

Recognizing Regular Patterns in Heterogeneous Sequences

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Overview

- 1 History
- Regular Type Expressions (RTEs) by Example
- Theoretically Interesting Implementation Challenges
 - Representation: RTE as AST
 - Construction: DFA Symbolic Finite Automata
 - Embedding: Complemented Type System Lattice
 - Determinism: Type Partitioning
 - Efficiency: Redundant Type Checks
- Final Thoughts

History



Publication History

 Regular Type Expressions (RTEs) introduced at ELS 2016 (European Lisp Symposium), implemented in Common Lisp.

https://www.lrde.epita.fr/wiki/Publications/newton.16.els

- See PhD Thesis 2018 for theoretical, implementation, and performance details https://www.lrde.epita.fr/wiki/Publications/newton.18.phd
- RTE Available:

Scala https://github.com/jimka2001/scala-rte
Clojure https://github.com/jimka2001/clojure-rte
Python https://github.com/jimka2001/python-rte
Common Lisp https://github.com/jimka2001/cl-rte

PADL 2025, Practical Aspects of Declarative Languages:
 Type-Checking Heterogeneous Sequences in a Simple Embeddable Type System

Goal

- Efficiently recognize *regular patterns* in mixed-type sequences.
- Supported in Scala as Seq[Any].

Example

Regular Type Expressions (RTEs)



We'd like to recognize sequences with *regular patterns*.

[1, 2, 2.3, 9.3, 3, 1.5F, 6.5, 4.8F, 2, 2.3]

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What's the pattern?

We'd like to recognize sequences with *regular patterns*.

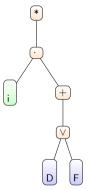
What's the pattern?

[
$$1$$
, $2.3, 9.3$, 3 , $1.5F, 6.5, 4.8F$, 2 , 2.3] floating points

We'd like to recognize sequences with *regular patterns*.

String-based regular expressions

- Match strings like: "iDDiFDFiD",
- ... we use surface syntax: "(i(D|F)+)*".
- ... representing expression: $(i \cdot (D \vee F)^+)^*$,



Abstract Syntax Tree (AST)

We'd like to recognize sequences with *regular patterns*.

```
[1, 2.3, 9.3, 3, 1.5F, 6.5, 4.8F, 2, 2.3]
```

String-based regular expressions

- Match strings like: "iDDiFDFiD",
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We propose Rational Type Expressions (RTEs)

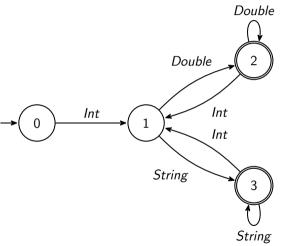
- Rational type expression: $(Int \cdot (Double \cup Float)^+)^*$
- Challenge Nº1: We need a surface syntax (and AST) for Scala.

[13 2.0 6.0 4 "a" "an" "the" -5 2.0 3.0 4.0 7 8.0]

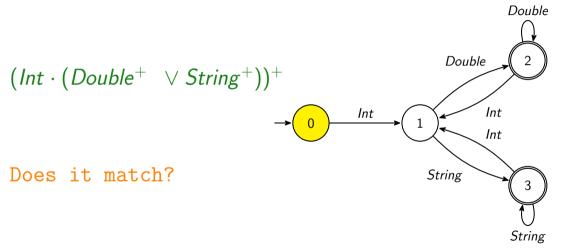
Does the sequence match the pattern? $(Int \cdot (Double^+ \vee String^+))^+$

We construct a finite automaton (DFA).

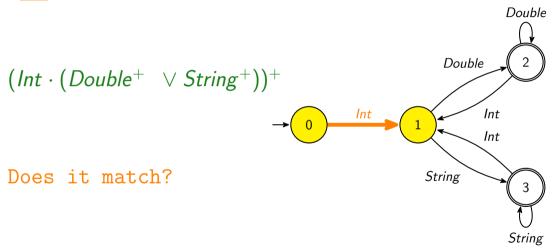
Challenge 1.2: How to construct a finite automaton from an RTE?

