

**Homework 2****Out:** 9.19.23**Due:** 9.27.23**1. [Asymptotic comparison, 25 points]**

For each of these problems enter “yes” or “no” indicating whether A is  $O$ ,  $o$ ,  $\Theta$ ,  $\omega$ ,  $\Omega$  of B. Justify your answers.

A	B	$O$	$o$	$\Theta$	$\omega$	$\Omega$
$n^3 + 2n + 100$	$20n^3 - 5n + 2$					
$2489^{200}$	$\log_{2489}(n)$					
$n^7$	$3^n$					
$n$	$\sum_{i=1}^n \frac{50}{i}$					
$200 n^9$	$e^n$					

**2. [Asymptotics, 25 points]**

Place the following functions from asymptotically smallest to largest. When two functions have the same asymptotic order, put an equal sign between them. Provide an explanation for your ordering.

$1, n^{\frac{1}{540}}, (n)^{540}, \sqrt{n+540}, \log_n 540, \log_{540} n, \frac{540}{n}, 540n, n!, \frac{1}{\log n}, \left(\frac{540}{549}\right)^n, 24^{100}, n \log n$

**3. [Algorithmic intuition, 50 points]**

Write and briefly explain the following C++ function:

~~*long MaxProduct(string file);*~~

~~that accepts an input file containing sequences of integers. Each sequence starts on a new line, may continue on several subsequent lines, contains at most 100 numbers, and ends with the number 999999 (which is not part of the sequence).~~

~~The function outputs to the screen the maximum contiguous sub-sequence product of up to 3 numbers for each sequence, one output per line. A contiguous sub-sequence is a sequence of 1, 2, or 3 numbers that are consecutive in the input. It returns the maximum of all the outputs.~~

~~Sample input:~~

~~1 2 3 999999  
5 2 2 30 999999  
6 9 10 1 999999~~

~~8 999999~~

Sample output:

~~6~~

~~120~~

~~54~~

~~-8~~

~~The overall max product is: 120~~

The *MaxProduct* method is a member function of the *MaxProductClass* class, which should be implemented in *MaxProduct.cpp* and declared in *MaxProduct.h*. Try to make your function as efficient as you can.

Submit your solution, in two files: *MaxProduct.cpp*, containing your function, and *MaxProduct.h*, which is required for your code to compile with the provided main file, *HW2\_Q3\_main.cpp*. Make sure to write your name in a comment at the top of the program, and verify that your program compiles with the provided file on the lab computers.

As a reminder, in order to compile multiple files on the command line, you will need to use something like:

~~> set enable devtoolset-10 bash~~

~~> g++ -std=c++17 main.cpp Problem3.cpp~~