

Diagram: Stabilization vs Observation

This diagram illustrates the two structural operations governing the framework:

Stabilization. Internal equilibration, decoherence, or gravitational settling. Modeled by an idempotent endofunctor

$$S : \mathcal{C} \rightarrow \mathcal{C}, \quad S^2 \cong S.$$

Observation. Projection to externally accessible descriptions. Modeled by a generally non-faithful functor

$$\Pi : \mathcal{C} \rightarrow \mathcal{O}.$$

The diagram compares the two composites:

$$\Pi \circ S \quad (\text{stabilize then observe})$$

and

$$S_{\mathcal{O}} \circ \Pi \quad (\text{observe then coarse-grain}).$$

These are related by a natural transformation

$$\eta_X : \Pi(SX) \longrightarrow S_{\mathcal{O}}(\Pi X).$$

$$\begin{array}{ccccc}
 & & & & \\
 & & & & \\
 X & \xrightarrow{S} & SX & \xrightarrow{\Pi} & \Pi(SX) \\
 & \searrow \Pi & & & \swarrow \eta_X \\
 & & \Pi X & \xrightarrow{S_{\mathcal{O}}} & S_{\mathcal{O}}(\Pi X)
 \end{array}$$

Non-invertibility of η_X expresses a structural mismatch between internal stabilization and observable structure. Persistent non-invertibility characterizes black-hole regions.