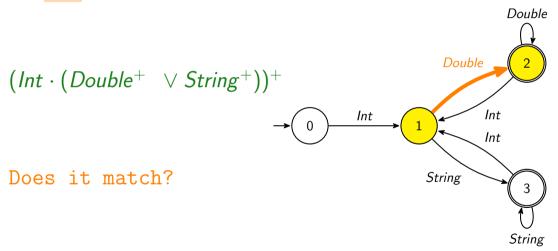


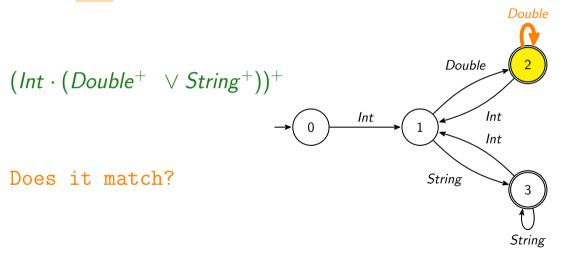
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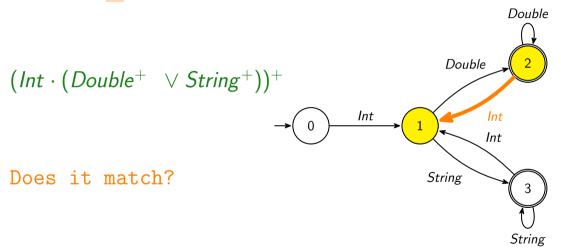


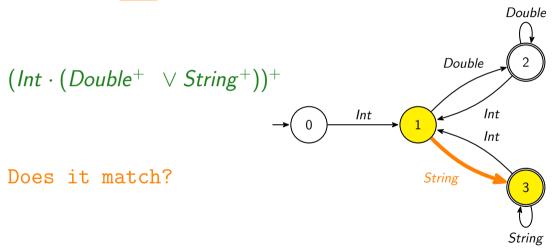
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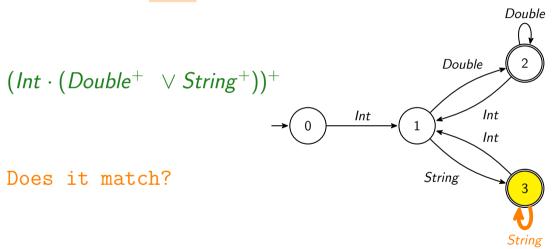


