pong} \mapsto \varPhi_{\mathit{srv}} * \\ \mathit{half}^{\gamma} \ \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) \end{cases} 
     let m_2 = \text{recvfresh } sh [m_1] \text{ in}
     assert (fst m_1 = "Hello");
     assert (fst m_2 = "World")
{True}
```

{True}

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
       let m_1 = recv sh in
       send sh "World" saecho;
 \begin{cases} \mathit{sh} \overset{\mathit{sa.ip.}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{echo}), (\mathit{sa}, \text{``World''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{pong} \mapsto \varPhi_{\mathit{srv}} * \\ \mathit{half}^{\gamma} \ \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) \end{cases} 
      let m_2 = \text{recvfresh } sh [m_1] \text{ in}
\begin{cases} sh \overset{\text{sa.in}}{\rightarrow} \mathsf{Some}(sa) * sa \leadsto (\_,\_) * \\ sa \mapsto \varPhi_{\mathit{clt}} \ \gamma * sa_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \text{ "World" } * m_1 = (\text{"Hello"},\_) * m_2 = (\mathit{str}_2,\_) * \varPhi_{\mathit{clt}} \ \gamma \ (\_,\mathit{str}_2,\mathit{sa}) \end{cases} 
      assert (fst m_1 = \text{"Hello"});
      assert (fst m_2 = "World")
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
       let m_1 = recv sh in
       send sh "World" saecho;
 \begin{cases} sh \overset{\varsigma sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\{(\_, str_1, sa)\}, \{(sa, \text{``Hello''}, sa_{echo}), (sa, \text{``World''}, sa_{echo})\}) * \\ sa \mapsto \varPhi_{clt} \ \gamma * sa_{pong} \mapsto \varPhi_{srv} \ * \\ \mathtt{half}^{\gamma} \ \text{``World''} * m_1 = (\text{``Hello''}, \_) \end{cases} 
      let m_2 = \text{recvfresh } sh [m_1] \text{ in}
\begin{cases} sh \overset{\varsigma sa.ip}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\_,\_) * \\ sa \mapsto \varPhi_{\mathit{clt}} \ \gamma * sa_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \text{ "World" } * \textit{m}_1 = (\text{"Hello"},\_) * \textit{m}_2 = (\textit{str}_2,\_) * \mathsf{half}^{\gamma} \ \textit{str}_2 \end{cases}
      assert (fst m_1 = \text{"Hello"});
      assert (fst m_2 = "World")
 {True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
       let sh = socket in
       socketbind sh sa:
       send sh "Hello" saecho:
       let m_1 = recv sh in
       send sh "World" saecho;
\begin{cases} \mathit{sh} \overset{\mathit{sa.ip}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\{(\_, \mathit{str}_1, \mathit{sa})\}, \{(\mathit{sa}, \text{``Hello''}, \mathit{sa}_{echo}), (\mathit{sa}, \text{``World''}, \mathit{sa}_{echo})\}) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{pong} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \ \text{``World''} * \mathit{m}_1 = (\text{``Hello''}, \_) \end{cases}
       let m_2 = \text{recvfresh } sh [m_1] \text{ in}
\begin{cases} sh \overset{\text{sa.ip}}{\longrightarrow} \mathsf{Some}(sa) * sa \leadsto (\_,\_) * \\ sa \mapsto \varPhi_{c/t} \ \gamma * sa_{\mathsf{pong}} \mapsto \varPhi_{srv} * \\ \mathsf{half}^{\gamma} \text{ "World" } * m_1 = (\text{"Hello"},\_) * m_2 = (\text{"World"},\_) * \mathsf{half}^{\gamma} \text{ } str_2 \end{cases}
       assert (fst m_1 = \text{"Hello"});
       assert (fst m_2 = "World")
 {True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
     let sh = socket in
     socketbind sh sa:
     send sh "Hello" saecho:
     let m_1 = recv sh in
     send sh "World" saecho;
     let m_2 = \text{recvfresh } sh [m_1] \text{ in}
\begin{cases} \mathit{sh} \overset{\mathit{sa.in}}{\hookrightarrow} \mathsf{Some}(\mathit{sa}) * \mathit{sa} \leadsto (\_,\_) * \\ \mathit{sa} \mapsto \varPhi_{\mathit{clt}} \ \gamma * \mathit{sa}_{\mathsf{pong}} \mapsto \varPhi_{\mathit{srv}} * \\ \mathsf{half}^{\gamma} \text{ "World" } * \mathit{m}_1 = (\text{"Hello"},\_) * \mathit{m}_2 = (\text{"World"},\_) * \mathsf{half}^{\gamma} \ \mathit{str}_2 \end{cases}
     assert (fst m_1 = "Hello");
     assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
   let sh = socket in
   socketbind sh sa:
   send sh "Hello" saecho:
   let m_1 = recv sh in
   send sh "World" saecho;
   let m_2 = \text{recvfresh } sh [m_1] \text{ in}
   assert (fst m_1 = \text{"Hello"});
   assert (fst m_2 = "World")
{True}
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
   let sh = socket in
   socketbind sh sa:
   send sh "Hello" saecho:
   let m_1 = recv sh in
   send sh "World" saecho;
   let m_2 = \text{recvfresh } sh [m_1] \text{ in}
   assert (fst m_1 = \text{"Hello"});
   assert (fst m_2 = "World")
{True}
Is it safe?
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
   let sh = socket in
   socketbind sh sa:
   send sh "Hello" saecho:
   let m_1 = recv sh in
   send sh "World" saecho;
   let m_2 = \text{recvfresh } sh [m_1] \text{ in}
   assert (fst m_1 = \text{"Hello"});
   assert (fst m_2 = "World")
{True}
Is it safe? Yes! \\
```

```
\{\mathsf{FreeAddr}(\mathsf{sa}) * \mathsf{sa} \leadsto (\emptyset,\emptyset) * \mathsf{dyn} \; \mathsf{sa} * \mathsf{sa}_{\mathsf{pong}} \mapsto \Phi_{\mathsf{srv}}\}
   let sh = socket in
   socketbind sh sa:
   send sh "Hello" saecho:
   let m_1 = \operatorname{recv} sh in
   send sh "World" saecho;
   let m_2 = \text{recvfresh } sh [m_1] \text{ in}
   assert (fst m_1 = \text{"Hello"});
   assert (fst m_2 = "World")
{True}
Is it safe? Yes! \\
At least with respect to the distributed semantics.
```

Case Studies in Aneris

There are many case studies on top of Aneris

- ► Reliable Communication Library
- Distributed Causal Memory
- ► Conflict-Free Replicated Data Types

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Feel free to look around at https://github.com/logsem/aneris and ask questions at hinrichsen@cs.au.dk