

1(a)

$$V_{\text{opt}}(s, d) = \begin{cases} \text{Utility}(s) & \text{if } \text{IsEnd}(s) \\ \text{Eval}(s) & \text{if } d=0 \\ \max_{a \in \text{Actions}(s)} V_{\text{opt}}(\text{Succ}(s, a), d) & \text{if } \text{Player}(s) = a_0 \\ \vdots & \vdots \\ \max_{a \in \text{Actions}(s)} V_{\text{opt}}(\text{Succ}(s, a), d) & \text{if } \text{Player}(s) = a_{n-1} \\ \max_{a \in \text{Actions}(s)} V_{\text{opt}}(\text{Succ}(s, a), d-1) & \text{if } \text{Player}(s) = a_n \end{cases}$$

3(a)

$$V_{\text{opt}, \pi}(s, d) = \begin{cases} \text{Utility}(s) & \text{if } \text{IsEnd}(s) \\ \text{Eval}(s) & d=0 \\ \max_{a \in \text{Actions}(s)} V_{\text{opt}, \pi}(\text{Succ}(s, a), d) & \text{Player}(s) = a_0 \\ \sum_{a \in \text{Actions}(s)} \frac{1}{|\text{Actions}(s)|} V_{\text{opt}, \pi}(\text{Succ}(s, a), d) & \text{Player}(s) = a_1 \\ \vdots & \vdots \\ \sum_{a \in \text{Actions}(s)} \frac{1}{|\text{Actions}(s)|} V_{\text{opt}, \pi}(\text{Succ}(s, a), d) & \text{Player}(s) = a_{n-1} \\ \sum_{a \in \text{Actions}(s)} \frac{1}{|\text{Actions}(s)|} V_{\text{opt}, \pi}(\text{Succ}(s, a), d+1) & \text{Player}(s) = a_n \end{cases}$$