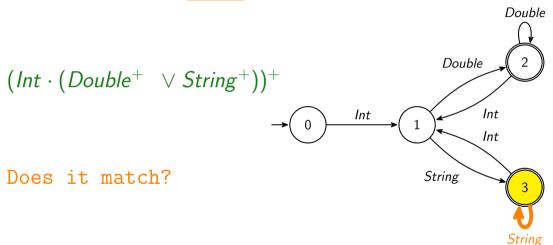


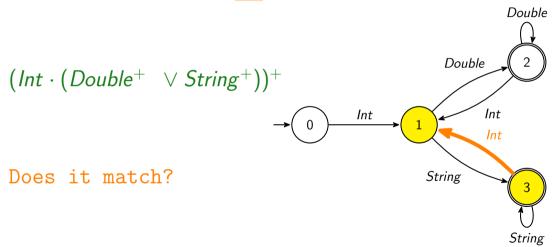


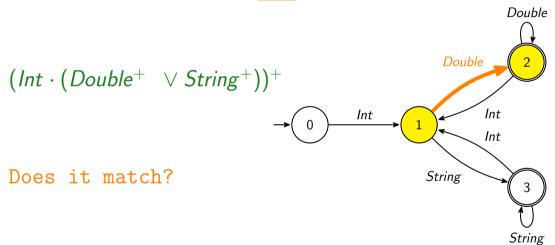


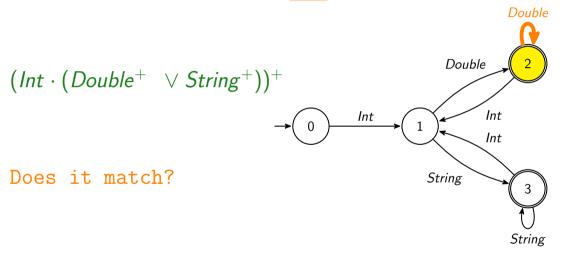


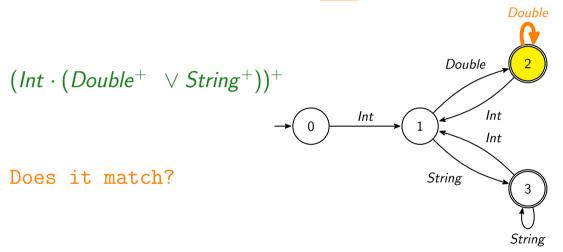


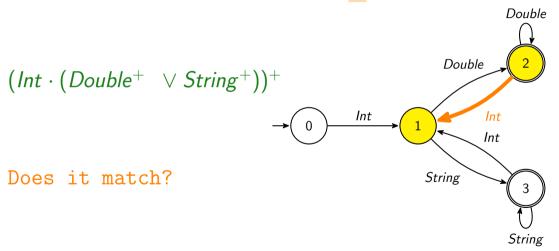


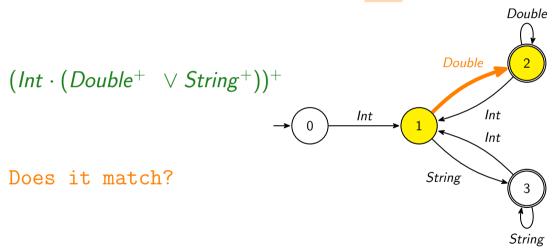




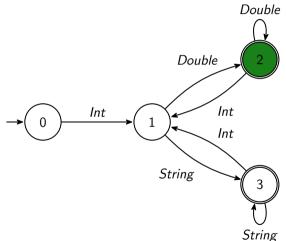








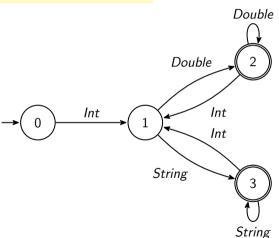
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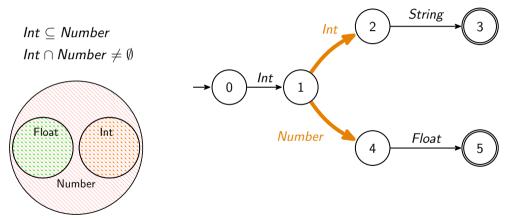
Yes, it's a match!

Decision procedure is O(n), independent of syntactical complexity of the RTE.

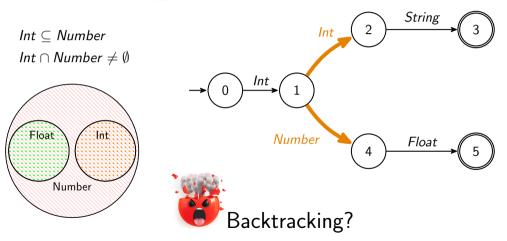




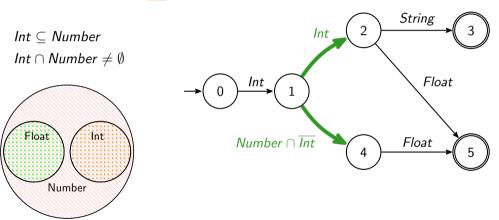
Suppose sequence = [2, 3, 5.6F]



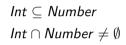
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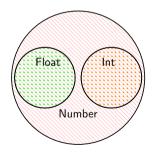


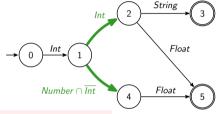
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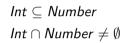


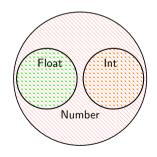


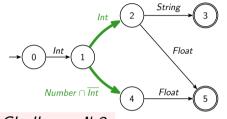


Challenge №3: How to support Int \(\cap \overline{Number}\) in Scala?

Suppose sequence = [2, 3, 5.6F]







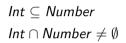
Challenge №3: How to support $Int \cap \overline{Number}$ in Scala?

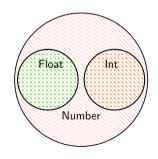
Challenge №4: How to partition types?

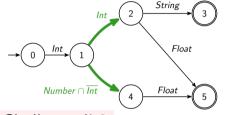
E.g., type decomposition

 $\{String, Int, Number\} \rightarrow \{String, Int, Number \cap \overline{Int}\}$

Suppose sequence = [2, 3, 5.6F]







Challenge №3: How to support Int \(\cap \overline{Number}\) in Scala?

Challenge №4: How to partition types?

Challenge №5: How to avoid duplicate type checks?

Challenges of the Project

- Challenge Nº 1: RTE Representation: Representing an RTE in Scala?
- Challenge № 2: DFA Construction: Constructing from RTE?
- Challenge № 3: Type Lattice: Union, intersection, complement types?
- Challenge № 4: Determinism: Type partitioning?
- Challenge № 5: Efficiency: Avoiding redundant type checks at run-time?

