



# Econ 2250: Stats for Econ

Fall 2022

[Source for pic stats above.](#)

## **Announcements**

- Homework 4 is due on Thursday (9/22)
- Sample test will be available end of next week
- Class on next Friday will be async (virtual on Loom)

## **What we will do today?**

- Review HW3
- Read through Hw4
- Review AND and OR rules for unconditional prob
- Discuss Conditional Probability

# Basic Rules of Probability

1. For any event  $P(E) [0,1]$
2. If an event cannot occur  $P(E) = 0$
3. If an event is certain to occur  $P(E) = 1$
4. The sum of the probability of all outcomes must equal 1.

Likelihood of event

$$P(\text{event}) = \frac{\text{\# of outcomes of event}}{\text{\# of outcomes in } \Omega}$$

# Probability Jargon

**Marginal Probability:**  $P(A)$

**Joint Probability:**  $P(A \text{ and } B) = P(A, B)$

**Conditional Probability:**  $P(A \text{ given } B) = P(A|B)$

$$P(A|B) = P(A, B) / P(B)$$

**NOTICE:**  $P(A|B)$  NOT EQUAL  $P(B|A)$

# Bayes Rule

- $P(A|B) = P(B|A) * P(A) / P(B)$
- NOTE: we often do not have access to  $P(B)$  and have to calculate by looking at all possible cases:
- $P(B) = P(B|A) * P(A) + P(\text{not } B|\text{not } A) * P(\text{not } A)$ 
  - a.  $P(\text{not } A) = 1 - P(A)$
  - b.  $P(\text{not } B|\text{not } A)$  IS UNKNOWN, needs to be given

Here are some examples of bayes rule

<https://www.mathsisfun.com/data/bayes-theorem.html>

Make sure to check out the test questions at the bottom. You should be able to identify

$P(A|B)$  (what you're looking for),

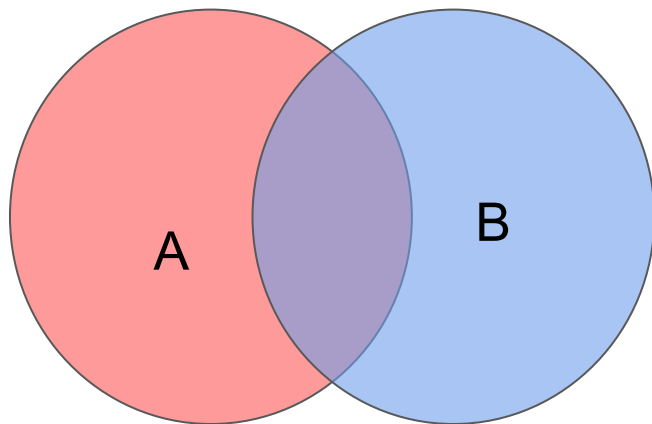
$P(B|A)$  the prior,

$P(A)$  the marginal of the conditional that you are looking for, and

$P(B)$  marginal of the condition (or how to find it)

If no  $P(B)$ , define  $P(A)P(B|A) + P(\text{not } A)P(\text{not } A|\text{not } B)$

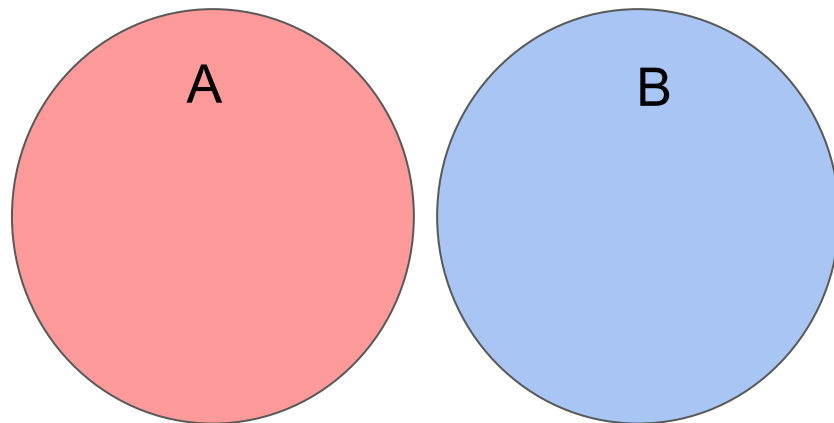
Non-mutually exclusive



$$P(A \cup B)$$

$$P(A) + P(B) - P(A \cap B)$$

Mutually exclusive

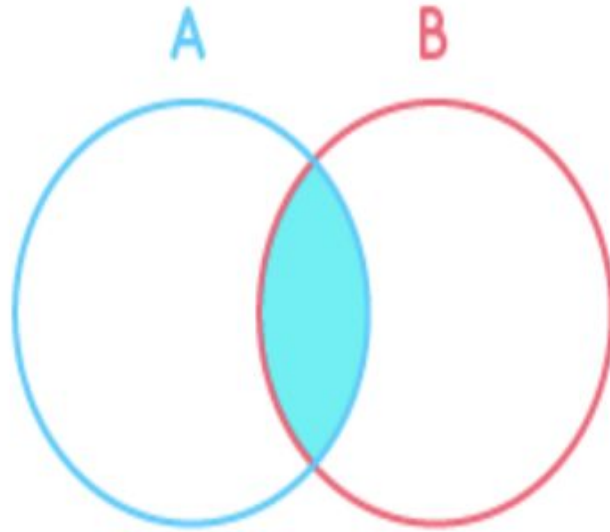


$$P(A \cup B)$$

$$P(A) + P(B)$$



Independent



$$P(A \cap B)$$

$$P(A) * P(B)$$

## Summary of probabilities

Event	Probability
A	$P(A) \in [0, 1]$
not A	$P(A^c) = 1 - P(A)$
A or B	$P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $P(A \cup B) = P(A) + P(B) \quad \text{if A and B are mutually exclusive}$
A and B	$P(A \cap B) = P(A B)P(B) = P(B A)P(A)$ $P(A \cap B) = P(A)P(B) \quad \text{if A and B are independent}$
A given B	$P(A   B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B A)P(A)}{P(B)}$

End of class form



(<https://forms.gle/UKa1VTomUy8ys3RL8>)