

CSI2110
Assignment#2
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I used eclipse to write the code, so all the source code (the *.java file) are in the folder called src. And all the .class file are in folder called bin, but the bin is empty since I delete all the .class file before submission.

The file called output is the output obtained by the main program.

There is also a .pdf file called README, just in case the .txt file won't open in Windows system computer(this txt file is generated by Mac system). It happened before.

Part3

A) Priority queue Q implemented using a Sorted List.

The overall running time in term of big Oh of the algorithm is $O(N*N)$.

- Initializing Q implemented using a Sorted List is $O(1)$.
- Initializing "leafWhereLetterIs" is $O(65536)$, which is also $O(1)$.
- Assigning each position to null of the array "leafWhereLetterIs" is $O(65536)$, which is $O(1)$.
- Inside of the first loop, checking "if (frequencies[i]>0)" for n time for the worst case.
- Therefore, inside the if condition, the worst case, first two assignments take $O(N)$ time.
- Except "heap.insert(node, node)" , it takes $O(N*N)$ time, since each time the if condition is true, "heap.insert(node,node)" will be executed, each time the method executed, it takes $O(N)$ time to insert. Therefore, if the "if" condition is true n times, the method "heap.insert(node,node)" will be called n times. The running time then will be $O(N*N)$.
- creating a "HuffmanNode" is $O(1)$
- Assigning a position in the "leafWhereLetterIs" is $O(1)$
- "heap.insert" is $O(N)$
- Inside the while loop, "heap.removeMin()" is $O(N)$, since the while condition will be checked n times.
- primitive operation is $O(N)$
- Initializing a Node is $O(N)$
- e1.getValue().parent is $O(N)$
- "heap.insert" is $O(N*N)$

B)Priority queue Q implemented using a Unsorted List.

The overall running time of the algorithm is now $O(N*N)$.

-Since most of operations and assignment remains the same running time except all

“heap.insert” and “heap.removeMin” methods.
 –Inside of the first loop, “heap.insert(node,node)” now change to $O(N)$, because the insert methods now takes only $O(1)$ time, and the worst case is that the if condition is true for n times, therefore, the methods “heap.insert(node,node)” will be executed n times, so the running time is $O(N)$.
 –Inside of the while loop, “heap.removeMin()” will now be $O(N \times N)$ time.
 –So ignore all lower $O()$ running time, the overall is $O(N \times N)$.

C) Priority queue Q implemented using a Heap.

The overall running time is $O(N \times \log N)$.
 –Most of operations remains the same running time except all “heap.insert” and “heap.removeMin” methods.
 –Inside of the first loop, the if condition will be checked, the worst case, n times, therefore “heap.insert(node,node)” will be executed n times, an each time it takes $O(\log N)$ time, so the overall is $O(N \times \log N)$.
 –“heap.insert” is $O(\log N)$.
 –Inside the while loop, the while loop condition will be checked size-1 time, thus n times.
 –“heap.removeMin()” will be executed n times, each time takes $O(\log N)$, overall $O(N \times \log N)$.

The algorithm code with foot note

```
private HuffmanNode BuildTree(int[] frequencies,char[] letters) {

    HeapPriorityQueue<HuffmanNode, HuffmanNode> heap =
        new HeapPriorityQueue<HuffmanNode,
        HuffmanNode>(frequencies.length+1); //  $O(1)$ 

    leafWhereLetterIs =new HuffmanNode[(int)'\uffff'+2]; // need  $2^{16}+1$ 
    spaces //  $O(65536)$ 
    for (int i=0; i< (int)'\uffff'+2; i++)
        leafWhereLetterIs[i]=null; // loop  $O(65536)$ 

    for (int i=0; i<frequencies.length; i++) {
        if (frequencies[i]>0) { //check condition for  $n$  times

            HuffmanNode node= new HuffmanNode( (int)letters[i],
            frequencies[i],null,null,null); // $O(n)$ 

            leafWhereLetterIs[(int)letters[i]]=node; //  $O(n)$ 

            heap.insert(node,node); // 1)  $O(N \times N)$  2)  $O(N)$  3)  $O(N \times \log N)$ 

        }
    }
}
```

```

}

HuffmanNode specialNode= new HuffmanNode( EndOfText,
0,null,null,null);//O(1)
leafWhereLetterIs[EndOfText]=specialNode; //O(1)
heap.insert(specialNode,specialNode); // 1) O(N) 2) O(1) 3)
O(logN)

while(heap.size() > 1){ //check for size-1 times, n times

    Entry<HuffmanNode, HuffmanNode> e1 = heap.removeMin();// 1) O(N)
2) O(N*N) 3) O(logN * N )
    Entry<HuffmanNode, HuffmanNode> e2 = heap.removeMin();// 1) O(N)
2) O(N*N) 3) O(logN * N )

    int newFrequency = e1.getKey().getFrequency() +
e2.getKey().getFrequency(); //O(N)

    HuffmanNode newTree = new HuffmanNode(0,newFrequency,null,
e1.getValue(), e2.getValue());//O(N)
    e1.getValue().parent = newTree;//O(N)
    e2.getValue().parent = newTree;//O(N)

    heap.insert(newTree, newTree); //1) O(N*N) 2) O(N) 3) O(logN *
N )
}
Entry<HuffmanNode, HuffmanNode> e = heap.removeMin();// 1) O(1) 2)
O(N) 3) O(logN)

return e.getValue();

}

```