Challenge №1: RTE Representation

How to represent an RTE in Scala?

- Surface syntax: declarative, expressive, composable
- Programmatic interface: reflective, algebraic manipulation

RTFs

What are Regular Type Expressions?

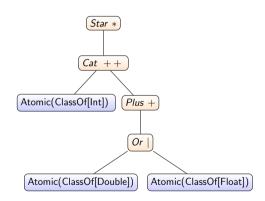
Mathematical notation:

```
(Int \cdot (Double \cup Float)^+)^*
```

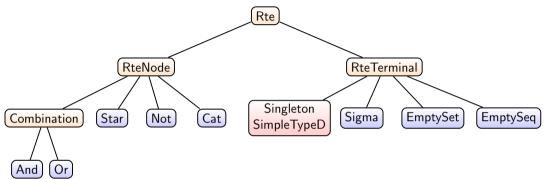
Scala notation: AST

```
val I:Rte = Atomic(classOf[Int])
val F:Rte = Atomic(classOf[Float])
val D:Rte = Atomic(classOf[Double])
val re:Rte = (I ++ (D | F).+).*
```

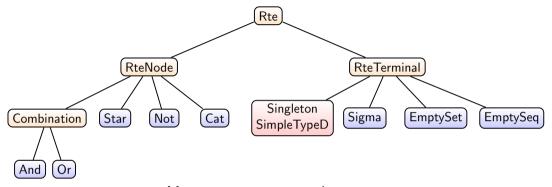
• Leaf nodes interface to Scala Type System



Rte class quasi-ADT, Algebraic Data Type



Rte class quasi-ADT, Algebraic Data Type



More on SimpleTypeD later ...

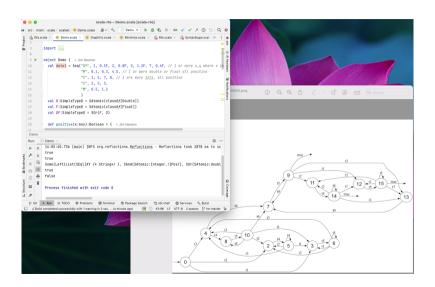
Challenge №2: DFA Construction

Given an RTE, generate a finite automaton.

- Well-known techniques exists to construct DFAs from RE
 - Brzozowski Derivative
- Adapt them to work with RTEs
- Enforce determinism

Demo

Sample Flow



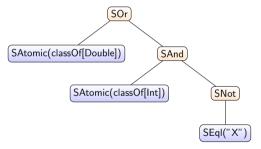
Challenge №3: Type Lattice

How to support types like $Int \cap \overline{Number}$ in Scala?

- Support complemented type lattice
- Embed a dynamic type system into an existing programming language.
- Answer type membership and subtype questions.

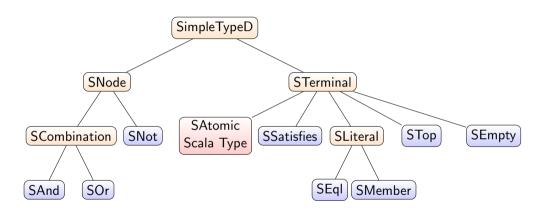
Example SimpleTypeD Expression Tree: AST

```
val Int = SAtomic(classOf[Int])
val Double = SAtomic(classOf[Double])
val td:SimpleTypeD = SOr(Double, SAnd(Int, SNot(SEql("X"))))
```



- A type designator is an expression tree (AST).
- Leaf nodes interface to Scala classes via SAtomic(...).
- ...and to literal Scala values via SEq1(...)
- ...and to predicate functions via SSatisfies(...)

SimpleTypeD class quasi-ADT



Type Membership Predicate

Boolean type membership question is always answerable.

```
SAtomic(classOf[Int]).typep(-42) // returns true
// returns true
 (SAtomic(classOf[String]) || SAtomic(classOf[Int])).typep(7)
// define predicate
def oddp(a:Any):Boolean = {
   a match
     case a:Int => a % 2 != 0
     case _ => false
 SSatisfies(oddp).typep(36) // returns false
```

Subtype Predicate

Semi-Boolean Subtype predicate sometimes unanswerable.

```
val Str:SimpleTypeD = SAtomic(classOf[String])
val Int:SimpleTypeD = SAtomic(classOf[Int])
val Num:SimpleTypeD = SAtomic(classOf[Number])
val odd:SimpleTypeD = SSatisfies(oddp, "oddp")
Str.subtypep(Int) // returns Some(false)
Int.subtypep(Num) // returns Some(true)
SSatisfies(oddp).subtypep(Int) // returns None
```

Unanswerable because:

- Impossible to compute, e.g. SSatisfies.
- Code is incomplete.
- JVM supports run-time loaded classes.
- Limitations of support libraries (discussed later).

