

$$T_j^{(0)} = h_j \left(\frac{f(a) + f(b)}{2} + \sum_{i=1}^{n_j-1} f(x_i) \right), \quad h_j = \frac{\pi}{2^j}, \quad n_j = 2^j$$

Romberg-Verfahren

$$T_j^{(k)} = T_j^{(k-1)} + \frac{T_j^{(k-1)} - T_{j-1}^{(k-1)}}{4^k - 1}$$

Rechnung für $j=0 \dots 4$

$$j=0, n_0=1, h_0=\pi$$

$$T_0^{(0)} = \frac{\pi}{2} (\cos(0^2) + \cos(\pi^2)) = 0.0236$$

$$j=1, n_1=2, h_1=\frac{\pi}{2}$$

$$T_1^{(0)} = \frac{\pi}{2} \cdot \frac{1}{2} (\cos(0^2) + 2\cos((\frac{\pi}{2})^2) + \cos(\pi^2)) = -1.221$$

$$j=2, n_2=4, h_2=\frac{\pi}{4}$$

$$T_2^{(0)} = \frac{\pi}{4} \cdot \frac{1}{2} \cdot (\cos(0^2) + 2(\cos((\frac{\pi}{4})^2) + \cos((\frac{3\pi}{4})^2)) + \cos(\pi^2)) = 0.586$$

$$j=3, n_3=8, h_3=\frac{\pi}{8}$$

$$T_3^{(0)} = \frac{\pi}{8} \cdot \left(\frac{f(0) + f(\pi)}{2} + \sum_{k=1}^7 f(k \cdot \frac{\pi}{8}) \right)$$

$$j=4, n_4=16, h_4=\frac{\pi}{16}$$

$$T_4^{(0)} = \frac{\pi}{16} \left(\frac{f(0) + f(\pi)}{2} + \sum_{k=1}^{15} f(k \cdot \frac{\pi}{16}) \right)$$