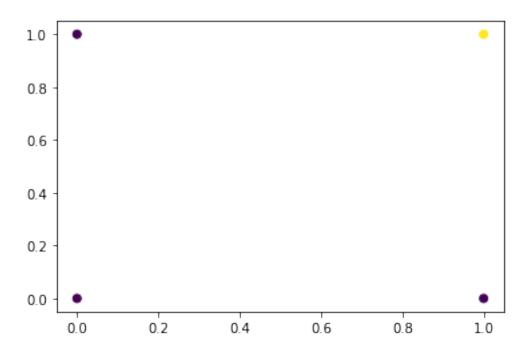
01_1_AND_Keras

December 22, 2020

```
[1]: import tensorflow as tf
    from tensorflow import keras
[2]: tf.__version__
[2]: '2.4.0'
[3]: import numpy as np
    import matplotlib.pyplot as plt
[4]: x_{data} = [[0, 0],
               [0, 1],
               [1, 0],
               [1, 1]]
    y_{data} = [0,
              0,
              0,
               1]
    \#x_{data} = np.array([[1, 2], [1, 5], [2, 2], [3, 3.5], [7, 5], [9, 4], [8, 2]])_{\sqcup}
     →#training_points
    #y_data = [1, 1, 1, 1, 0, 0, 0]
    x_data = np.array(x_data, dtype=np.float32)
    y_data = np.array(y_data, dtype=np.float32)
[5]: x_data.shape, y_data.shape
[5]: ((4, 2), (4,))
[6]: plt.scatter(x_data[:, 0], x_data[:, 1], c=y_data)
[6]: <matplotlib.collections.PathCollection at 0x7f7066bdb4a8>
```



```
[7]: from tensorflow.keras import layers
    from tensorflow.keras import activations
    from tensorflow.keras import optimizers
    from tensorflow.keras import models

[8]: model = models.Sequential()
    model.add(layers.Dense(2, input_dim=2))
    model.add(layers.Activation('tanh'))
    model.add(layers.Dense(1))
    model.add(layers.Activation('sigmoid'))

[9]: sgd = optimizers.SGD(lr=0.1)
    model.compile(loss='binary_crossentropy', optimizer=sgd, metrics=['accuracy'])

[10]: model.summary()
```

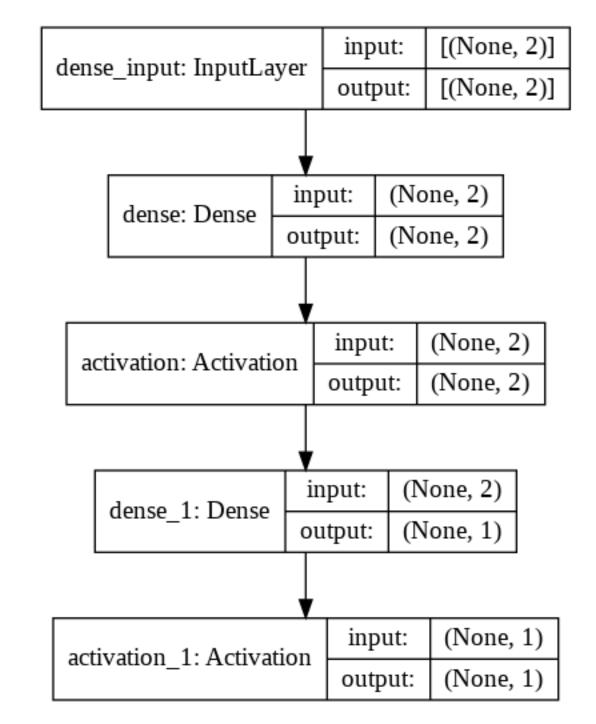
Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 2)	6
activation (Activation)	(None, 2)	0
dense_1 (Dense)	(None, 1)	3
activation_1 (Activation)	(None, 1)	0

Total params: 9
Trainable params: 9
Non-trainable params: 0

```
[11]: from tensorflow.keras.utils import plot_model plot_model(model, to_file='model_and.png', show_shapes=True)
```

[11]:



```
[12]: history = model.fit(x_data, y_data, batch_size=1, epochs=500)
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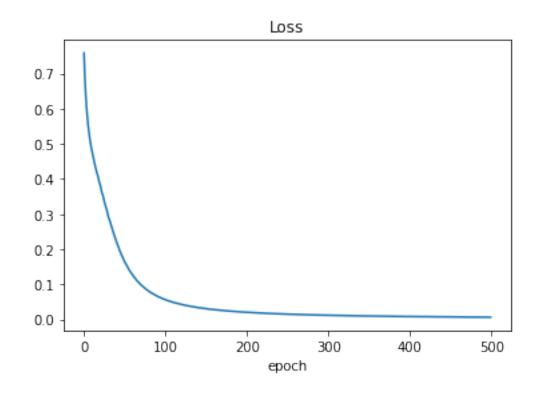
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                 ======] - Os 3ms/step - loss: 0.0072 - accuracy:
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[13]: plt.plot(history.history['loss'])
  plt.title('Loss')
  plt.xlabel('epoch')
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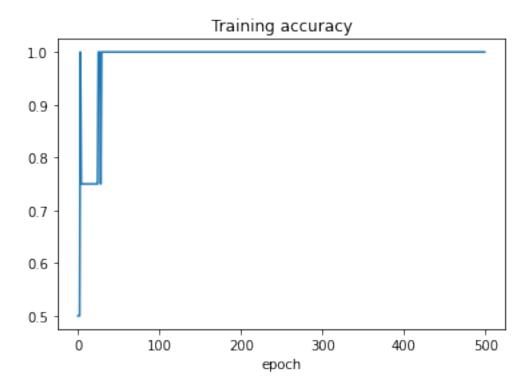
[13]: Text(0.5, 0, 'epoch')



```
[14]: plt.plot(history.history['accuracy'])
   plt.title('Training accuracy')
   plt.xlabel('epoch')
```

[14]: Text(0.5, 0, 'epoch')

[False]
[True]]



```
[15]: hypothesis = model.predict(x_data)
    print(hypothesis)

[[0.00102407]
    [0.00672129]
    [0.00525442]
    [0.9877707 ]]

[16]: predicted = hypothesis > 0.5
    print(predicted)
[[False]
    [False]
```