Simple Embedded Type System: SETS

At the point, what have we done?

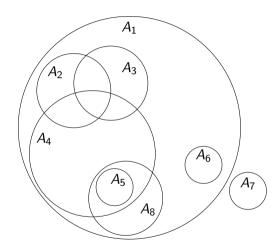
- Wrapped the Scala type system
- ... with a simple type system
- ... which supports a complemented type lattice
- ... with membership Boolean predicate
- ... with subtype semi-Boolean predicate
- ... which supports reflection

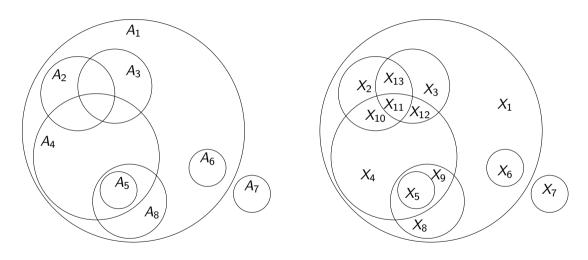
Cf: A Portable, Simple, Embeddable Type System [Newton, Pommellet] 2021 ELS

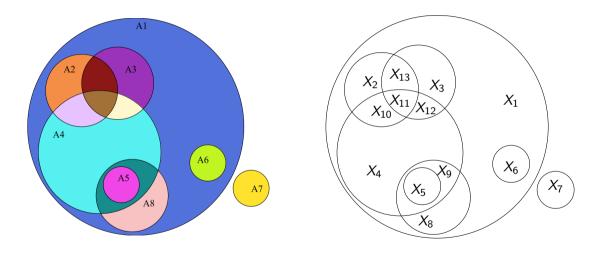
Challenge №4: Deterministic State Machines

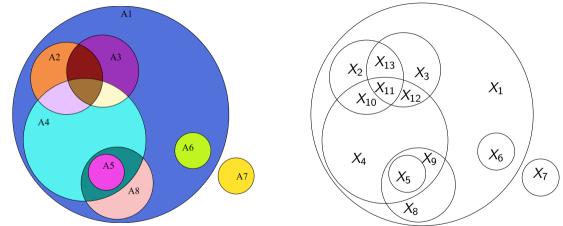
How to assure DFAs are deterministic by construction?

- Compute a partition of a given set of type designators,
- ... even (especially) when subtype relation is unknown.

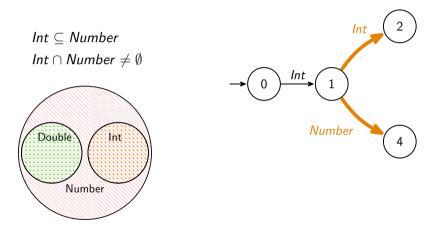




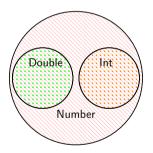


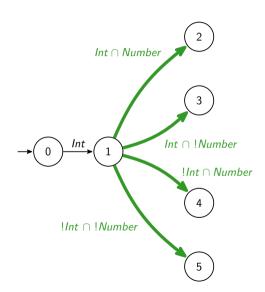


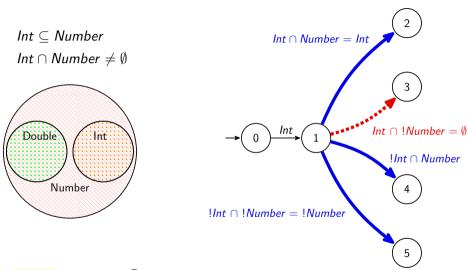
Cf: An Elegant and Fast Algorithm for Partitioning Types [Newton] 2023 ELS



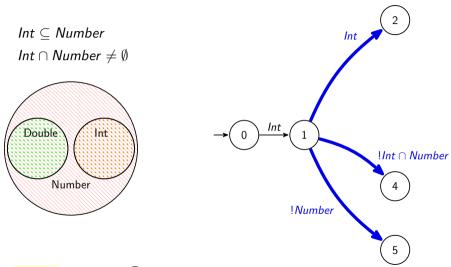
 $\begin{array}{l} \mathit{Int} \subseteq \mathit{Number} \\ \mathit{Int} \cap \mathit{Number} \neq \emptyset \end{array}$





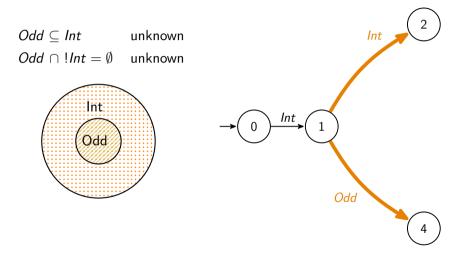


We can **decide** that state ③ is unreachable.

