

Competitive Programming Training

# Breadth-First Search

# Graph Traversal Methods

## Breadth-First Search (BFS)

visits the child vertices  
before visiting the sibling  
vertices

uses queues as data  
structure

## Depth-First Search (DFS)

visits the neighbor  
vertices before visiting  
the child vertices

uses stacks as data  
structure

## **Problem 1: Given a graph, check if there is a path between any pair of nodes**

- Pick any node and traverse the graph from said node
- After the traversal, check if every node has been visited at least once.

## Problem 2: Given an undirected graph, check the shortest distance between a given pair of nodes

- Pick the first node from the pair and start traversal using BFS
- During BFS, record the current length of the path visited
  - ◆ If there is an edge between  $u$  and  $v$ , then
    - $\text{dist}[v] = \text{dist}[u] + 1$
- When the second node is encountered, the distance stored is the shortest distance
- Note that this only works on undirected graphs

### Problem 3: Given an undirected graph, check if the graph is a tree

- In a tree, the number of nodes is exactly 1 more than the number of edges
- In addition, the given graph has to be connected (Problem 1)
- If both conditions are true, then the given graph is a tree

