

Breadth First Search

Problem:

Given an undirected graph represented as an adjacency list, perform a Breadth-First Search (BFS) traversal starting from a specified node, and print the graph structure and the BFS traversal order.

Description:

This program models an undirected graph using an adjacency list, where each node has a list of adjacent nodes (neighbors). The program performs the following tasks:

1. **Print the graph structure:** It displays the graph's adjacency list representation, showing each node and its adjacent nodes.
2. **BFS Traversal:** It uses a queue to perform a BFS traversal starting from a given node, visiting all reachable nodes and printing the order in which nodes are visited.

Code:

```
#include <iostream>
#include <vector>
#include <queue>

using namespace std;

void printGraph(const vector<vector<int>> &adjList)
{
    cout << "Graph Structure (Adjacency List):" << endl;
    for (int i = 1; i < adjList.size(); ++i)
    {
        cout << i << " -> ";
        for (int neighbor : adjList[i])
        {
            cout << neighbor << " ";
        }
        cout << endl;
    }
}

void bfs(int start, vector<vector<int>> &adjList)
{
    vector<bool> visited(adjList.size(), false);
    queue<int> q;

    q.push(start);
    visited[start] = true;

    cout << "\nBFS Traversal: ";
    while (!q.empty())
    {
```

```

    int node = q.front();
    q.pop();
    cout << node << " ";

    for (int neighbor : adjList[node])
    {
        if (!visited[neighbor])
        {
            q.push(neighbor);
            visited[neighbor] = true;
        }
    }
}
cout << endl;
}

int main()
{
    vector<vector<int>> adjList = {
        {}, // 0 (unused)
        {2, 3}, // 1 -> 2, 3
        {1, 4, 5}, // 2 -> 1, 4, 5
        {1}, // 3 -> 1
        {2}, // 4 -> 2
        {2} // 5 -> 2
    };

    // Print the graph structure
    printGraph(adjList);

    // Perform BFS traversal starting from node 1
    bfs(1, adjList);

    return 0;
}

```

Output:

```

Graph Structure (Adjacency List):
1 -> 2 3
2 -> 1 4 5
3 -> 1
4 -> 2
5 -> 2

BFS Traversal: 1 2 3 4 5

```

Approach:

- **Graph Representation:** The graph is represented as an adjacency list, where each index corresponds to a node and contains a list of its adjacent nodes.
- **BFS Traversal:** The `bfs` function starts from the given node and uses a queue to explore its neighbors in breadth-first order. It marks nodes as visited when they are traversed to avoid revisiting them.
- **Graph Printing:** The `printGraph` function prints each node along with its adjacent nodes.

Complexity Analysis:

- **Time Complexity:**
 - Printing the graph structure takes $O(E)$ time, where E is the number of edges in the graph because each edge is printed once.
 - The BFS traversal also takes $O(V + E)$ time, where V is the number of vertices and E is the number of edges. This is because each node and each edge is processed once.
- **Space Complexity:**
 - The space complexity is $O(V)$ due to the space required to store the visited nodes and the queue used for BFS traversal.
 - The adjacency list requires $O(V + E)$ space to store the graph's edges and vertices.

Thus, the overall time complexity is $O(V + E)$, and the space complexity is $O(V + E)$.