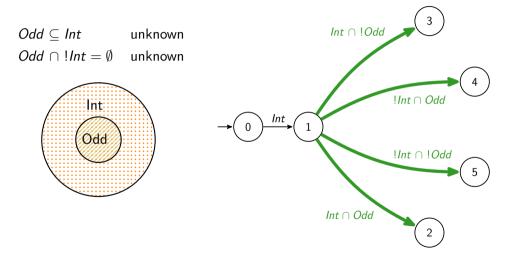


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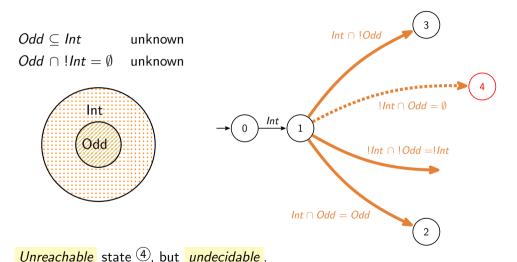
Non-determinism by SSatisfies



Non-determinism by SSatisfies

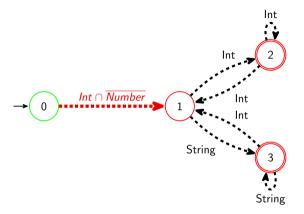


Non-determinism by SSatisfies



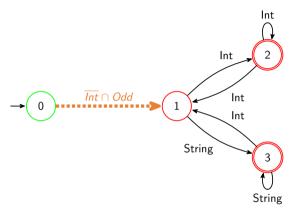
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Unsatisfiable Transitions



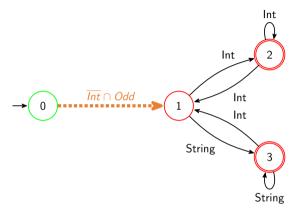
- If we determine a type is empty, then the transition is *unsatisfiable*.
- Thus we can eliminate the transition and unreachable states.

Indeterminate Transitions



- If we cannot determine a type is empty, the transition may still be unsatisfiable.
- However, we *cannot eliminate* the transition and unreachable states.

Indeterminate Transitions

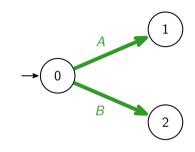


- We can always determine type membership.
- DFAs with indeterminate transitions *correctly* match sequences in O(n).

```
final class A() {}
final class B() {}

class C() {}
trait D() {}

abstract class E() {}
trait F {}
```



class G() extends E with F {}

$$A \cap B = \emptyset$$

Both are final; they have no common *inhabited* subclass.

```
final class A() {}
final class B() {}

class C() {}
trait D() {}

abstract class E() {}
trait F {}
```

$$C \cap D = unknown$$

Is there a class *somewhere* which inherits from both?

class G() extends E with F {}

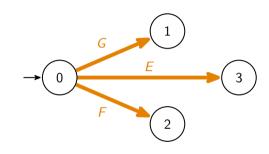
```
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trait D() {}

abstract class E() {}
trait F {}

class G() extends E with F {}

Explicit subtype relation.



$$G \subset E \implies G \cap E \neq \emptyset$$

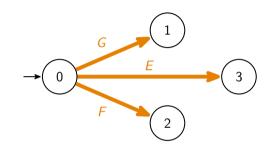
```
final class A() {}
final class B() {}
```

class C() {}
trait D() {}

abstract class E() {}
trait F {}

class G() extends E with F {}

G inherits from E and F.

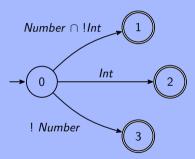


$$E \cap F \neq \emptyset$$

- If *currently* no subclass exists, JVM might *later* run-time load subclass.jar
- With Java > 8.x, Scala cannot dependably compute list of subclasses.
- Library github.com/ronmamo/reflections no longer maintained.
 - https://github.com/ronmamo/reflections/issues/324
 - https://users.scala-lang.org/t/help-with-org-reflections-api
 - https://stackoverflow.com/questions/52879584

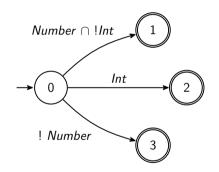
Challenge №5: Redundant Type Check

Select correct transition, avoiding redundant type checks.



Sequential Type Check

A DFA state may have several disjoint transitions, each with its own type label.



```
val N = SAtomic(classOf[Number])
val I = SAtomic(classOf[Int])

if (N & !I).typep(x)

Some(1)
else if I.typep(x)

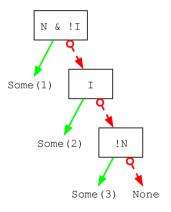
Some(2)
else if (!N).typep(x)

Some(3)
else
None
```

Some types may be checked multiple times. We can rewrite the code to *eliminate redundant checks* .

Decision Tree Structure

We programmatically manipulate if then ... else ... using a lazy decision tree.



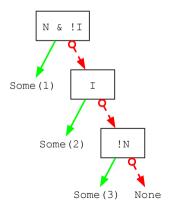
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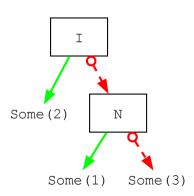
if (N & !I).typep(x)
Some(1)
else if I.typep(x)
Some(2)
else if (!N).typep(x)
Some(3)
else
None
```

Decision Tree, Before and After

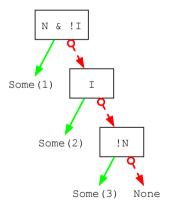
Viewing the decision tree before/after

Rewrite: $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$

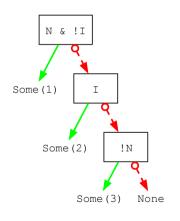


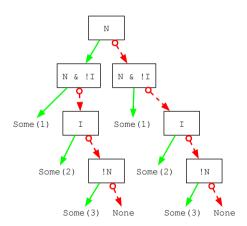


Duplicate tree, and introduce if N.typep(x) then ... else ...

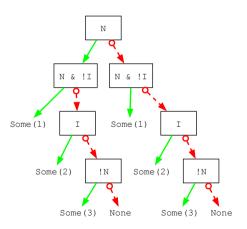


Duplicate tree, and introduce if N.typep(x) then ... else ...

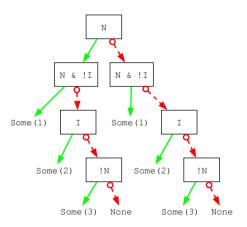




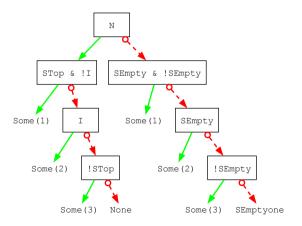
Duplicate tree, and introduce if N.typep(x) then ... else ...



In then part: Supertypes of N \rightarrow STop . In else part: Subtypes of N \rightarrow SEmpty .

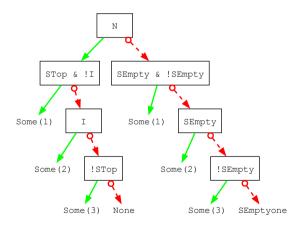


In then part: Supertypes of N \rightarrow STop . In else part: Subtypes of N \rightarrow SEmpty .



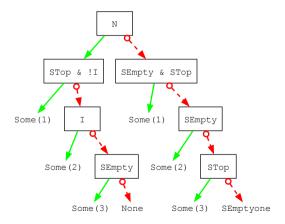
Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$

$$!STop \rightarrow SEmpty \rightarrow STop$$

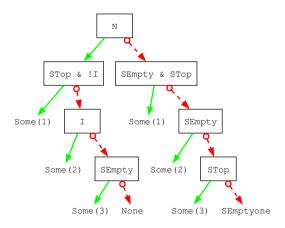


Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$

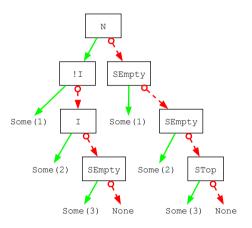
$$!STop \rightarrow SEmpty \rightarrow STop$$



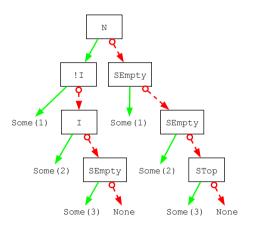
Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$
(STop & x) \rightarrow x (SEmpty & x) \rightarrow SEmpty



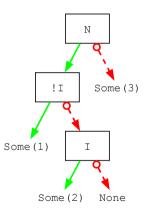
Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$
(STop & x) \rightarrow x (SEmpty & x) \rightarrow SEmpty



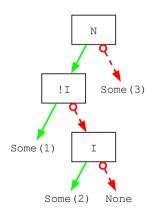
Rewrite: $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$ Replace Stop with then branch. Replace SEmpty with else branch

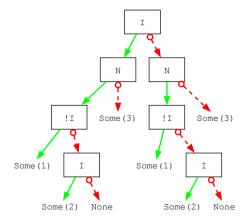


Rewrite: $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$ Replace Stop with then branch. Replace SEmpty with else branch.

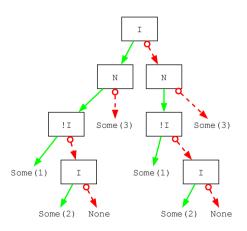


Duplicate tree, and introduce if I.typep(x) then ... else ...

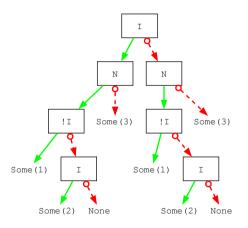




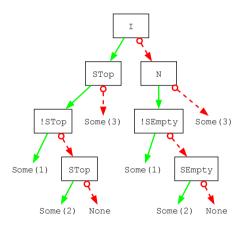
Duplicate tree, and introduce if I.typep(x) then ... else ...



In then part: Supertypes of $I \to STop$. In else part: Subtypes of $I \to SEmpty$.

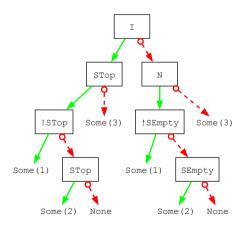


In then part: Supertypes of $I \to STop$. In else part: Subtypes of $I \to SEmpty$.

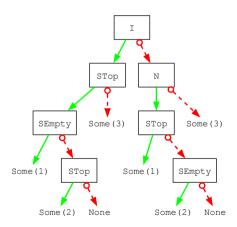


Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$

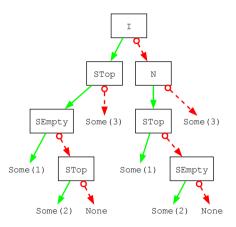
$$!STop \rightarrow SEmpty \rightarrow STop$$



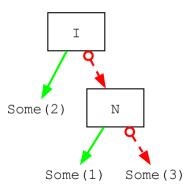
Rewrite: $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$ $!STop \rightarrow SEmpty \rightarrow STop$



Rewrite: $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$ Replace Stop with then branch. Replace SEmpty with else



Rewrite:
$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$$
Replace Stop with then branch. Replace SEmpty with else



Rewrite: Summary

Code has been rewritten so that any type check occurs no more than once.

```
val N = SAtomic(classOf[Number])
val I = SAtomic(classOf[Int])
                                                 if I.typep(x)
if (N & !I).typep(x)
                                                   Some(2)
 Some(1)
                                                 else if N.tvpep(x)
else if I.typep(x)
                                                     Some(1)
 Some(2)
                                                 else
else if (!N).typep(x)
                                                   Some(3)
 Some(3)
else
 None
```

And it is clear the code never returns None.

Summary: Challenges of the Project

- Challenge Nº 1: RTE Representation: Representing an RTE in Scala?
- Challenge № 2: DFA Construction: Constructing from RTE?
- Challenge № 3: Type Lattice: Union, intersection, complement types?
- Challenge № 4: Determinism: Type partitioning?
- Challenge № 5: Efficiency: Avoiding redundant type checks at run-time?

Perspectives

- Open/Closed world-view of Java types/classes
- Publish a summary of our techniques and results (PADL 2025).
- Move away from Scala 2
- Find replacement (or fix) for abandoned library: github.com/ronmamo/reflections

Conclusion

- Efficient pattern recognition for heterogeneous sequences for Scala
- Available here:

```
Scala https://github.com/jimka2001/scala-rte
Clojure https://github.com/jimka2001/clojure-rte
Python https://github.com/jimka2001/python-rte
Common Lisp https://github.com/jimka2001/cl-rte
```

- Critical Feedback Welcome!
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 - jimka.issy@gmail.com
 - Discord: jimka2001



THANK YOU

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